

IRFU PHD STUDENT SEMINAR

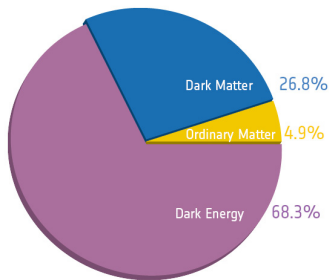
**A fast stochastic approach for cosmological constraints  
using weak-lensing peak counts**

Chieh-An Lin, Martin Kilbinger

SAP, CEA Saclay

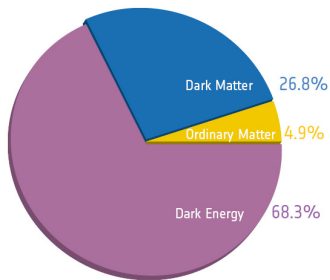
Irfu, CEA Saclay — July 2<sup>nd</sup>, 2015

# Context

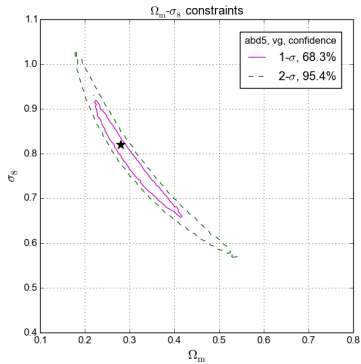


(Source: Planck)

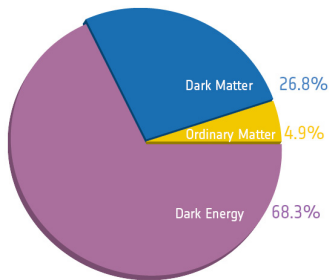
# Context



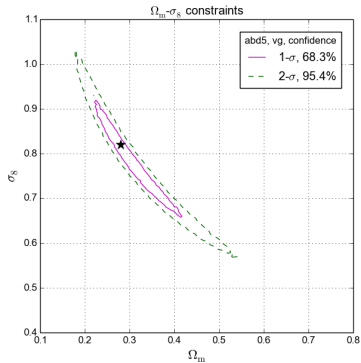
(Source: Planck)



## Context



(Source: Planck)



To constrain cosmological parameters

# Outline

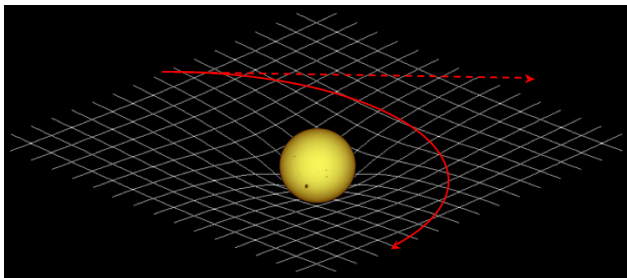
- 1 What is weak lensing?
- 2 Peak counts from weak lensing
- 3 Our model
- 4 Results
- 5 Perspectives and summary

# Outline

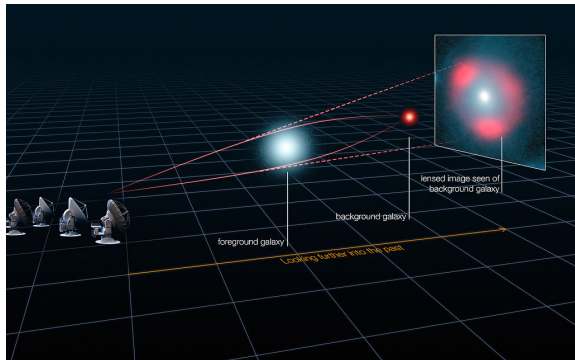
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# What is weak lensing?

