

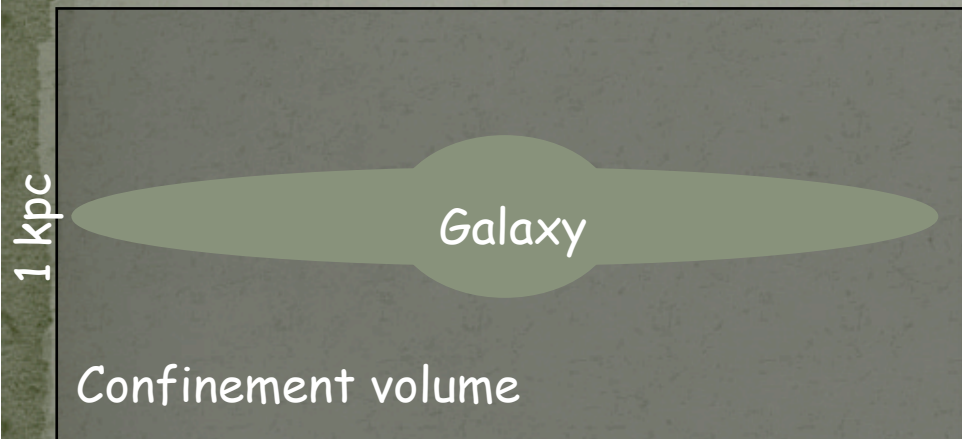
ON THE ORIGIN OF LEPTONS AND HADRONS IN THE COSMIC RADIATION

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SUPERNOVA PARADIGM: I-ENERGETICS

$$\omega_{\text{CR}} = 0.5 \text{ eV cm}^{-3}$$



30 kpc

$$V_{\text{conf}} = \pi R^2 h = 2 \times 10^{67} \text{ cm}^3$$

$$W_{\text{CR}} = \omega_{\text{CR}} V_{\text{conf}} \approx 2 \times 10^{55} \text{ erg}$$



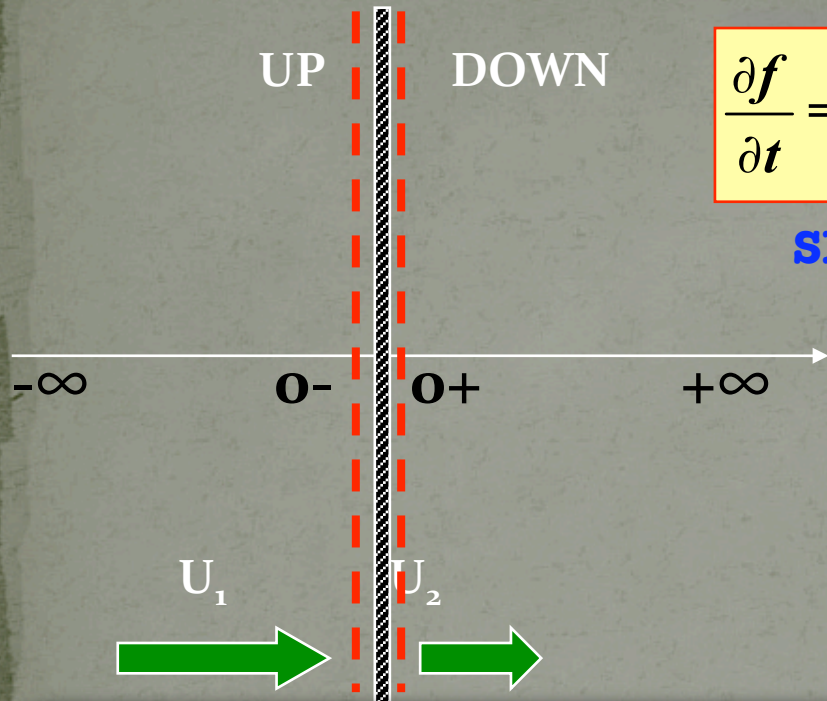
$$L_{\text{CR}} \approx \frac{W_{\text{CR}}}{\tau_{\text{conf}}} \approx 5 \times 10^{40} \text{ erg s}^{-1}$$

$$L_{\text{SN}} = R_{\text{SN}} E_{\text{kin}} \approx 3 \times 10^{41} \text{ erg s}^{-1}$$

REQUIRED EFFICIENCY

10-20 %

SUPERNOVA PARADIGM: II-Energy conversion



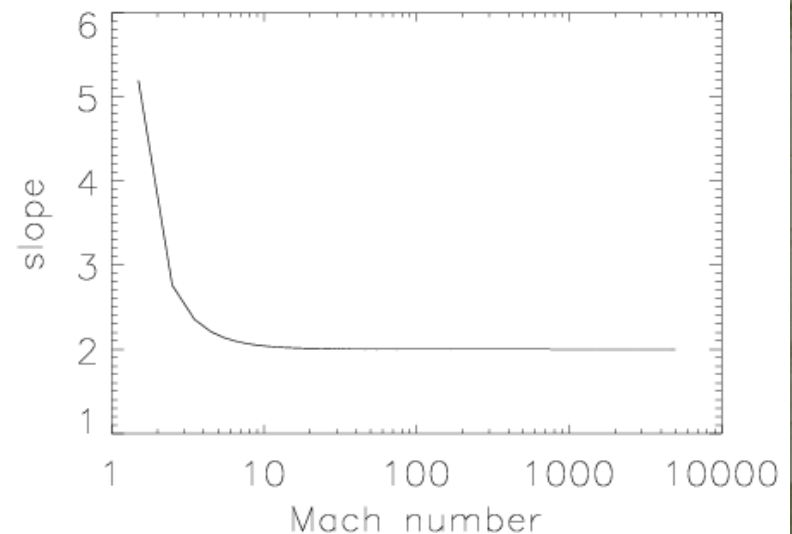
$$\frac{\partial f}{\partial t} = \frac{\partial}{\partial x} \left[D \frac{\partial f}{\partial x} \right] - u \frac{\partial f}{\partial x} + \frac{1}{3} \frac{du}{dx} p \frac{\partial f}{\partial p} + Q(x, p, t)$$

SPECTRUM

$$N(E) \propto \left(\frac{E}{E_0} \right)^{-\gamma} \quad \gamma = \frac{R + 2}{R - 1}$$

R COMPRESSION FACTOR

1. Power law spectrum
2. Slope only F(R)
3. No dependence on diffusion
4. For strong shocks slope ~2
5. No absolute normalization



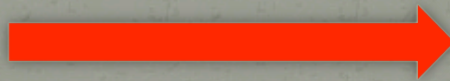
MAXIMUM ENERGY

**ACCELERATION
TIME**

$$\tau_{acc} = \frac{3}{U_1 - U_2} \left[\frac{D_1(E)}{U_1} + \frac{D_2(E)}{U_2} \right]$$

What if we use the ISM diffusion coefficient inferred from B/C?

