



**ISYA 2024 – THE INTERSTELLAR MEDIUM (ISM):  
LECTURE 3.  
Heating & Cooling – The Phases of the ISM**

**Frédéric GALLIANO**

**CEA Paris-Saclay, France**

**October 1st, 2024**

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## 1 COOLING & HEATING OF THE GAS

- The gas heating processes
- The gas cooling function
- The five thermal phases of the ISM

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- Solutions in simple cases
- Dust radiative transfer with more complex geometries

# Outline of the Lecture

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## 3 STAR-FORMING REGIONS

- The Structure of Star-Forming Regions
- H II regions
- PhotoDissociation Regions (PDRs)

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## 4 CONCLUSION

- Take-away points
- References

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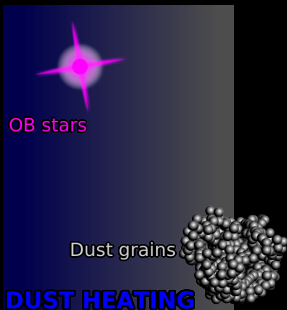
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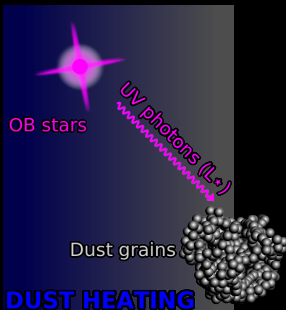
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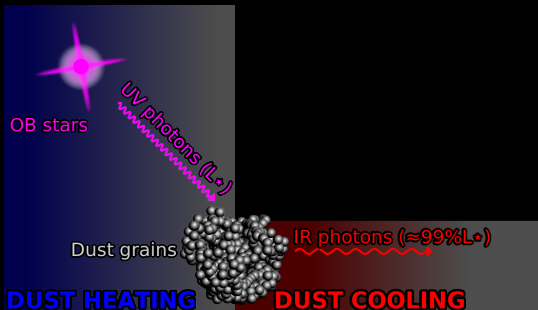




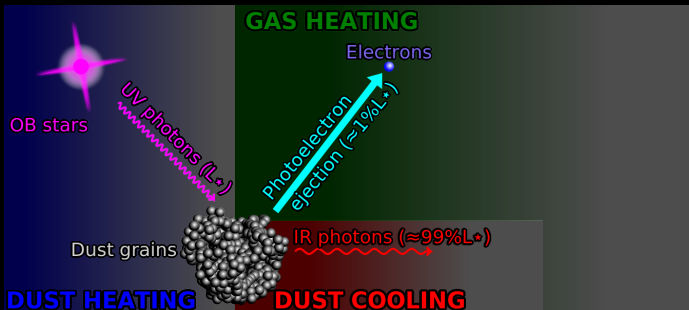
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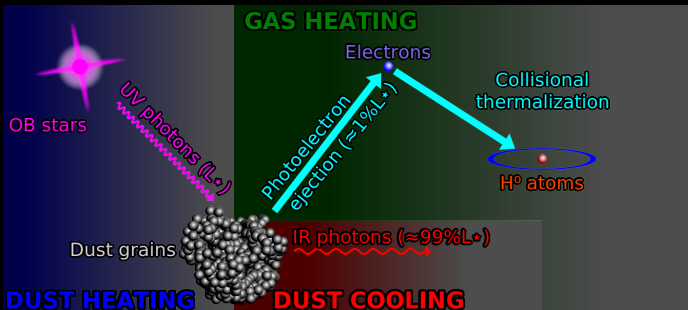
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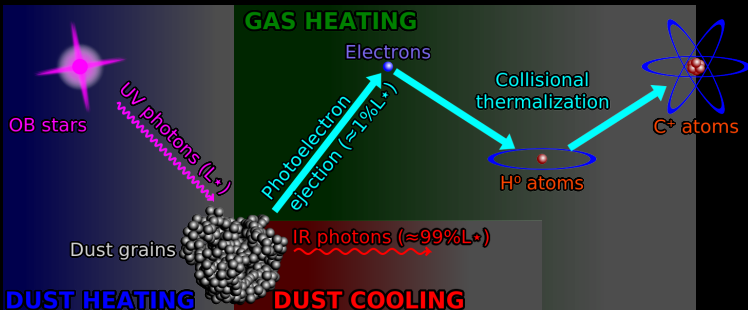
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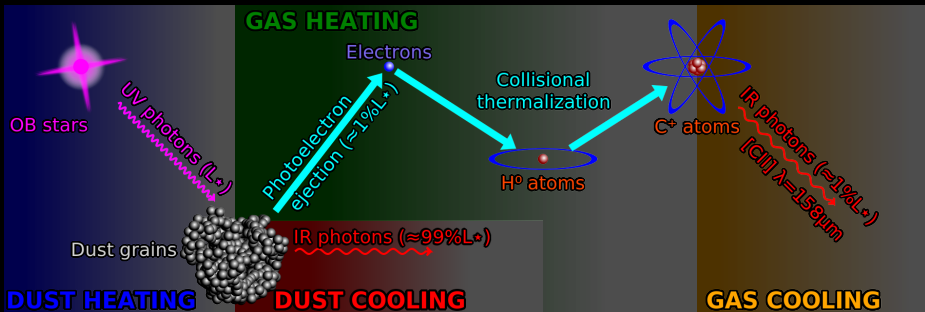
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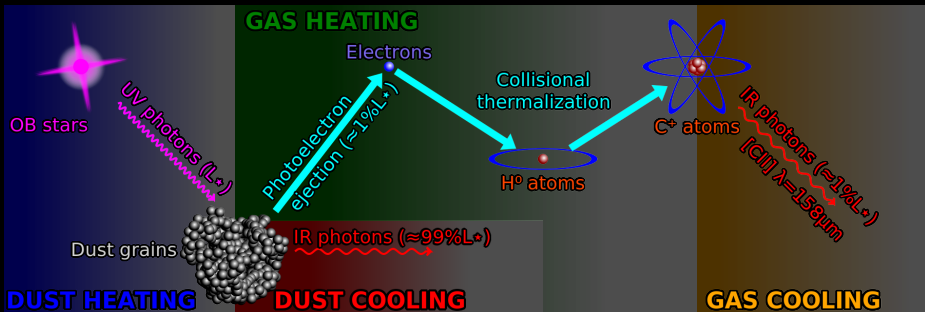
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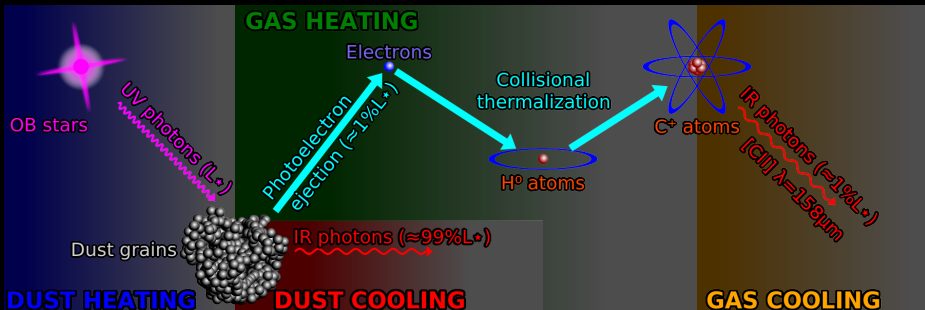
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The main neutral gas heating mechanism