Light deflection in general relativity



# What is weak lensing?



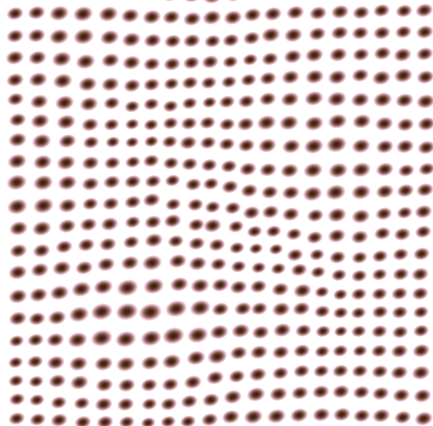
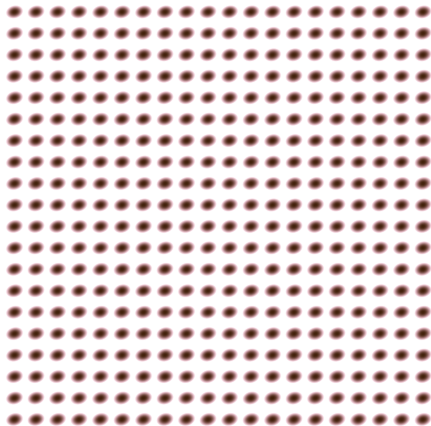
## Strong lensing: Einstein ring

(Source: ALMA, ESA-Hubble, NASA)



# What is weak lensing?

## Weak lensing

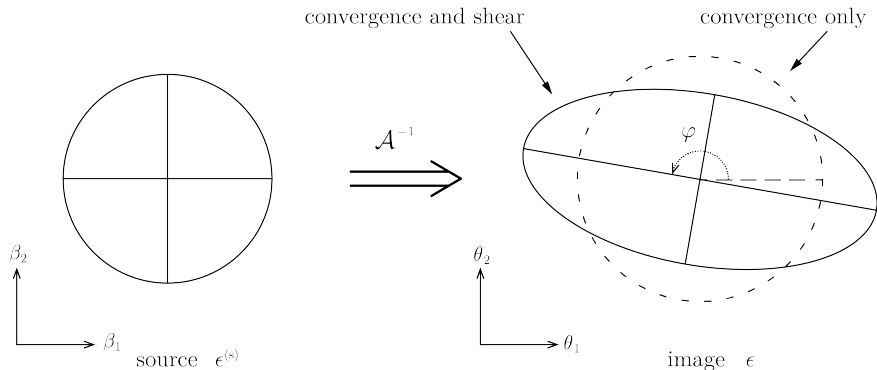


# What is weak lensing?

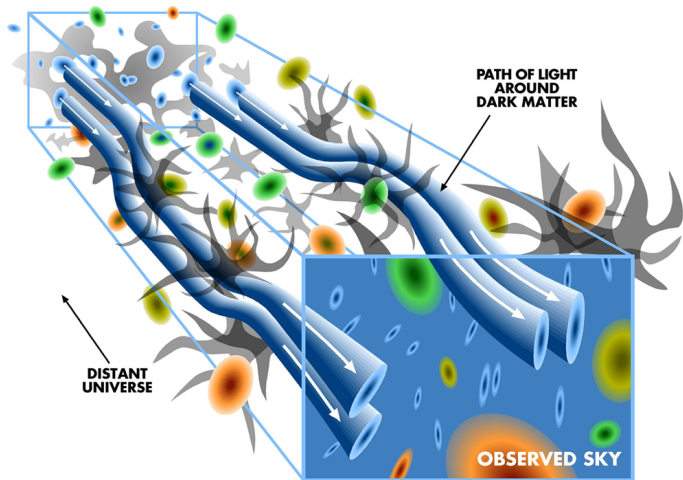
$$\mathcal{A}(\boldsymbol{\theta}) = \begin{pmatrix} 1 - \kappa - \gamma_1 & -\gamma_2 \\ -\gamma_2 & 1 - \kappa + \gamma_1 \end{pmatrix}$$

$\kappa$ : convergence, “projected mass density”

