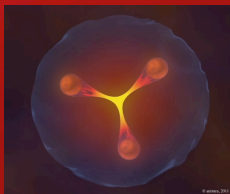
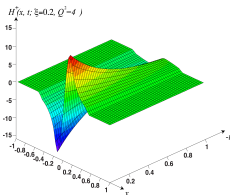
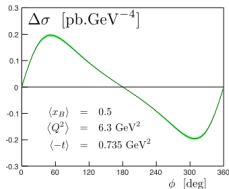
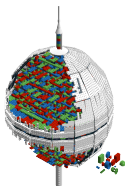


DE LA RECHERCHE À L'INDUSTRIE



www.cea.fr

Global Analysis of Generalized Parton Distribution Data: Tools and Strategy



SPhN Scientific Council | Hervé MOUTARDE

May 23rd, 2014

PARTONS project

- Correlation of the **longitudinal momentum** and the **transverse position** of a parton in the nucleon.
- Deeply Virtual Compton Scattering (DVCS) recognized as the theoretically cleanest channel to access GPDs.

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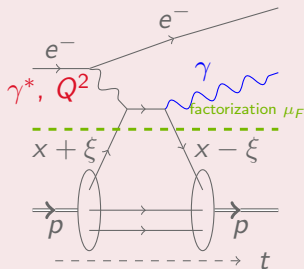
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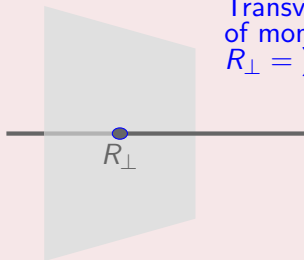
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Transverse center of momentum R_{\perp}

$$R_{\perp} = \sum_i x_i r_{\perp i}$$



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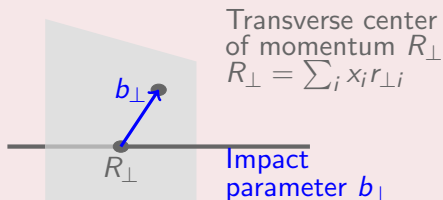
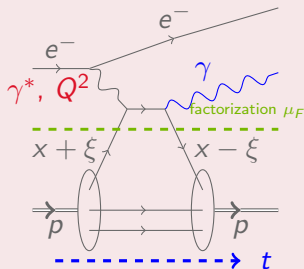
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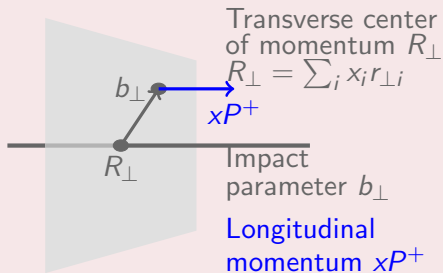
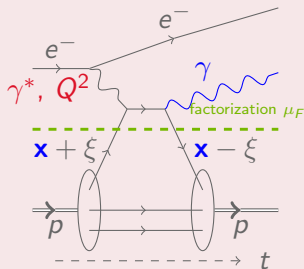
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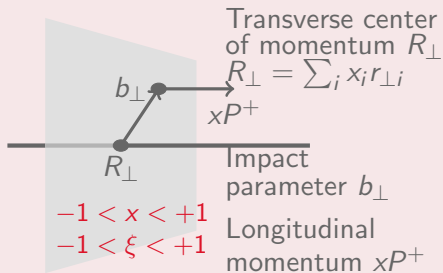
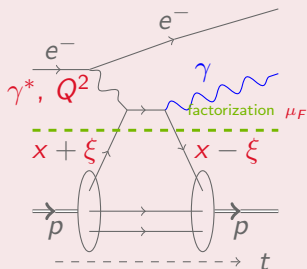
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- GPD $F^i(x, \xi, t, \mu_F)$ for each parton type $i = g, u, d, \dots$

PARTONS
project

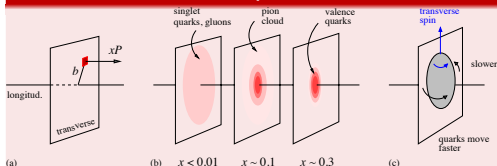
- **Probabilistic interpretation** of Fourier transform of $\text{GPD}(x, \xi = 0, t)$ in **transverse plane**.

$$\rho(x, b_{\perp}, \lambda, \lambda_N) = \frac{1}{2} \left[H(x, 0, b_{\perp}^2) + \frac{b_{\perp}^j \epsilon_{ji} S_{\perp}^i}{M} \frac{\partial E}{\partial b_{\perp}^2}(x, 0, b_{\perp}^2) + \lambda \lambda_N \tilde{H}(x, 0, b_{\perp}^2) \right]$$

- Notations : quark helicity λ , nucleon longitudinal polarization λ_N and nucleon transverse spin S_{\perp} .

Burkardt, Phys. Rev. **D62**, 071503 (2000)

Can we obtain this picture from exclusive measurements?



Weiss, AIP Conf. Proc. **1149**, 150 (2009)

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- Most general structure of matrix element of energy momentum tensor between nucleon states:

$$\left\langle N, P + \frac{\Delta}{2} \left| T^{\mu\nu} \right| N, P - \frac{\Delta}{2} \right\rangle = \bar{u} \left(P + \frac{\Delta}{2} \right) \left[A(t) \gamma^{(\mu} P^{\nu)} + B(t) P^{(\mu} i \sigma^{\nu)\lambda} \frac{\Delta_\lambda}{2M} + \frac{C(t)}{M} (\Delta^\mu \Delta^\nu - \Delta^2 \eta^{\mu\nu}) \right] u \left(P - \frac{\Delta}{2} \right)$$

with $t = \Delta^2$.

- Key observation: **link between GPDs and gravitational form factors**

$$\int dx x H^q(x, \xi, t) = A^q(t) + 4\xi^2 C^q(t)$$

$$\int dx x E^q(x, \xi, t) = B^q(t) - 4\xi^2 C^q(t)$$

Ji, Phys. Rev. Lett. **78**, 610 (1997)

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■ Spin sum rule:

$$\int dx x (H^q(x, \xi, 0) + E^q(x, \xi, 0)) = A^q(0) + B^q(0) = 2J^q$$

Ji, Phys. Rev. Lett. **78**, 610 (1997)

■ **Shear** and **pressure** of the nucleon considered as a continuous medium:

$$\langle N | T^{ij}(\vec{r}) | N \rangle = s(r) \left(\frac{r^i r^j}{\vec{r}^2} - \frac{1}{3} \delta^{ij} \right) + p(r) \delta^{ij}$$

Polyakov and Shuvaev, hep-ph/0207153

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1 Study of exclusive processes

2 Metrology of Generalized Parton Distributions

3 Understanding of QCD dynamics through GPD modeling

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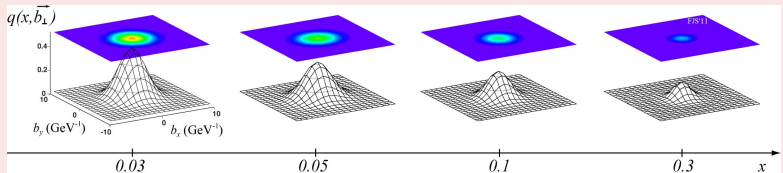
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What do we learn from this picture?