[C II] $_{158\mu m}$ , [O I] $_{63\mu m}$   $\rightarrow$  usually the brightest ISM lines in galaxies (e.g.; Cormier et al. 2019).

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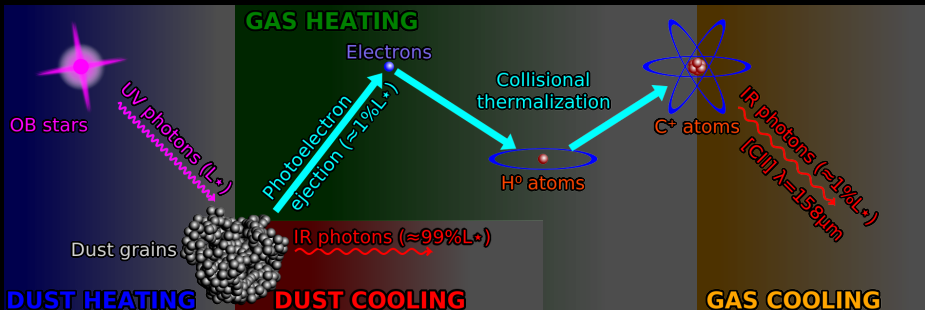
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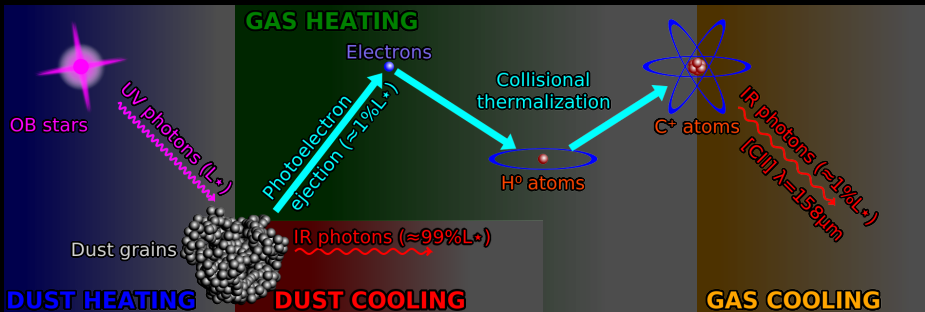
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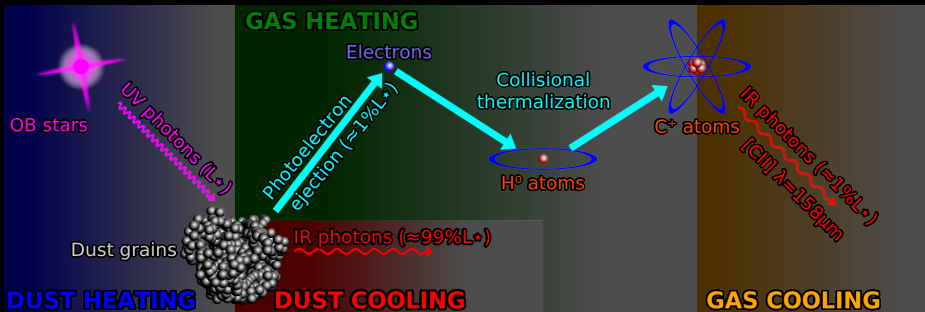
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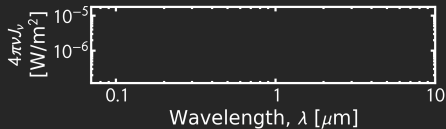
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Most of the grain cumulated area is in small sizes  $\Rightarrow$  PE dominated by PAHs & nanograins.