$\gamma = \gamma_1 + i\gamma_2$ : cosmic shear, distortion



# What is weak lensing?

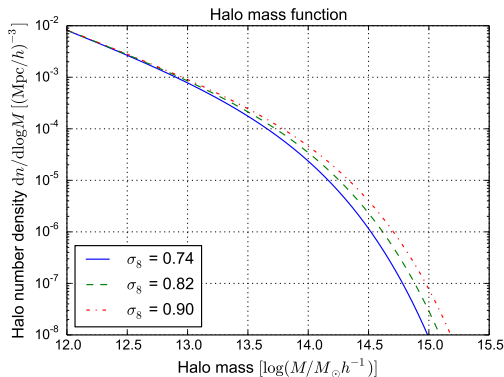
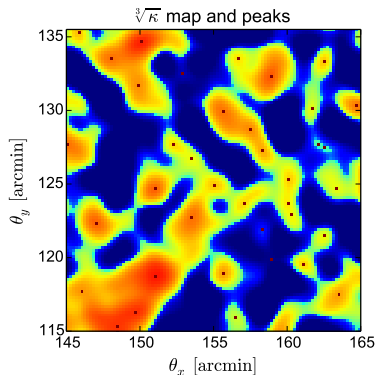


(Source: LSST)

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# Peak counts from weak lensing



- Local maxima of the projected mass
- Direct tracers of massive regions
- Probe mass function

# Peak counts from weak lensing

Peak counts are part of higher-order statistics, complementary to Gaussian information

## Peak-count modeling

- Analytical models
- $N$ -body simulations
- Fast stochastic methods (this talk)

## Difficulties

- Observational effects: photo- $z$ , masks, and others
- Additional features: intrinsic alignment, baryonic effects

## Challenges

How to predict weak-lensing peak counts in realistic conditions?

How to extract cosmological information from peaks?

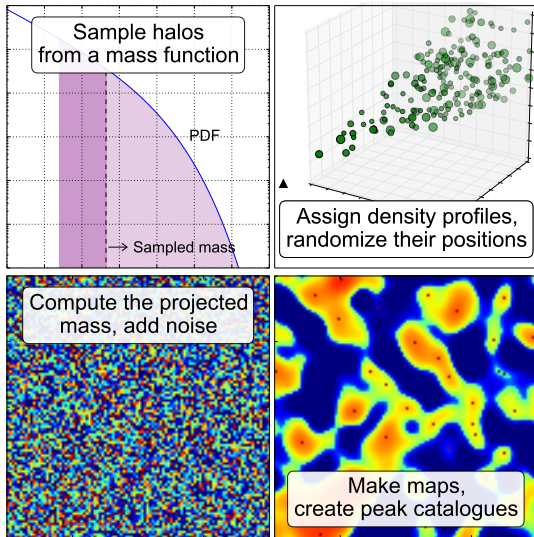
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# Our model

A fast stochastic forward model (See Lin & Kilbinger 2015a, A&A, 576, A24 for details)



# Our model

## Hypotheses

- Diffuse, unbound matter does not significantly contribute to peak counts
- Spatial correlation of halos has a minor influence

## Public code



# CAMELUS

Counts of Amplified Mass Elevations  
from Lensing with Ultrafast Simulation

<http://www.cosmostat.org/software/camelus/>

# Advantages

Fast

Flexible

Full PDF information

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## Fast

Only few seconds for creating a 25-deg<sup>2</sup> field, without MPI or GPU programming

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Straightforward to include observational effects (e.g. photo- $z$  errors, masks) and additional features (e.g. intrinsic alignment, baryonic effects)

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## Full PDF information

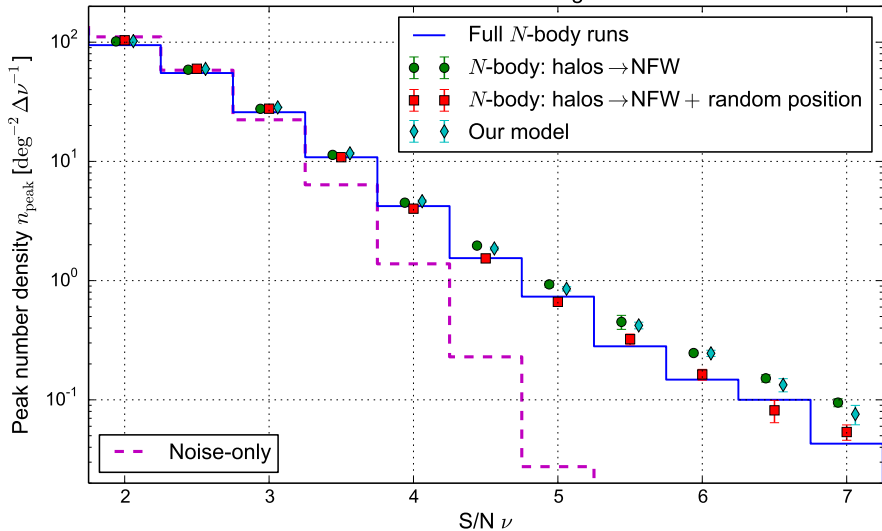
Free from the Gaussian likelihood assumption, allow more flexible constraint methods (copula, varying covariances,  $p$ -value evaluation, approximate Bayesian computation, etc.)

