Theoretical interpretation of GeV-TeV cosmic rays

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With special thanks to Philipp Mertch









TeV Particle Astrophysics, Paris, 19-23 July 2010

We have witnessed a renaissance in γ -ray astronomy

 \rightarrow the sources of low energy cosmic rays may soon be known: **SNRs**?

 \geq Do the observed γ -rays arise from hadronic interactions (π^0 decays), or from inverse-Compton scattering by (radio synchrotron emitting) electrons ?

➤ Can 1st-order Fermi acceleration at SNR shocks explain the spectrum (injection, magnetic field amplification, diffusion losses vs anisotropy) ?

> What are the 'unidentified' γ -ray sources in the Milky Way – are there new source classes (micro-quasars, PWN, binaries ...), acceleration mechanisms ?





HESS Southern Plane Survey 2005



Galactic Longitude (°)

RXJ1713.7-3946 (HESS, 2004)



Much progress has been made but these questions are *not* fully answered ...

to *unambiguously* identify the cosmic ray sources, we need to detect TeV neutrinos!

... also the *PAMELA* and *Fermi* 'anomalies' have highlighted the limitations of the standard diffusion model

Supernova remnants are believed to be 'Pevatrons' – responsible for the acceleration of galactic cosmic rays upto the 'knee' at ~few x 10³ TeV



If O(10%) of the shock K.E. of ~ 10^{51} erg can be converted into cosmic rays, then the cosmic ray energy density of ~ 0.3 eV/cm^3 can be maintained by ~3 SN/century

Cosmic ray acceleration in *RXJ1713.7-3946*: electrons or protons?



 γ -ray emission well fitted by IC scattering of ~10² TeV electrons on CMB/starlight ... alternatively γ -rays may be from decays of π^0 s produced by ~10³ TeV protons

There is no *definite* evidence yet that SNRs accelerate *protons* to high energies ... this will be *proved* only when the **neutrinos** from π^0 decay are detected

1st-order Fermi acceleration by shock waves (DSA)



Shock velocity $v_s: \beta = v_s/c$

Simple diffusion theory: prob. of CR crossing shock > *m* times is $(1-\beta)^m$

Average fractional energy gained at each crossing is: $\Delta \varepsilon / \varepsilon = \beta$

 \Rightarrow differential spectrum: $\propto \varepsilon^{-2}$

However if ~10% of the shock wave K.E. is converted into relativistic particles, then backreaction of cosmic ray pressure on shock will make spectrum somewhat **harder and slightly concave** (*cf.* radio observations) ... but *time-integrated* spectrum

will be close to Fermi form (Caprioli, Amato & Blasi, Astropart.Phys.33:160,2010)

If cosmic rays diffuse out of Galaxy on a time-scale decreasing $\propto 1/\varepsilon^{0.6}$, then the observed spectrum $\propto \varepsilon^{-2.6}$ is matched (but why is no anisotropy $\propto \varepsilon^{0.6}$ observed?)

The 'standard model' for galactic cosmic rays

SNR shock waves accelerate relativistic particles by Fermi mechanism
 power law spectrum (synchrotron radio/X-ray + γ-ray emission)
 Diffusion through magnetic fields in Galaxy (disk + halo)



Secondary production during propagation: p

 p, e⁺, N'
 e[±] lose energy through synchrotron & inverse Compton scattering
 <u>Measurables:</u> Energy spectra of individual species, diffuse radiation

Diffusion of galactic cosmic rays

Transport equation:



Green's function: describes flux from a discrete, burst-like source ... integrate over spatial distribution and time-variation of injection

GALPROP (Moskalenko & Strong 1998) can solve the 3D time-dependent transport equation but yields ~the same answer for the *equilibrium* fluxes as the 'leaky box' model in which cosmic rays are assumed to have small energy dependent escape probability ⇒ exponential distribution of path lengths between cosmic ray sources and Earth



Escape through diffusion: $\tau_{\rm esc} \sim E^{-\delta}$, with $\delta \sim 0.6$ (from secondary/primary ratios) Energy loss through synchrotron radiation/IC scattering: $\tau_{\rm cool} \sim E^{-1}$