$$\tau_{acc} \approx \tau_{age}$$

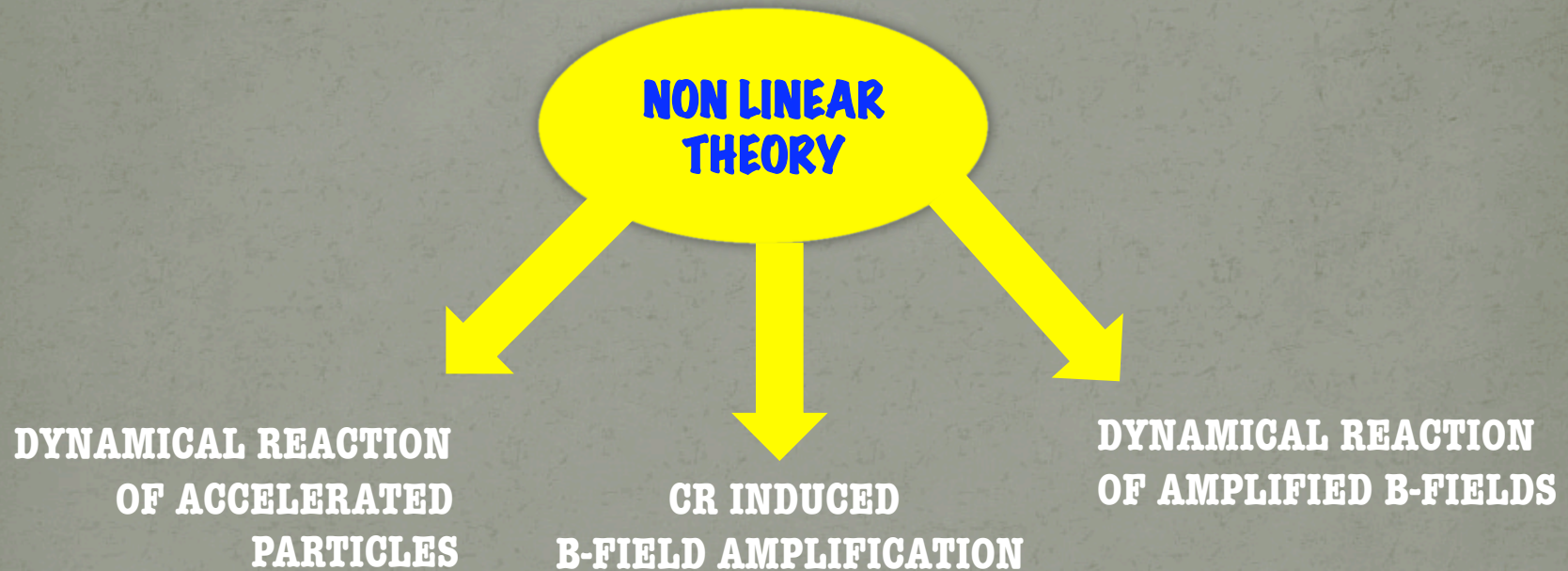


$$E_{max} \sim 1-100 \text{ GeV}$$

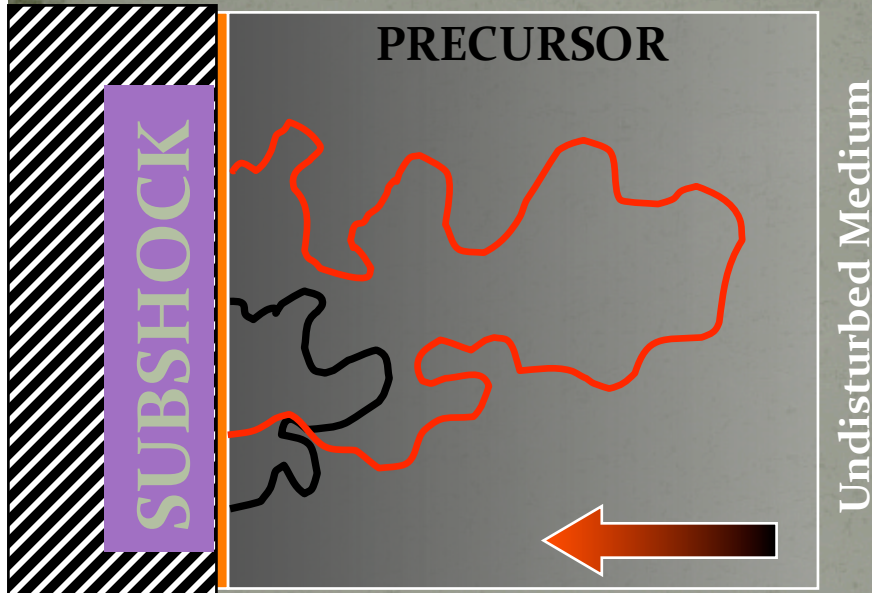
**IF DIFFUSIVE SHOCK ACCELERATION IS THE CONVERSION
MECHANISM IN SNR, IT MUST BE COMPLETED WITH SOME
PROCESS THAT ALLOWS TO REACH PeV ENERGIES**

BEYOND TEST PARTICLES: *Non linear DSA*

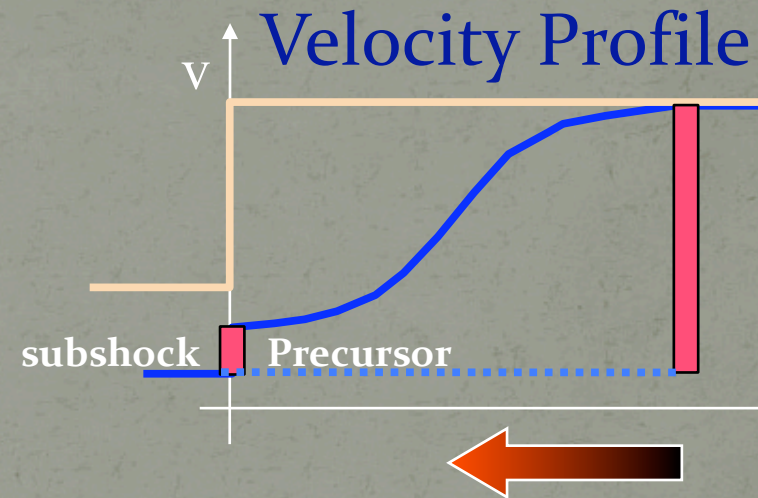
Berezhko & Voelk, PB, Amato & PB, Ellison et al...