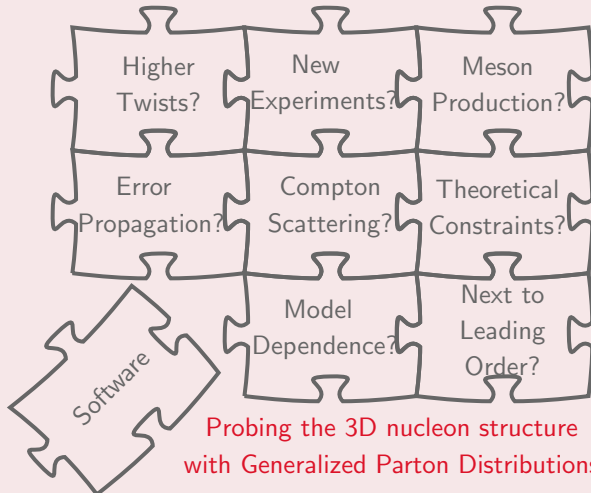


Anatomy of the nucleon.

Three generic motivations for the study of parton correlations.

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Common tools for different technical questions.



Probing the 3D nucleon structure
with Generalized Parton Distributions

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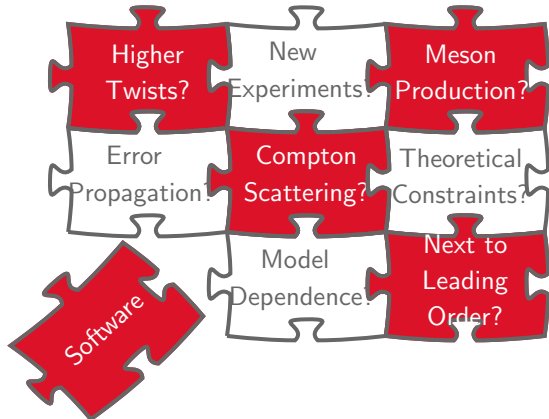
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Study of exclusive processes



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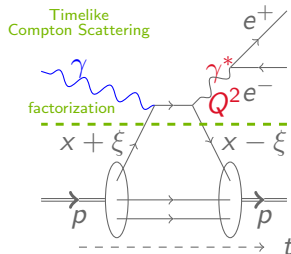
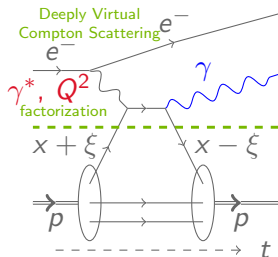
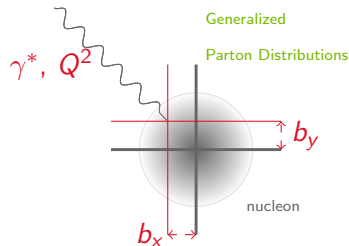
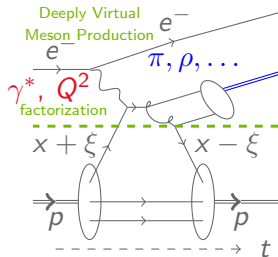
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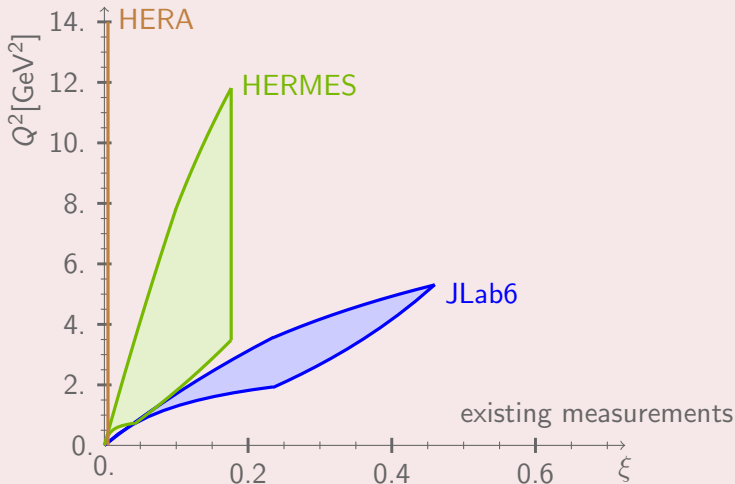
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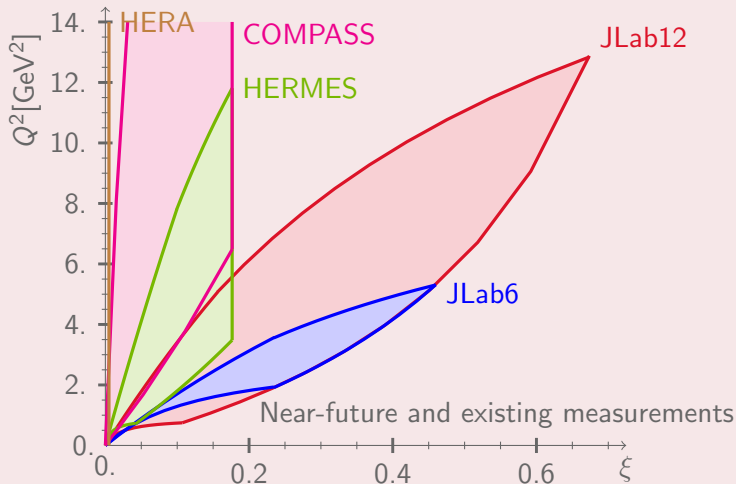
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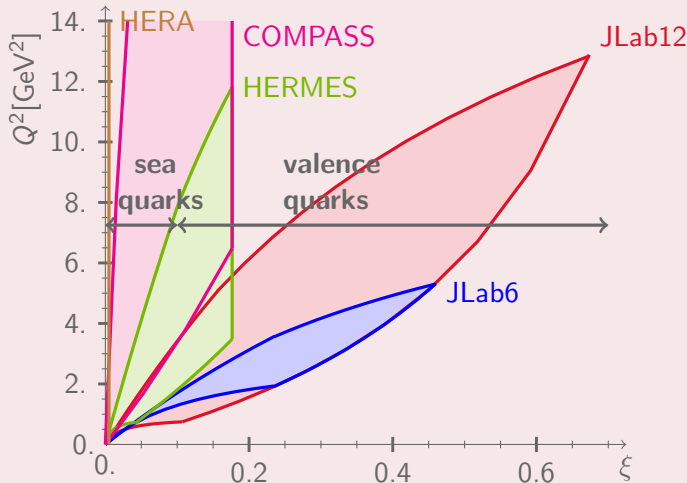
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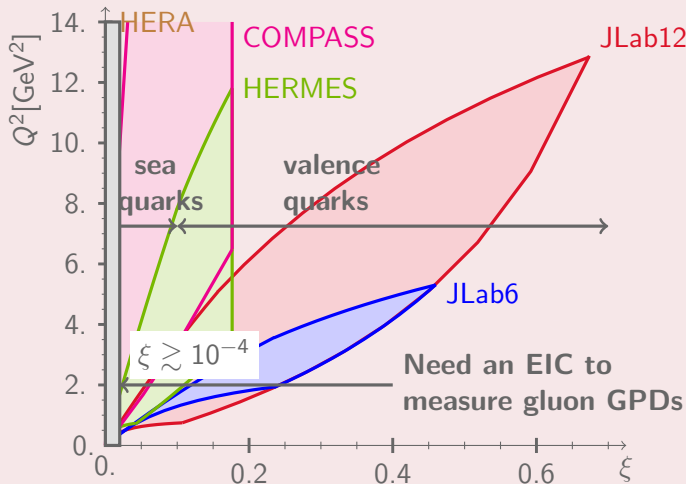
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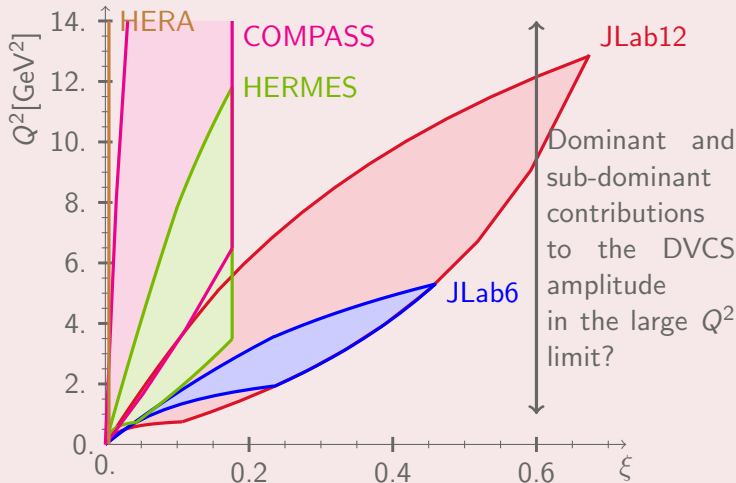
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A DVMP-based model vs DVCS data.

