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# Critical Current Characterization under Pure Bending Strains of Pre-bent Cu-Nb/Nb<sub>3</sub>Sn Strands for Practical React-and-Wind Process

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- Nb-rod-method Cu-Nb reinforced Nb<sub>3</sub>Sn (Cu-Nb/Nb<sub>3</sub>Sn) wires have been successfully developed for commercialization of the React-and-Wind (R&W) processed Nb<sub>3</sub>Sn coils. Superconducting performance of the Cu-Nb/Nb<sub>3</sub>Sn wires are improved by applying the pre-bending treatment at room temperature, because of releasing the residual stress of Nb<sub>3</sub>Sn filaments (pre-bending strain effects).
- The purpose of this study is to obtain information of the efficient use of the pre-bending strain effects for optimizing critical current ( $I_c$ ) characteristics under pure bending strain on the R&W coil design.
- The Cu-Nb/Nb<sub>3</sub>Sn strands of diameter 0.8 mm were heat-treated at 670 °C for 96 hours on stainless steel grooved cylindrical holders of different radii 10.1-32.1 mm. After the half of the reacted strands were applied repeating pre-bending strain  $\pm 0.5\%$ , each of the pre-bent strands and as-reacted (without pre-bent) strands was transferred to a Ti-6Al-4V alloy grooved cylindrical holder of radius 15.6 mm, and those  $I_c$  measurements were carried out under applied pure bending strains range from -0.9% to +0.84% at 11-17 T, 4.2 K.
- As a result, the pre-bent strand showed no deterioration of  $I_c$  in the applied pure bending strain of range of +0.5% from -0.5% and had larger  $I_c$  than that of as-reacted strand at no pure-bending strain. In this paper, the  $I_c$  enhancements of the pre-bent Cu-Nb/Nb<sub>3</sub>Sn strands under pure bending strains are analyzed by using the  $I_c$  characteristics under axial strains.

# Nb-rod-method Cu-Nb/Nb<sub>3</sub>Sn strands

## Advantage of Nb-rod-method Cu-Nb reinforced Nb<sub>3</sub>Sn strand

- ✓ Mass productivity is superior to In-situ-method.
- ✓ Design of the equivalent diameter of Nb-rod, the placement, the volume ratio for control of the properties.
- ✓ High  $I_c$  characteristics under the large axial tensile stress
- ✓ High RRR, because impurities are not easily incorporated into the Cu matrix.

TABLE I MAIN PARAMETERS OF CU-NB/NB<sub>3</sub>SN STRANDS

Items	Unit	Parameter
Superconductor	-	Bronze- processed Nb <sub>3</sub> Sn
Reinforcement	-	Nb-rod-method Cu-20vol%Nb
Bronze	-	Cu-14wt%Sn-0.2wt%Ti
Sn diffusion barrier	-	Ta
Filament diameter	μm	3.3
Diameter	mm	0.80
Filament region dia.	mm	0.51
Volume fraction Cu / Cu-Nb / non-Cu (Ta)	%	18 / 37 / 45(5)
Twist pitch /direction	mm	24 / Left hand helix