Energy spectra

Primary e -

Production: $q \propto E^{-2.2}$ (from radio spectrum) $\log J$ Propagation: min $[\tau_{esc}, \tau_{cool}] \propto E^{-0.6}, E^{-1}$ Observed: $n \propto E^{-2.8}, E^{-3.2}$ Primary protons/nuclei Production: presumably same as e^{-1} Propagation:

Observed: $n \propto E^{-2.8}$

 $\log E$

 $\propto E^{\cdot}$



2.8



All measured ratios consistent with 'leaky box' model with $\tau_{\rm esc} \sim E^{-\delta}$, $\delta \sim 0.4$ -0.6

NB: Kolmogorov spectrum for interstellar magnetic field turbulence implies $\delta = 1/3$, while Kraichnan spectrum implies $\delta = 1/2$

The 'two zone' model



Maurin, Taillet, Donato, Salati, Barrau & Boudoul [astro-ph/0212111]

Semi-analytic formulation provides better insight and estimation of uncertainties

But none of this would be particulary interesting if it were not for the *PAMELA* 'anomaly' ...

PAMELA has measured the positron fraction:

 $\frac{\phi_{e^+}}{\phi_{e^+}+\phi_{e^-}}$

Anomaly \Rightarrow excess above 'astrophysical background'

Source of anomaly:

- Dark matter?
- Pulsars?
- Supernova remnants?



PAMELA was designed to search for cosmic anti-matter



... positrons from the annihilations or decays of dark matter in the Galaxy would *naturally* have a hard spectrum corresponding to rising e^+ fraction

Indeed dark matter has been widely invoked as the source of the 'excess' e^+

DM annihilation

Rate $\propto n_{\rm DM}^2$

(e.g. few hundred GeV neutralino LSP or Kaluza-Klein state)



Bergström, Bringmann & Edjsö, PR D78:127850,2008

DM decay

Rate $\propto n_{\rm DM}/\tau_{\rm DM}$ (lifetime ~10⁹ x age of universe e.g. dim-6 operator suppressed by $M_{\rm GUT}$ for a TeV mass techni-baryon)



Nardi, Sannino & Strumia, JCAP 0901:043,2009



Fermi LAT also sees 'excess' e^{\pm} over expectation (Abdo *et al*, PRL 102:181101,2009) (although it does *not* confirm the peak seen earlier by *ATIC-2*)

But DM annihilation requires huge 'boost factor' to match flux

→ Such a large annihilation #-section would imply *negligible* relic abundance unless an *inverse* velocity dependence is invoked e.g. 'Somerfeld enhancement' (this requires hypothetical light gauge bosons to provide new long range force) Arkani-Hamed *et al*, PR D79:015014,2009



... no such problem for decaying dark matter (just tune the lifetime!)

Numerical simulations of structure formation through gravitational instability in cold dark matter show that the Milky Way formed from the merger of smaller structures (+ tidal stripping baryonic infall, disk formation *etc*) over several billion years ...

So the distribution of dark matter *is* clumpy, however the 'boost factor' due to this is estimated to be no more than a factor of ~2-10 (Lavalle *et al*, A&A 479:427,2008)

But the observed antiproton flux is *consistent* with the background expectation (from standard cosmic ray propagation in the Galaxy)

This is a serious constraint on *all* dark matter models of the *PAMELA* anomaly

Can fit with DM decay or annihilation only if DM particles are 'leptophilic' which is rather contrived

... In any case, most such models are now ruled out by *Fermi* [arXiv:1002.4415]



The 'background' is the production of secondary e^{\pm} during propagation (calculated using GALPROP)



However *e*[±] lose energy readily during propagation, so only *nearby* sources dominate at high energies ... the usual background calculation is then *irrelevant*



A nearby cosmic ray accelerator?

