

Do we need fine-tuning to create primordial black holes?: Nakama & Wang, arXiv:1811.01126

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Outline

- Fine tuning in cosmology
- Present Limits on abundance of PBHDM
- PBH formation: toy spherical collapse model
- Tuning of primordial fluctuations to get PBHDM

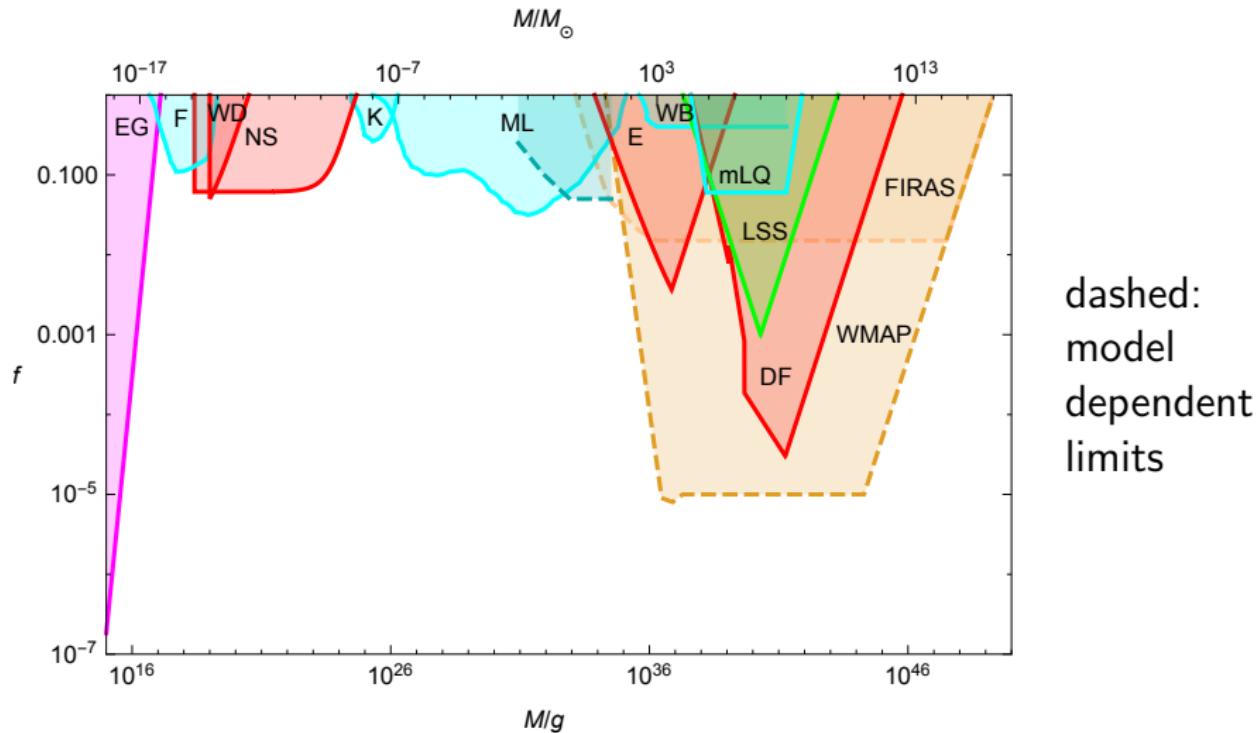
Some numbers that might be fine-tuned

- $\rho_{\text{CDM}}/\rho_{\Lambda} \approx 0.5$ (today)
- $\rho_B/\rho_{\text{CDM}} \approx 0.2$ (since baryogenesis and cdmgenesis)
- $\rho_{\text{He}}/\rho_B \approx 0.05$ (since nucleosynthesis, $T \approx 60\text{keV}$)
- $\rho_{\text{stars}}/\rho_B \approx 0.01$ (since $z \approx 1$)

A time-independent CDM-to-baryon ratio of order unity is especially peculiar because baryogenesis (CP violation) and CDMgenesis (e.g. wimp freezout) are unrelated in most models.

Baryonic structures are not formed if $\rho_b > \rho_{cdm}$ (Silk damping destroys galaxy-size perturbations) or if $\rho_b < \rho_{cdm}/300$ (no radiative cooling to form disks). So if ρ_b/ρ_{cdm} is a random variable (e.g. on the string landscape), then anthropic selection plays a role.