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## Validation

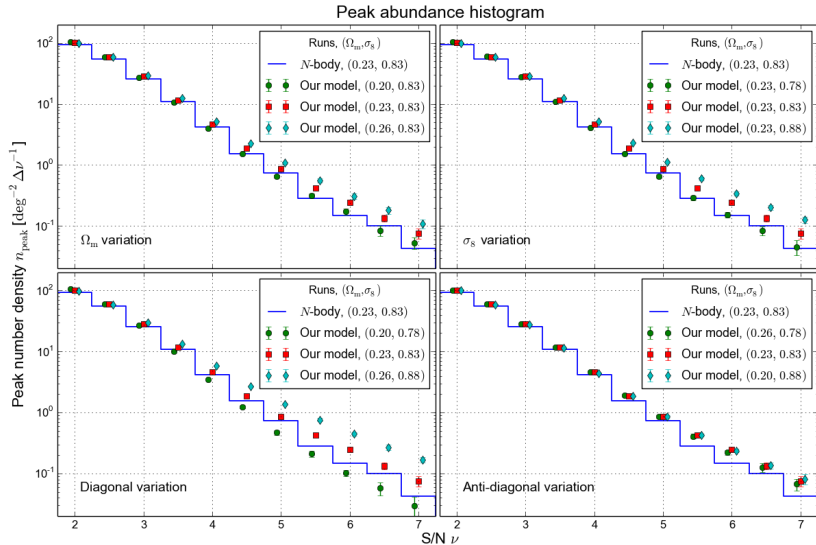
Peak abundance histogram



Lin &amp; Kilbinger (2015a)

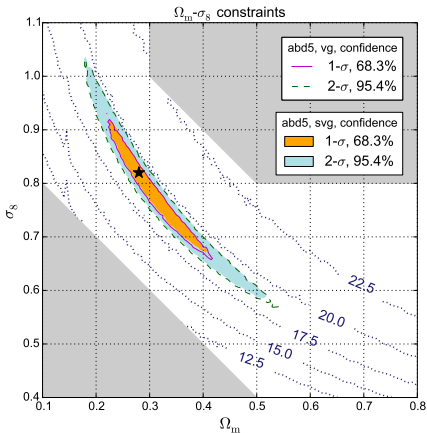
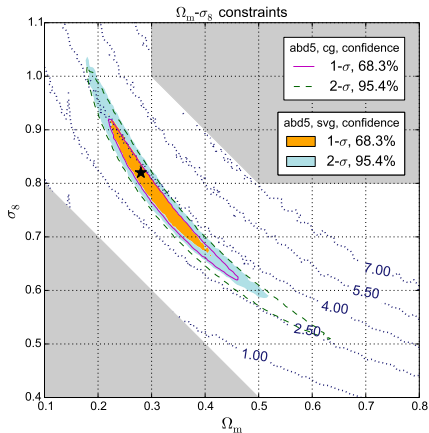


# Dependance on parameters



Lin &amp; Kilbinger (2015a)

# Cosmology-dependent covariances

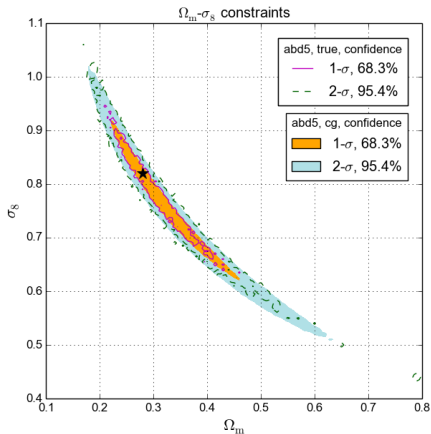


cg = constant covariance (lines, left panel)  
 svg = semi-varying covariance (colored zones)  
 vg = varying covariance (lines, right panel)