# Thermal Phases | The Photoelectric Heating Efficiency

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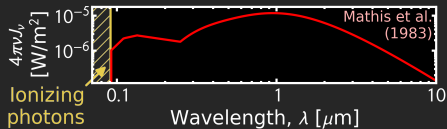
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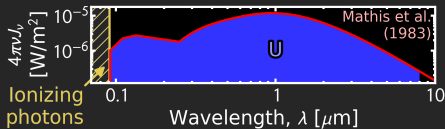


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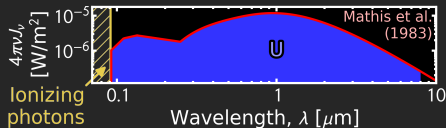


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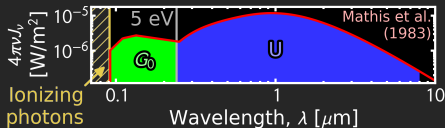
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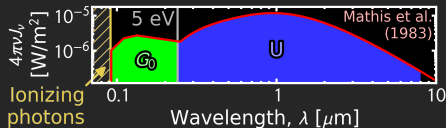


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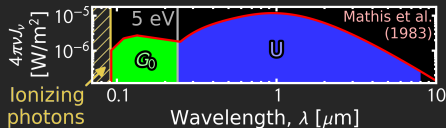


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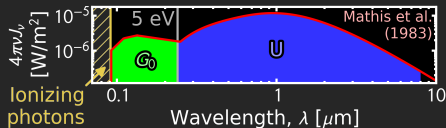


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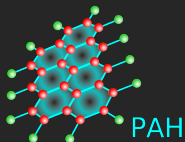
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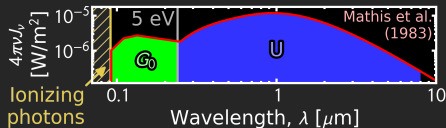


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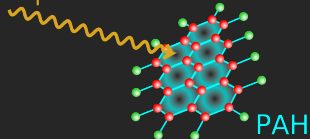
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UV photon

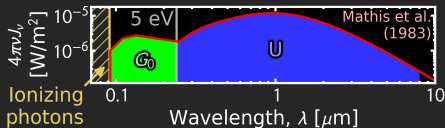


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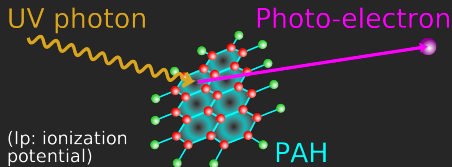
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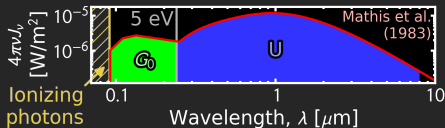


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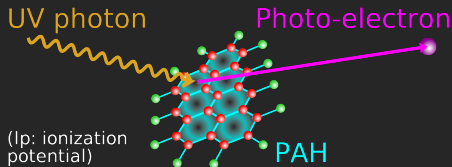
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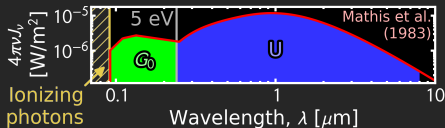
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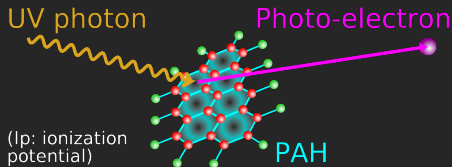
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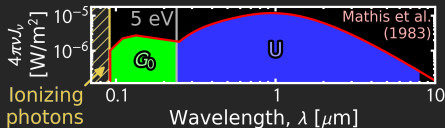
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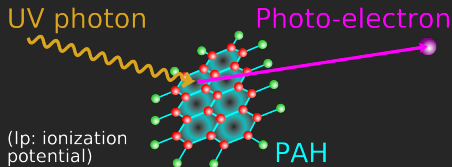
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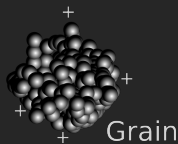