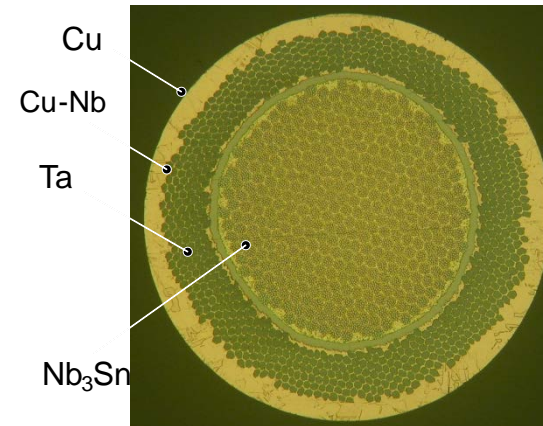
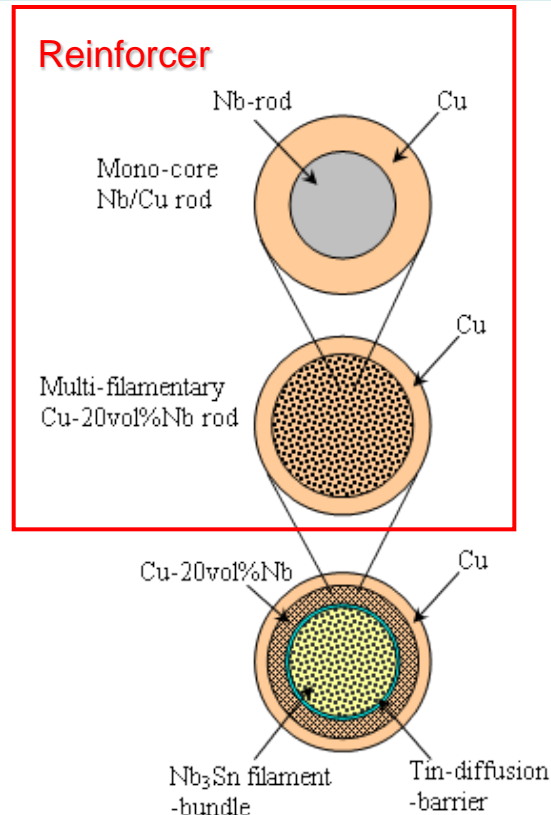


Fig. 1. Cross-section of Nb-rod-method Cu-Nb/Nb<sub>3</sub>Sn strand

TABLE II Strain characteristics Determined by using ITER 2008 strain scaling parameters for the tested strands

Parameter	As-reacted	Pre-bent
$C_{a1}$	43.84	48.17
$C_{a2}$	9.37	1.42
$\epsilon_{0a}$	0.113%	0.175%
$\epsilon_m$	-0.291%	-0.143%
$B_{c2m0}$	35.00	34.84
$T_{cm0}$	11.26	10.49
$C$	99823	85025
$p$	0.834	0.750
$q$	2.195	1.819

$$I_c(B, T, \epsilon_0) = \pi d^2 [4(1 + \lambda)]^{-1} J_c(B, T, \epsilon_0)$$

$$J_c(B, T, \epsilon) = CB^{-1} s(\epsilon) (1 - t^{1.52}) (1 - t^2) b^p (1 - b)^q$$

$$B_{c2}^*(T, \epsilon) = B_{c20m}^* s(\epsilon) (1 - t^{1.52})$$

$$T_c^*(T, \epsilon) = T_{c0m}^* s(\epsilon)^{1/3} (1 - B / B_{c2}^*(0, \epsilon))^{1/1.52}$$

$$s(\epsilon) = 1 + \left( \left( C_{a1} \sqrt{\epsilon_{sh}^2 + \epsilon_{0a}^2} - \sqrt{(\epsilon - \epsilon_{sh})^2 + \epsilon_{0a}^2} \right) - C_{a2} \epsilon \right) \times (1 - C_{a1} \epsilon_{0a})^{-1}$$