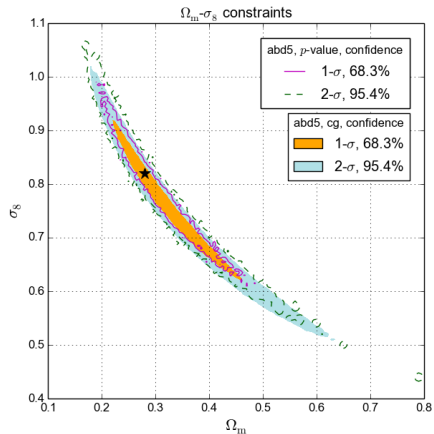
	cg	svg	vg
FoM	46	57	56

Lin & Kilbinger (2015b)

# Non-analytical constraints



With the true likelihood



With  $p$ -value

Lin & Kilbinger (2015b)

# Approximate Bayesian computation

Approximate Bayesian computation (ABC) is an efficient technique which provides constraints by bypassing likelihood estimation.

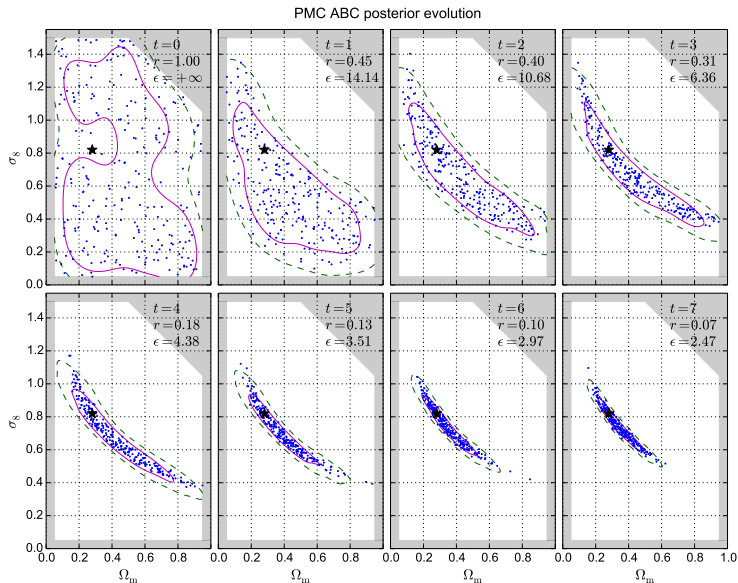
This is an accept-reject process which samples directly under an approximate posterior.

## Requirements

- Stochastic model
- Suitable data vector
- Metric

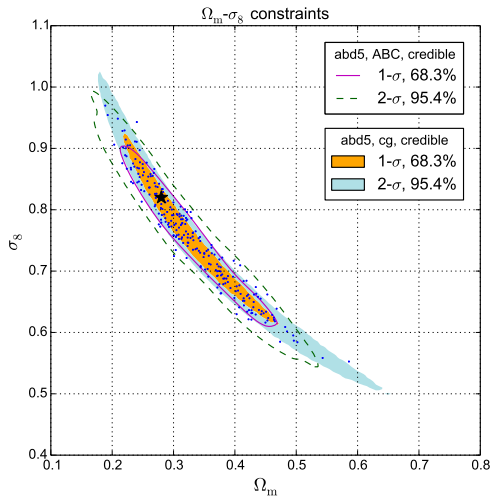
This is combined with the population Monte Carlo technique (PMC), a time series solution for accelerating the algorithm.

