

Pulsar models

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In the talk:

- Models of pulsars as sources of high energy photons.
- Why the composition of pulsar winds (e^\pm content in the context of CR positrons) is connected to the pulsed emission properties?
- Are the results from Fermi LAT challenging to the models?

Pulsars and Cosmic-Ray Positrons

Individual nearby pulsars

Millisecond pulsars - Buesching et al., 2008

Middle-age pulsars - Buesching et al. 2008,
Malyshev et al. 2009,

Galactic population

Chi et al. 1996,
Malyshev et al. 2009,
Barger et al. 2009

Reacceleration and evolution of magnetospheric pairs when trapped in PWNe. Semi-empirical treatment used to obtain the input for subsequent propagation.

Pulsars are treated just as time-dependent energy suppliers at the rate of $\sim L_{sd}(t)$.

This list is not complete.

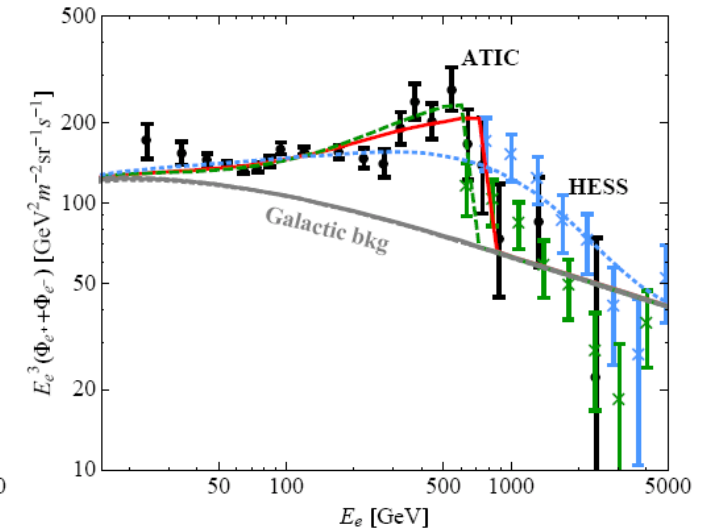
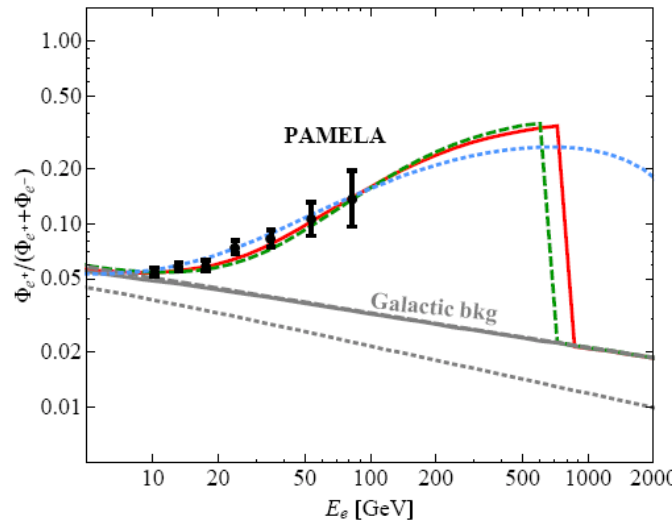
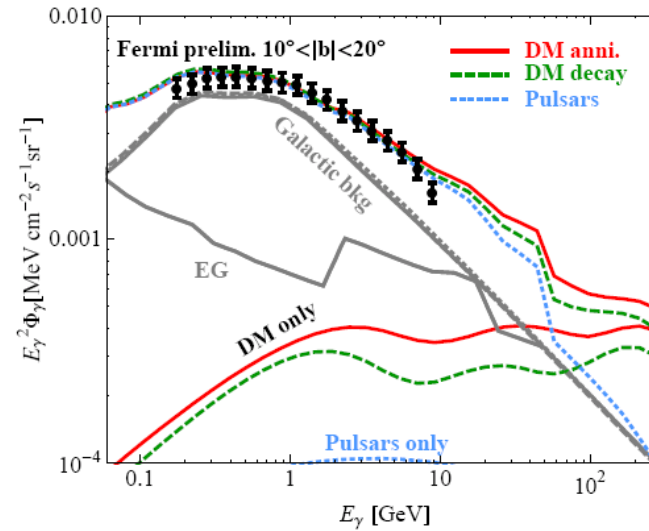
Galactic population of pulsars

Barger et al.2009

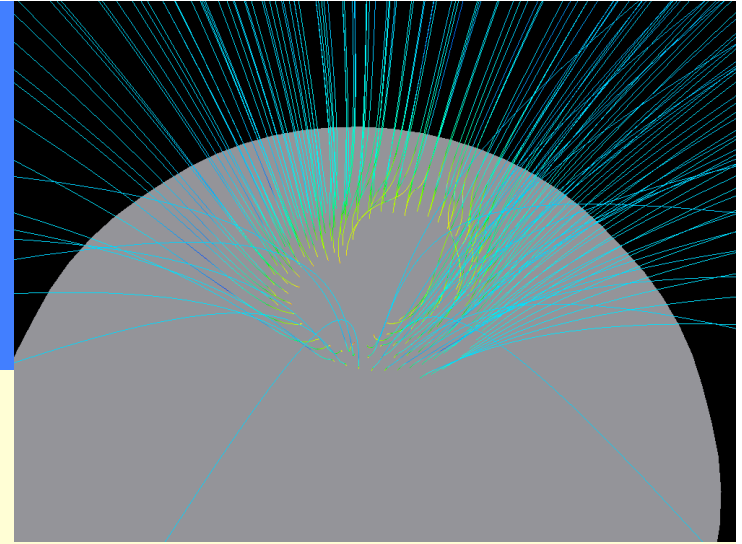
Assumed pair injection spectrum and spatial distribution of pulsars

$$\frac{dN_{e^\pm}}{dE} \propto E^{-\alpha} e^{-E/E_p}$$

+ propagation
using GALPROP



Why do pulsars radiate in high energy domain?



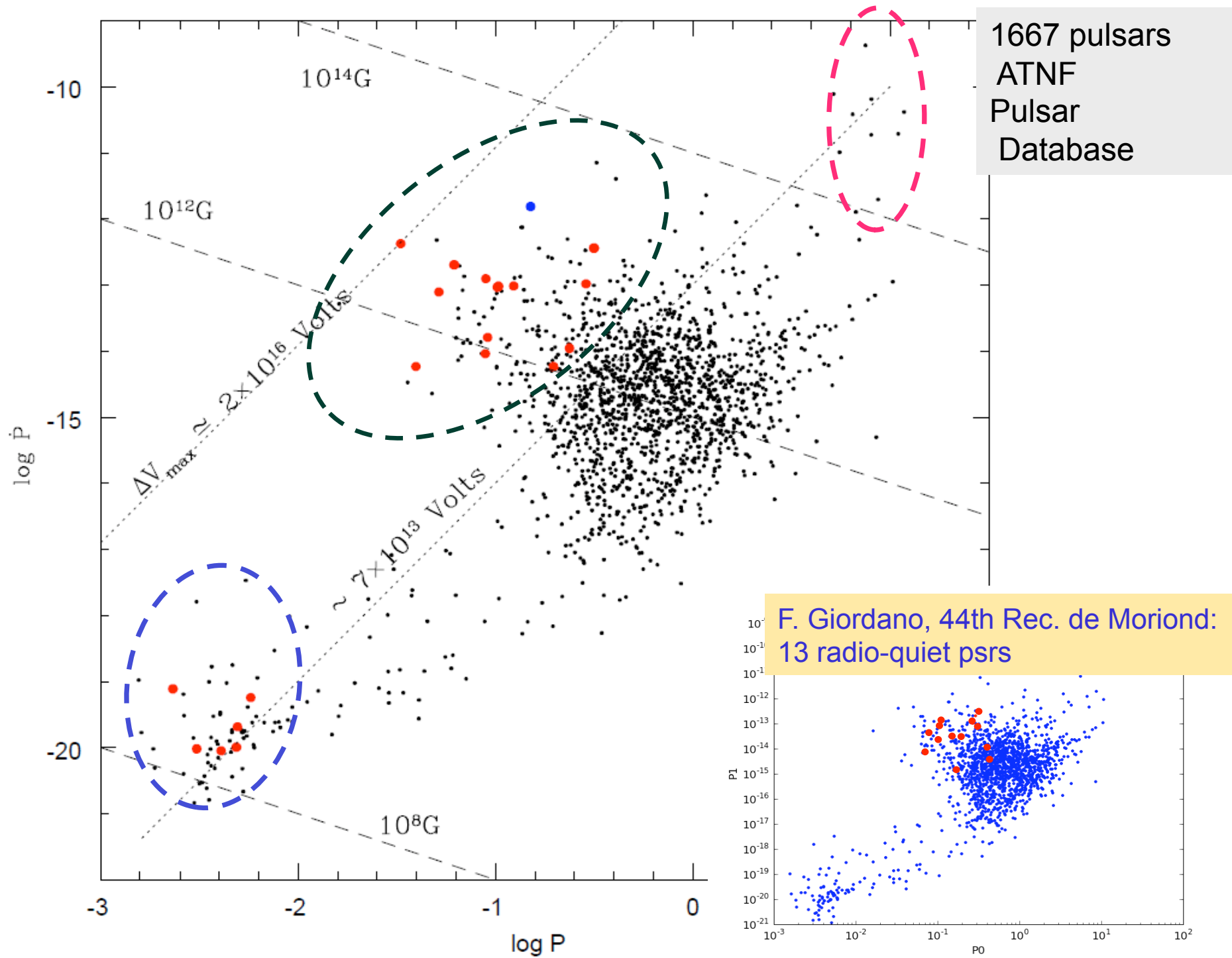
1) Rotating, strongly
magnetized neutron stars ->
unipolar inductors

2) Maximum potential drop (for vacuum rotator)

$$V_{\max} \approx 6 \times 10^{12} B_{12} P^{-2} \text{ Volts,}$$

i.e. for young pulsars V_{\max} can exceed 10^{16} Volts

Actual potential drops are much smaller, but high enough
to accelerate charged particles to ultrarelativistic energies
emitting in turn high energy photons.