Are the GPDs extracted from DVMP and DVCS really the same?

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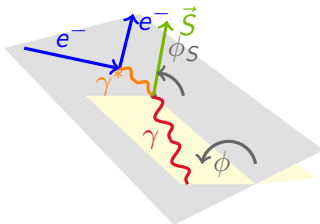
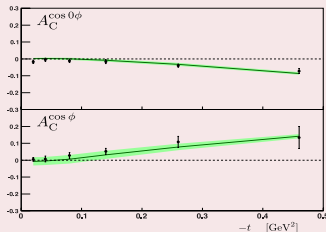
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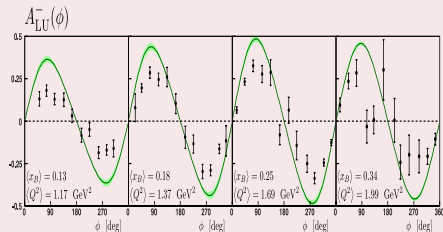
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Beam charge asymmetry HERMES



Beam spin asymmetry CLAS



First universality check

- No model parameter was tuned to analyse DVCS.
- Comparison to all DVCS data.

Kroll et al.

Eur. Phys. J. **C73**, 2278 (2013)

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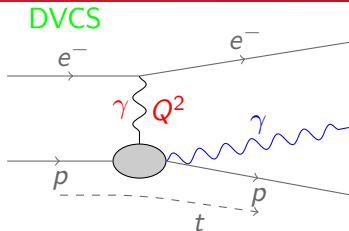
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Compton Form Factors (CFF)

- Parametrize amplitudes.

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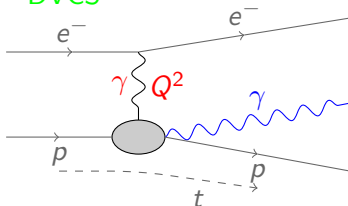
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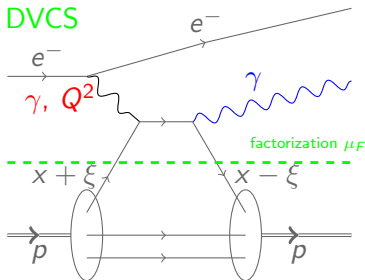
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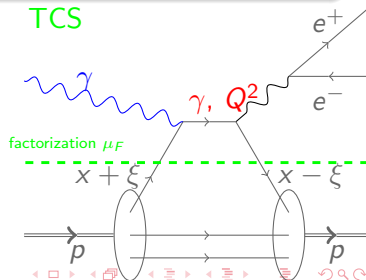
Compton Form Factors (CFF)

- Parametrize amplitudes.
- Evaluation at LO.

DVCS



TCS



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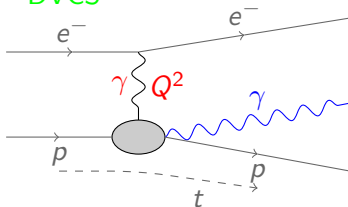
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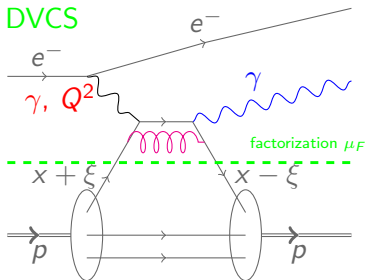
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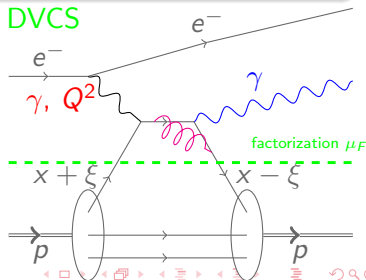
Compton Form Factors (CFF)

- Parametrize amplitudes.
- Evaluation at LO.
- Evaluation at **NLO**.

DVCS



DVCS



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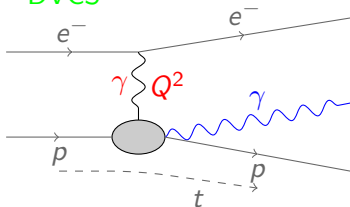
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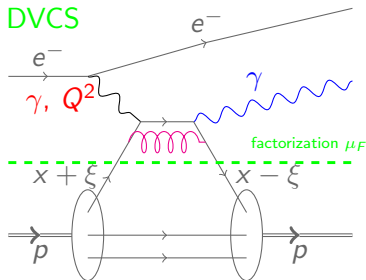
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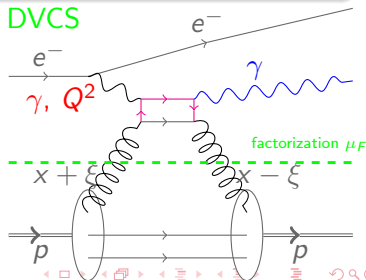
Compton Form Factors (CFF)

- Parametrize amplitudes.
- Evaluation at LO.
- Evaluation at **NLO**.
- Other diagrams at NLO, including **gluon GPDs**.