Rise in e^+ fraction could be due to secondaries being produced *during* acceleration ... which are then accelerated along with the primaries

(Blasi, PRL 103:051104,2009)

... generic feature of a *stochastic* acceleration process, if $\tau_{1\rightarrow 2} < \tau_{acc}$ (Cowsik 1979, Eichler 1979)

This component *naturally* has a harder spectrum and fits *PAMELA* data (adjusting 1 free parameter)



-39d30 17h11n 17h15

RXJ1713.7-3946, HESS





Propagation in Galaxy

Diffusive (1st-order Fermi) shock acceleration

Acceleration determined by compression ratio:

$$r = \frac{u_1}{u_2} = \frac{n_2}{n_1} , \quad \gamma = \frac{3r}{r-1}$$

Solve transport equation, $u\frac{\partial f}{\partial x} = D\frac{\partial^2 f}{\partial x^2} + \frac{1}{3}\frac{\mathrm{d}u}{\mathrm{d}x}p\frac{\partial f}{\partial p}$ $f \xrightarrow{x \to -\infty} f_{\mathrm{inj}}(p), \quad \left|\lim_{x \to \infty} f\right| \ll \infty$

Solution for x < 0:

$$f = f_{\rm inj}(p) + (f^0(p) - f_{\rm inj}(p))e^{-x \, u_1/D(p)}$$

where

$$f^{0}(p) = \gamma \int_{0}^{p} \frac{\mathrm{d}p'}{p'} \left(\frac{p'}{p}\right)^{\gamma} f_{\mathrm{inj}}(p') + Cp^{-\gamma}$$







DSA with secondary production

• Secondaries have same spectrum as primaries:

$$q_{e^{\pm}} \propto f_{CR} \propto p^{-\gamma}, \quad \gamma = \frac{3r}{r-1} \quad r = \frac{u_1}{u_2} = \frac{n_2}{n_1}$$

- Only particles with $|x| \lesssim D(p)/u$ are accelerated
- Bohm diffusion: $D(p) \propto p$
- Fraction of accelerated secondaries is $\,\propto p\,$
- Steady state spectrum

$$n_{e^{\pm}} \propto q_{e^{\pm}} \left(1 + \frac{p}{p_0} \right) \propto p^{-\gamma} + p^{-\gamma+1}$$

$$\Rightarrow rising \text{ positron fraction!}$$



Diffusion near shock front

r'i

- Diffusion coefficient not known *a priori* in neighbourhood of shock
- 'Bohm diffusion' sets a *lower* limit:

$$D^{\mathrm{Bohm}} = r_{\ell} \frac{c}{3} \propto \frac{E}{Z}$$

- Actual rate parametrised by 'fudge factor': $D = D^{\text{Bohm}} \mathcal{F}^{-1}$
- *F*⁻¹ determined by fitting to one secondary/primary ratio ... then can *predict* other ratios
- Can in principle determine diffusion rate from simulations (difficult!)

Inhomogeneity in the SNR distribution as the origin of the PAMELA anomaly

Shaviv, Nakar & Piran, PRL 103:111302,2009

<u>Idea:</u> Electrons from nearby SNRs cool above ~ 20 GeV (through synchrotron and inverse-Compton losses) before reaching us ... but protons do *not* cool, so secondary positron production is less affected \Rightarrow enhancement of e^+/e^-

But with usual propagation parameters $(D_0 \sim 10^{28} \text{ cm}^2 \text{ s}^{-1}, \delta \sim 0.6, \tau_{esc} \sim 10^{16} \text{ s})$ find break energy to be 2 TeV, *not* 20 GeV ... also nearby 'invisible' SNRs (e.g. *Geminga*) will fill in dips in the spectrum



Periodic

It is not just the few (optically) observed SNRs which contribute to observed cosmic rays ... there must be many other *bidden* SNRs (if there are ~3 SN/century and cosmic rays diffuse in Galaxy for ~10⁷ yr)