Radiative processes in pulsar magnetospheres

1. Curvature radiation

2. Inverse Compton Scattering (resonant + non-resonant)

3. Magnetic pair creation ($1\gamma \rightarrow e^\pm$)

4. Photon-photon pair creation ($2\gamma \rightarrow e^\pm$)

5. Synchrotron radiation

6. Photon splitting ($1\gamma \rightarrow 2\gamma$)

Daugherty & Harding 1982

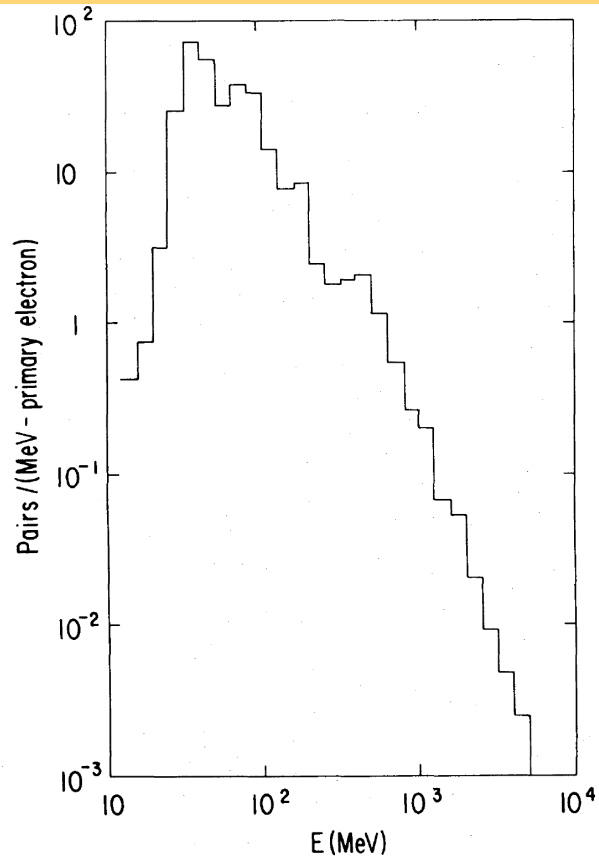


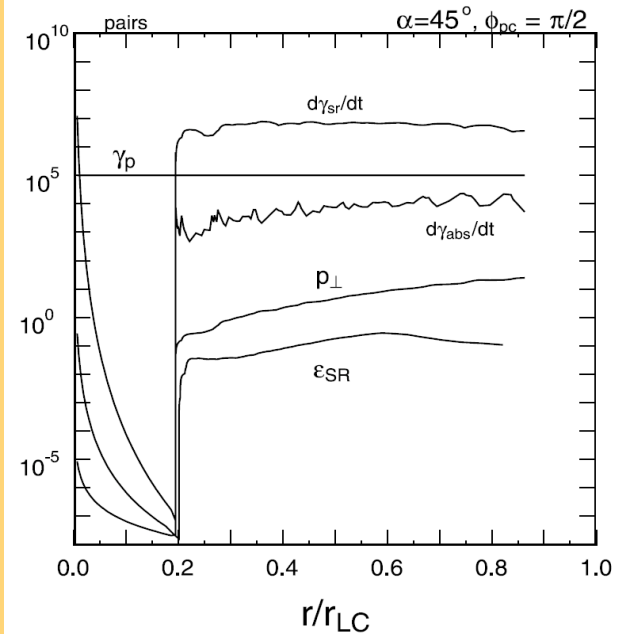
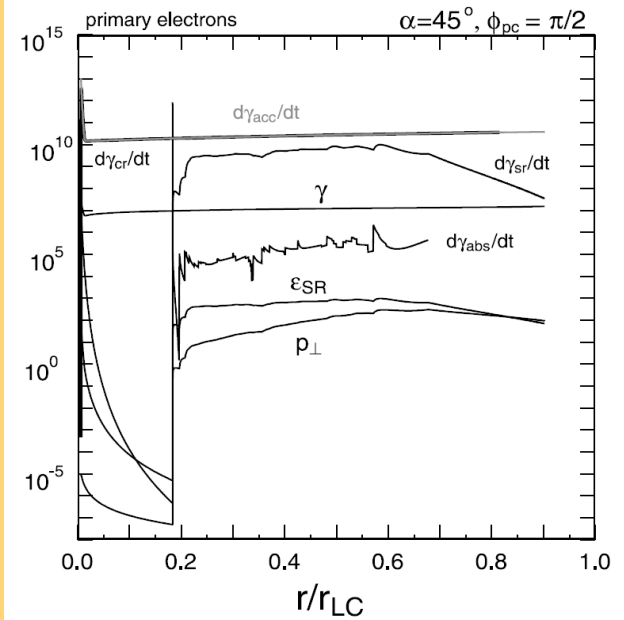
FIG. 7.—Differential e^+e^- spectrum from a cascade with initial electron energy 10^{13} eV, surface field 10^{12} gauss, magnetic colatitude $\theta_0 = 1.0$, and period of the Crab, $P = 0.033$ s.

The pairs spectrum: broken power-law

$$\gamma_{\min} = 10^2, \gamma_{\text{break}} = 5 \times 10^3, \gamma_{\max} = 2 \times 10^5$$

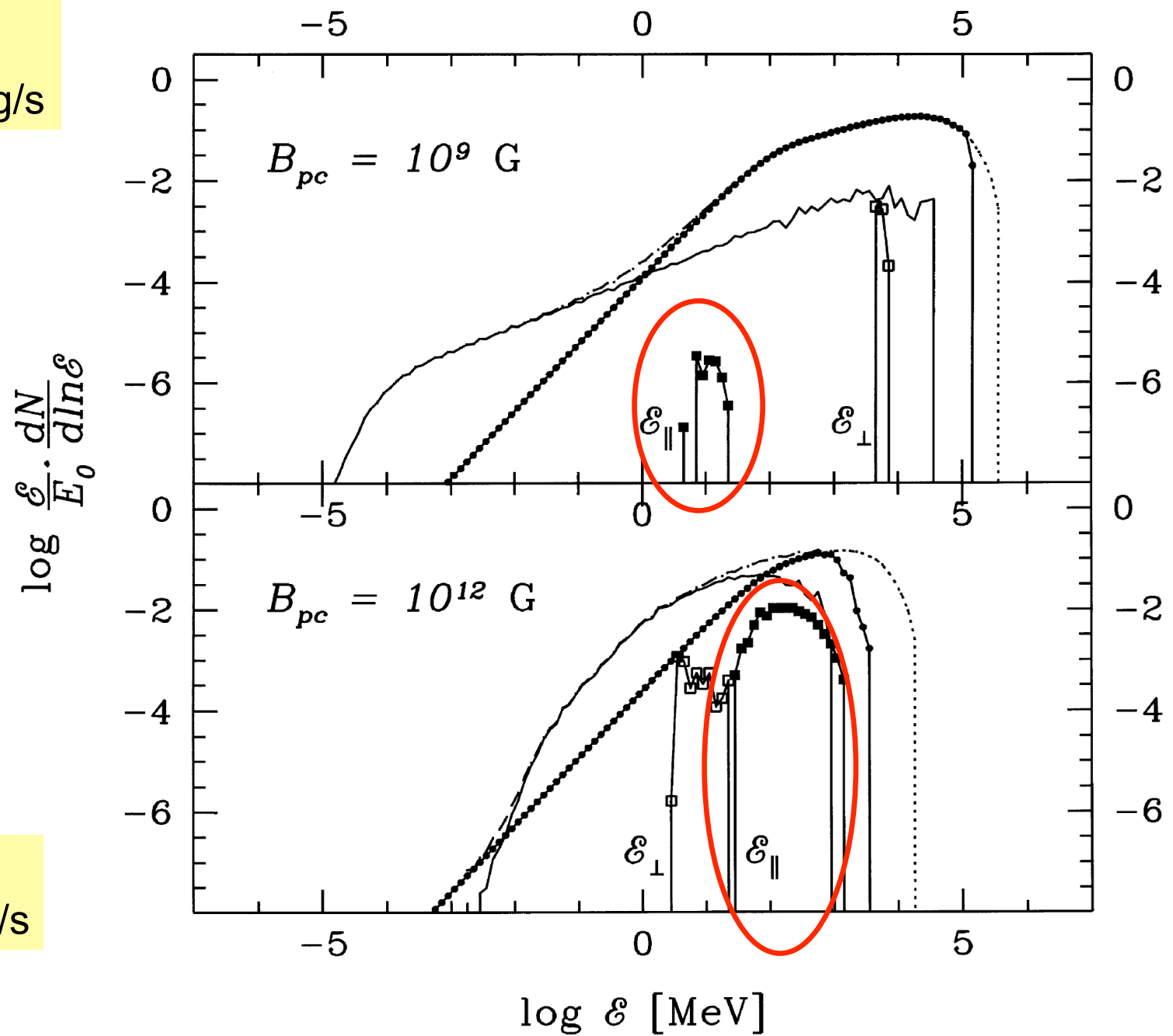
$$\delta_1 = 2.0, \delta_2 = 2.8$$

Harding, Stern, Dyks, Frackowiak 2008



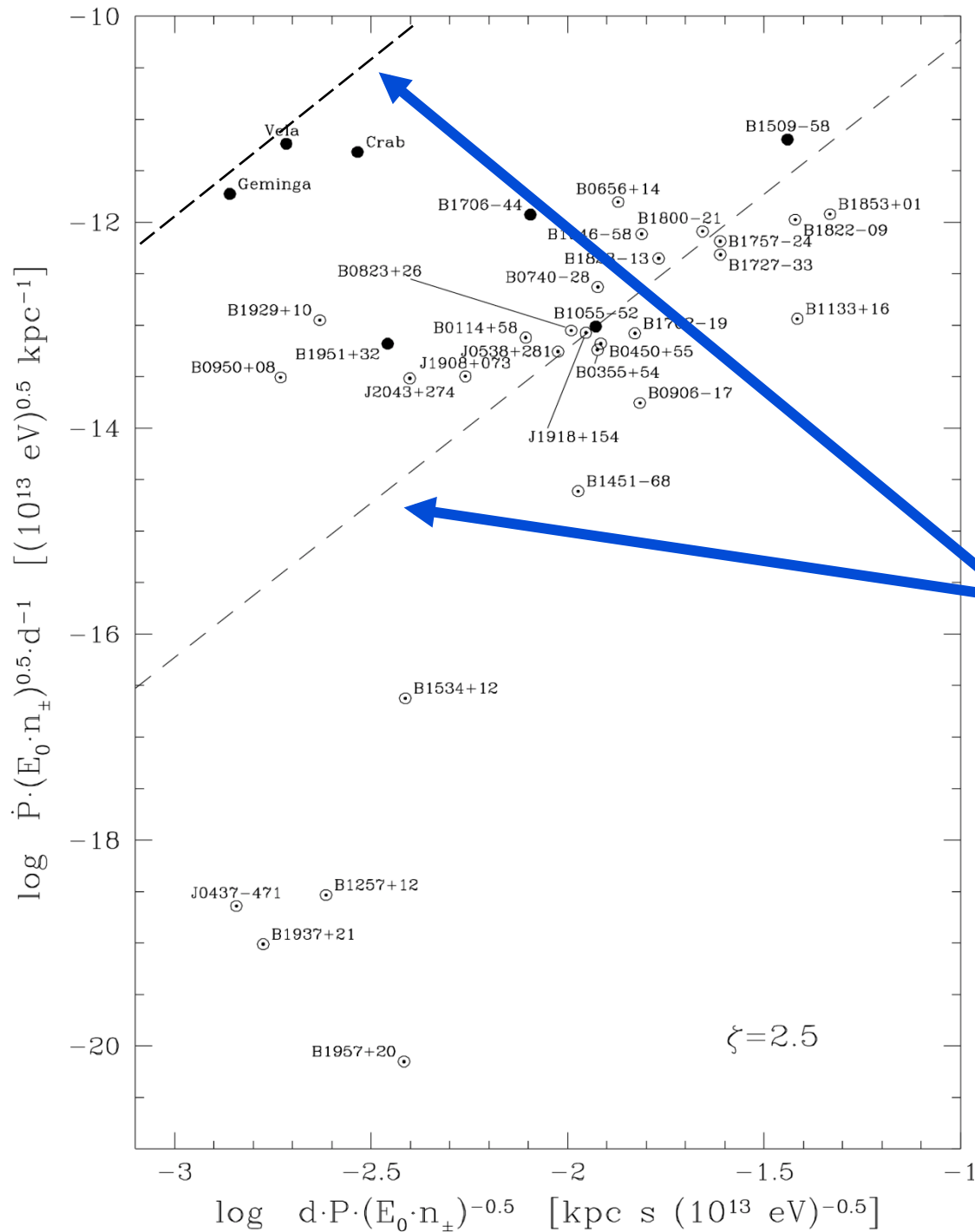
$$P = 0.003 \text{ s}$$

$$L_{\text{sd}} = 10^{35} \text{ erg/s}$$



$$P = 0.056 \text{ s}$$

$$L_{\text{sd}} = 10^{36} \text{ erg/s}$$



Dyks 1998

Lines of constant values
of
 $\dot{N}(e_{\pm})/d^2$

Simple criterium
to choose
promising nearby
pulsars

(in addition to
the pulsar age)