DYNAMICAL REACTION



Undisturbed Medium

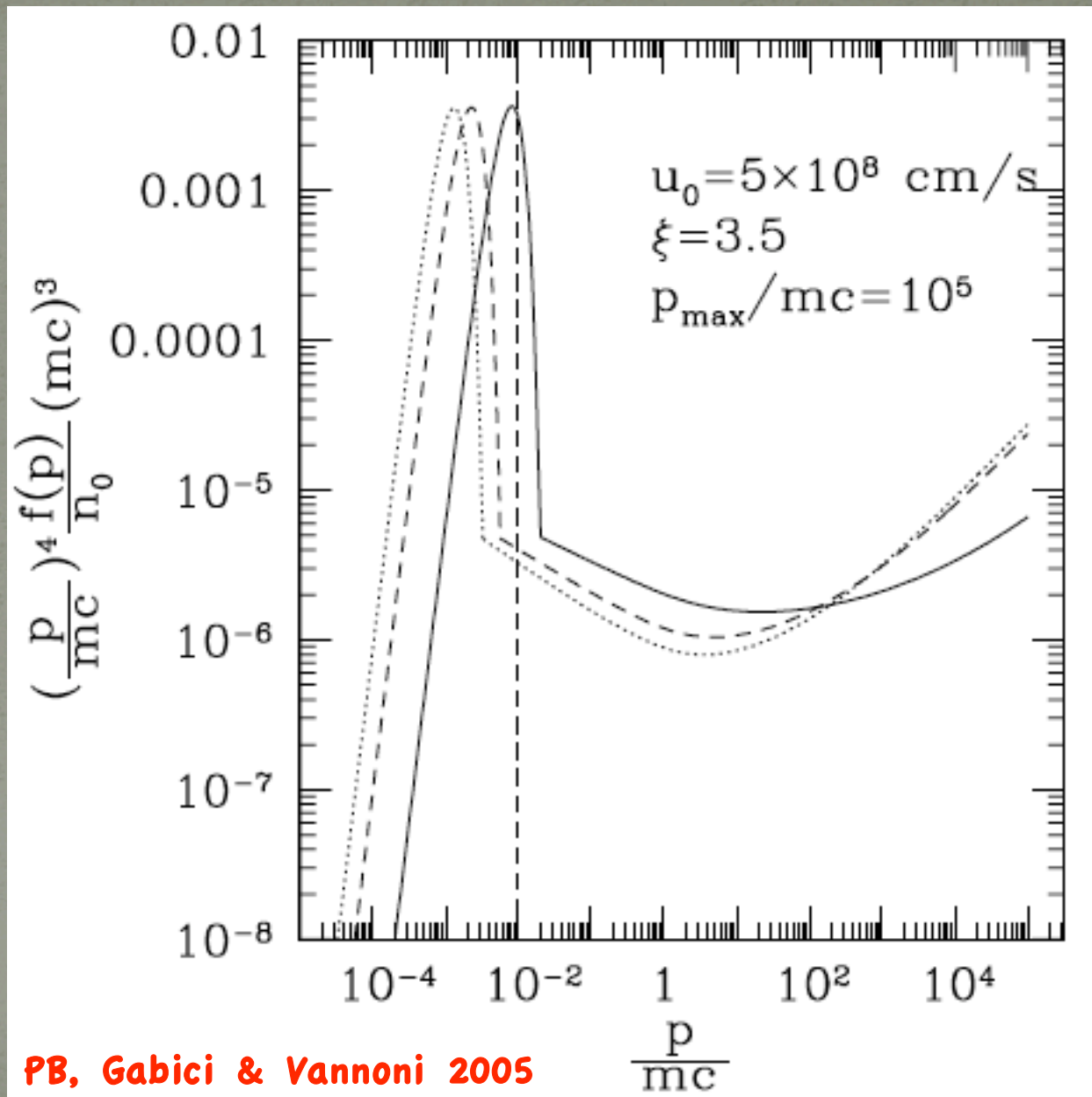


CR TRANSPORT EQUATION

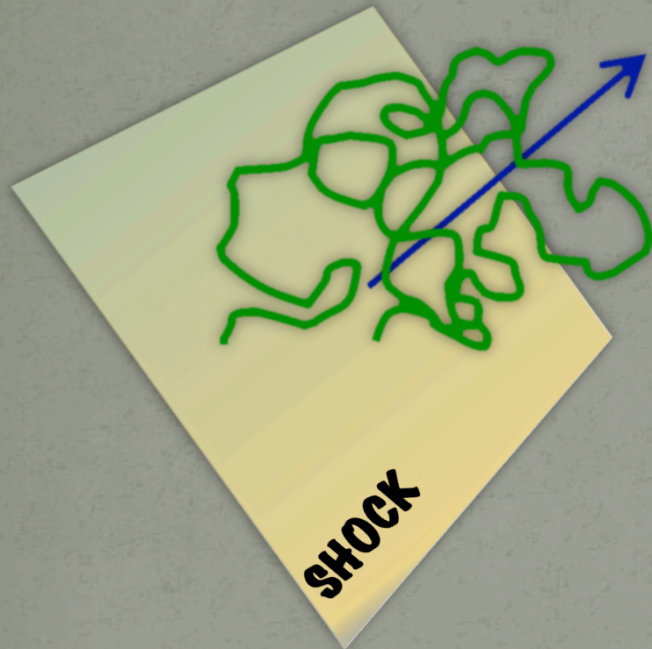
+

MASS, MOMENTUM, ENERGY
CONSERVATION EQUATIONS

1. NO POWER LAW SPECTRA
2. HIGH ACCEL. EFFICIENCY
3. REDUCED HEATING
4. ESCAPE FLUX



MAGNETIC FIELD AMPLIFICATION



SMALL PERTURBATIONS IN THE LOCAL B-FIELD CAN BE AMPLIFIED BY THE SUPER-ALFVENIC STREAMING OF THE ACCELERATED PARTICLES

$$\tau = \frac{1}{\Omega(\delta B / B)^2}$$

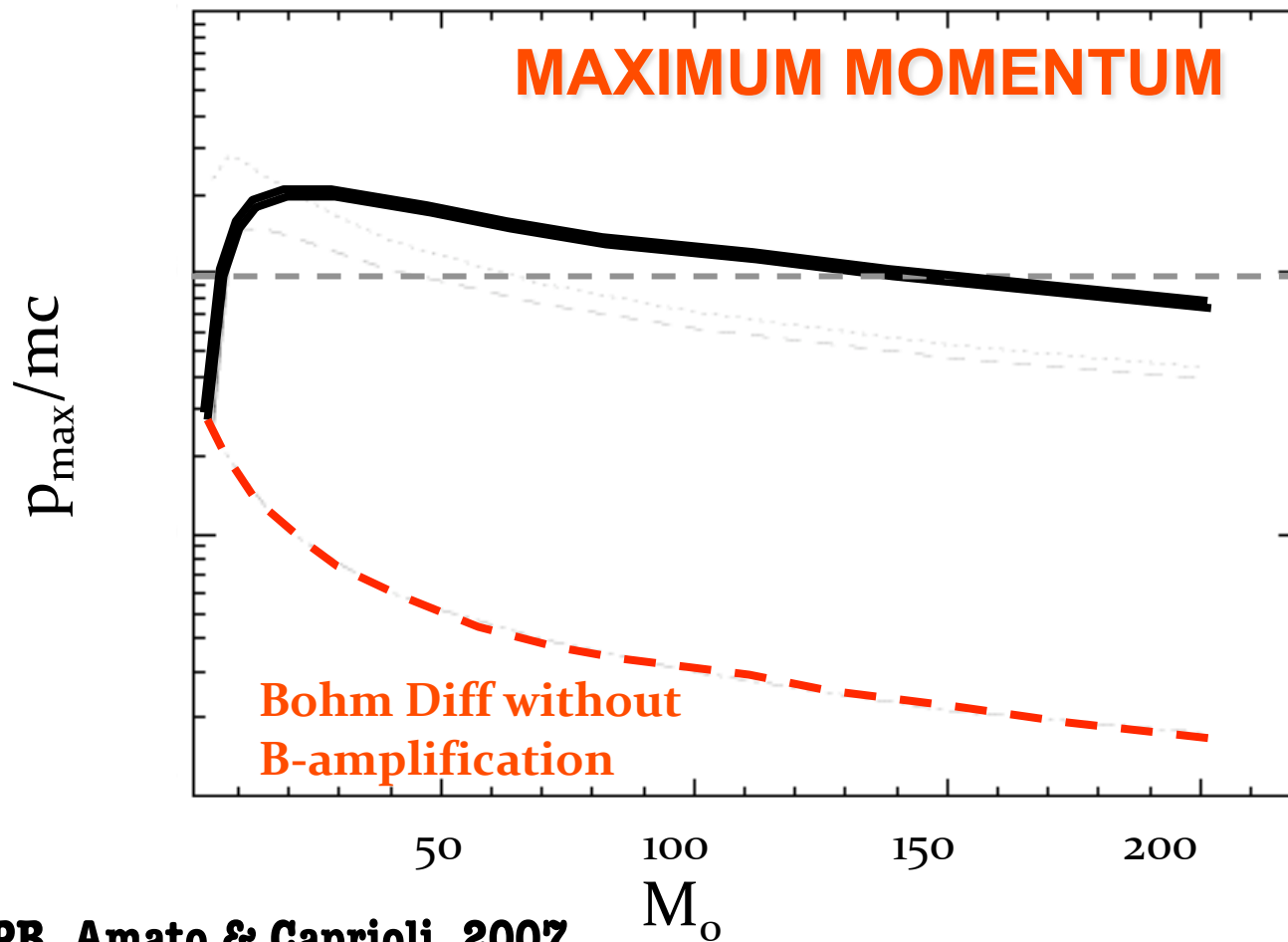
$$\frac{dP_{CR}}{dt} = \frac{n_{CR} m_p \gamma_{CR} (v_S - v_A)}{\tau}$$

$$\frac{dP_W}{dt} = \Gamma_W \frac{\delta B^2}{4\pi v_A}$$

$$\Gamma_W = \frac{n_{CR}}{n} \left(\frac{v_S - v_A}{v_A} \right) \Omega_{cyc}$$

GROWTH RATE

WHY IS IT INTERESTING: I. Reaching the knee?



PB, Amato & Caprioli, 2007

WHY IS IT INTERESTING: II. Large B observed?

TYPICAL THICKNESS OF FILAMENTS:
 10^{-2} - 10^{-3} pc

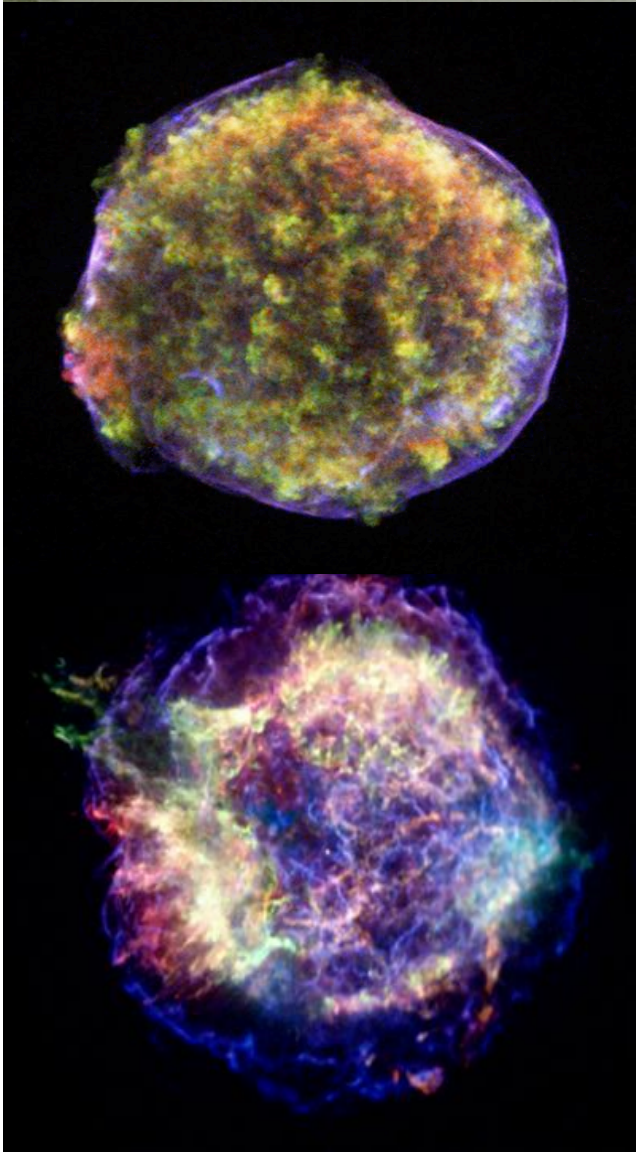
The synchrotron limited thickness is:

$$\Delta x = \sqrt{4D(E)\tau_{syn}(E)} \approx 4 pc B_{\mu}^{-3/2}$$

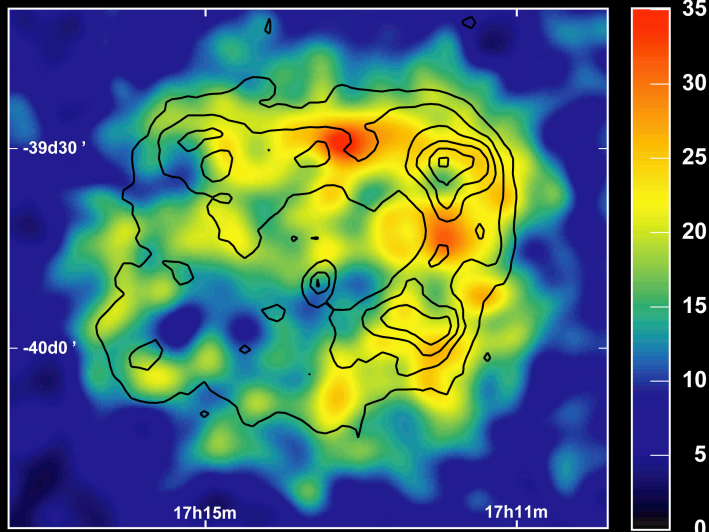


$$B \approx 100 \mu\text{Gauss}$$

COMPATIBLE WITH ESTIMATE FROM VARIABILITY
(Uchiyama et al. 2007)

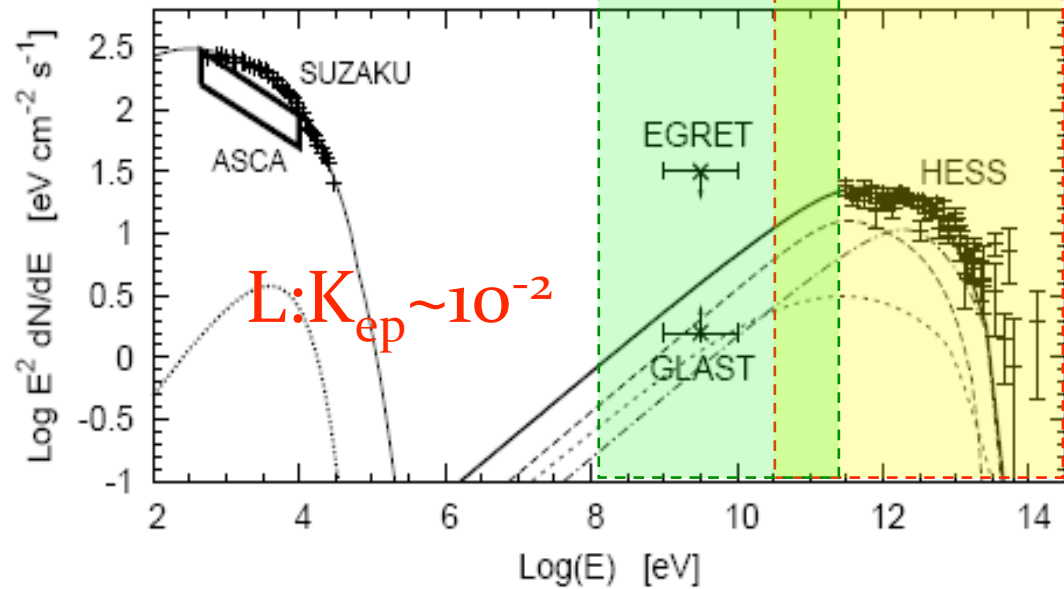
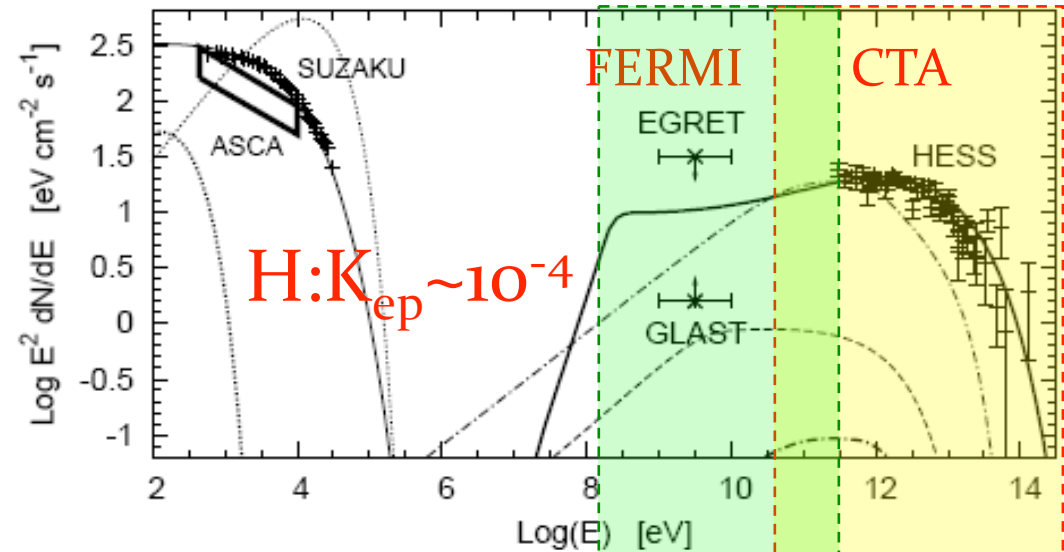


PHENOMENOLOGY OF INDIVIDUAL SNR



Aharonian et al. 2007

Morlino, Amato & PB 2009



CRs versus ACCELERATED PARTICLES

WHAT IS THE SPECTRUM OF CR AT EARTH?



**ESCAPE TOWARDS
UPSTREAM**

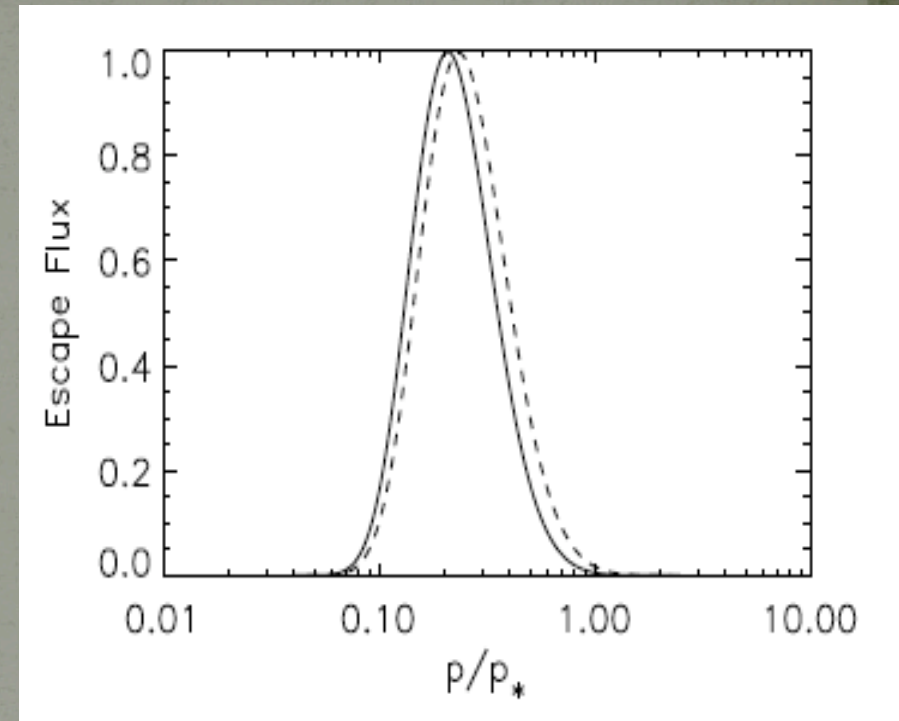
**ESCAPE FROM
DOWNSTREAM AFTER
ADIABATIC LOSSES**