Known

Simulated



Ahlers, Mertsch & Sarkar, PRD80:123017,2009

Statistical distribution of SNRs





Parameters of the Monte Carlo

Diffusion Model									
	$10^{28}{ m cm}^2{ m s}^{-1}$ 0.6 3 kpc	$\left. \begin{array}{c} \ \ \ \ \ \ \ \ \ \ \ \ \ $							
b	$10^{-16}{\rm GeV^{-1}s^{-1}}$								
Source Distribution									
$t_{\rm max}$	$1 \times 10^8 \mathrm{yr}$	$P^{8} \mathrm{yr}$ from $E_{\mathrm{min}} \simeq 3.3 \mathrm{GeV}$							
$ au_{ m SNR}$	$10^4{ m yr}$	from observations							
N	3×10^6	from number of observed SNRs							
Source Model									
$R_{e^{-}}^{0}$	$1.8 \times 10^{50} {\rm GeV^{-1}}$	fit to e^- flux at $10 \mathrm{GeV}$							
Γ	2.4 average γ -ray spectral index								
$E_{\rm max}$	$20{ m TeV}$	20 TeV typical γ -ray maximum energy							
$E_{\rm cut}$	$20{ m TeV}$	DSA theory							
R^0_+	$7.4 \times 10^{48} {\rm GeV^{-1}}$	$\gamma ext{-rays}$							
$K_{\rm B}$	15	free parameter (for fixed Γ)							

Normalising the source spectra



Normalisation of primary e^- : fit absolute e^- flux at low energies

\mathbf{N} \mathbf{I} \mathbf{C} \mathbf{I} \mathbf{T} \mathbf{m} \mathbf{I}	\int	$\pi^0 + \dots$	\rightarrow	$2\gamma + \dots$
Normalisation of secondary $e^{\perp}: p + p$	\rightarrow $\left\{ \right.$	$\pi^{\pm} + \dots$	\rightarrow	$e^{\pm} + \dots$

Source	Other name(s)	Г	$J^{0}_{\gamma} \div 10^{-12}$	E_{\max}	d	$Q_{\gamma}^0 \div 10^{33}$
			$[(\mathrm{cm}^2\mathrm{s}\mathrm{TeV})^{-1}]$	[TeV]	[kpc]	$[(\mathrm{sTeV})^{-1}]$
HESS J0852-463	RX J0852.0-4622 (Vela Junior)	2.1 ± 0.1	21 ± 2	> 10	0.2	0.10
HESS J1442 -624	RCW 86, SN 185 (?)	2.54 ± 0.12	3.72 ± 0.50	$\gtrsim 20$	1	0.46
HESS J1713-381	CTB 37B, G348.7+0.3	2.65 ± 0.19	0.65 ± 0.11	$\gtrsim 15$	7	3.812
HESS J1713-397	RX J1713.7-3946, G347.3-0.5	2.04 ± 0.04	21.3 ± 0.5	17.9 ± 3.3	1	2.55
HESS J1714 -385	CTB 37A	2.30 ± 0.13	0.87 ± 0.1	$\gtrsim 12$	11.3	13.3
HESS $J1731 - 347$	G 353.6-07	2.26 ± 0.10	6.1 ± 0.8	$\gtrsim 80$	3.2	7.48
HESS J1801 -233^{a}	W 28, GRO J1801-2320	2.66 ± 0.27	0.75 ± 0.11	$\gtrsim 4$	2	0.359
HESS J1804 -216^{b}	W 30, G8.7-0.1	2.72 ± 0.06	5.74	$\gtrsim 10$	6	24.73
HESS J1834 -087	W 41, G23.3-0.3	2.45 ± 0.16	2.63	$\gtrsim 3$	5	7.87
MAGIC J0616+225	IC 443	3.1 ± 0.3	0.58	$\gtrsim 1$	1.5	0.156
Cassiopeia A		2.4 ± 0.2	1.0 ± 0.1	$\gtrsim 40$	3.4	1.38
J0632 + 057	Monoceros	2.53 ± 0.26	0.91 ± 0.17	N/A	1.6	0.279
Mean	~ 2.5		$\gtrsim 20$		~ 5.2	
Mean, excluding sour	~ 2.4		$\gtrsim 20$		~ 5.7	
Mean, excluding sour	~ 2.3		$\gtrsim 20$		~ 4.2	

Fitting the $e^+ + e^-$ flux



The propagated primary $e^$ spectrum is much too *steep* to match the Fermi LAT data ... but the *accelerated* secondary $e^+ + e^-$ component has a harder spectrum so fits the 'bump'!