Spectra and lightcurves

as a result of

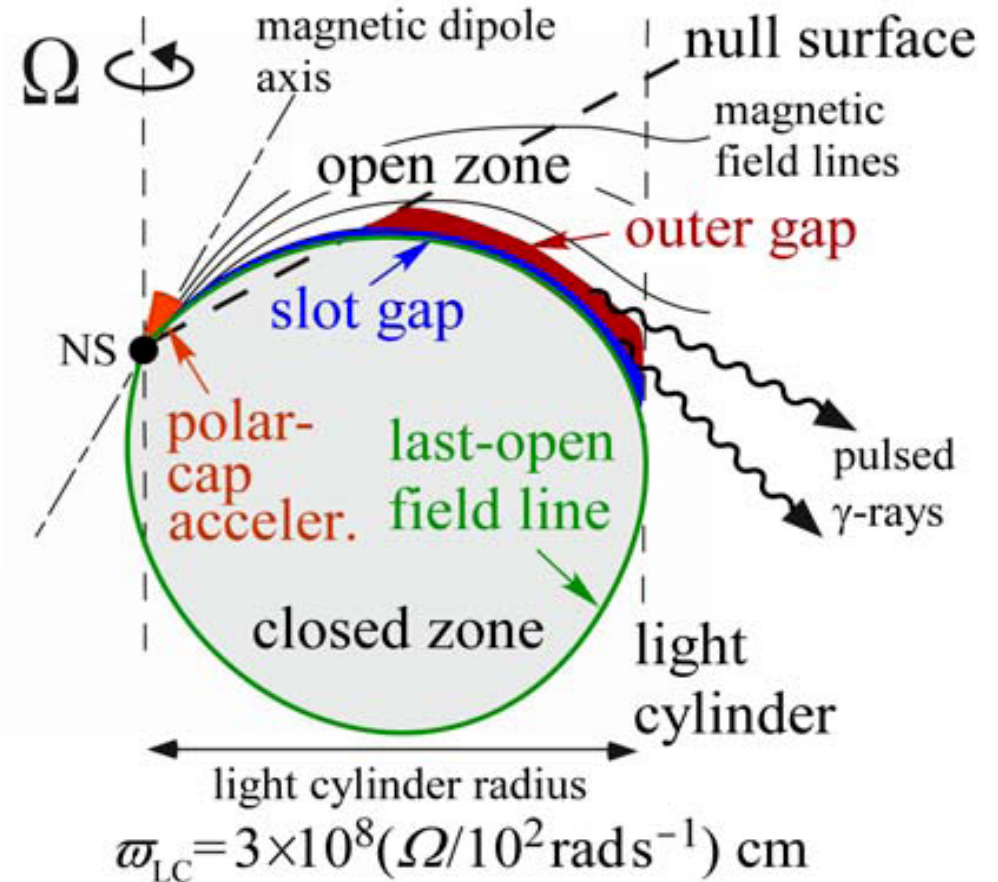
- specific radiative processes,
- location and spatial extent of the emitters,
- geometry (i.e. inclination and viewing angles)

3D models of magnetospheric gaps

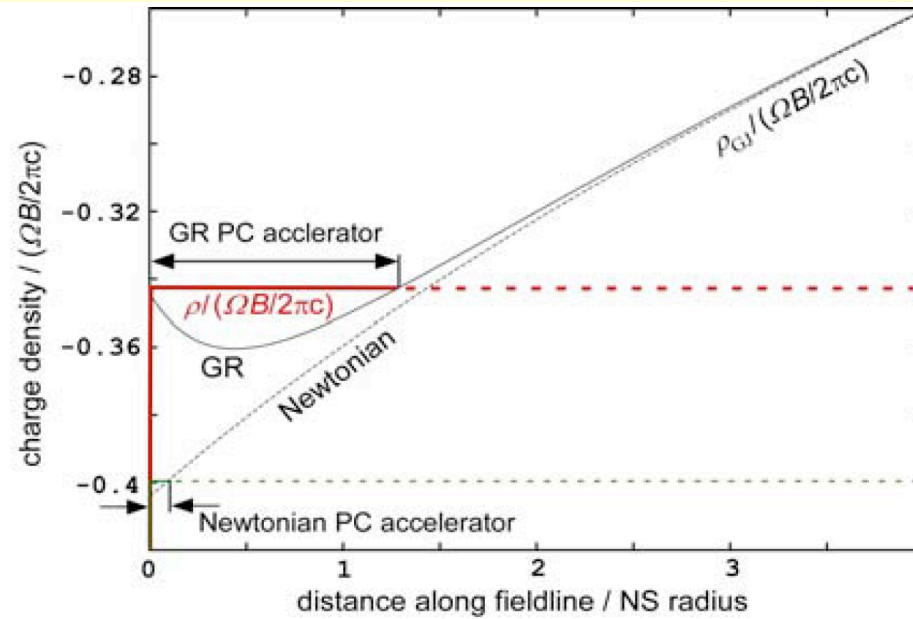
Fig. by K. Hirotani

Variety of sizes and shapes of the accelerating gaps lead to a variety of energy spectra and anisotropies of emission.

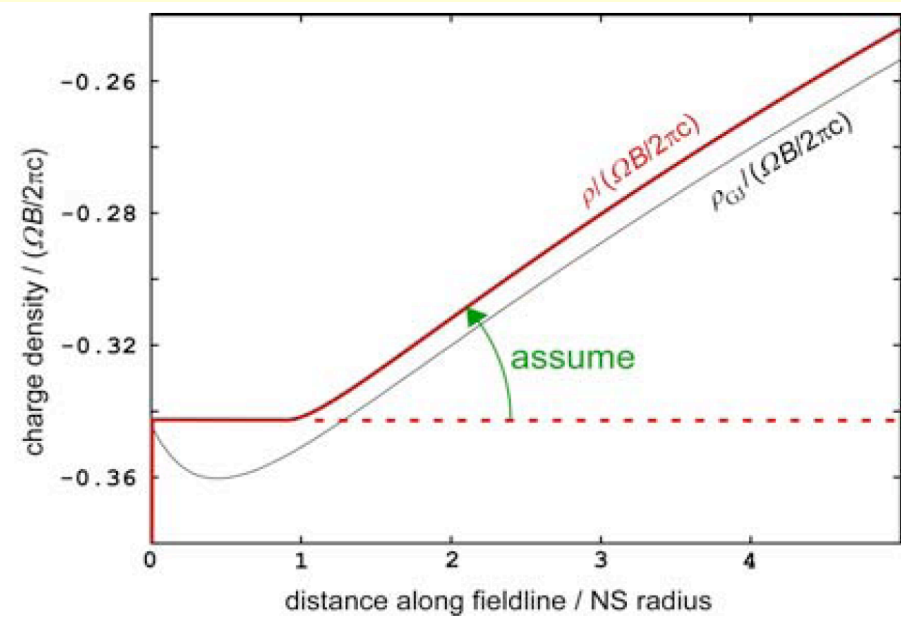
'Observed' characteristics depend strongly on inclination angle and line of sight w.r.t. the spin axis.



Extended Polar Gap
Tsygan & Muslimov



Slot Gap
Muslimov & Harding 2004



$$\nabla \cdot \mathbf{E} = 4\pi (\rho - \rho_{\text{corot}})$$

Slot Gap versus Outer Gap

(an example for the Crab parameters)

Full electrostatic potential drop

$$\Delta V (\text{SG}) \sim 10^{13} \text{ V}$$

$$\Delta V (\text{OG}) \sim 10^{15} \text{ V}$$

Gap width:

$$h_{\text{SG}} \cong 0.04$$

$$h_{\text{OG}} \cong 0.14$$

Outer Gaps more powerful than
Slot Gaps in terms of gamma-ray
luminosity

Slot Gap versus Outer Gap

(an example for the Crab parameters)

Similar Multiplicities:

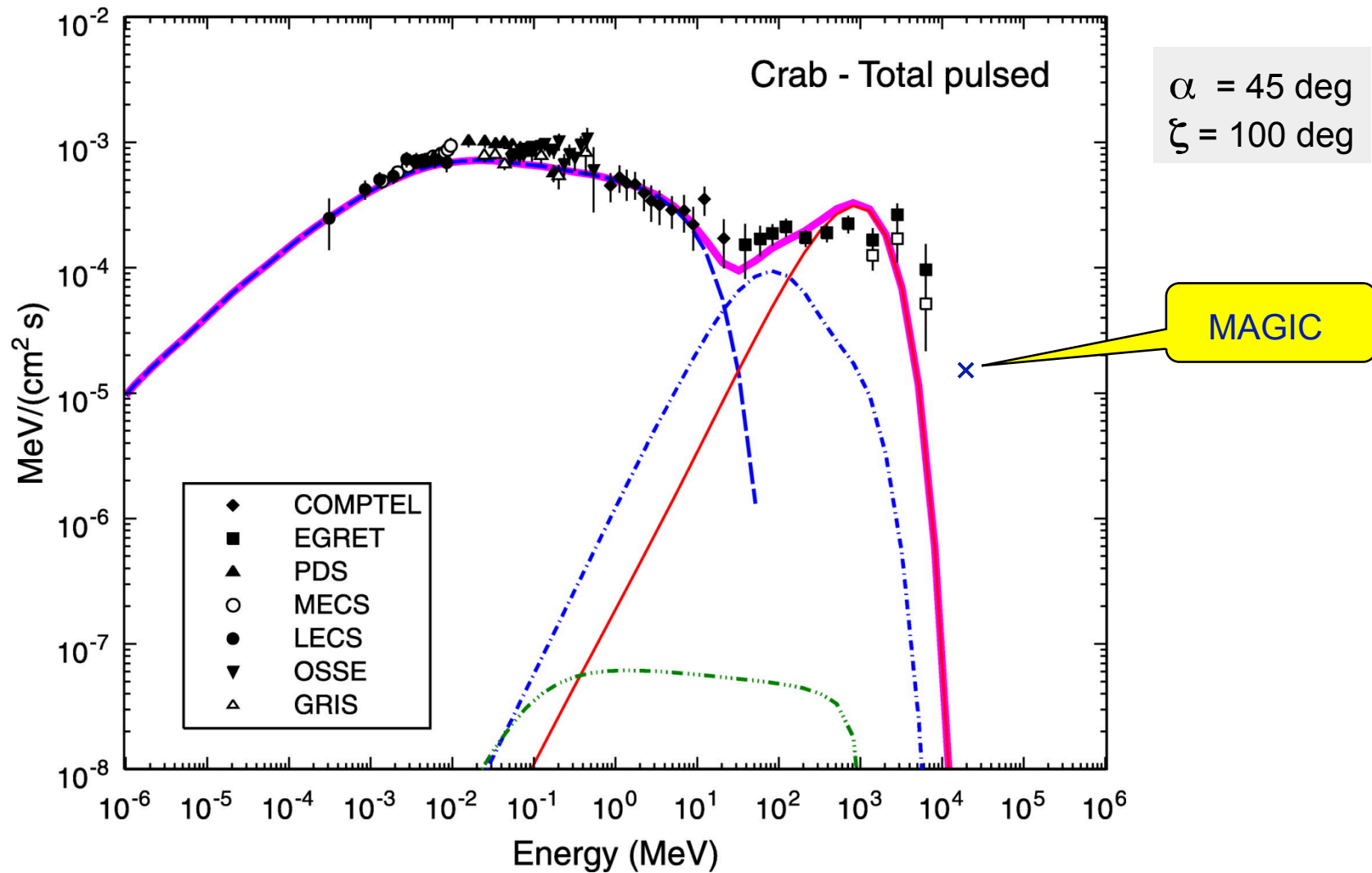
$$M_{e^\pm} \sim 10^4 - 10^5$$

The rate of e^\pm -pairs in the wind:

$$M_{e^\pm} dN_{GJ} / dt \approx 3 \times 10^{38} \text{ s}^{-1}$$

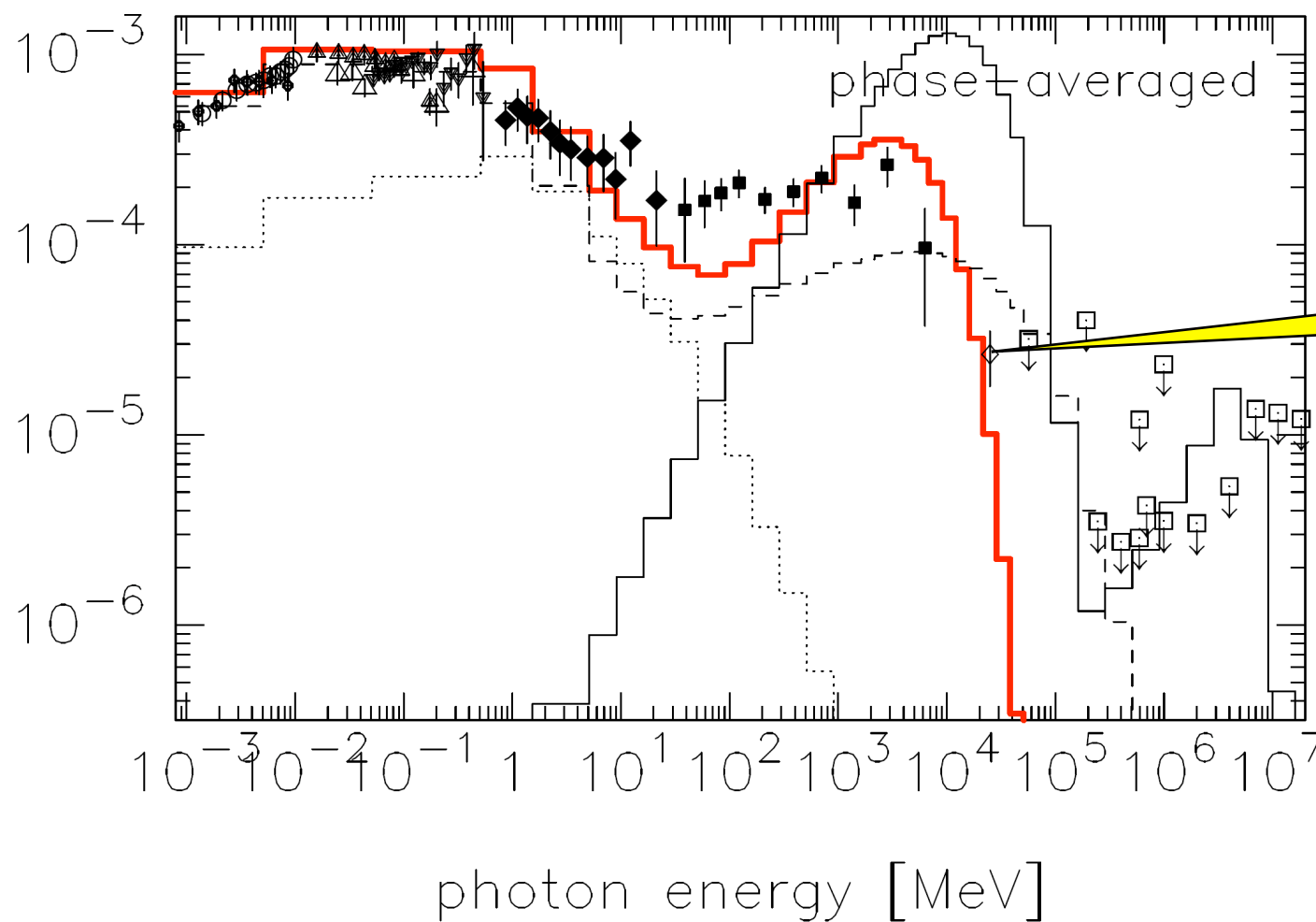
~ 100 times smaller than required
for the Crab nebula

CR + SR (primaries) + SR (pairs) + ICS (primaries with radio)



Synchro-curvature + ICS (pairs with IR)

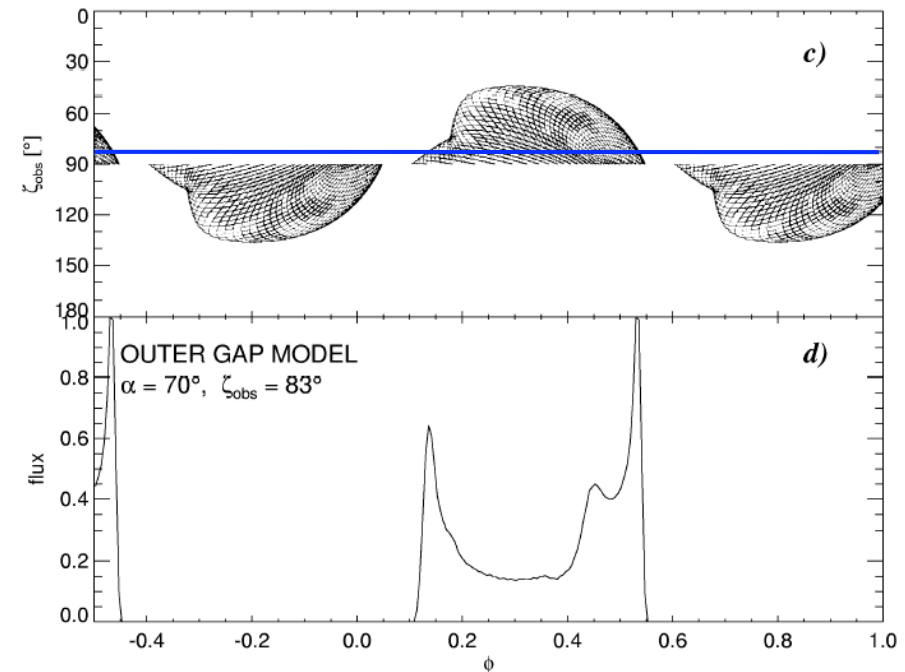
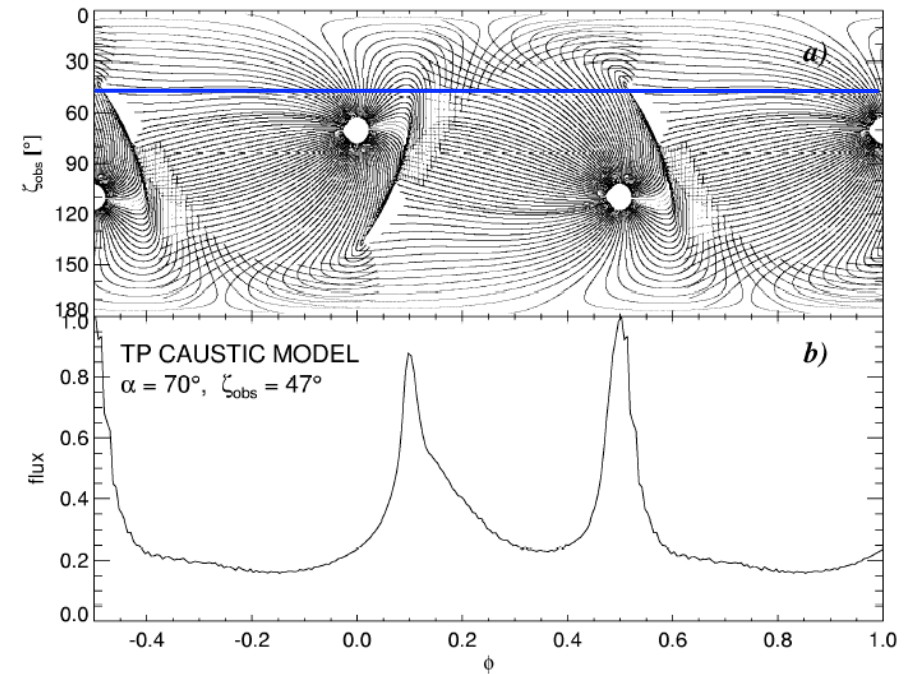
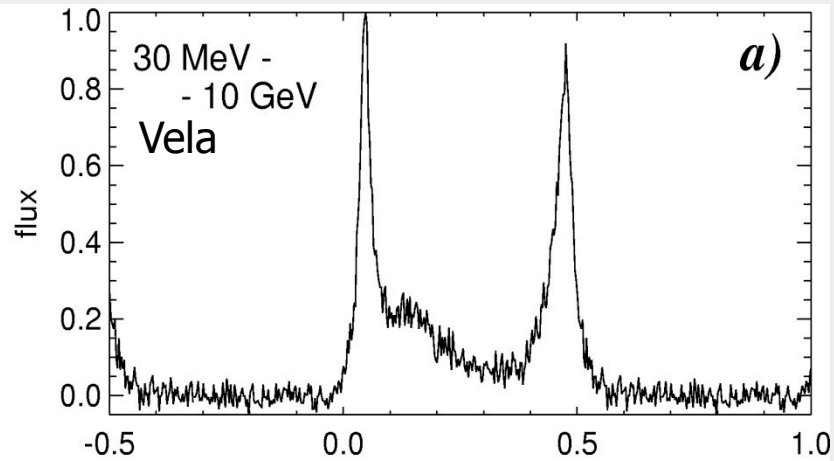
Intrinsic: black line Escaping: red line