ESCAPE FLUX WITH TIME

$$E_{MAX}(t) \propto \xi_c(t) t^{-1/2}$$

$$R_{sh}(t) = 2.7 \times 10^{19} \text{cm} \left(\frac{E_{51}}{n_1} \right)^{1/5} t_{kyr}^{2/5}$$

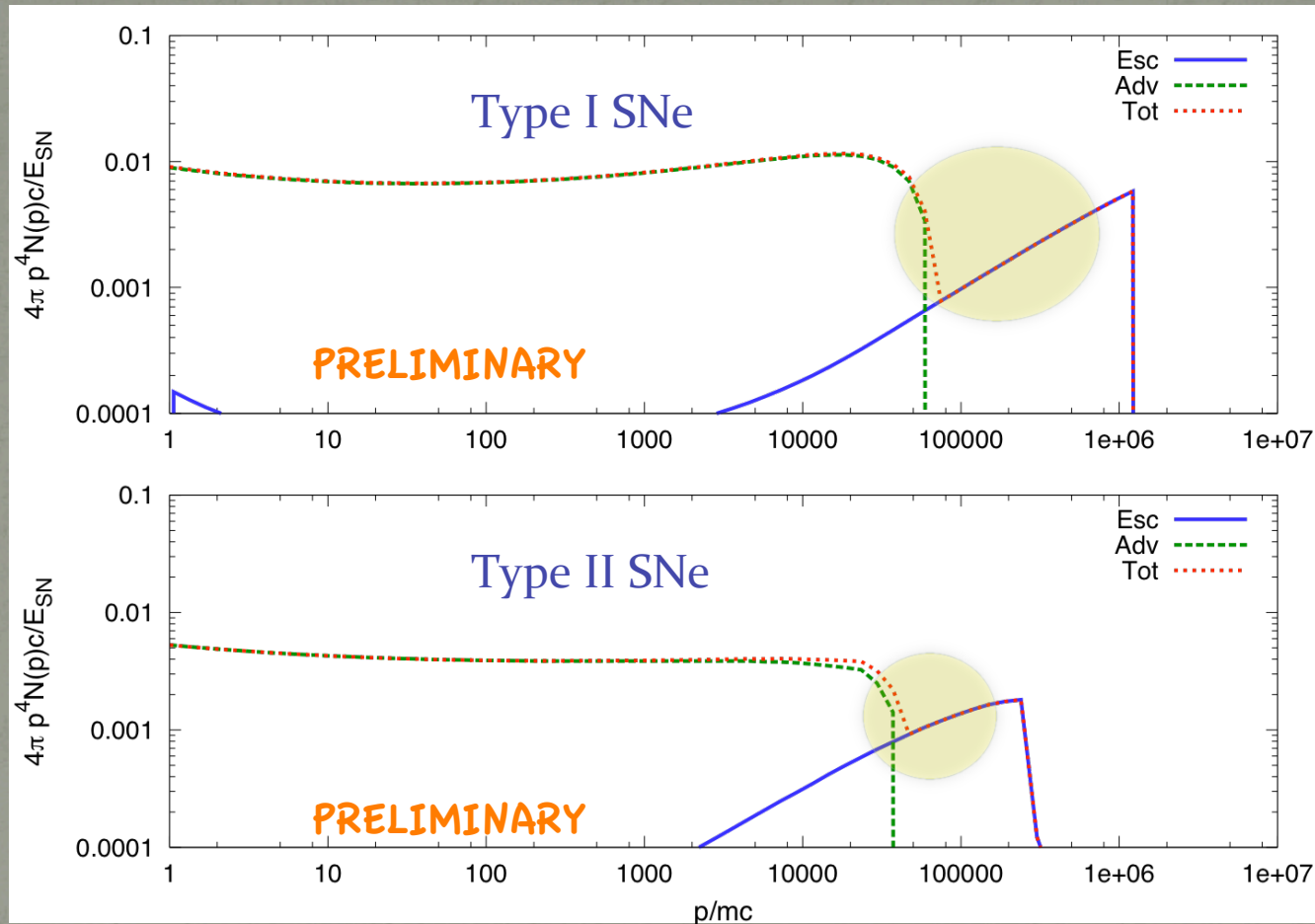
$$V_{sh}(t) = 4.7 \times 10^8 \text{cm/s} \left(\frac{E_{51}}{n_1} \right)^{1/5} t_{kyr}^{-3/5}$$



$$EQ(E)dE \approx F_{esc}(t) \frac{1}{2} \rho V_s^3 4\pi R_{sh}^2 \frac{dE_{max}}{dt} dE \propto t^{1/2} dE \propto E^{-1} dE$$

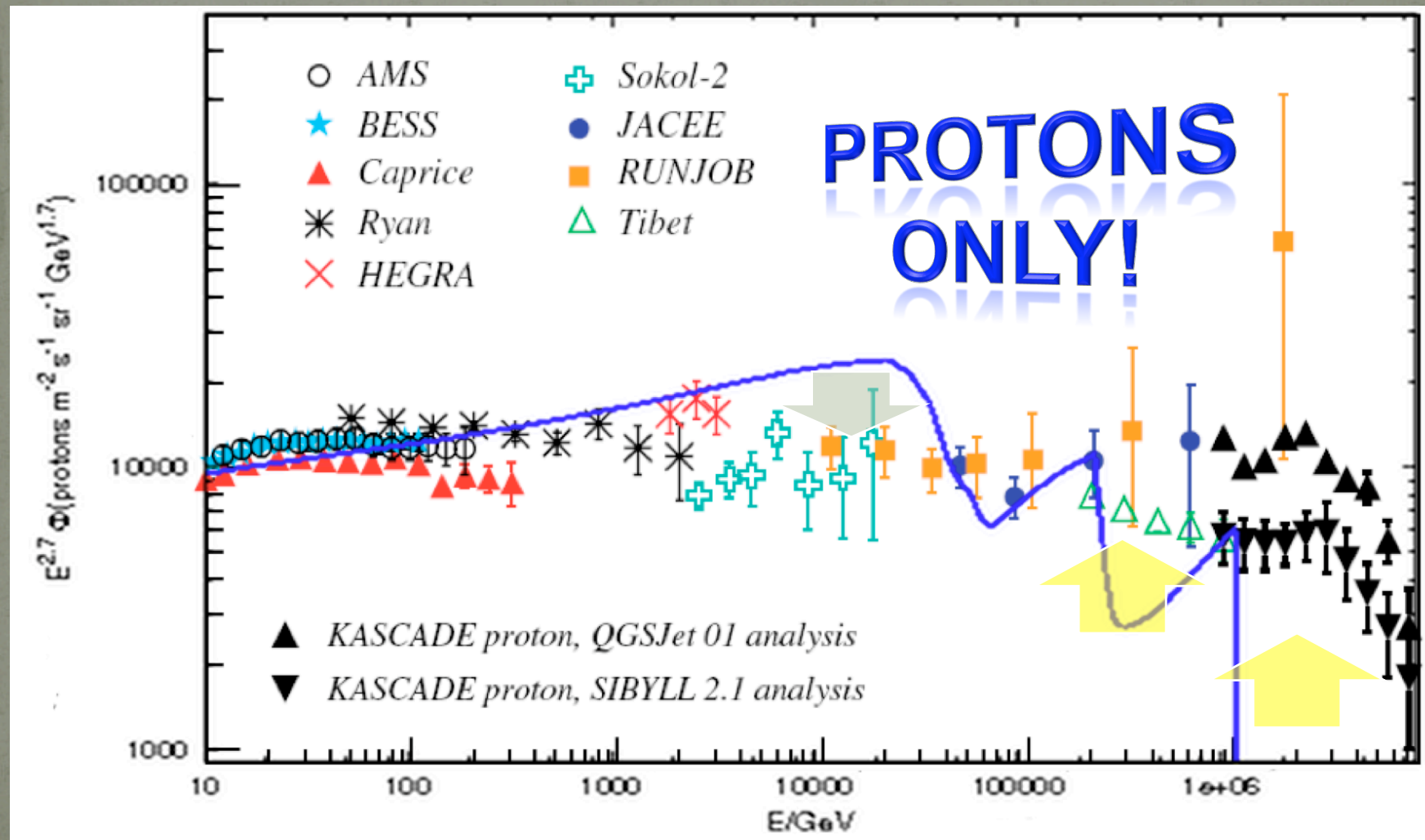
E^{-2} WITH NO CONNECTION WITH THE INTRINSIC SPECTRUM!!!