DVCS



DVCS

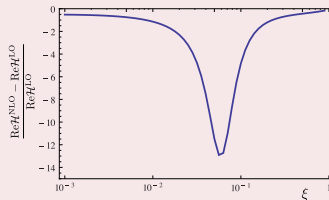
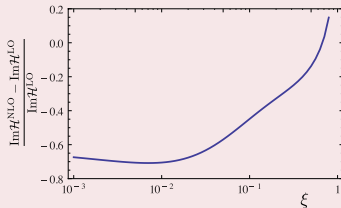
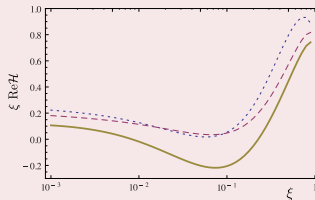
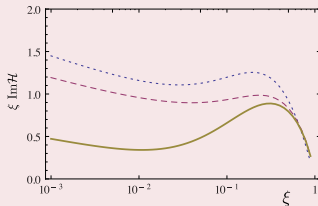


Spacelike CFF \mathcal{H} : large NLO contribution.

Mostly due to gluons, maximum in HERMES / COMPASS kinematic region.

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project

$Re\mathcal{H}$ at LO and NLO ($t = -0.1 \text{ GeV}^2$, $Q^2 = \mu_F^2 = 4. \text{ GeV}^2$)



Moutarde *et al.* , Phys. Rev. **D87**, 054029 (2013)

dotted: LO dashed: NLO quark corrections solid: full NLO

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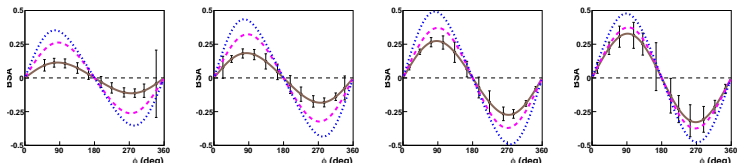
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Preliminary result



dotted: LO dashed: NLO quark corrections solid: full NLO

■ Comparison with KG model.

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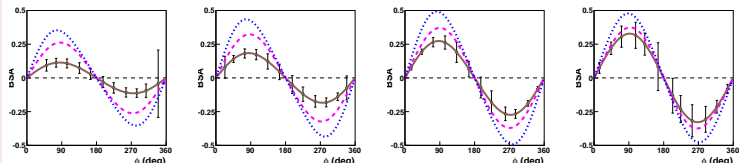
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dotted: LO dashed: NLO quark corrections solid: full NLO

- Comparison with KG model.
- Compare differences between LO and NLO computations to **experimental statistical uncertainty** considering full NLO computation as nominal result.

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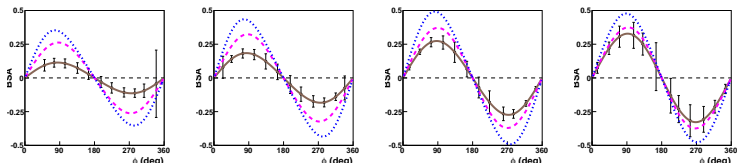
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Preliminary result



dotted: LO dashed: NLO quark corrections solid: full NLO

- Comparison with KG model.
- Compare differences between LO and NLO computations to **experimental statistical uncertainty** considering full NLO computation as nominal result.
- Need resummed expressions!

Altinoluk *et al.*, JHEP **1210**, 049 (2012)

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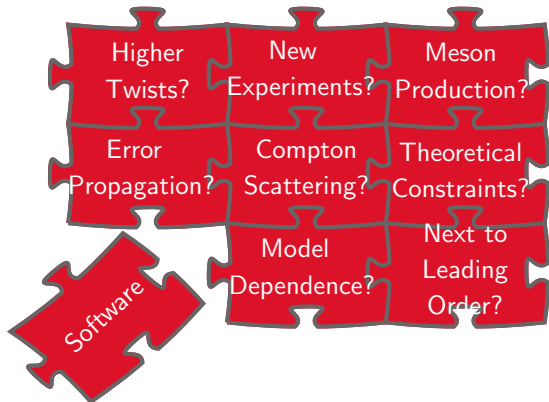
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Metrology of Generalized Parton Distributions



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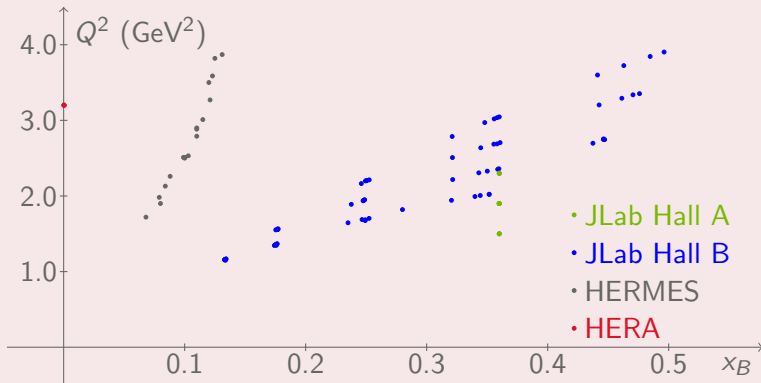
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What is large Q^2 ?



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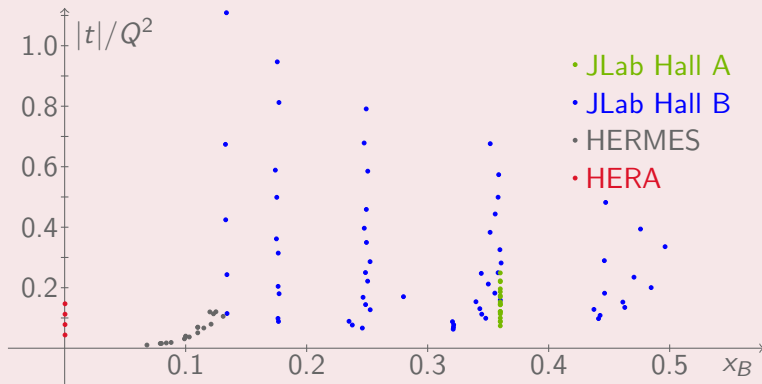
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What is large Q^2 ?



■ Q^2 is **not so large** for most of the data.

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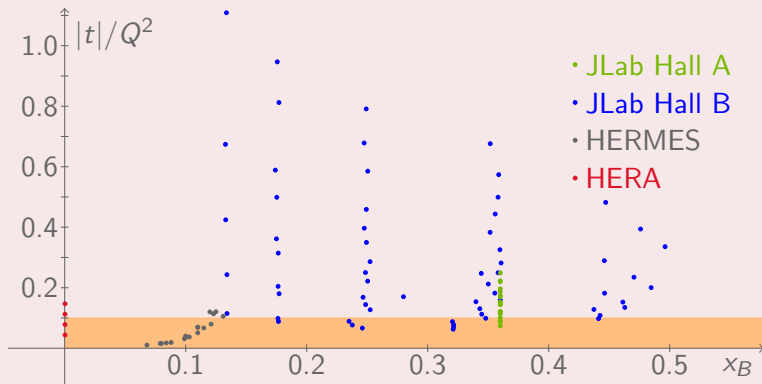
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What is large Q^2 ?