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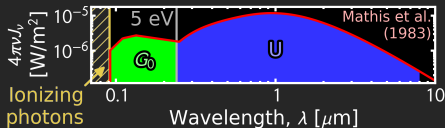


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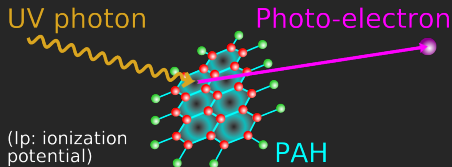
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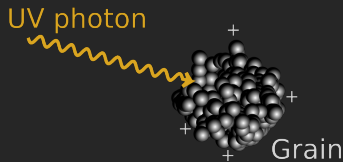


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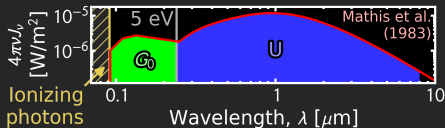


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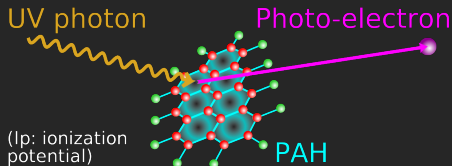
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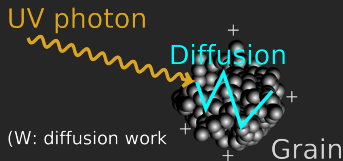


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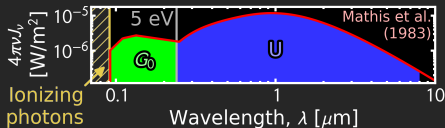


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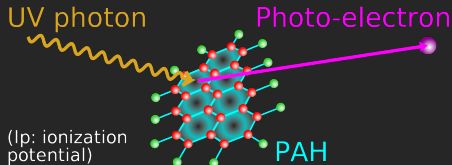
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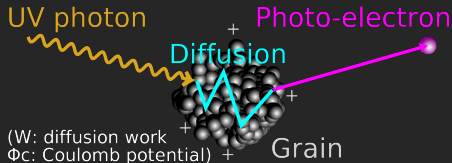


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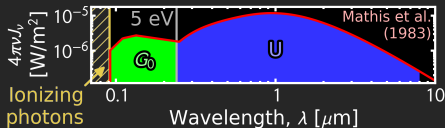


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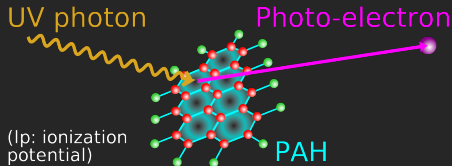
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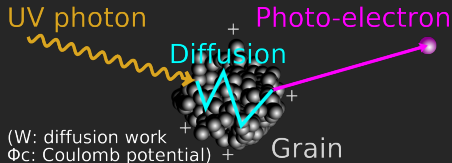


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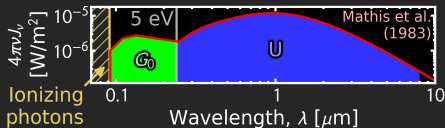
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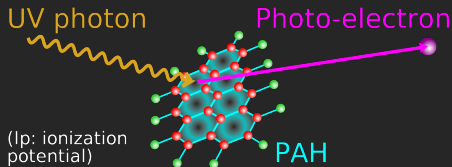
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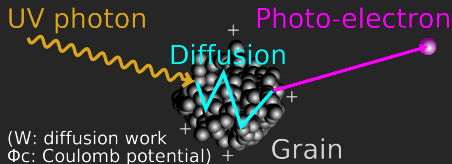


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Empirical heating rate (Bakes & Tielens, 1994; Wolfire et al., 2022)

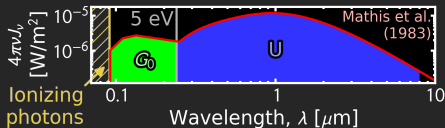


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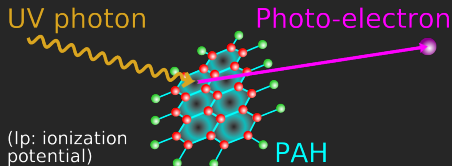
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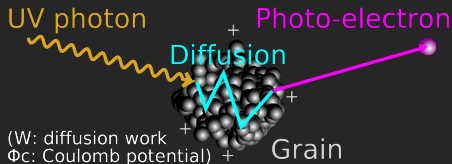


## The photoelectric effect on PAHs



$$\epsilon_{\text{PE}}^{\text{PAH}}(\nu) \simeq Y \left( \frac{h\nu - I_p}{h\nu} \right)$$

## The photoelectric effect on grains



$$\epsilon_{\text{PE}}^{\text{grain}}(\nu) \simeq Y \left( \frac{h\nu - W - \phi_c}{h\nu} \right)$$