PROTON SPECTRUM AT EARTH



Caprioli, PB & Amato 2009

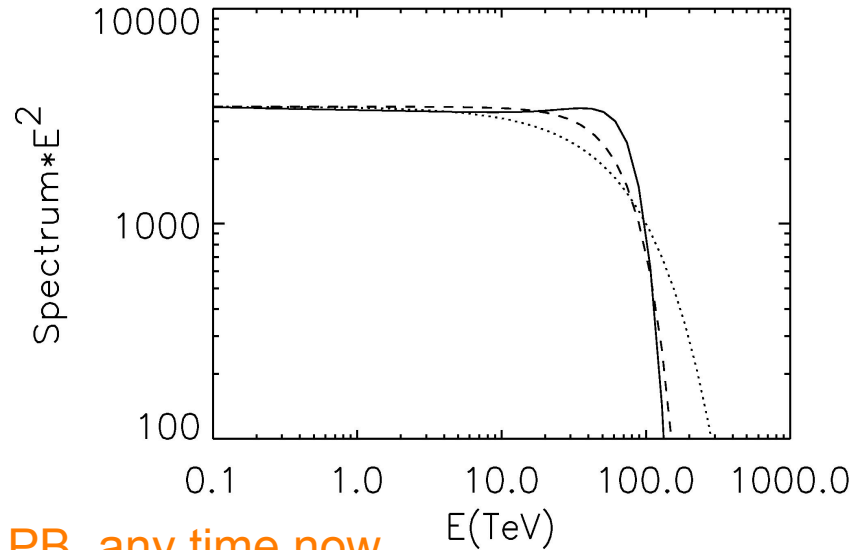
PROTONS AT EARTH



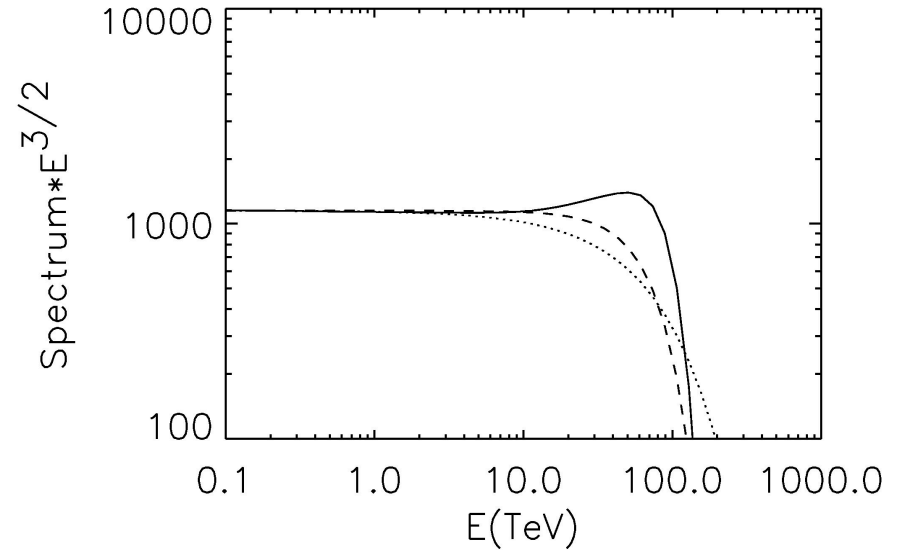
ELECTRONS

1. COMPLICATED BY ENERGY LOSSES (ESPECIALLY CLOSE TO E_{\max})
2. PILE UPS MAY BE PRODUCED BY LOSSES
3. INJECTION NOT UNDERSTOOD AT ALL (THIS IS THE NATURE OF THE K_{ep} USUALLY USED)
4. PROPAGATION (LEAKY BOX VS DISC)

SPECTRA AT INJECTION



PB, any time now



THE SHAPE OF THE CUTOFF DEPENDS ON THE DIFFUSION COEFFICIENT

FOR BOHM DIFFUSION THE CUTOFF IS $\text{EXP}[-(E/E_{\text{MAX}})^2]$

ELECTRONS AFTER PROPAGATION

LET US ASSUME THAT LOSSES DOMINATE



$$n(E) = Q(E)\tau_{loss}(E) \sim E^{-\gamma-1}$$



$$n(E) = \frac{Q(E)\tau_{loss}(E)}{\sqrt{4D(E)\tau_{loss}(E)}} \sim E^{-\gamma-1-\frac{1}{2}(\delta-1)}$$

PRIMARY PROTONS:

$$n_{CR}(E) = N_{CR}(E) R \tau_{esc}(E) \propto E^{-\gamma} E^{-\delta}$$

PRIMARY ELECTRONS:

$$n_e(E) = N_e(E) R \text{Min}[\tau_{esc}(E), \tau_{loss}(E)] \propto E^{-\gamma_e} E^{-\beta}$$

b= d for diffusion

b=1 for losses

SECONDARY POSITRONS INJECTION:

$$q_+(E')dE' = n_{CR}(E)dE n_H \sigma_{pp} c \propto E^{-\gamma-\delta}$$

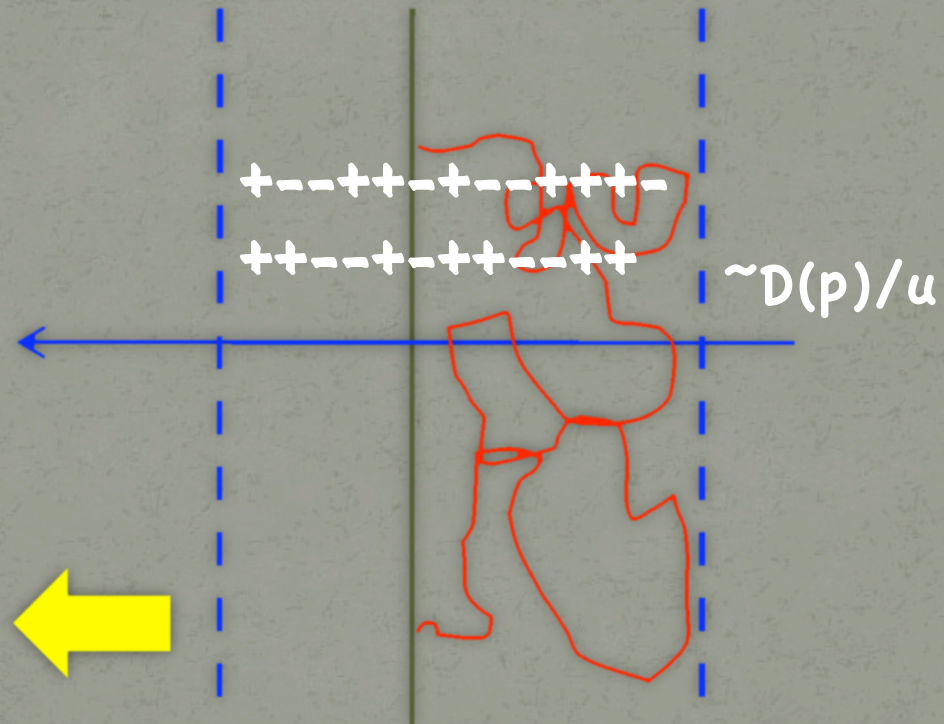
SECONDARY POSITRONS EQUILIBRIUM:

$$n_+(E) = q_+(E) \text{Min}[\tau_{esc}(E), \tau_{loss}(E)] \propto E^{-\gamma-\delta-\beta}$$

$$\frac{n_+}{n_e} \propto E^{-(\gamma-\gamma_e)-\delta}$$

CHARGED SECONDARY PARTICLES IN THE SOURCES

PB 2009



Advection
+ Diffusion

CHARGED SECONDARY PARTICLES

THE EQUATION DESCRIBING ANY CHARGED PARTICLE IN THE SHOCK REGION IS:

$$u \frac{\partial f_{\pm}}{\partial x} = D(p) \frac{\partial^2 f_{\pm}}{\partial x^2} + \frac{1}{3} \frac{du}{dx} p \frac{\partial f_{\pm}}{\partial p} + Q_{\pm}(x, p)$$

AT THE SHOCK

$$p \frac{\partial f_{\pm,0}}{\partial p} = -\gamma f_{\pm,0} + \gamma \frac{D_1(p)}{u_1^2} \left(\frac{1}{\xi} + r^2 \right) \quad \xi \approx 0.05$$

SOLUTION AT THE SHOCK

$$f_{\pm,0}(p) = \gamma \left(\frac{1}{\xi} + r^2 \right) \int_0^p \frac{dp'}{p'} \left(\frac{p'}{p} \right)^\gamma \frac{D_1(p')}{u_1^2} Q_1(p')$$

1. In terms of momentum dependence this scales as $D(p)Q(p) \sim p^{-g+1}$
2. The coefficient in front expresses the re-energization of the secondary particles by the shock (CONSERVES PARTICLE NUMBER BUT INCREASES THE E_n/Part)
3. Of course the final f is cut off at the same momentum as that of the parent protons