- Q^2 is **not so large** for most of the data.
- **Higher twists**, finite- t and target mass corrections?

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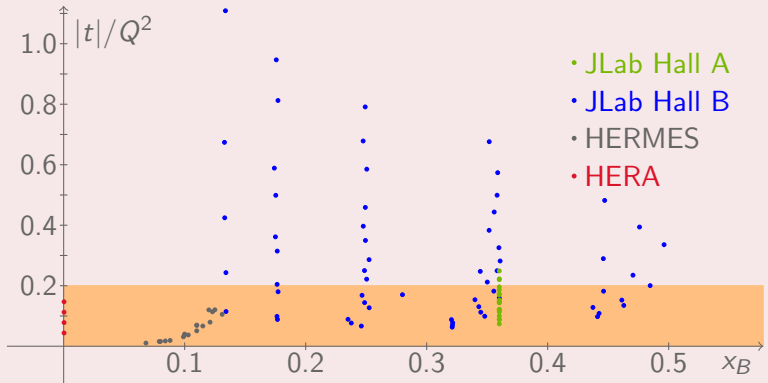
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What is large Q^2 ?



- Q^2 is **not so large** for most of the data.
- **Higher twists**, finite- t and target mass corrections?
- **Consistent modeling** of GPDs beyond leading twist?

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Local fits

Take each kinematic bin independantly of the others.
Extraction of $Re\mathcal{H}$, $Im\mathcal{H}$, ... as independent parameters.

Global fit

Take all kinematic bins at the same time. Use a parametrization of GPDs or CFFs.

Hybrid : Local / global fit

Start from local fits and add smoothness assumption.

Neural networks

Exploratory stage for GPDs.

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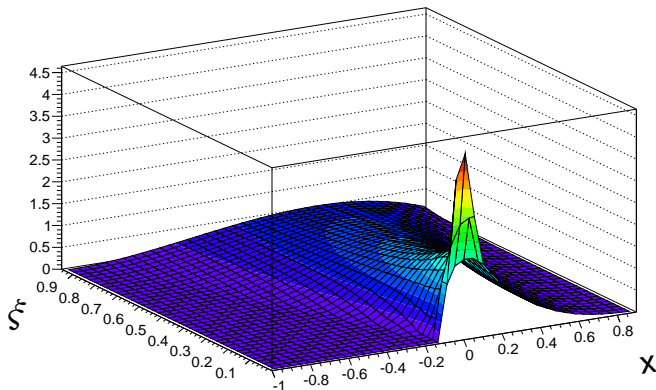
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Conclusions

- **Dominance** of twist 2 and **validity** of a GPD analysis of DVCS data.
- *ImH* **best determined**. Large uncertainties on *ReH*.
- However sizable **higher twist contamination** for DVCS measurements.
- Already some indications about the **invalidity** of the *H*-dominance hypothesis with **unpolarized data**.

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GPD H at $t = -0.23 \text{ GeV}^2$ and $Q^2 = 2.3 \text{ GeV}^2$.



GPD model: see Kroll *et al.* , Eur. Phys. J. **C73**, 2278 (2013)

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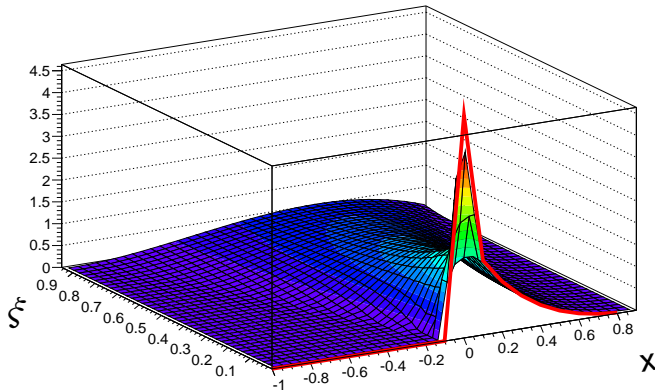
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Need to know $H(x, \xi = 0, t)$ to do transverse plane imaging.



GPD model: see Kroll *et al.* , Eur. Phys. J. **C73**, 2278 (2013)

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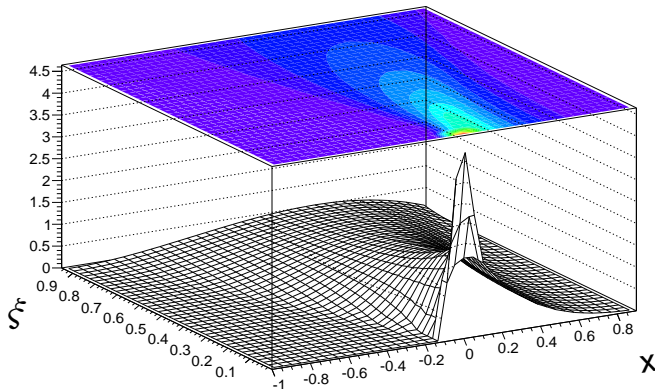
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What is the physical region?



GPD model: see Kroll *et al.* , Eur. Phys. J. **C73**, 2278 (2013)

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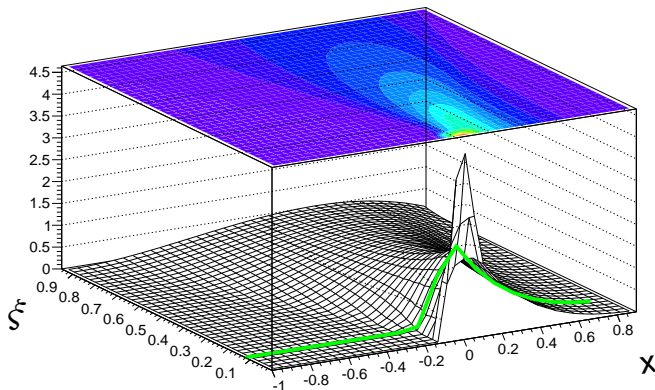
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ξ_{\min} from finite beam energy.



GPD model: see Kroll *et al.* , Eur. Phys. J. **C73**, 2278 (2013)

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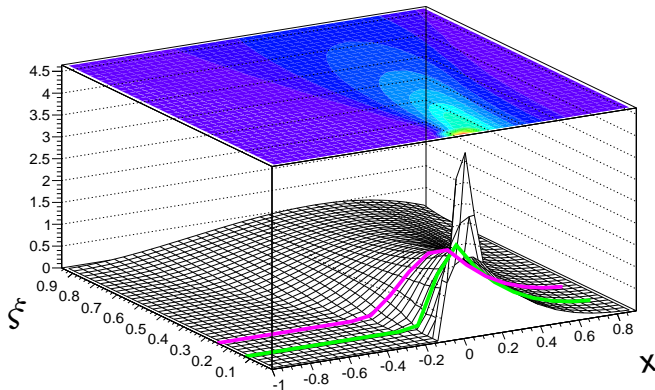
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ξ_{\max} from kinematic constraint on 4-momentum transfer.