## Empirical heating rate (Bakes & Tielens, 1994; Wolfire et al., 2022)

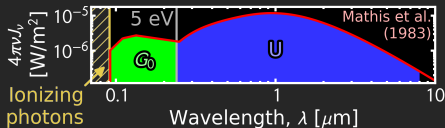
$$\epsilon_{\text{PE}} \simeq \frac{4.87 \times 10^{-2}}{1 + 4 \times 10^{-3} \gamma^{0.73}} + \frac{3.65 \times 10^{-2} (T/10^4 \text{ K})^{0.7}}{1 + 2 \times 10^{-2} \gamma}$$

# Thermal Phases | The Photoelectric Heating Efficiency

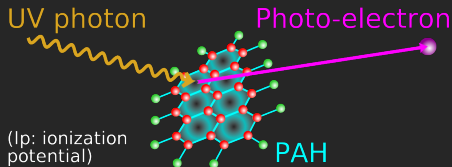
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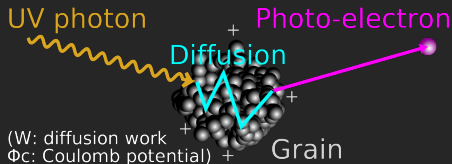


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The heating rate due to the photoionization of specie  $i$

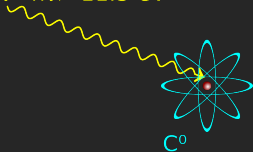
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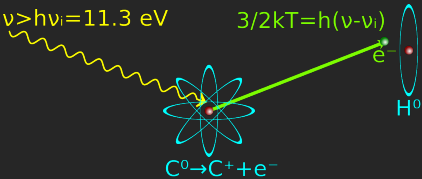
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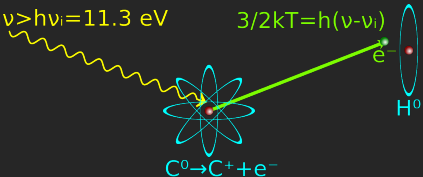
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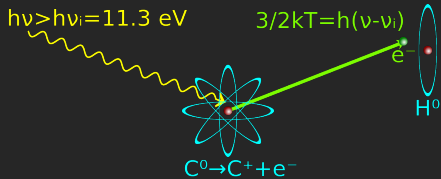
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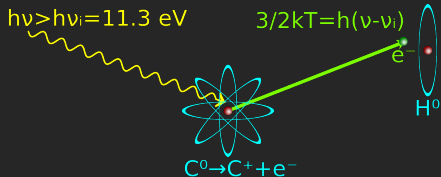


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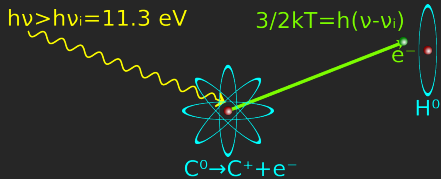


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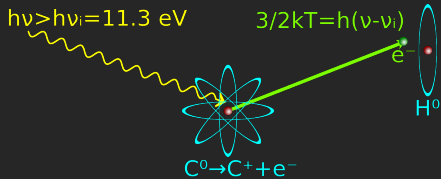


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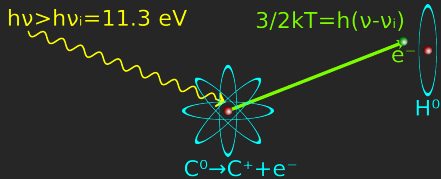
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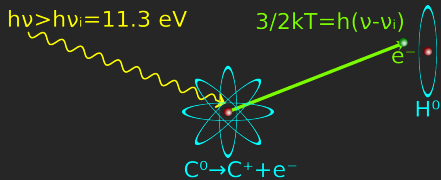
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In the ionized gas

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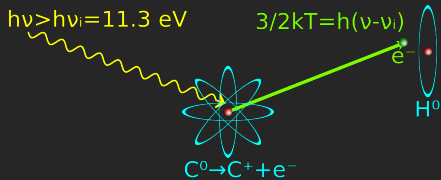
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- $\Rightarrow$  dominant heating process in H II.