SOLUTION AT x

AT A GENERIC LOCATION x DOWNSTREAM OF THE SHOCK, THE SOLUTION CAN ONLY BE:

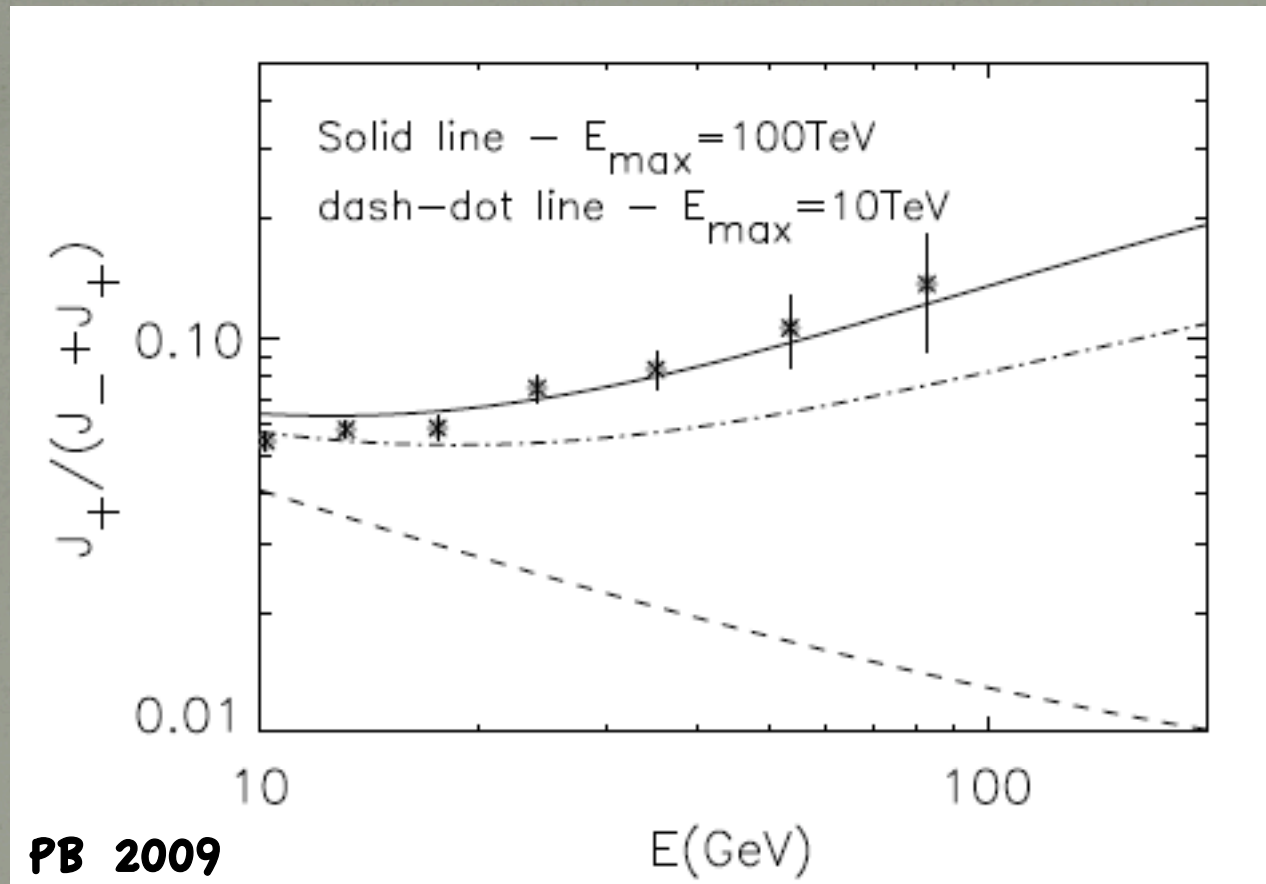
$$f_{\pm}(x, p) = f_{\pm,0}(p) + \frac{Q_2}{u_2} x \quad 0 \leq x \leq u_2 \tau_{SN}$$

**ACCELERATION
TERM**



**STANDARD TERM, THE
SAME AS FOR GAMMAS**

THE POSITRON "EXCESS"



THE PARAMETERS

$$D_B(E) = K_B \frac{1}{3} r_L(E) c = 3.3 \times 10^{22} K_B B_\mu^{-1} E_{GeV} \text{ cm}^2 \text{ s}^{-1}$$

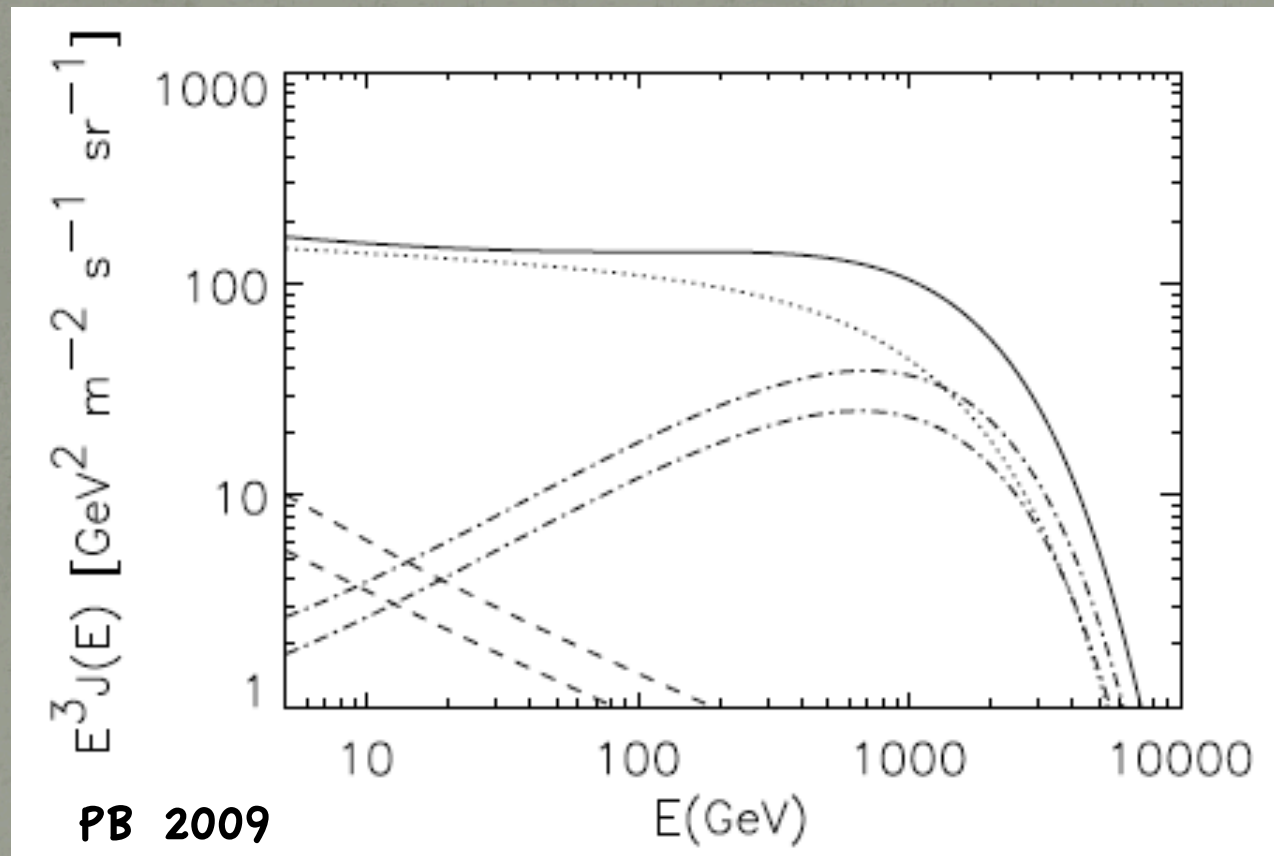
TYPICAL VALUES REQUIRED ARE

$$K_B \approx 10 - 20 \quad B_\mu \approx 1 \quad u_1 \approx 500 - 1000 \text{ km/s} \quad n \approx 1 - 3 \text{ cm}^{-3}$$