GPD model: see Kroll *et al.* , Eur. Phys. J. **C73**, 2278 (2013)

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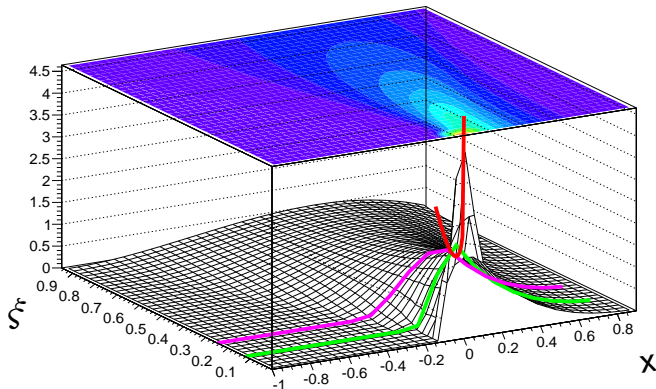
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The cross-over line $x = \xi$.



GPD model: see Kroll *et al.* , Eur. Phys. J. **C73**, 2278 (2013)

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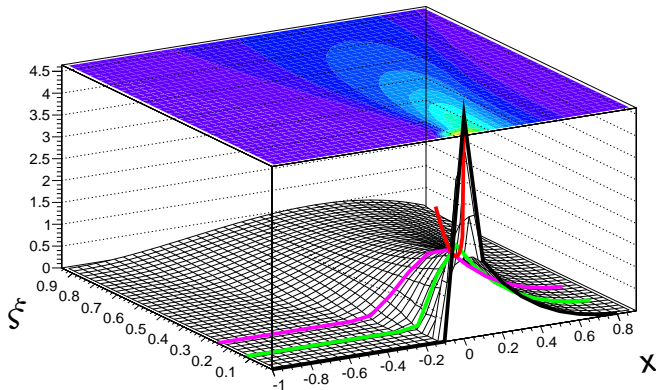
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The black curve is what is needed for transverse plane imaging!



GPD model: see Kroll *et al.* , Eur. Phys. J. **C73**, 2278 (2013)

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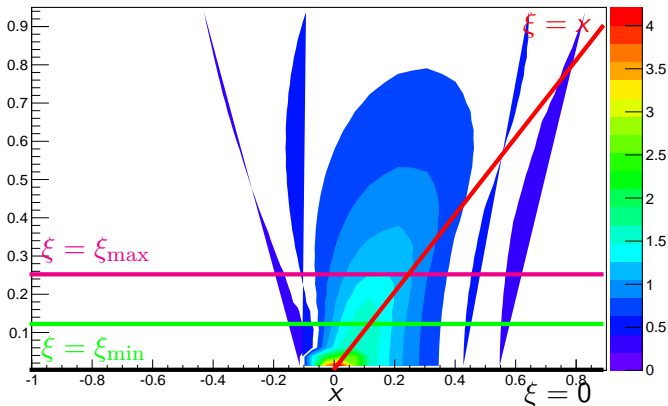
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Density plot of H at $t = -0.23 \text{ GeV}^2$ and $Q^2 = 2.3 \text{ GeV}^2$



GPD model: see Kroll *et al.* , Eur. Phys. J. **C73**, 2278 (2013)

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- Systematic and statistical errors **added in quadrature**.
No distinction yet between different experiments.
- Evaluation of model-dependence:
 - Local fits: **almost model-independent** but low interpretation capability.
 - Global fits: test parameterization and extracting strategy on **pseudo-data generated from models in database**.
- Opportunities: neural networks, bayesian analysis?
- **Programming to an interface**: existing C++ software already allows transparent change of GPD models.
- **Code refactoring** (design patterns) to incorporate proper GPD evolution.
- Planned: scripts for **systematic studies** e.g. impact of a given dataset on J^u , etc.

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- **All-order proof of factorization** of DVCS amplitude.
Collins and Freund, Phys. Rev. **D59**, 074009 (1999)
- Hard scattering kernel computed at **next-to-leading order** at leading twist.
Belitsky and Müller, Phys. Lett. **B417**, 129 (1998)
- Evolution equations computed at **next-to-leading order**.
Belitsky *et al.* , Nucl. Phys. **B574**, 347 (2000)
and ref. therein
- Finite- t and target mass corrections computed at **leading order**: kinematic power corrections to **twist 4 accuracy**.
Braun *et al.* , Phys. Rev. Lett. **109**, 242001 (2012)

GPD fitting: 3 to 4 active teams worldwide

- Theory status **does play in favor of** "GPD being the most attractive sector in the study of nucleon structure".

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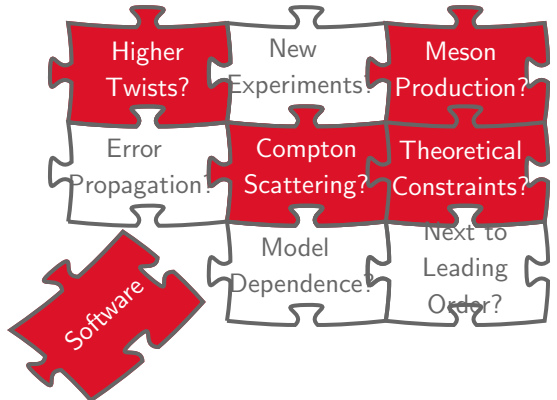
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GPD "measurements" ?

- **Already achieved**: experimentally constrained models.
- Next steps: **Measured** transverse plane images and information on **nonperturbative QCD**?

Understanding of QCD dynamics through GPD modeling

Understanding of QCD dynamics through GPD modeling



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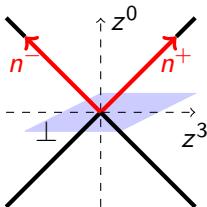
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$$\begin{aligned}
 F^q &= \frac{1}{2} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle p' | \bar{q} \left(-\frac{z}{2} \right) \gamma^+ q \left(\frac{z}{2} \right) | p \rangle_{z^+=0, z_\perp=0} \\
 &= \frac{1}{2P^+} \left[H^q \bar{u}(p') \gamma^+ u(p) + E^q \bar{u}(p') \frac{i\sigma^{+\alpha} \Delta_\alpha}{2M} u(p) \right] \\
 \tilde{F}^q &= \frac{1}{2} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle p' | \bar{q} \left(-\frac{z}{2} \right) \gamma^+ \gamma_5 q \left(\frac{z}{2} \right) | p \rangle_{z^+=0, z_\perp=0} \\
 &= \frac{1}{2P^+} \left[\tilde{H}^q \bar{u}(p') \gamma^+ \gamma_5 u(p) + \tilde{E}^q \bar{u}(p') \frac{\gamma^5 \Delta^+}{2M} u(p) \right]
 \end{aligned}$$