$$\epsilon_{sh} = C_{a2} \epsilon_{0a} / \sqrt{C_{a1}^2 - C_{a2}^2}$$

$$\epsilon = \epsilon_{\text{applied}} + \epsilon_m$$

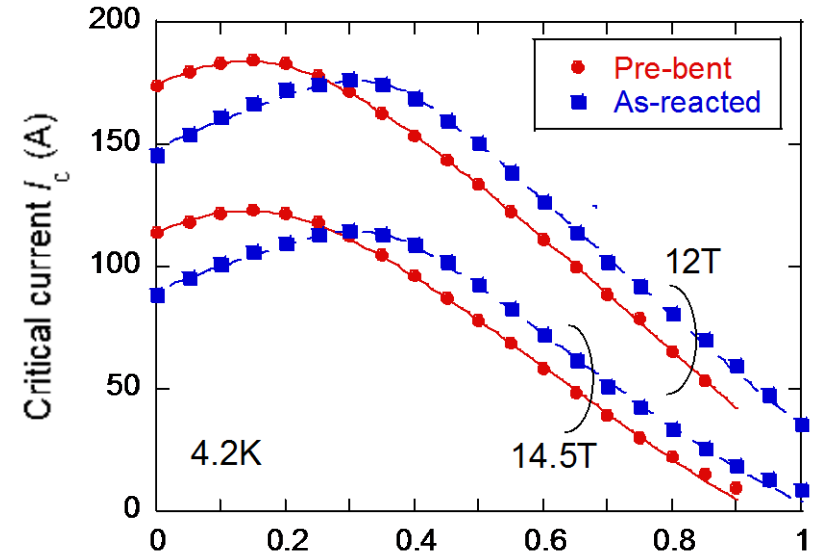


Fig. 2.  $I_c$  characteristics of Cu-Nb/Nb<sub>3</sub>Sn strands as a function of axial tensile strain. Solid and dashed lines are calculated by using ITER2008 strain scaling parameters of TABLE II.

#### Reference

- L. Bottura and B. Bordini, "J<sub>c</sub>(B, T, ε) Parameterization for the ITER Nb<sub>3</sub>Sn Production," *IEEE Trans. Appl. Supercond.*, vol. 19, no. 3, Jun. 2009, pp. 1521-1524.
- M. Sugimoto, H. Tsubouchi, S. Endoh, A. Takagi, K. Watanabe, S. Awaji, and H. Oguro, "Development of Nb-rod-method Cu-Nb reinforced Nb<sub>3</sub>Sn Rutherford cables for react-and-wind processed wide-bore high magnetic field coils," *IEEE Trans. Appl. Supercond.*, vol. 25, no. 3, Jun. 2015, Art. ID. 6000605.

# Heat treatments, pre-bending and pure-bending process

Pre-bending strain

$$\varepsilon_{pb}^+ = \frac{d_0}{2} \cdot \left( \frac{1}{R_h} - \frac{1}{R_{pb1}} \right)$$

$$\varepsilon_{pb}^- = \frac{d_0}{2} \cdot \left( \frac{1}{R_h} - \frac{1}{R_{pb2}} \right)$$

Pure-bending strain

$$\varepsilon_{\text{pure-bend,peak}} = \frac{d_b}{2} \cdot \left( \frac{1}{R_h} - \frac{1}{R_b} \right)$$

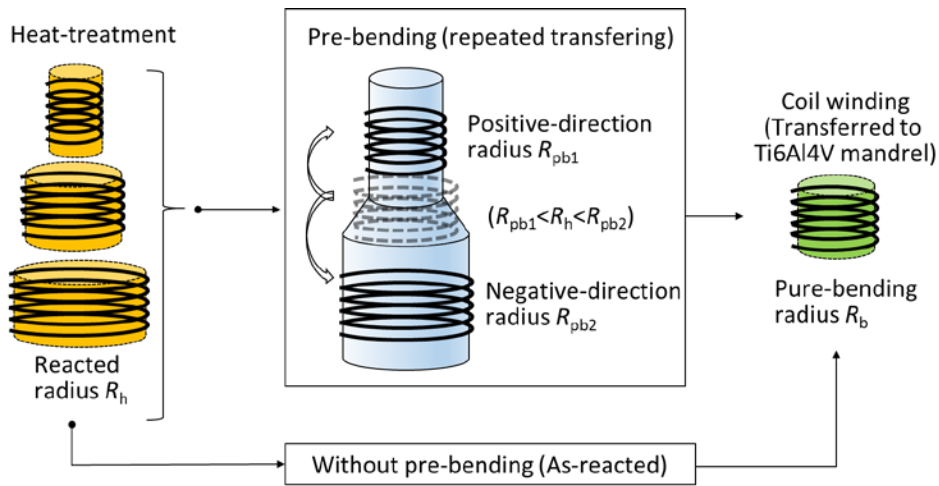


Fig. 3. Schematic image of Heat treatments, pre-bending and the pure-bending process.