# Approximate Bayesian computation



Lin &amp; Kilbinger (2015b)

# Approximate Bayesian computation



Very good agreement

Time comparison:

- Likelihood  $\approx 8000 \times 1000$  simulations to run
- ABC  $\approx 250 \times 1 \times 100$  simulations to run

Lin & Kilbinger (2015b)

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# Future works

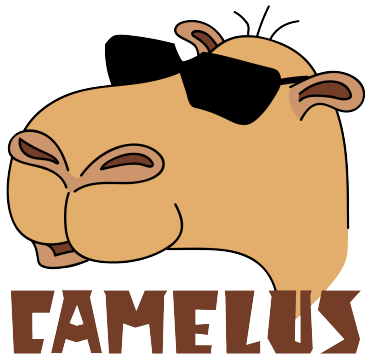
- Peak extraction from nonlinear filters
- Intrinsic ellipticity alignment
- Baryonic effects
- Tomography studies
- Application to CFHTLenS data



# Summary

- A fast stochastic model for WL peak counts
- Fast, flexible, full PDF information
- A robust and efficient constraining method: ABC

Thank you for your attention



<http://www.cosmostat.org/software/camelus/>

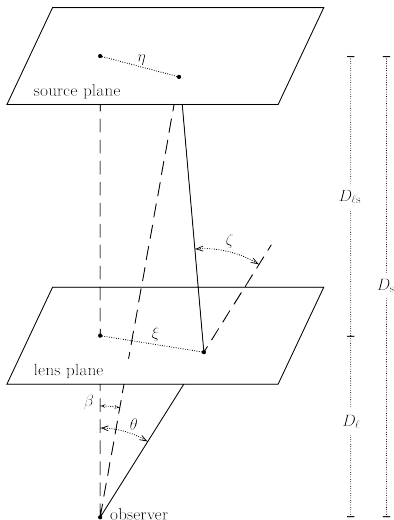
<http://linc.tw/>

**Backup slides**

# Born approximation

$$\mathcal{A}_{ij}(\boldsymbol{\theta}) = \delta_{ij} - \frac{2}{c^2} \int_0^w dw' \frac{f_K(w-w')f_K(w')}{f_K(w)} \\ \times \phi_{,ij}(f_K(w')\boldsymbol{\theta}, w')$$

$$\kappa(\boldsymbol{\theta}, w) = \frac{3H_0^2\Omega_m}{2c^2} \int_0^w dw' \frac{f_K(w-w')f_K(w')}{f_K(w)} \\ \times \frac{\delta(f_K(w')\boldsymbol{\theta}, w')}{a(w')}$$

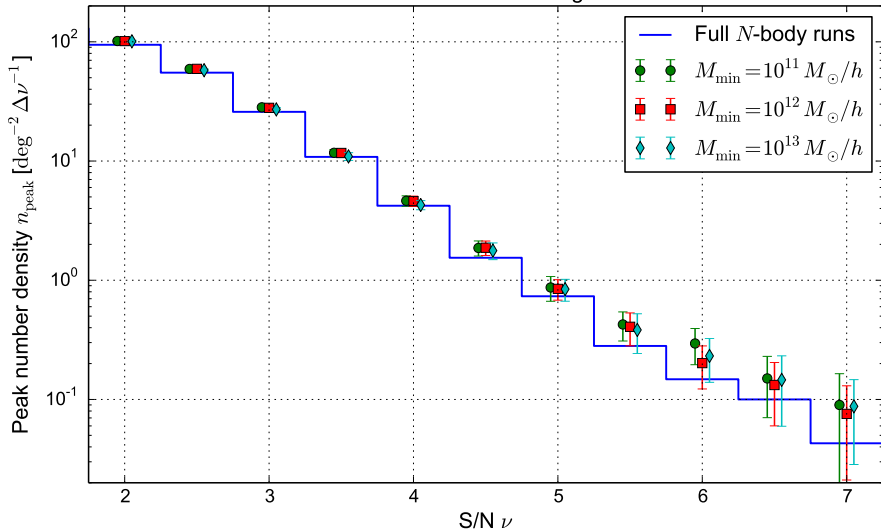


# Settings

- Fixed source redshift  $z_s = 1.0$
- Galaxy number density  $n_g = 25 \text{ arcmin}^{-2}$
- Pixel size  $\theta_{\text{pix}} = 0.2 \text{ arcmin}$
- Uncorrelated Gaussian shape noise, no IA
- Smoothing radius  $\theta_G = 1 \text{ arcmin}$