References

- Müller *et al.*, Fortschr. Phys. **42**, 101 (1994)
 Ji, Phys. Rev. Lett. **78**, 610 (1997)
 Radyushkin, Phys. Lett. **B380**, 417 (1996)

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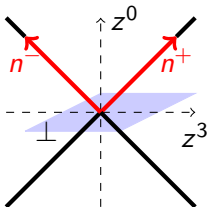
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 &= \frac{1}{2P^+} \left[\textcolor{red}{H}^q \bar{u}(p') \gamma^+ u(p) + \textcolor{red}{E}^q \bar{u}(p') \frac{i\sigma^{+\alpha} \Delta_\alpha}{2M} u(p) \right] \\
 \tilde{F}^q &= \frac{1}{2} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle p' | \bar{q} \left(-\frac{z}{2} \right) \gamma^+ \gamma_5 q \left(\frac{z}{2} \right) | p \rangle_{z^+=0, z_\perp=0} \\
 &= \frac{1}{2P^+} \left[\tilde{\textcolor{red}{H}}^q \bar{u}(p') \gamma^+ \gamma_5 u(p) + \tilde{\textcolor{red}{E}}^q \bar{u}(p') \frac{\gamma^5 \Delta^+}{2M} u(p) \right]
 \end{aligned}$$



8 GPDs per parton type at twist 2

- Partons with a **light-like** separation.
- **Quarks, gluon** and **transversity** GPDs.
- $\text{GPD}^{q,g} = \text{GPD}^{q,g}(x, \xi, t, \mu_F)$.

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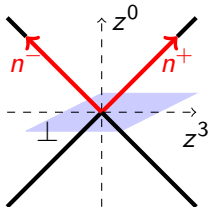
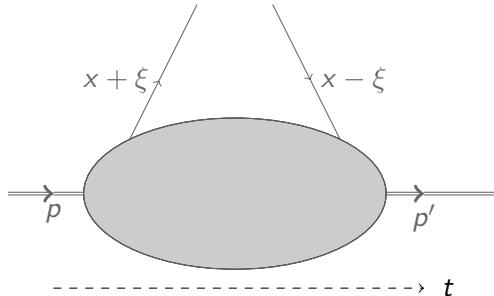
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Interpretation

- $x \in [\xi, 1]$: q emitted + q absorbed.
- $x \in [-\xi, +\xi]$: \bar{q} emitted + q absorbed.
- $x \in [-1, -\xi]$: \bar{q} emitted + \bar{q} absorbed.

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■ PDF forward limit

$$H^q(x, 0, 0) = q(x)$$

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- PDF forward limit
- Form factor sum rule

$$\int_{-1}^{+1} dx H^q(x\xi, t) = F_1^q(t)$$

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- PDF **forward limit**
- Form factor **sum rule**
- **Polynomiality**

$$\int_{-1}^{+1} dx x^n H^q(x, \xi, t) = \text{polynomial in } \xi$$

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- PDF forward limit
- Form factor sum rule
- Polynomiality
- Positivity

$$H^q(x, \xi, t) \leq \sqrt{q\left(\frac{x+\xi}{1+\xi}\right) q\left(\frac{x-\xi}{1-\xi}\right)}$$

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- PDF **forward limit**
- Form factor **sum rule**
- **Polynomiality**
- **Positivity**
- H^q is an **even function** of ξ from time-reversal invariance.

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- **Polynomiality**
- **Positivity**
- H^q is an **even function** of ξ from time-reversal invariance.
- H^q is **real** from hermiticity and time-reversal invariance.

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- H^q has support $x \in [-1, +1]$.

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- PDF **forward limit**
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- H^q is an **even function** of ξ from time-reversal invariance.
- H^q is **real** from hermiticity and time-reversal invariance.
- H^q has support $x \in [-1, +1]$.
- **Soft pion theorem** (pion target)

$$H^{I=1}(x, \xi = 1, t = 0) = \phi_\pi \left(\frac{1+x}{2} \right)$$

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- **Soft pion theorem** (pion target)

Numerous theoretical constraints on GPDs.

- There is no known GPD parameterization **relying only on first principles**.
- Modeling becomes a key issue.

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- **Factorized Ansatz.** For $i = g, \text{ sea or val}$:

$$H_i(x, \xi, t) = \int_{|\alpha|+|\beta|\leq 1} d\beta d\alpha \delta(\beta + \xi\alpha - x) f_i(\beta, \alpha, t)$$

$$f_i(\beta, \alpha, t) = e^{b_i t} \frac{1}{|\beta|^{\alpha' t}} h_i(\beta) \pi_{n_i}(\beta, \alpha)$$

$$\pi_{n_i}(\beta, \alpha) = \frac{\Gamma(2n_i + 2)}{2^{2n_i+1} \Gamma^2(n_i + 1)} \frac{(1 - |\beta|)^2 - \alpha^2}{(1 - |\beta|)^{2n_i+1}}^{n_i}$$

- Expressions for h_i and n_i :

$$h_g(\beta) = |\beta| g(|\beta|) \quad n_g = 2$$

$$h_{\text{sea}}^q(\beta) = q_{\text{sea}}(|\beta|) \text{sign}(\beta) \quad n_{\text{sea}} = 2$$

$$h_{\text{val}}^q(\beta) = q_{\text{val}}(\beta) \Theta(\beta) \quad n_{\text{val}} = 1$$

- Designed to study DVMP. Recently applied to DVCS.

Goloskokov and Kroll, Eur. Phys. J. **C42**, 281 (2005)

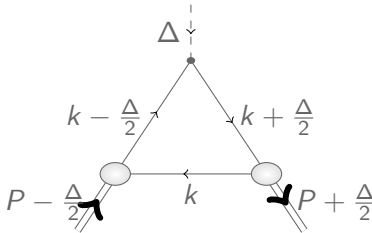
Kroll *et al.*, Eur. Phys. J. **C73**, 2278 (2013)

Mezrag *et al.*, Phys. Rev. **D88**, 014001 (2013)

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$$\langle x^m \rangle^q = \frac{1}{2(P^+)^{n+1}} \left\langle \pi, P + \frac{\Delta}{2} \left| \bar{q}(0) \gamma^+ (i \overleftrightarrow{D})^m q(0) \right| \pi, P - \frac{\Delta}{2} \right\rangle$$

- Compute **Mellin moments** of the pion GPD H .



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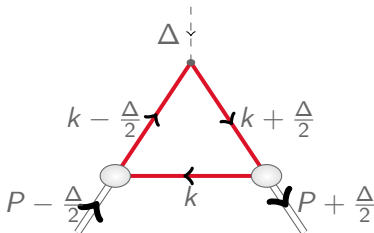
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- Compute **Mellin moments** of the pion GPD H .
- Resum **infinitely many** contributions.