Limits: B.Carr et al: 1607.06077



$M < 10^{-17} M_\odot$: Hawking rad; $10^{-7} < M < 10 M_\odot$: Microlensing
 $M > 10^2 M_\odot$: disruption of stellar systems (binaries, disks...).

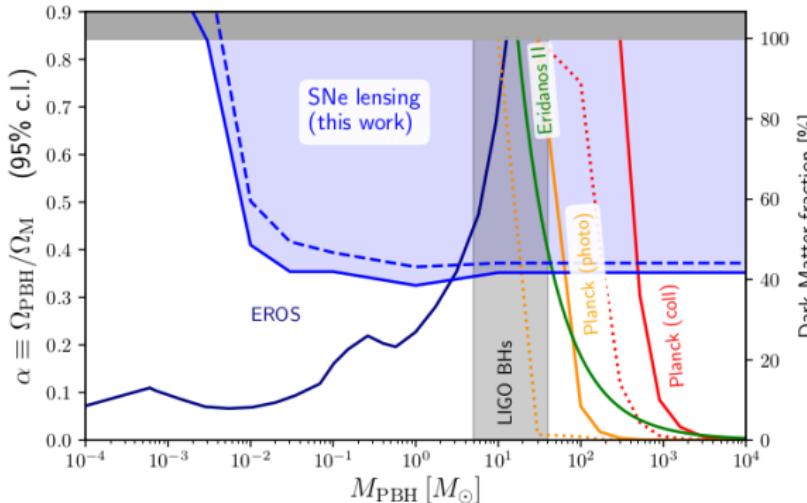
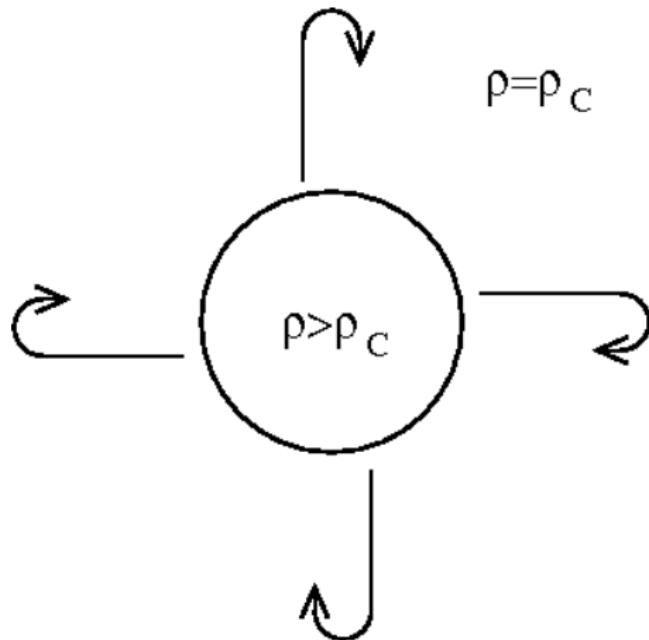


FIG. 3. Bounds on the abundance of PBHs as a function of the mass (95 % confidence level). The analysis of SNe lensing using the JLA (solid) and Union 2.1 compilations (dashed) constrain the PBH fraction in the range $M \gtrsim 0.01 M_\odot$. This range includes the masses of black hole events observed by the Laser Interferometer Gravitational-Wave Observatory (gray), only weakly constrained by previous data including microlensing (EROS [29]), the stability of stellar compact systems (Eridanus II [30] [31]) and CMB [32] [33]. The CMB excluded regions correspond to Planck-TT (solid), Planck-full (dotted) for the limiting cases of collisional (red) and photo-ionization (orange) (see [33] for details).

Lack of SN
microlensing

Zumalacárregui &
Seljak
arXiv:1712.02240

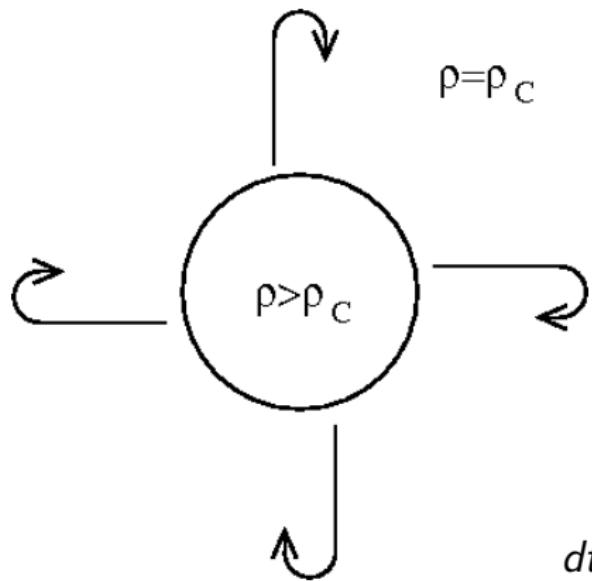
Spherical collapse model



A critical matter-only universe with a small spherical expanding region with $\rho > \rho_c$.