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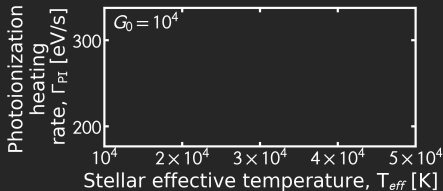
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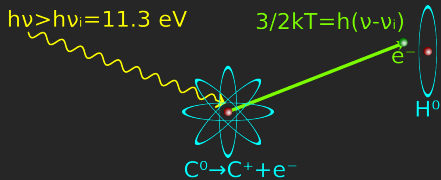
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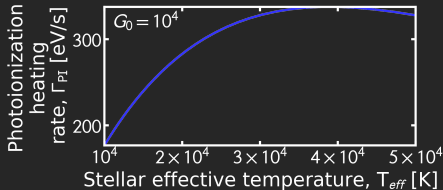
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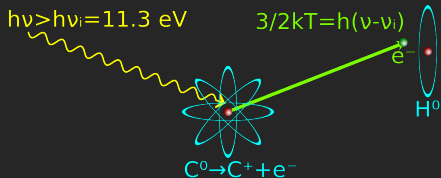
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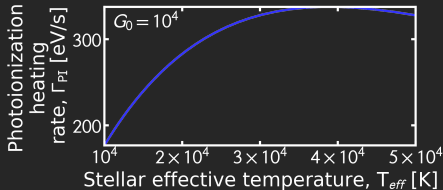
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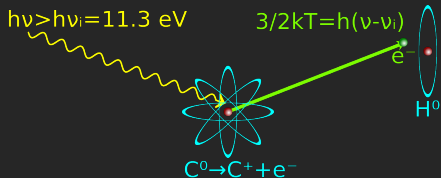
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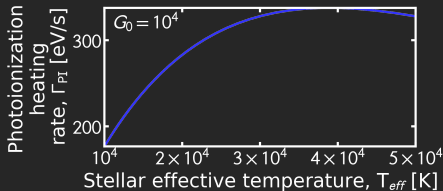
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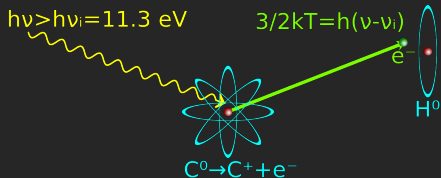


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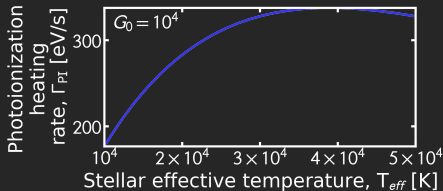
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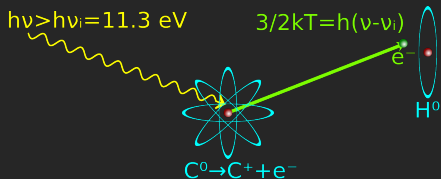


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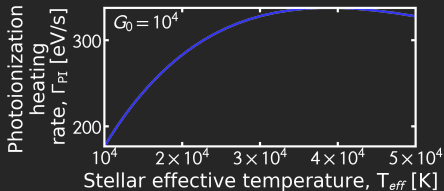
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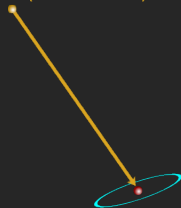
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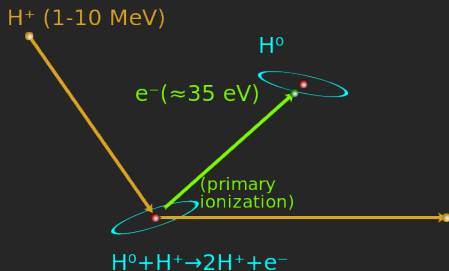
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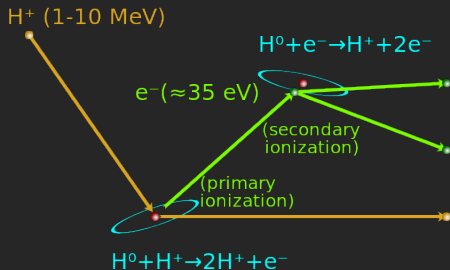
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# Thermal Phases | Cosmic-Ray, X-Ray & Shock Heating

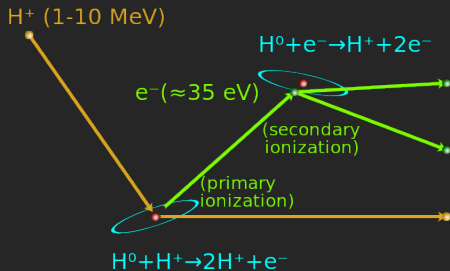
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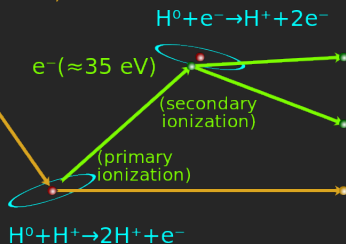
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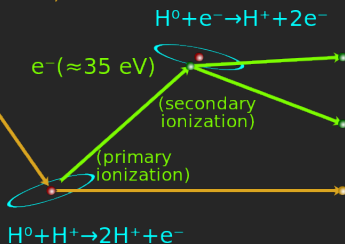
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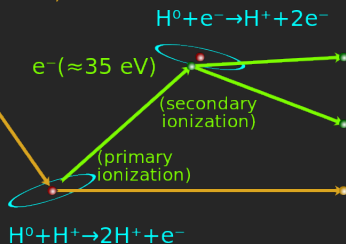
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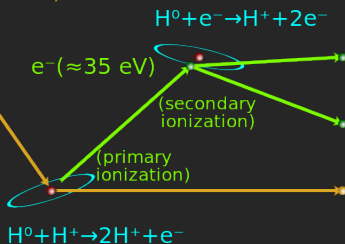
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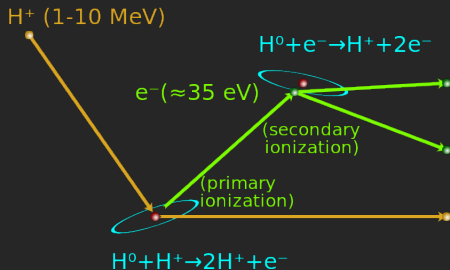
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## Shock Heating