TABLE III  
Process condition on Heat treatment and Pre-bending

Heat-treatment	Pre-bending for $\varepsilon_{pb} = \pm 0.5\%$		Pure-bending	
$R_h$ (mm)	$R_{pb1}$ (mm)	$R_{pb2}$ (mm)	$R_b$ (mm)	$\varepsilon_{\text{pure-bend.}}(\%)$
32.1	22.9	54.2	15.6	+0.84
24.6	18.8	35.8	15.6	+0.60
19.6	15.8	26.1	15.6	+0.33
15.6	13.1	19.5	15.6	0
12.9	11.2	15.5	15.6	-0.34
11.3	10.0	13.2	15.6	-0.62
10.1	9.0	11.6	15.6	-0.90

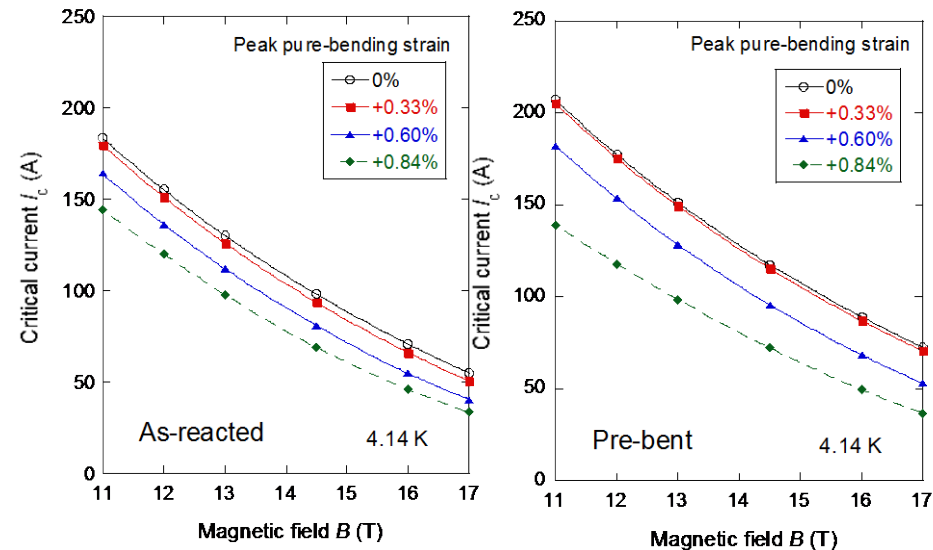


Fig. 4.  $I_c$ - $B$  characteristics under pure-bending strains of Cu-Nb/Nb<sub>3</sub>Sn strand.