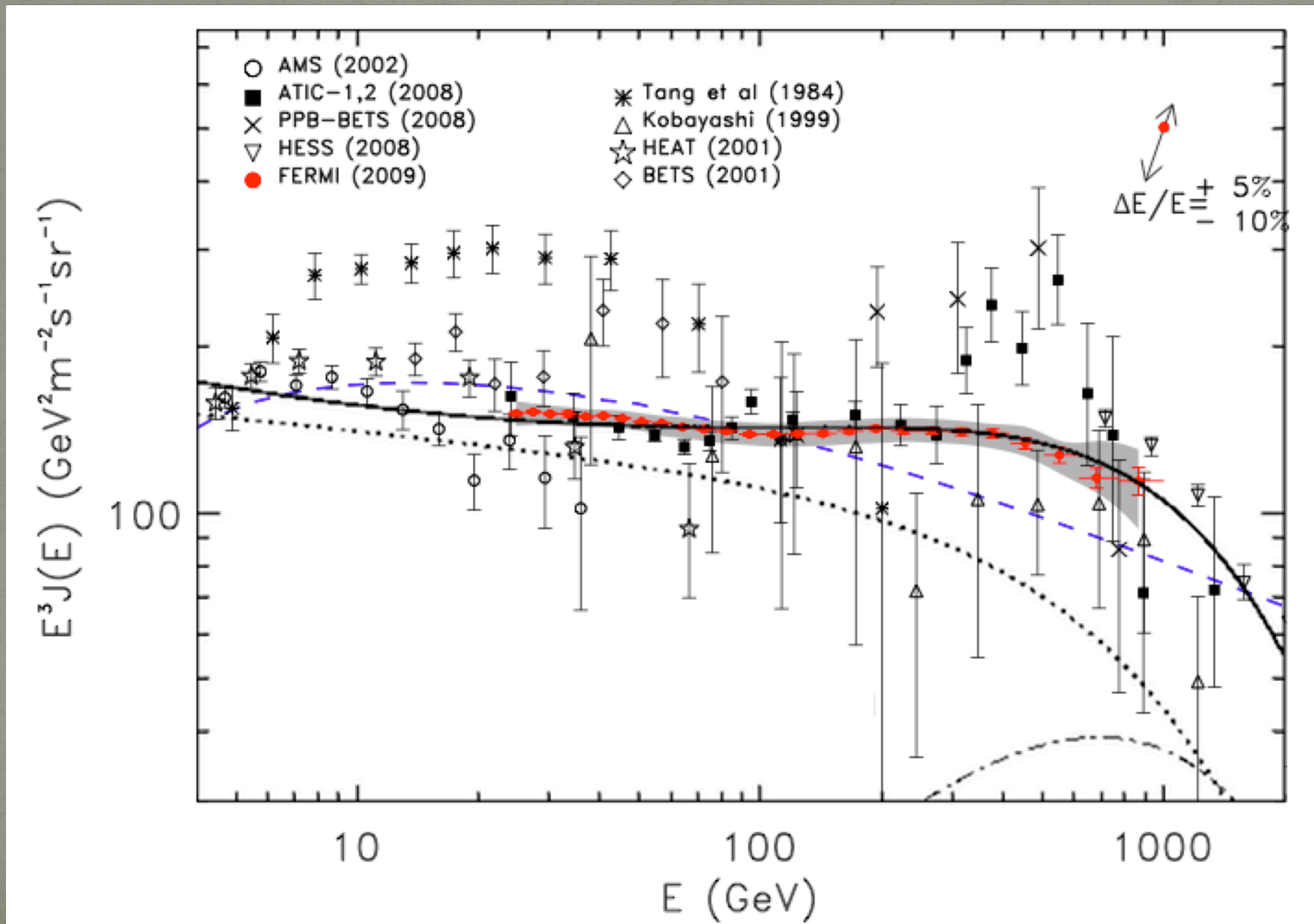
**THESE MAY BE SUITABLE FOR AN OLD SN-I OR A SN-II
OUTSIDE THE BUBBLE CREATED BY THE WIND OF
THE PRE-SN STAR**

**THE BULK OF CR ARE ACCELERATED DURING THIS PHASE
WHICH IS THE ONE THAT LASTS THE MOST...**

THE ELECTRON SPECTRUM



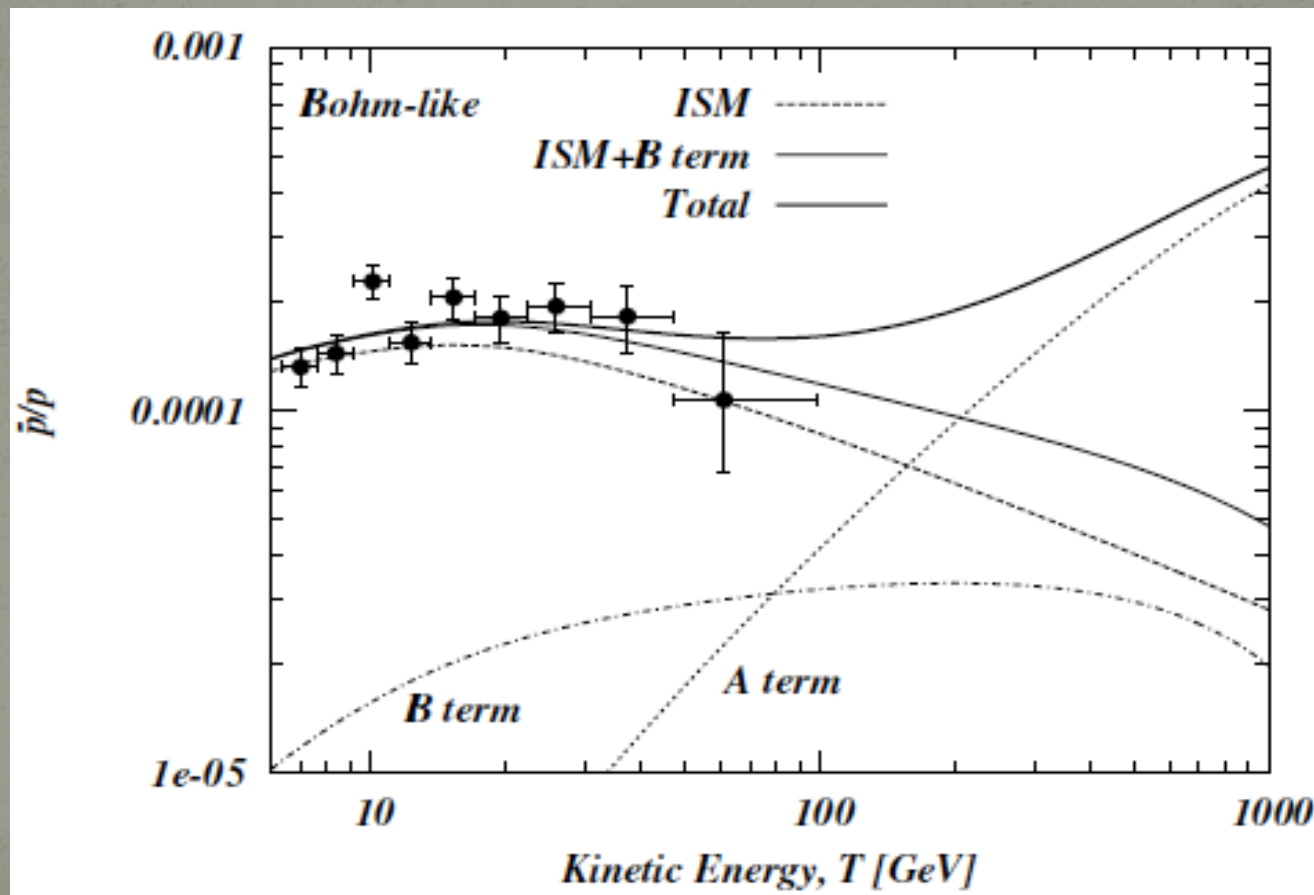
THE ELECTRON SPECTRUM



ANTIPROTONS

PB & Serpico (2009)

SIMPLER CALCULATIONS BECAUSE NO ENERGY LOSSES:



CONCLUSIONS

1. IN ORDER TO REPRODUCE THE CR SPECTRUM, NUCLEI ARE CRUCIAL
2. ACCELERATION UP TO THE KNEE IS UNDERSTOOD IF B IS AMPLIFIED
3. FOR ELECTRONS THERE ARE MORE UNCERTAINTIES BOTH ON ACCELERATION AND PROPAGATION
4. POSITRONS ARE MAINLY DIFFUSE SECONDARIES IN THE ISM AT ENERGIES BELOW 10 GeV
5. BUT AT HIGHER ENERGIES THE CONTRIBUTION OF SOURCES MAY DOMINATE
6. THE SPECTRUM OF e^-+e^+ AT HIGH ENERGY CAN BE DOMINATED BY SECONDARY e^-+e^+ FROM SOURCES