Overdense region acts like a mini-closed universe:
Gravity excess stops the its expansion starting a contraction phase

Spherical collapse model



Spherical symmetry \Rightarrow dynamics of $R(t)$ independent of rest of universe.
Conservation of energy of test particle
a boundary:

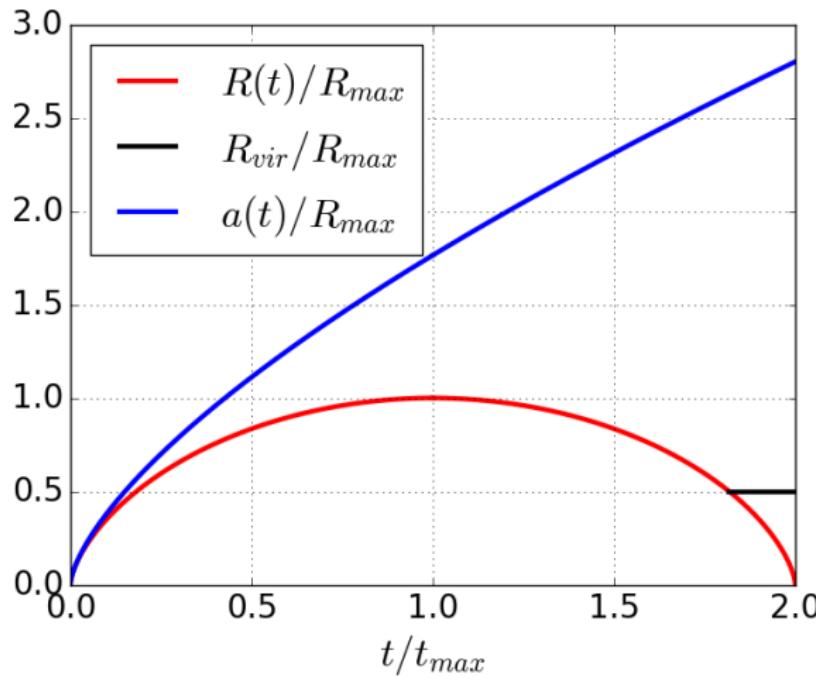
$$(1/2)\dot{R}^2 - \frac{GM}{R} = -\frac{GM}{R_{max}}$$

M = mass contained in spherical region (time-independent)

$$dt = \frac{dR}{\sqrt{2\Phi_g} \sqrt{R_{max}/R - 1}} \Rightarrow t(R)$$

Model characterized by R_{max} and $\Phi_g = GM/R_{max} < \sim 10^{-5}$)

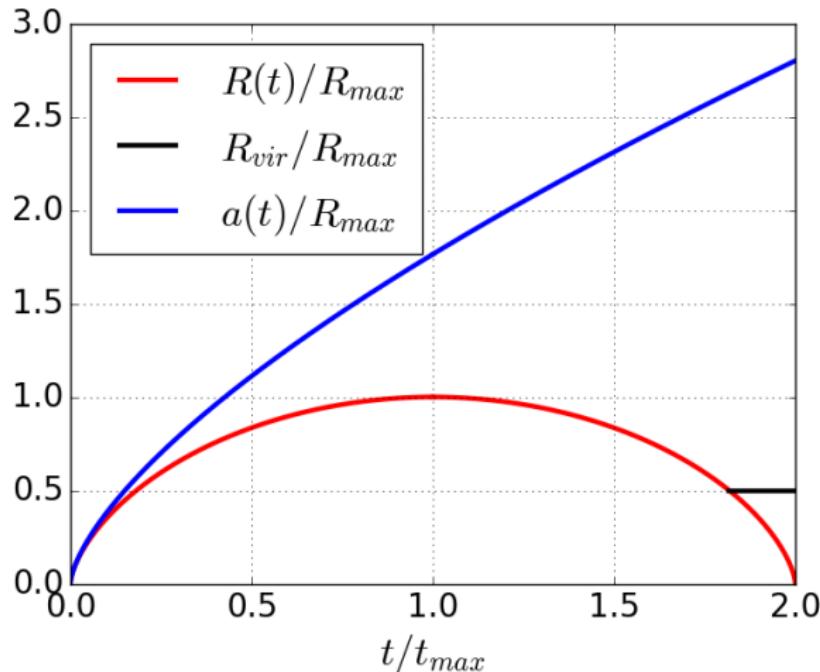
$R(t)$: expansion, collapse, virialization