# Thermal Phases | Cosmic-Ray, X-Ray & Shock Heating

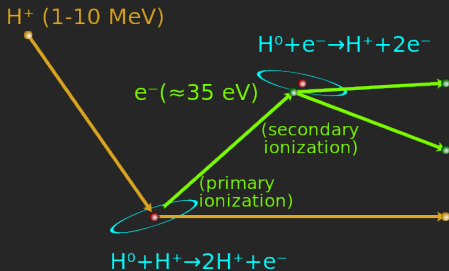
## Cosmic-Ray (CR) heating

- Low-energy CRs (1–10 MeV) are the most numerous.
- They penetrate dense clouds where there are no UV photons.

• CR rate:  $\zeta_{\text{CR}} \simeq (0.5 - 3) \times 10^{-16} \text{ s}^{-1}$ .

→  $\Gamma_{\text{CR}} \simeq \zeta_{\text{CR}} \times 10 \text{ [eV/s]}$ .

⇒ CRs are the most efficient heating source in dense molecular clouds.



## X-ray heating

- Similar interaction as cosmic rays but with lower energy.
- X-rays penetrate less deeply into clouds:

**Near bright X-ray sources:** (binary, AGNs, *etc.*) → only regions where it dominates.

**Diffuse X-ray background:**  $\Gamma_{\text{XR}} \simeq 10^{-33} \text{ [W/H]}$ .

## Shock Heating

- $\Gamma_{\text{shock}} \simeq 1/2 m_{\text{H}} v_{\text{shock}}^2 \times R_{\text{SN}} \times f_{\text{V}}$ ,  $w/ v_{\text{shock}} \simeq 300 \text{ km/s}$ ,  $R_{\text{SN}} \simeq 1/(100 \text{ year})$  &  $f_{\text{V}} \simeq 2 \times 10^{-7}$ .

# Thermal Phases | Cosmic-Ray, X-Ray & Shock Heating

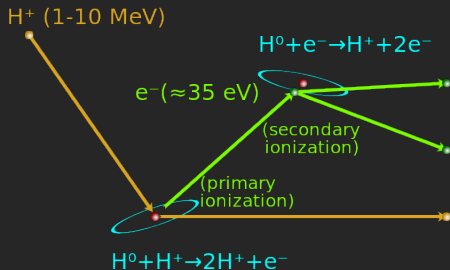
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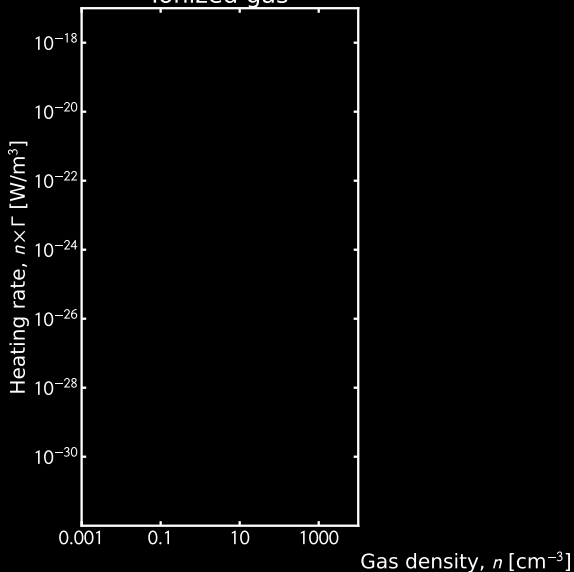
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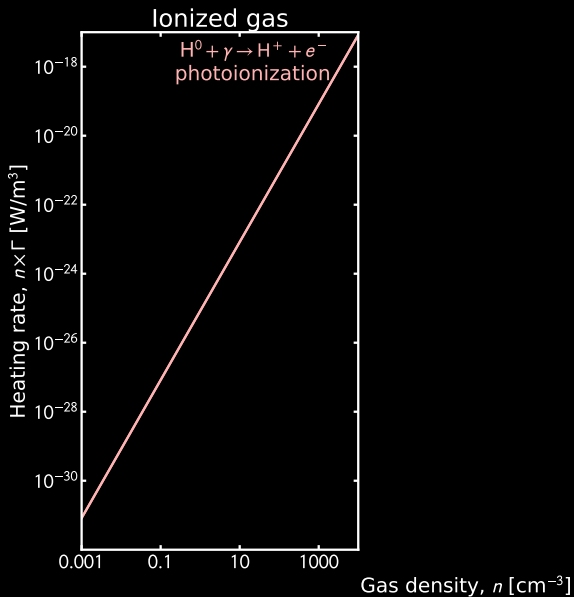
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- ⇒ dominant heating process in the hot, intercloud, coronal gas.