# Our model is not sensitive to $M_{\min}$

Peak abundance histogram



# Approximate Bayesian computation

## Steps

- Sample parameters  $\pi_i$  from the prior
- For each  $\pi_i$ , generate one  $x_i$  from the model
- Accept  $\pi_i$  if  $|x_i - x^{\text{obs}}| \leq \epsilon$ , reject it otherwise
- Reconstruct the posterior from accepted  $\pi_i$

# Approximate Bayesian computation

ABC's accept-reject process is actually a sampling under  $P_\epsilon$  (green curve):

$$P_\epsilon(\pi|x^{\text{obs}}) = A_\epsilon(\pi)P(\pi),$$

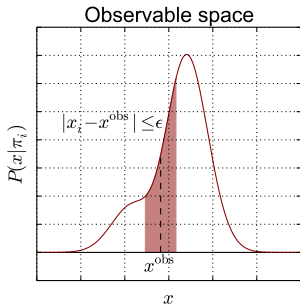
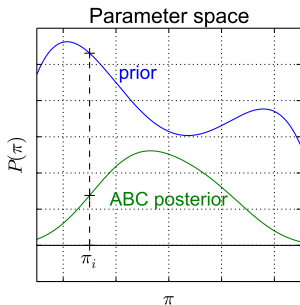
where  $P(\pi)$  stands for the prior (blue curve) and

$$A_\epsilon(\pi) \equiv \int dx P(x|\pi) \mathbb{1}_{|x-x^{\text{obs}}| \leq \epsilon}(x),$$

is the accept probability under  $\pi$  (red area). One can see that

$$\lim_{\epsilon \rightarrow 0} A_\epsilon(\pi_0)/\epsilon = P(x^{\text{obs}}|\pi_0) = \mathcal{L}(\pi_0),$$

so  $P_\epsilon$  is proportional to the true posterior when  $\epsilon \rightarrow 0$ .





# Publications

## Refereed papers

- **Lin C.-A.**, Umetsu K., Kilbinger M., & Coupon J. (2015). In preparation.
- **Lin C.-A.** & Kilbinger M. (2015b). *A new model to predict weak-lensing peak counts II. Parameter constraint strategies*. Submitted to A&A.
- **Lin C.-A.** & Kilbinger M. (2015a). *A new model to predict weak-lensing peak counts I. Comparison with  $N$ -body simulations*. A&A, 576, A24.

## Proceeding

- **Lin C.-A.** & Kilbinger M. *A New Model to Predict Weak Lensing Peak Counts*. Statistical Challenges in 21st Century Cosmology, Lisbon, May 2014.

## Talks

- IAP Seminar Series, Paris, to be determined.
- IAS Seminar Series, Orsay, France, Jan 2015.
- ASIAA Seminar Series, Taipei, Jan 2015.
- International Workshop on Cosmology and Sparsity 2, Nice, Sep 2014.
- Euclid Consortium Meeting, Marseille, May 2014.
- DIM-ACAV Colloquium, Paris, Oct 2013.

## Posters

- Theoretical and Observational Progress on Large-scale Structure of the Universe, Garching, Germany, Jul 2015.
- Statistical Challenges in 21st Century Cosmology, Lisbon, May 2014.

# Experiences

## Education

- 2012-2013: MSc in high energy physics, École Polytechnique, Palaiseau, France.
- 2009-2013: Diplôme d'ingénieur, École Polytechnique.
- 2007-2009: Classe préparatoire aux grandes écoles, Lycée Louis le Grand, Paris.
- Until 2007: Secondary education in Taichung, Taiwan.

## Teaching

- Teaching assistant, Introduction to Quantum Mechanics, spring 2015, École Polytechnique.
- High school project supervisor, Matière noire, fall 2014.
- Teaching assistant, Nonlinear Optics MOOC, since fall 2014, École Polytechnique.
- Teaching assistant, Quantum Mechanics and Statistical Physics, spring 2013, École Polytechnique.
- High school level tutor, 2009-2010, Collège Saint-François, France.

## Outreach & Miscellaneous

- PhD student representative for the Laboratory Council of SAP/AIM.
- Lin C.-A. (2015). *Popular Astrophysics from Interstellar*. Taiwan Natural Science, 125, 84.
- Popular science animator, 2013-2014, Palais de la découverte, Paris.
- Volunteer educator, 2009-2010, Collège Saint-François, France.