At t_{max} , small density contrast:

$$\frac{M}{\frac{4\pi}{3}R(t_{max})^3} \approx 5.5\bar{\rho}(t_{max})$$

Gravitational potential



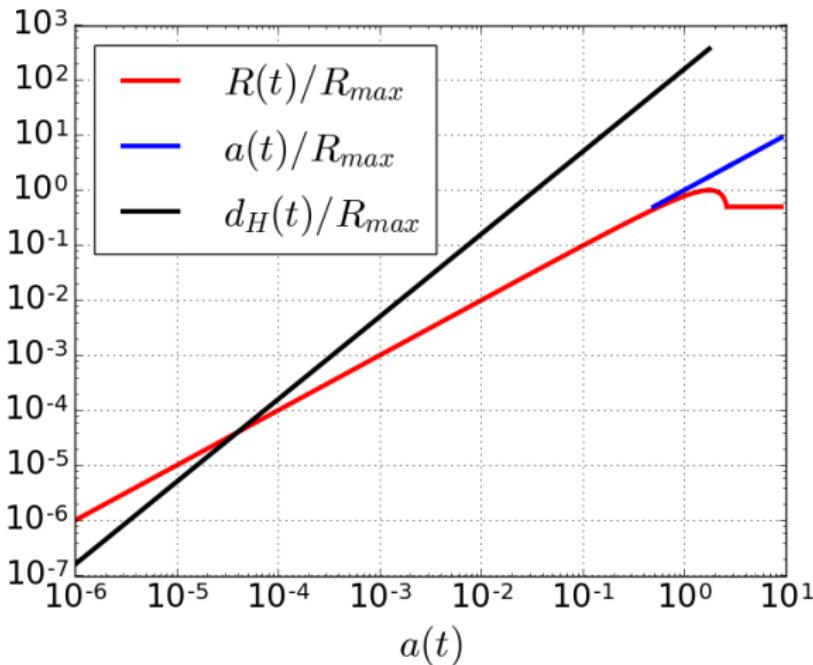
Potential fluctuation at $t \ll t_{max}$ equals potential at maximum expansion:

$$\frac{G(4\pi R^3/3)\Delta\rho}{R(t)} = \frac{GM}{R_{max}}$$

and \approx depth of virialized potential well:

$$\frac{GM}{R_{vir}} \approx 2 \frac{GM}{R_{max}}$$

$R(a)$: Hubble entry



$$R(t) \propto a$$

$$d_H(t) \propto a^{1.5} \\ = \sqrt{3/8\pi G \bar{\rho}}$$

$$\Rightarrow R_{max} \approx R_{enter}/\Phi_g \\ \approx \sqrt{\Phi_g} d_H(t_{max})$$

The only bound structures that can be formed during the radiation epoch are black holes ($\Phi_g \sim 1$): they form fast enough to avoid dispersal by acoustic waves after entry (since $R_{enter} \sim R_{max}$)

Primordial Black Holes as DM

- Should form before nucleosynthesis
(since nucleosynthesis $\Rightarrow \Omega_b h^2 = 0.02 < \Omega_m h^2$ from CMB)

- Form at Hubble entry:

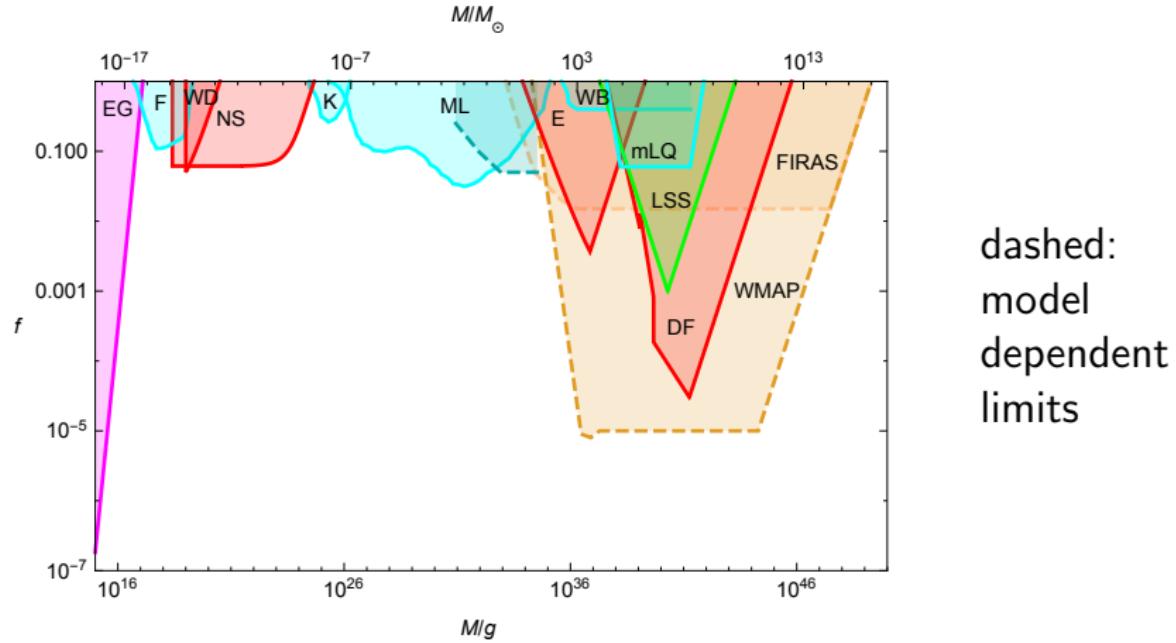
$$\begin{aligned} M_{BH}(t_{\text{enter}}) &\approx d_H^3(t_{\text{enter}})\rho(t_{\text{enter}}) \\ &\approx (G T_{\text{enter}}^4)^{-3/2} T_{\text{enter}}^4 \\ &\approx m_{pl}^3 / T_{\text{enter}}^2 \end{aligned}$$

- Fraction, f_{col} , of space that must collapse in order to make a fraction f_{BH} of today's darkmatter:

$$\begin{aligned} \rho_{BH} &\approx f_{BH} 10^4 \rho_\gamma \approx f_{BH} 10^4 T_0^4 \text{ (today)} \\ &\approx f_{col} T_{\text{enter}}^4 \times (T_0 / T_{\text{enter}})^3 \\ \Rightarrow f_{col} &\approx f_{BH} 10^4 T_0 / T_{\text{enter}} \approx f_{BH} 10^4 T_0 M_{BH}^{1/2} / m_{pl}^{3/2} \end{aligned}$$

$$T_{\text{enter}} = 1 \text{ GeV} \quad M_{BH} = 1 M_\odot \quad f \approx f_{BH} 10^{-9}$$

Limits: B.Carr et al: 1607.06077



dashed:
model
dependent
limits

$$T_{\text{enter}} = 1 \text{ MeV} \quad M_{BH} = 10^6 M_\odot \quad f \approx f_{BH} 10^{-6}$$

$$T_{\text{enter}} = 1 \text{ GeV} \quad M_{BH} = 1 M_\odot \quad f \approx f_{BH} 10^{-9}$$

$$T_{\text{enter}} = 10^8 \text{ GeV} \quad M_{BH} = 10^{-16} M_\odot \quad f \approx f_{BH} 10^{-17}$$

Collapse fraction for Gaussian perturbations

$$P(\phi) \sim \exp(-\phi^2/2\sigma_\phi^2)$$

$$f_{col} \sim P(\phi = 1) \sim \exp(-1/2\sigma_\phi^2) \approx f_{BH} T_{eq} M_{BH}^{1/2} / m_{pl}^{3/2} \approx f_{BH} 10^{-9}$$
$$\Rightarrow \text{need } \sigma_\phi \approx 0.1 \text{ if } f_{BH} \sim 1$$

- No PBH if $\sigma_\phi \approx 10^{-5}$
⇒ new physics needed if $f_{BH} \sim 1$
e.g. a second inflationary scalar field to give large k dependence to power spectrum
- σ_ϕ is a logarithmic function of ($f_{BH}, T_{eq}, M_{BH} \dots$)
Loose constraints on (f_{BH}, \dots) imply tight constraints on σ_ϕ .

Nakama and Wang: $1 > \rho_B/\rho_{CDM} > 1/300 \Rightarrow 0.083 < \sigma_\phi < 0.091$

Degree of fine-tuning = $(0.091 - 0.083)/0.87 \approx 0.08$