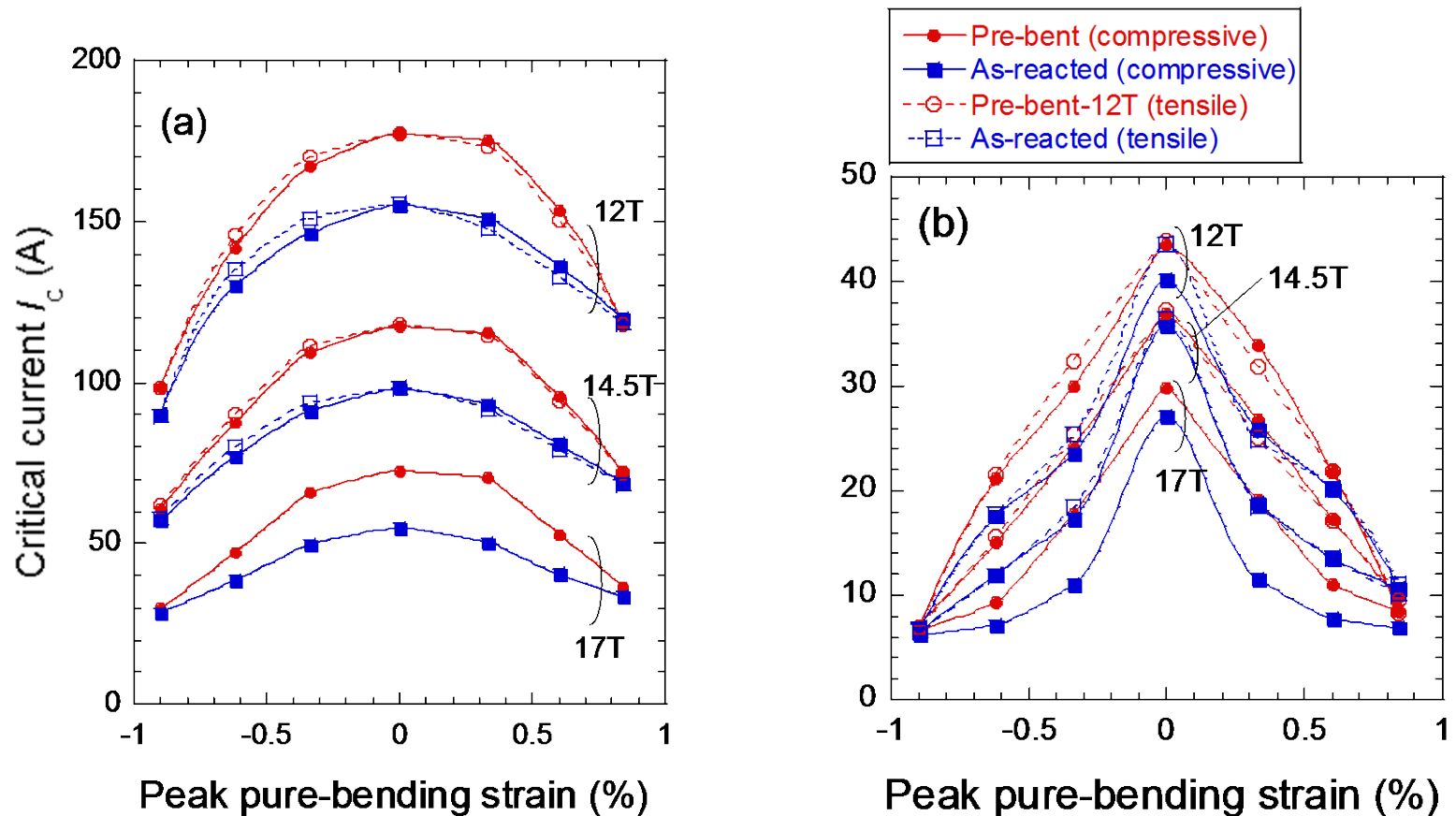


Fig. 5.  $I_c$  characteristics under pure-bending strains of Cu-Nb/Nb<sub>3</sub>Sn strand.  
 (a)  $I_c$  values (b)  $n$ -values

The relationship between  $I_c$  and the pure bending strain is shown in Fig. 5(a), and that of  $n$ -values is shown in Fig. 5(b). The pre-bent strands showed no deterioration of  $I_c$  in the applied pure bending strain of range of +0.5% from -0.5% and had larger  $I_c$  than that of as-reacted strand at no pure-bending strain. The  $I_c$  increase of pre-bent strands were conformed at 12-17 T. The degradation of  $n$ -values occurred at -0.90% because the peak pure-bending strain was larger than the irreversible strains  $\epsilon_{irr} = 0.85\%$  of this strand. The Nb<sub>3</sub>Sn filaments on the inside of the Ta barrier are supposed to be partially broken.

# Analysis of pure-bending strain effects of pre-bent Cu-Nb/Nb<sub>3</sub>Sn strands for practical R&W process

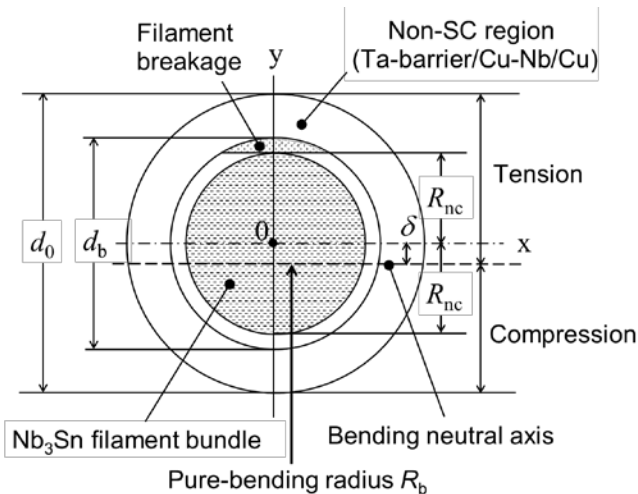


Fig. 6. Cross-section model of non-copper showing the neutral axis shift of  $\delta$ .