The predicted positron fraction



Nearby pulsars as source of e^{\pm}

- Highly magnetized, fast spinning neutron stars
- $\cdot \gamma$ -rays and electron/ positron pairs produced along the magnetic axis
- Spectrum *speculated* to be harder than background from propagation:

$$N \propto E_e^{\pm -1.6} e^{-E_e^{\pm}/100 \,\text{GeV}}$$



Combination of Galactic contribution and two nearby pulsars, Geminga (157 pc) and B0656+14 (290 pc), *can* fit *PAMELA* excess (and perhaps also *Fermi* bump)



Hooper, Blasi & Serpico, JCAP 0901:025,2009

However ~40% of rotational energy must be released as energetic e^+ – plausible? *Fermi* can detect expected anisotropy towards B0656+14 in ~5 years

What about the antiproton-to-proton ratio?

Blasi & Serpico, PRL 103:081103,2009



Secondary acceleration model predicts rise *beyon∂* 100 GeV ... will be tested soon by *AMS-*02

Nuclear secondary-to-primary Ratios

Dark matter✗Pulsars✗Acceleration of
secondaries (TBD)

If we see this, *both* dark matter and pulsar origin models would be ruled out! Since nuclei are accelerated in the *same* sources, the ratio of secondaries (e.g. Li, Be, B) to primaries (C, N, O) must also *rise* with energy beyond ~100 GeV



Can solve problem analytically ... but more complicated than for \bar{p}/p since energy losses must now be included

$$\Box \text{ Transport equation: } u \frac{\partial f_i}{\partial x} = D_i \frac{\partial^2 f_i}{\partial x^2} + \frac{1}{3} \frac{du}{dx} p \frac{\partial f_i}{\partial p} - \Gamma_i f_i + q_i$$

with boundary condition: $f_i(x,p) \xrightarrow{x \to -\infty} Y_i \delta(p-p_0)$

Solution:
$$f_i^+ = f_i^0 + \frac{q_i^+(x=0) - \Gamma_i^+ f_i^0}{u_+} x \text{ for } x > 0$$

$$f_{i}^{0}(p) = \int_{0}^{p} \frac{\mathrm{d}p'}{p'} \left(\frac{p'}{p}\right)^{\gamma} \mathrm{e}^{-\gamma(1+r^{2})(D_{i}^{-}(p)-D_{i}^{-}(p'))\Gamma_{i}^{-}/u_{-}^{2}}$$
$$\times \gamma \left[(1+r^{2}) \frac{D_{i}^{-}(p')q_{i}^{-}(x=0)}{u_{-}^{2}} + Y_{i}\delta(p'-p_{0}) \right]$$
$$\sim ``q_{i}^{-}(p) + D_{i}^{-}(p)q_{i}^{-}(p)''$$

Mertsch & Sarkar, PRL 103:081104,2009

Titanium-to-Iron Ratio



Titanium-to-iron ratio used to fix diffusion coefficient to be $\mathcal{F}^{-1} \simeq 40$ (NB: to fit e^+ excess requires ~10-20)

Mertsch & Sarkar, PRL 103:081104,2009



We can then predict another secondary/primary ratio e.g. B/C ...

... a *rise* would establish the nearby hadronic accelerator model

Have some of these old SNRs been seen already?



Galactic Longitude (deg)

A definitive test would be to detect neutrinos from these old SNRs ...



 5σ detection by *IceCube* in 3 yr!

Summary

Astroparticle physics has made enormous *experimental* progress but to definitively answer old questions e.g. the **origin of cosmic rays** or the **nature of dark matter** will require better *theoretical* modelling of the relevant astrophysical 'backgrounds'

The *PAMELA* anomaly may be the signature of a nearby *ba∂ronic* accelerator rather than dark matter - forthcoming data on antiprotons & B/C ratio (*AMS-02, PEBS*) will provide a resolution

... the source(s) should also be detectable directly in γ-rays (*HAWC*, *CTA*) and neutrinos (*IceCube*, *KM3NeT*)

This would be the first identification of cosmic 'pevatrons'