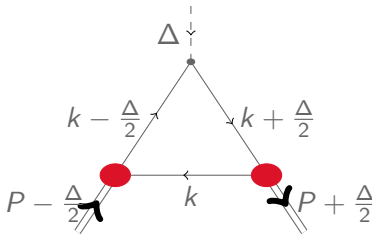


Dyson - Schwinger equation

$$\left(\text{---} \bigcirc \text{---} \right)^{-1} = \left(\text{---} \right)^{-1} + \text{---} \text{---} \bigcirc \text{---} \text{---}$$

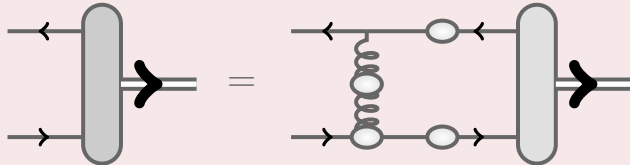
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$$\langle x^m \rangle^q = \frac{1}{2(P^+)^{n+1}} \left\langle \pi, P + \frac{\Delta}{2} \left| \bar{q}(0) \gamma^+ (i \overleftrightarrow{D}^+)^m q(0) \right| \pi, P - \frac{\Delta}{2} \right\rangle$$



- Compute **Mellin moments** of the pion GPD H .
- Resum **infinitely many** contributions.

Bethe - Salpeter equation



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$$\langle x^m \rangle^q = \frac{1}{2(P^+)^{n+1}} \left\langle \pi, P + \frac{\Delta}{2} \left| \bar{q}(0) \gamma^+ (i \overleftrightarrow{D})^m q(0) \right| \pi, P - \frac{\Delta}{2} \right\rangle$$

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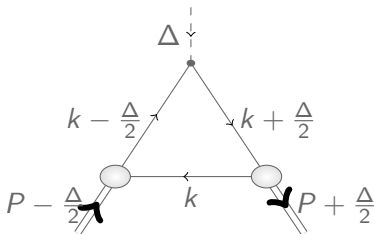
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- Compute **Mellin moments** of the pion GPD H .
- Resum **infinitely many** contributions.
- **Nonperturbative** modeling.

- Most GPD properties **satisfied by construction**.

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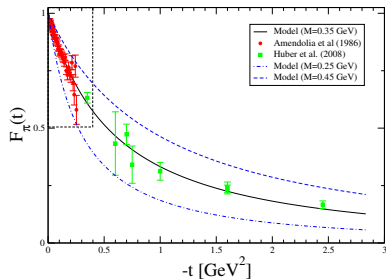
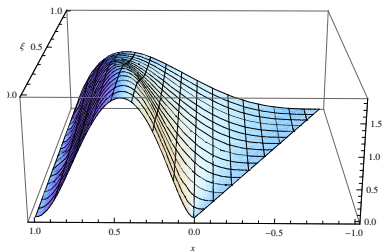
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Mezrag et al. , in preparation.

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- Helicity amplitude $\gamma_L^* N(p) \rightarrow V_L N(p')$ (small- t limit):

- Modified Perturbative Approach (MPA) result:

$$\mathcal{Im} \mathcal{M}_{V,\{0+,0+\}}^g = - \int_0^1 dy \int d^2 \underline{r} \sum_f C_V^f \left(\hat{\Psi}_V(y, -\underline{r}) \hat{\Psi}_{\gamma_L^*}^f(y, \underline{r}) \right) \times \left(\frac{\pi \sqrt{2\pi}}{N_c y \bar{y}} \alpha_s \frac{H^g(\xi, \xi, 0)}{2\xi} \right)$$

Besse, *in preparation*.

- k_T -factorization and dipole models result:

$$\mathcal{Im} \mathcal{M}_{V,\{0+,0+\}}^g = - \int_0^1 dy \int d^2 \underline{r} \sum_f C_V^f \left(\hat{\Psi}_V(y, -\underline{r}) \hat{\Psi}_{\gamma_L^*}^f(y, \underline{r}) \right) \times \left(\frac{s \hat{\sigma}(x, \underline{r})}{2\sqrt{2\pi}} \right)$$

Besse *et al.*, Nucl. Phys. **B867**, 19 (2013)

- Identify terms:

$$\hat{\sigma}(x, \underline{r}) \leftrightarrow \frac{\pi^2}{N_c} \left(\frac{4}{y \bar{y} Q^2} \right) \alpha_s H^g(\xi, \xi, 0) = \frac{\pi^2}{N_c} r_0^2 \alpha_s H^g(\xi, \xi, 0)$$

$$\text{with } r_0^2 = \frac{4}{y \bar{y} Q^2}$$

Summary

PARTONS project



French National Research Agency
ANR grant: 2012-16
P.I.: Irfu/SPhN

Introduction

Exclusive processes

- Factorization
- Kinematic reach of DVCS
- Universality tests
- Beyond leading order

GPD metrology

- Data selection
- Fitting strategies
- Modeling issues

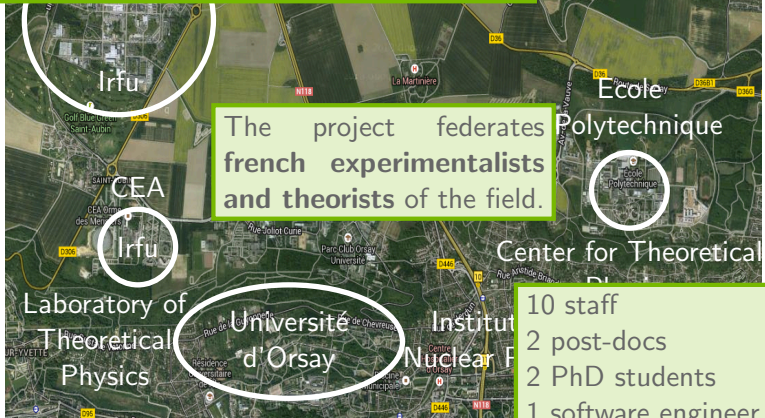
GPD modeling

- Formalism
- Models

Summary

PARTONS

Conclusions



PARTONS: PARTonic Tomography Of Nucleon Software.

Collaborations at the national and international levels.

PARTONS project

Joint work in progress

Experimental data analysis
New experiment design (e.g. JLab Hall C)
World data fits
GPD modeling
Perturbative QCD expertise

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Conclusions

Database

- World experimental data.
- Theoretical predictions.

Visualizing software

- 3D nucleon imaging.
- Measurements vs model expectations.

Interactive web site

- Free access to models and measurements.
- Popularization.

Design and performance

- **Uncertainties**
propagation: statistical and systematic.
- **Fitting** engine.
- **Versatility**: comprehensive studies varying models and approximations.
- **Reliability** and **speed**:
0.1 % numerical accuracy,
 \simeq 50 times faster than
Mathematica (achieved on
existing parts).

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PARTONS

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- Last decade demonstrated **relevance of GPD measurements**.
- **New facilities** will explore new kinematic ranges or provide challenging constraints for phenomenology.
- Field **mature for phenomenology**.
- **Get ready** for phenomenological analysis of forthcoming CLAS and COMPASS data.
- Need for **QCD-inspired models** to make progress.
- **Numerous results** on GPD phenomenology.
- Project **rescheduling** due to work in new directions:
 - DVMP software (originally end of project).
 - GPD modeling in Dyson - Schwinger approach.
- **Software package** expected to be ready for use in 2016.