Dyks & Rudak 2003

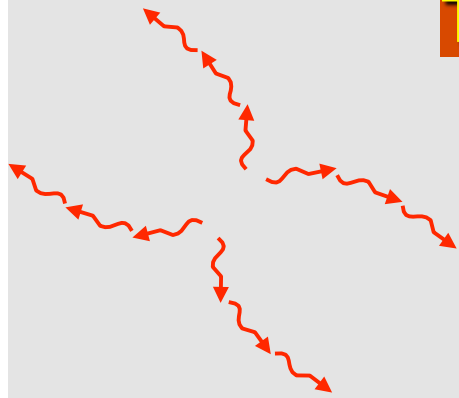
Two-pole caustic model and outer gap model

The Vela pulsar lightcurve (Kanbach 1998)

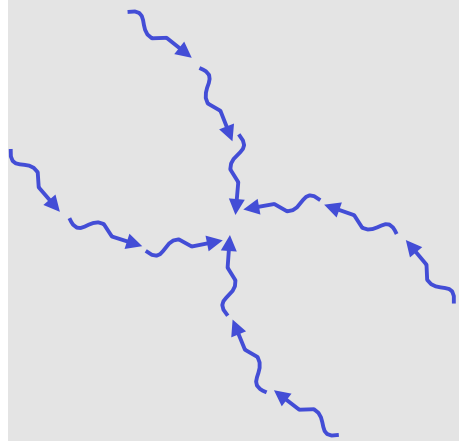


Two-pole caustic slot gap model

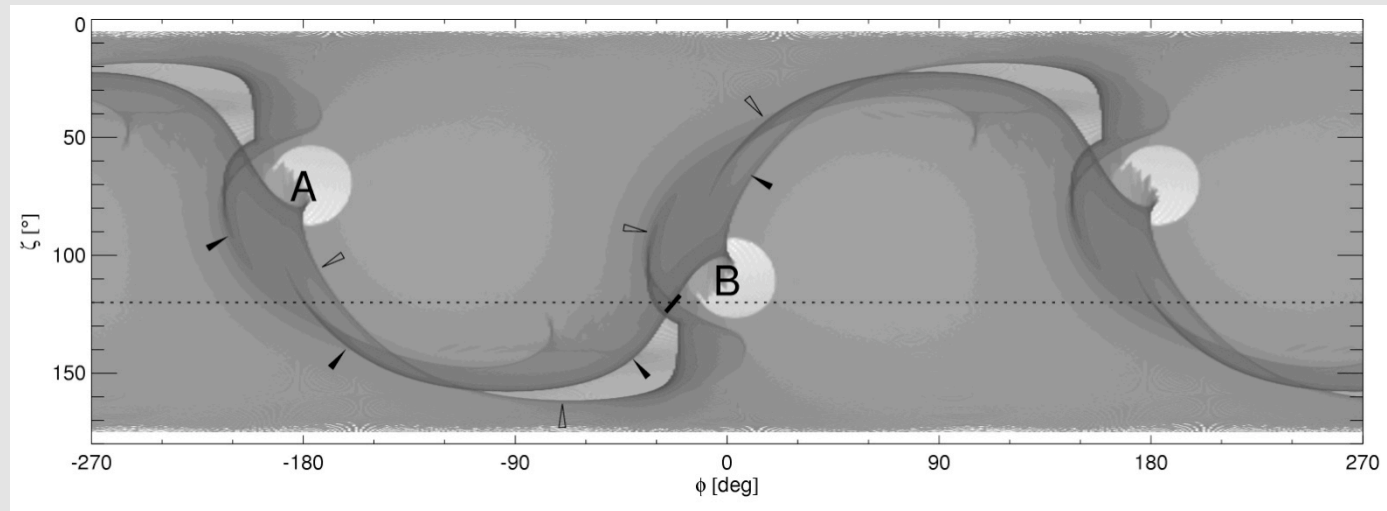
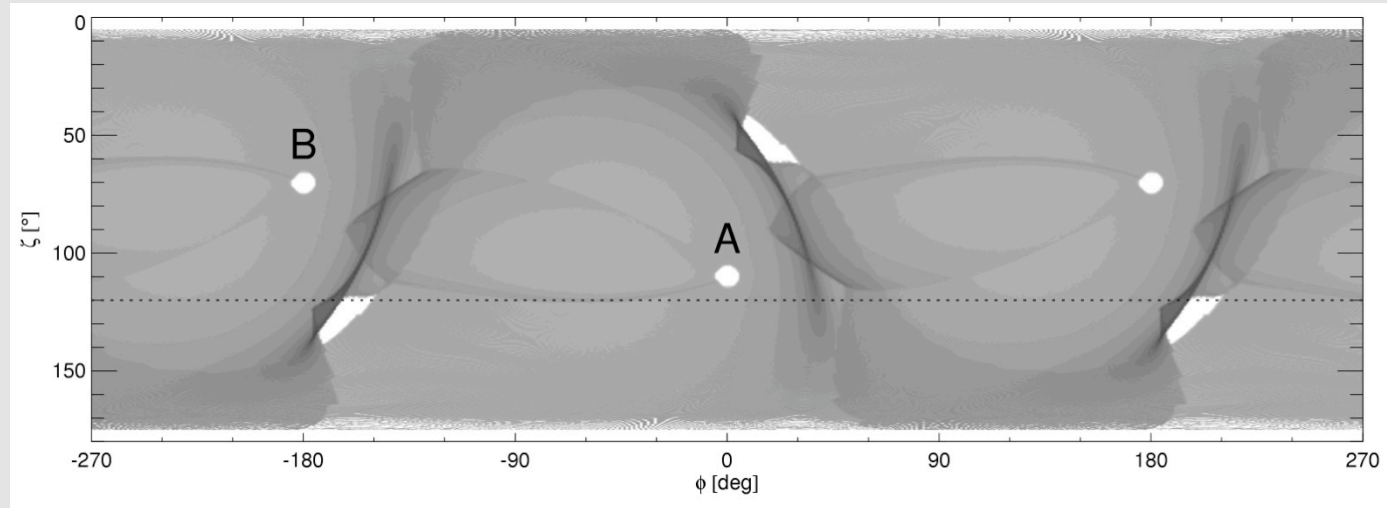
Dyks et al. 2005

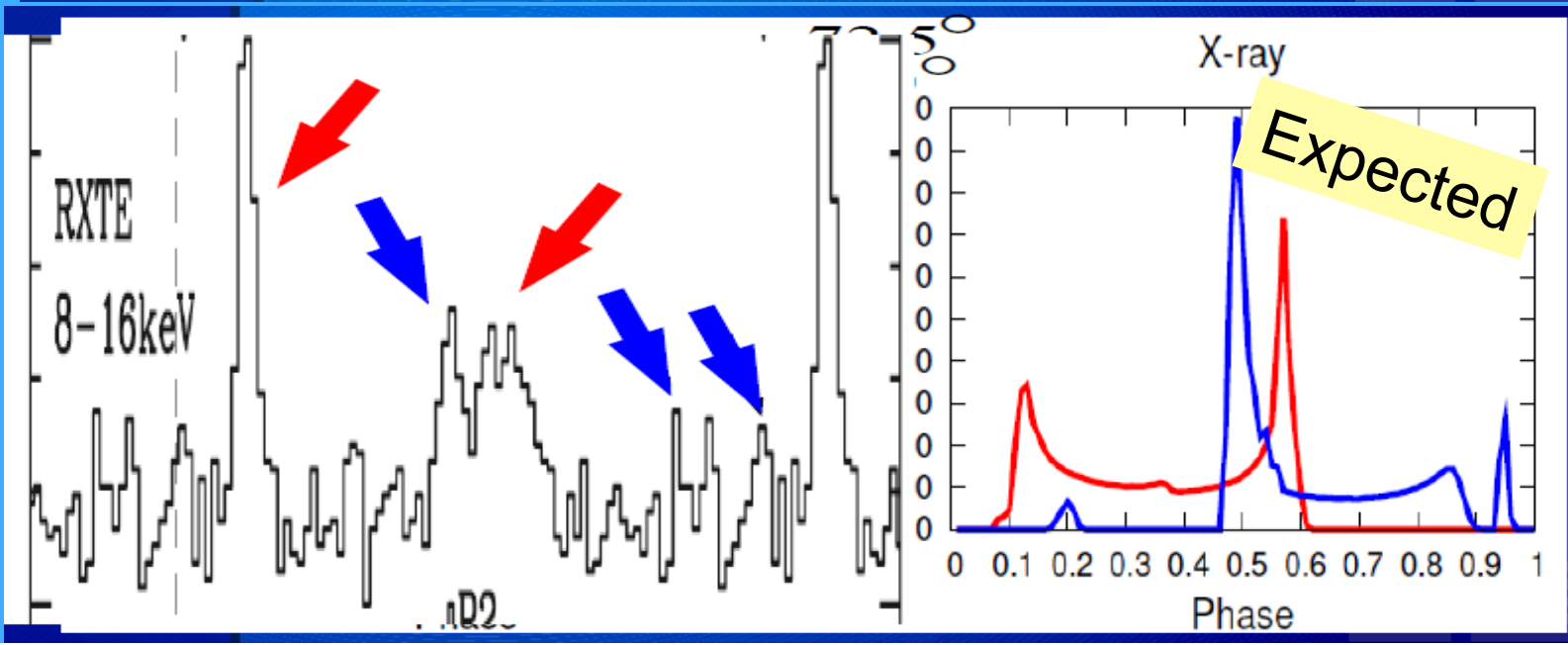
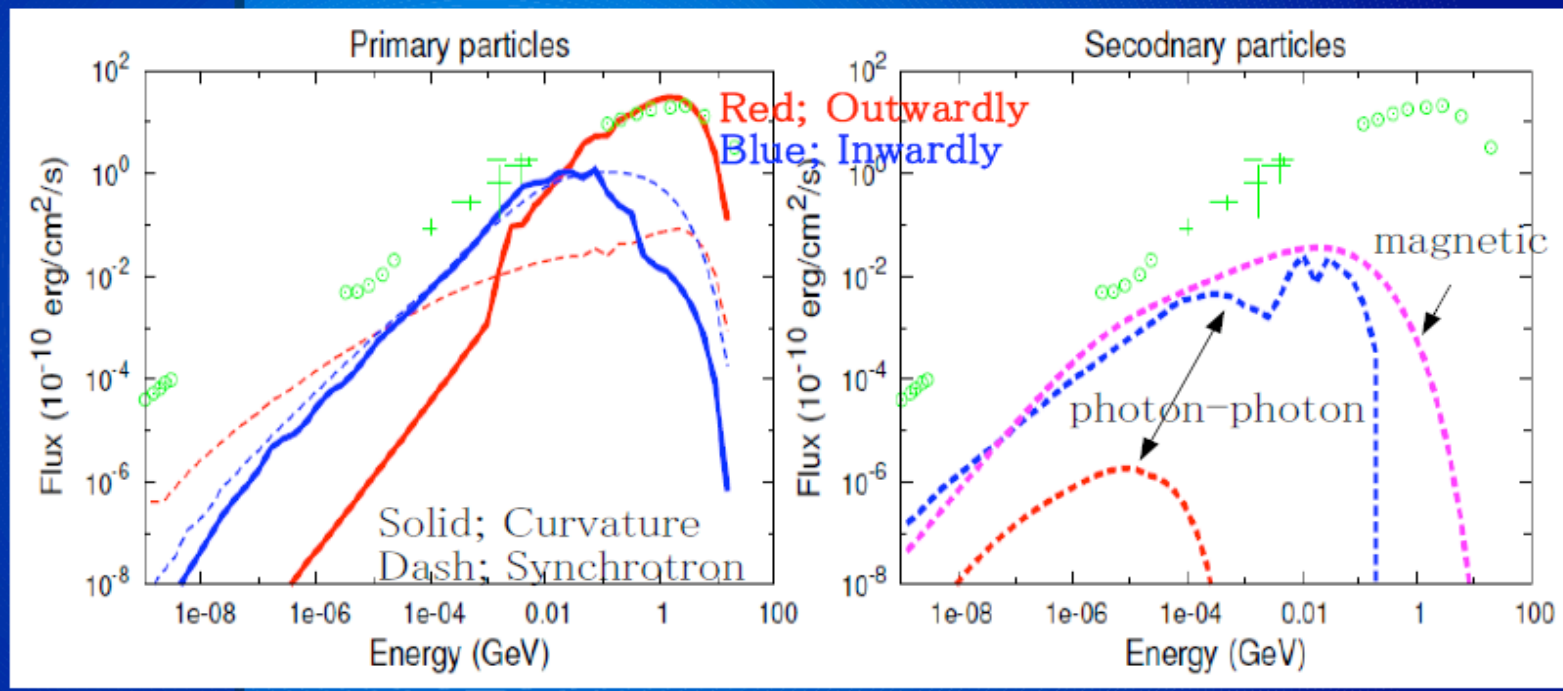