## ◆ Perfect current transfer model

$$I_c = 2 \int_{-R_{nc}}^{R_{nc}} j_c(\varepsilon_y) \sqrt{R_{nc}^2 - y^2} dy$$

$$\varepsilon_y = \varepsilon_0 + \varepsilon_{by} \quad \varepsilon_{by} = (y + \delta)/(R_b - \delta)$$

## ◆ No current transfer model

$$I_c = 2\pi \int_0^{R_{nc}} \left\{ \min \left[ j_c(\varepsilon_y) \Big|_{\varepsilon_y = \varepsilon_0 + \varepsilon_{by}}, j_c(\varepsilon_y) \Big|_{\varepsilon_y = \varepsilon_0 - \varepsilon_{by}} \right] \right\} y dy$$

$$\varepsilon_{by} = \begin{cases} -(y + \delta)/(R_b - \delta) & \text{for } j_c(\varepsilon_0 - y/R_b) < j_c(\varepsilon_0 + y/R_b) \\ +(y + \delta)/(R_b - \delta) & \text{for } j_c(\varepsilon_0 - y/R_b) > j_c(\varepsilon_0 + y/R_b) \end{cases}$$

## REFERENCES

- J. W. Ekin, "Strain Scaling law and the prediction of uniaxial and bending strain effects in multifilamentary superconductors," in *Filamentary A15 Superconductors*, Proceedings of the topical conference on A15 superconductors, Ed by M. Suenaga and A. Clark, Plenum Press, New York, 1980, pp. 187-203.
- M. Takayasu, L. Chiesa, d. L. Harris, A. Allegritti, and J. V. Minervini, "Pure bending strains of Nb<sub>3</sub>Sn wires," *Supercond. Sci. Technol.*, vol. 24, 2011, Art. ID. 045012.