Outward emission
along last open
field lines



Inward emission
along last open
field lines





Millisecond pulsars

Two groups with distinct properties in X-rays:

- 1) luminosity: relatively low,
spectrum: mostly thermal-like
lightcurve: broad single pulse

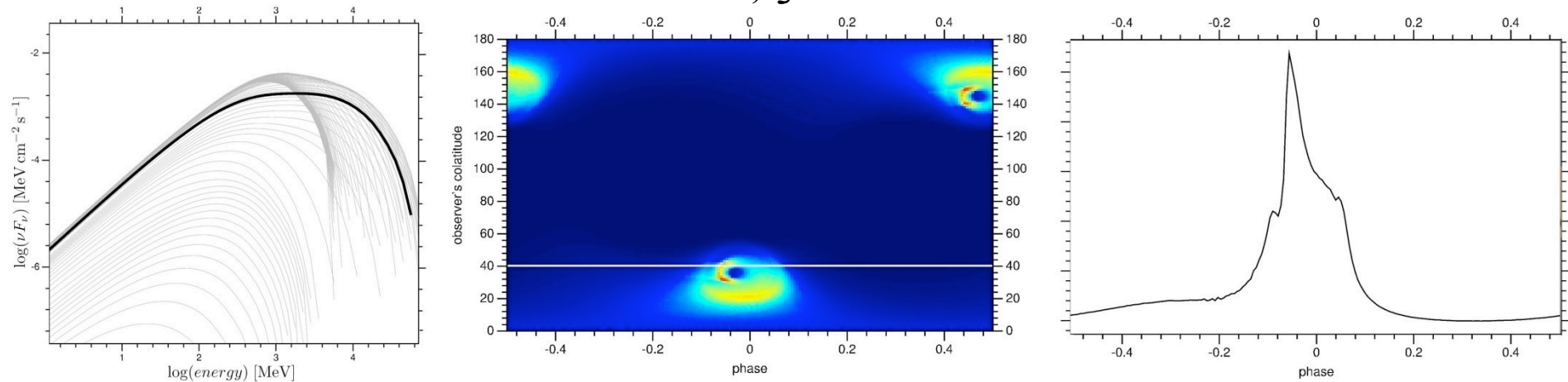
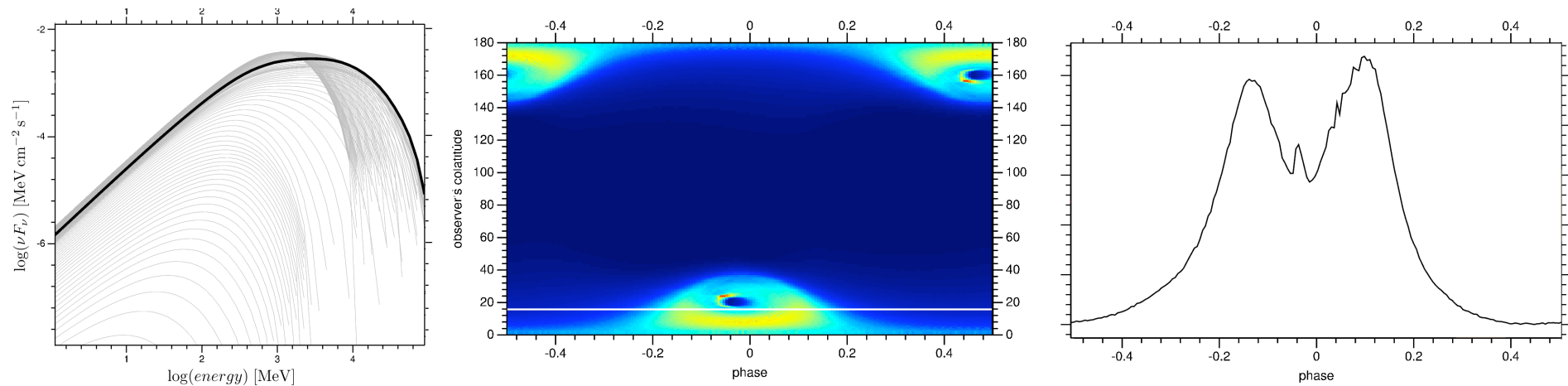
best known: J0437-4715

- 2) luminosity: relatively high,
spectrum: non-thermal,
lightcurve: two narrow peaks

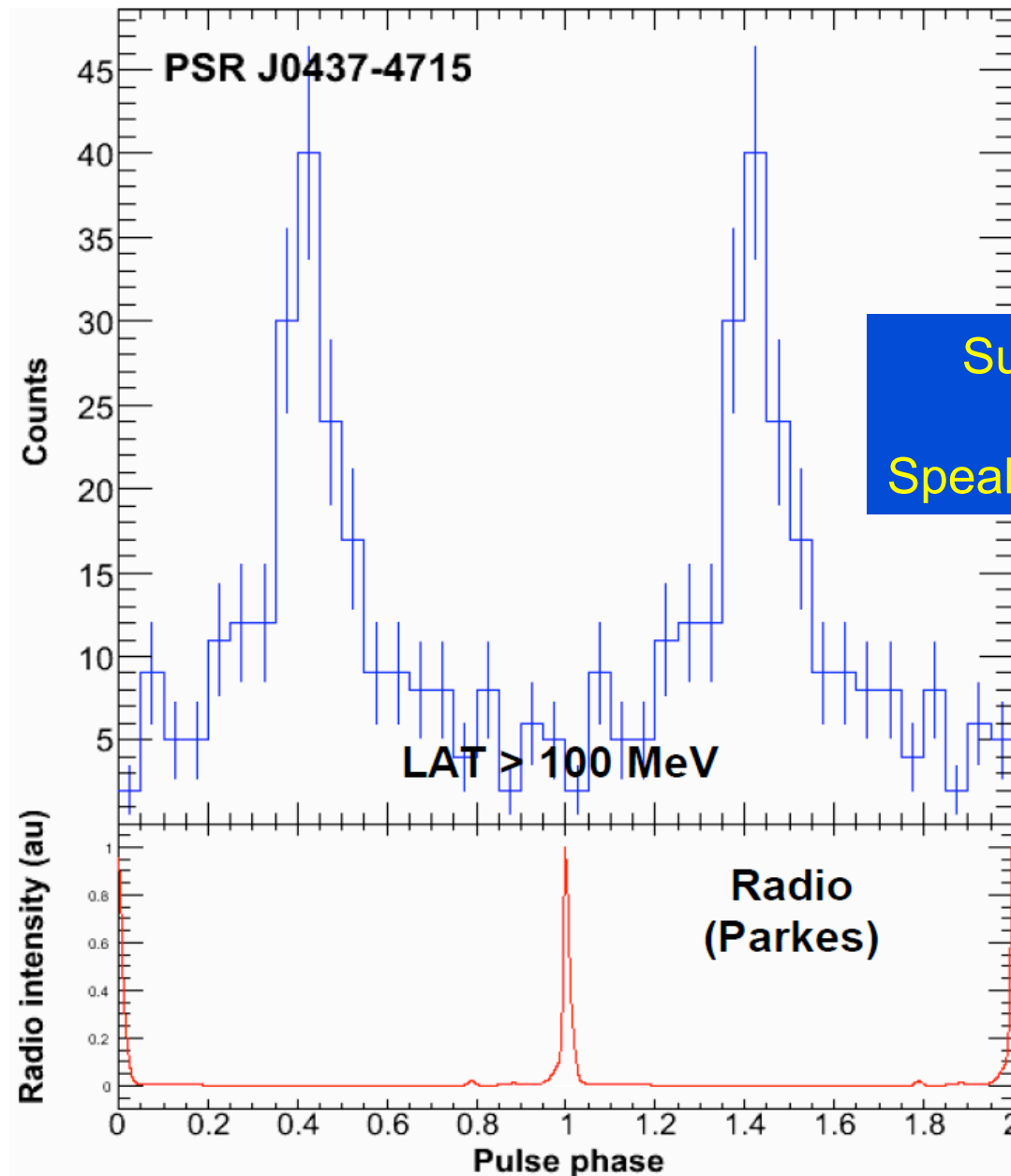
best known: B1821-24, J0218+4232

Are these properties reflected in gamma rays?

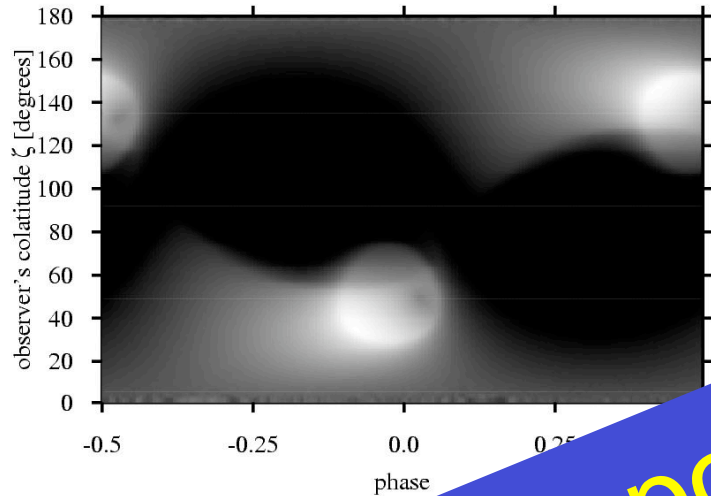
Photon maps and lightcurves above 100 MeV

 $\alpha = 35^\circ, \zeta = 40^\circ$  $\alpha = 20^\circ, \zeta = 16^\circ$ 

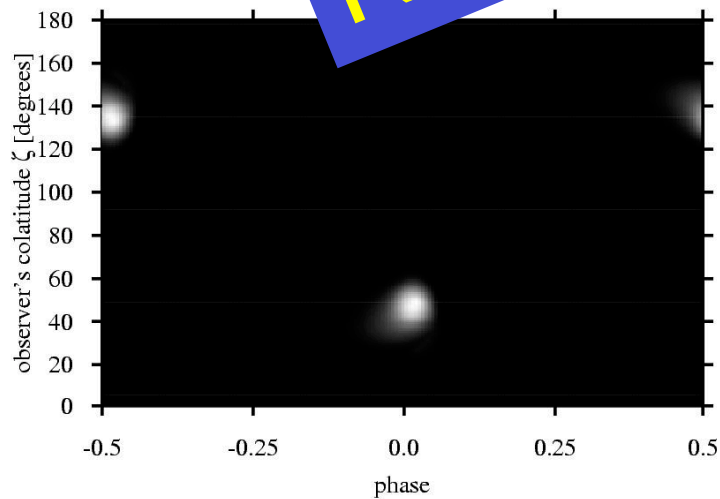
L. Guillemot, Rencontres de Moriond 2009, 7 February 2009



photon flux above 100 MeV



photon flux

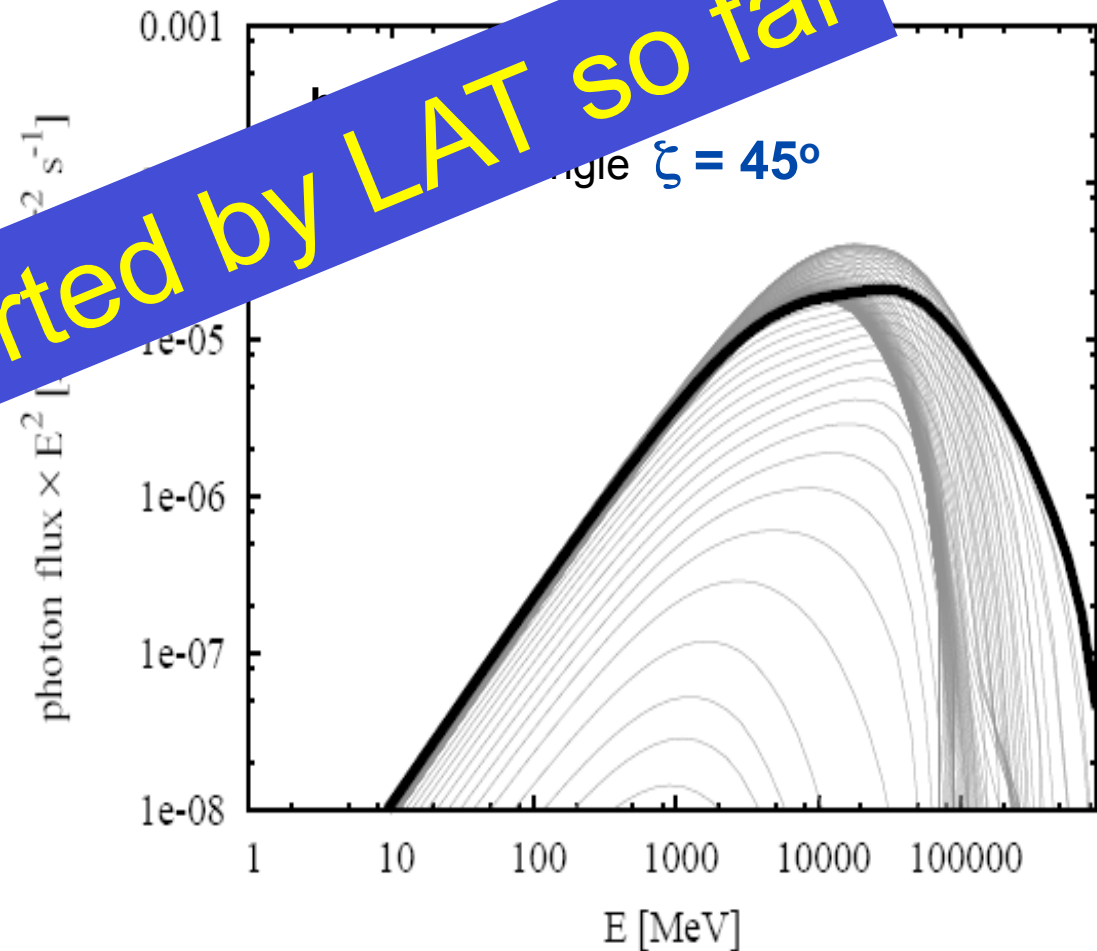


$P = 3.1$ ms, $B = 0.002$ TG

$\alpha = 50^\circ$

$d = 5.1$ km

Not reported by LAT so far



Which models are appropriate for MSPSRs ?

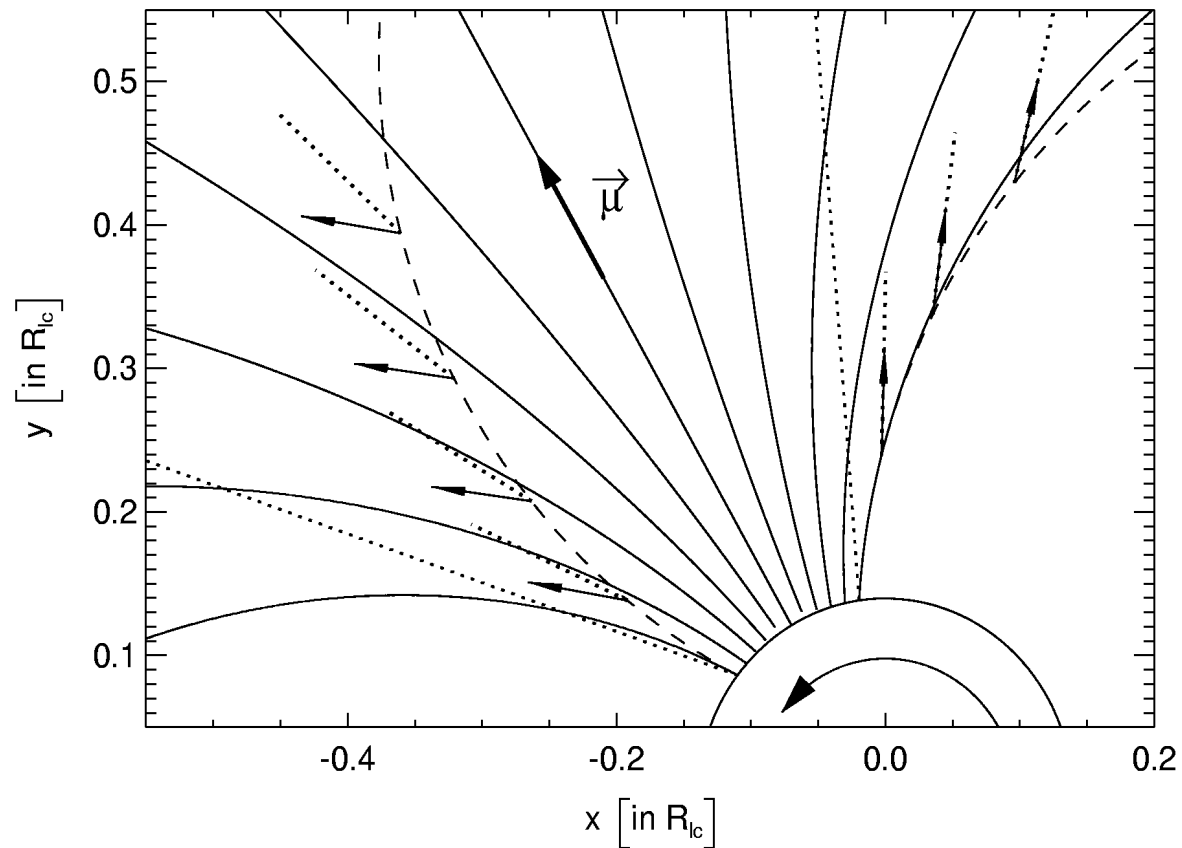
J0218+4232, B1821-24 (but not in gamma-rays so far), J00307+0451:

„mini-Crabs” (highly nonthermal MSPs):

- slot gap or outer gap activity

J0437-4715:

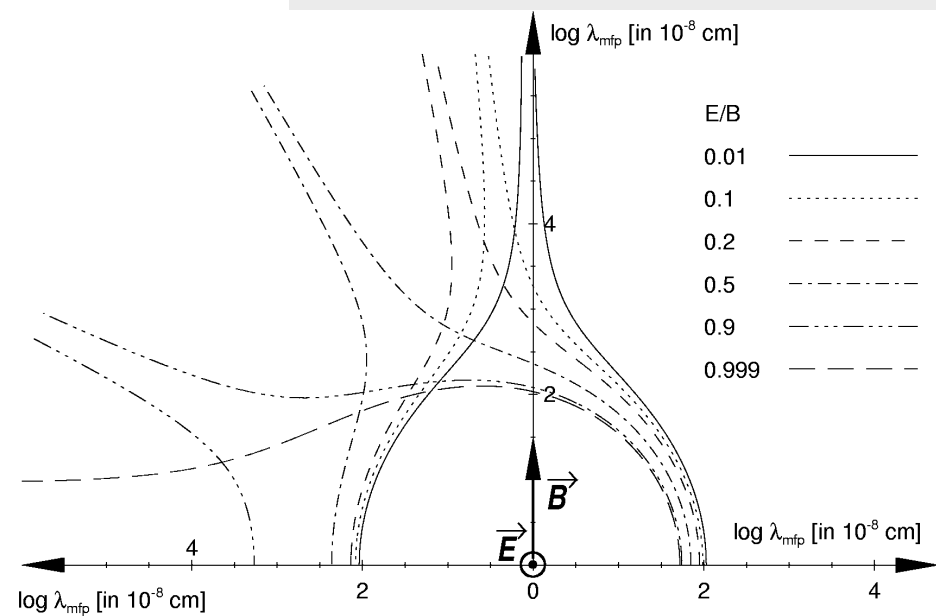
- outer gap activity (??), any room for polar caps?