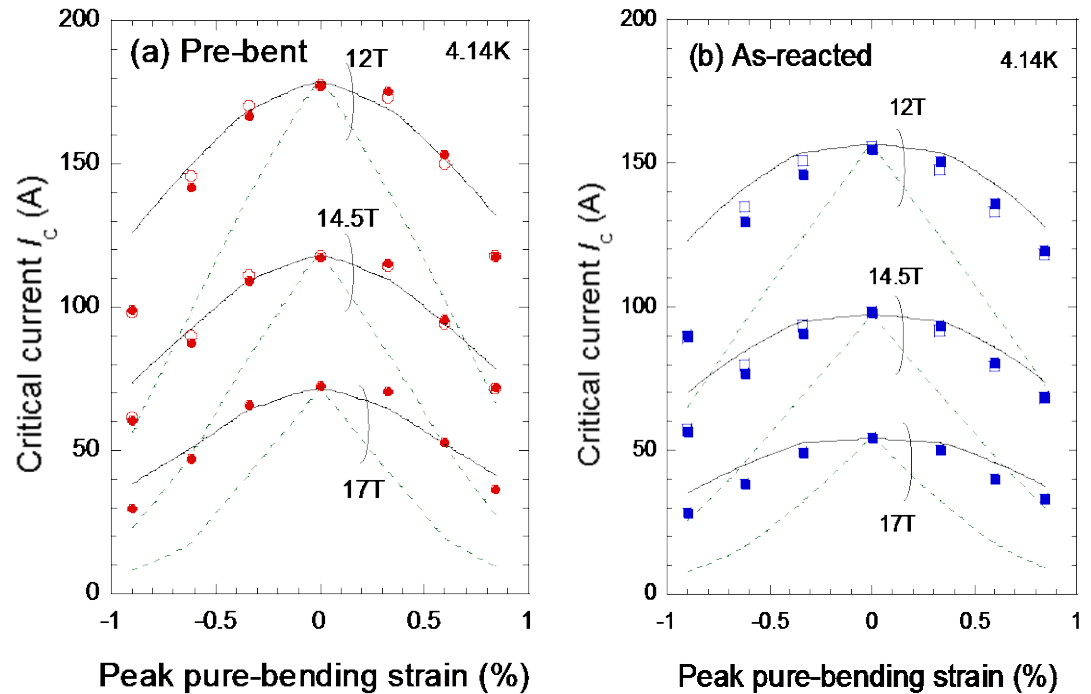


Fig. 7. Comparison between the measured  $I_c$  and calculated  $I_c$  values of (a) Pre-bent strands and (b) As-reacted strands. Perfect current transfer model (solid lines) fit well comparing to no current transfer model (dashed lines).

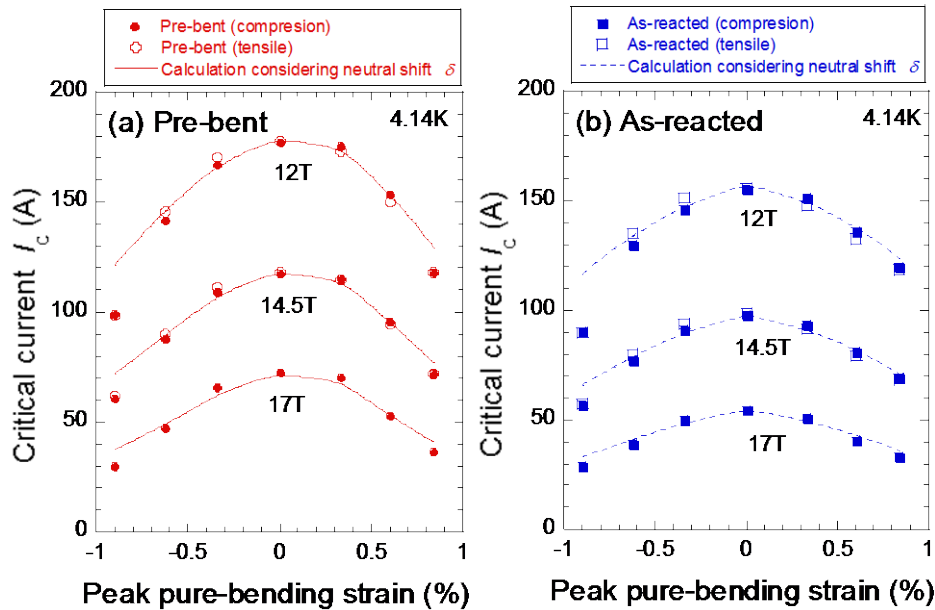


Fig. 8.  $I_c$  values calculated considering of neutral shift  $\delta$

The neutral axial shifts will be caused by the spring back effects of the strand after the pure-bending process. The neutral shift  $\delta$  at positive pure-bending and that at negative pure-bending of the pre-bent Cu-Nb/Nb<sub>3</sub>Sn strands were assumed to be -0.09 mm and -0.02 mm. On the other hand, those of as-reacted strands were assumed to be +0.03 mm and -0.04 mm. The difference will be related to residual strain.

## Summary

- Critical current characteristics under pure bending strains of pre-bent Cu-Nb/Nb<sub>3</sub>Sn strands were investigated.
- $I_c$  values of pre-bent strands were increased at pure-bending strain from -0.5% to 0.5% by the pre-bending treatment of  $\varepsilon_{pb} = \pm 0.5\%$  than those of the as-reacted strands.
- Analysis based perfect current transfer model can quantitatively explain the peak pure-bending strain dependence of  $I_c$  considering neutral axis shifts.
- It was confirmed that the appropriate pre-bending process of the Cu-Nb/Nb<sub>3</sub>Sn wires is very useful for practical manufacturing of R&W processed Nb<sub>3</sub>Sn magnets.