Rotation leads to non-axisymmetric magnetic absorption



Dyks & Rudak02



Expected signatures of one-photon magnetic absorption generated by rotation (can be relevant for slot gaps and polar caps)



Where to look for them?

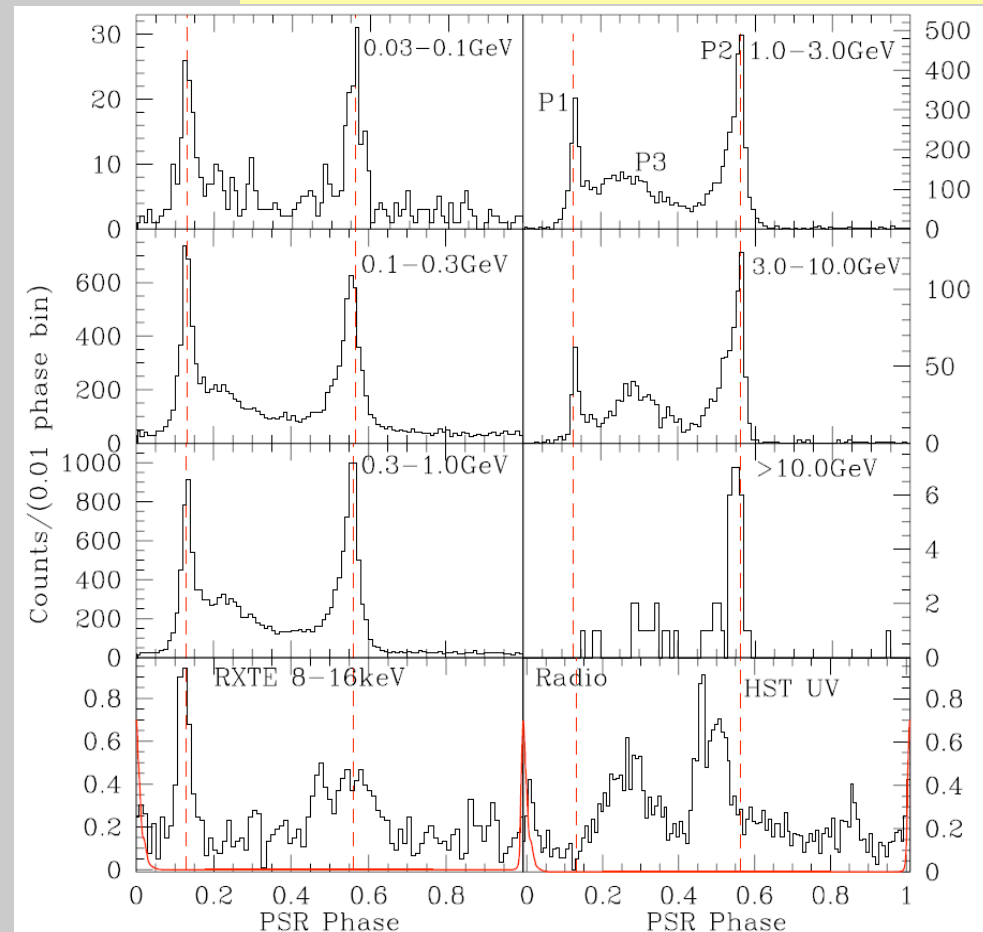
In gamma-ray lightcurves
with double-peak structure.

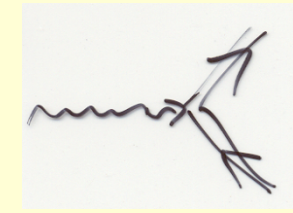
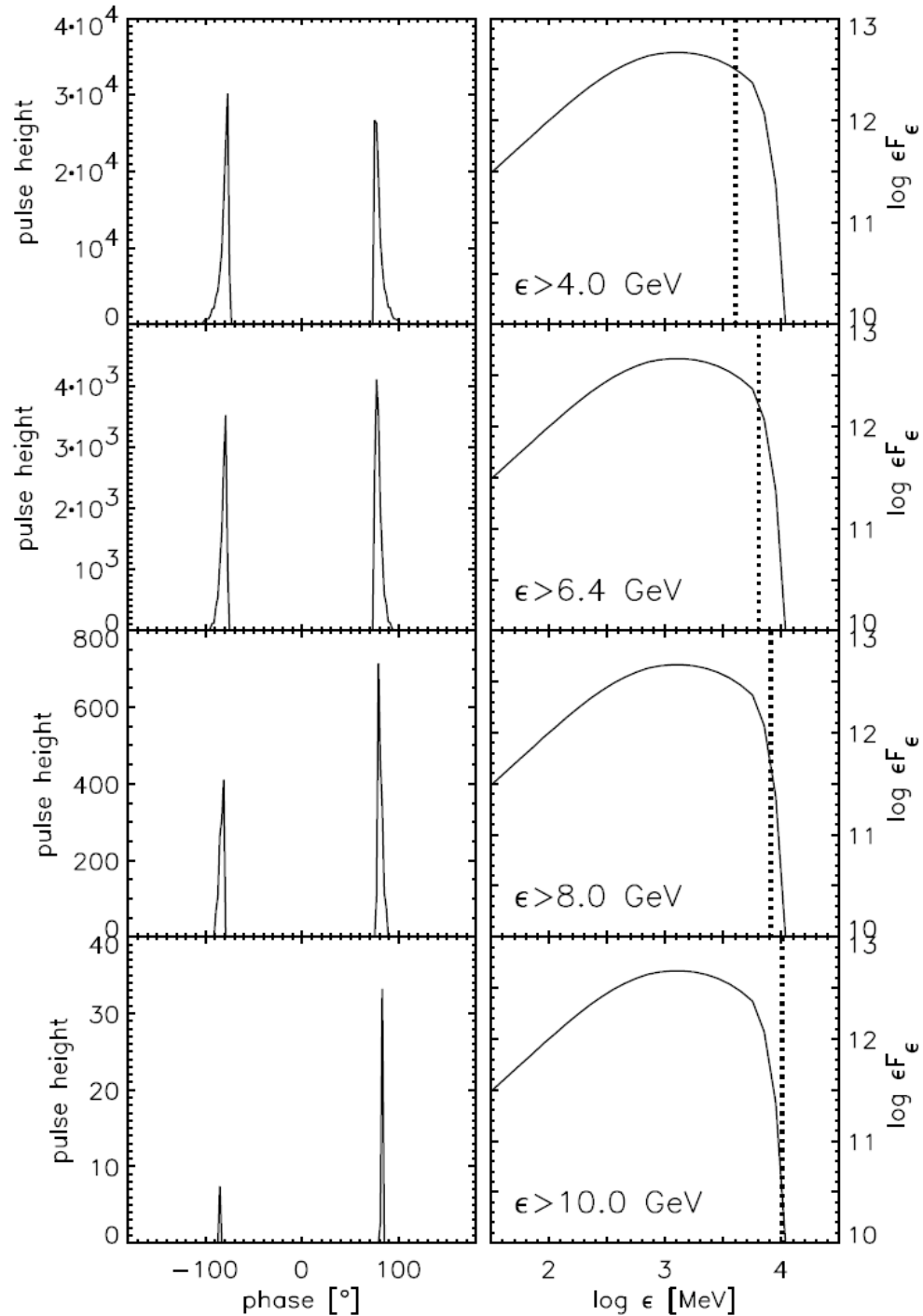
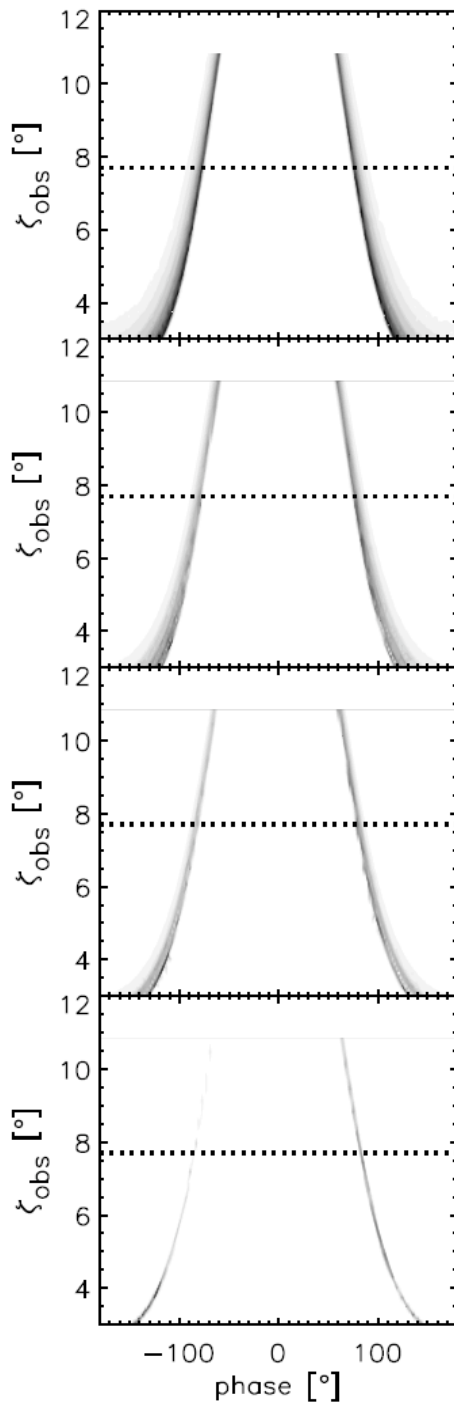
High photon-statistics close to
cutoff energy is required.

Asymmetric magnetic absorption:

- 1) Leading Peak becomes weaker than Trailing Peak close to cutoff energy
- 2) LP-TP separation changes dramatically at cutoff energy

The Vela pulsar, Abdo et al. 2008



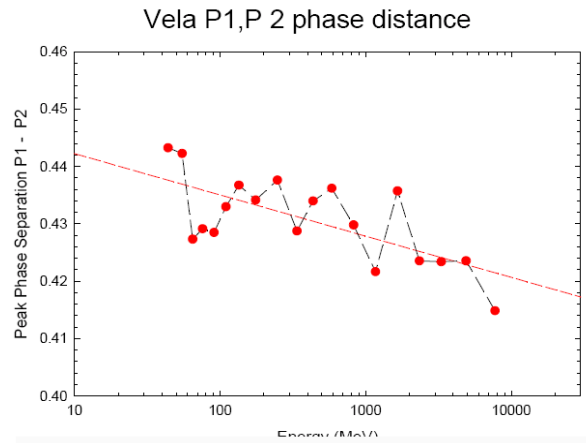


Numerical
example:

Vela-like
Model

(Dyks & Rudak
02)

Peak separation Vela



Fit (30-10000 MeV):
 $\Delta\phi = 0.449 - 7.19 \times 10^{-3} \log(E_{\text{MeV}})$