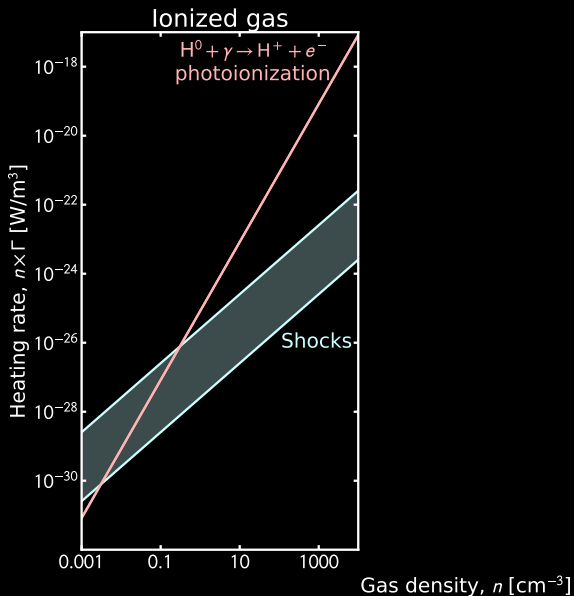




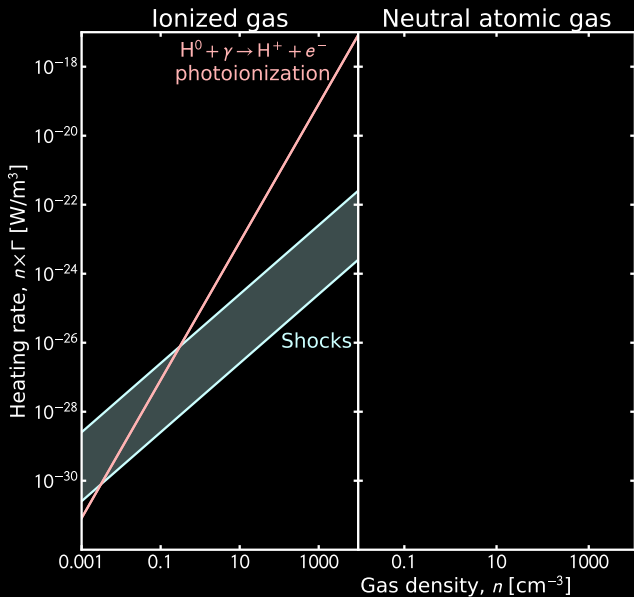
## Ionized gas



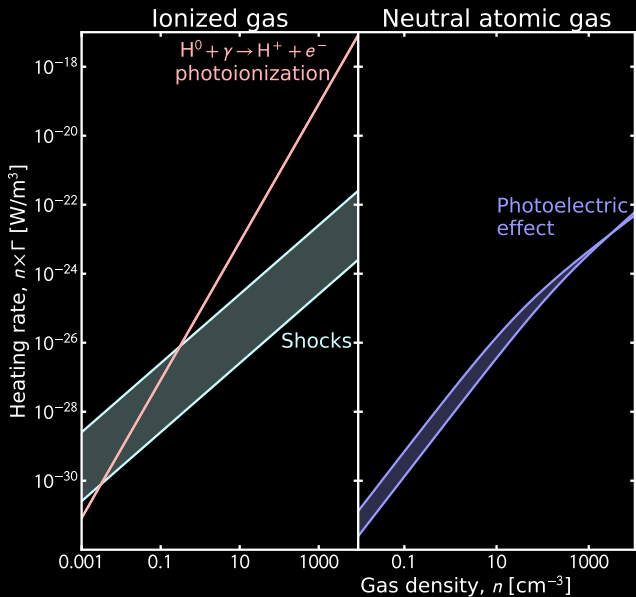




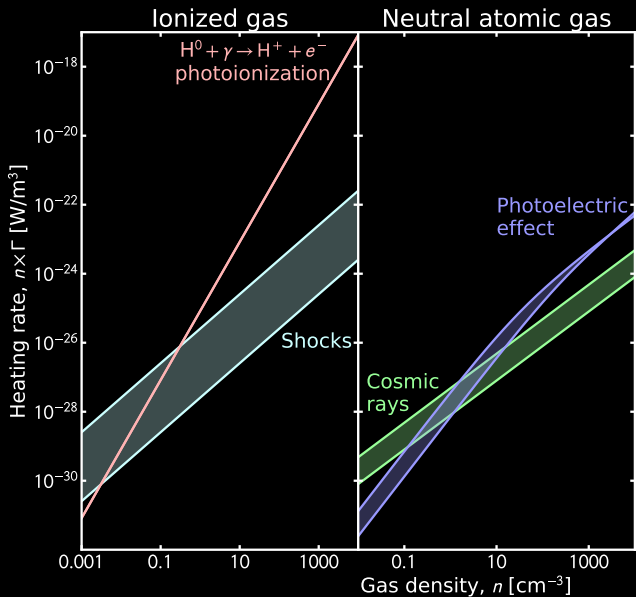
# Thermal Phases | Comparison of the Different Heating Processes



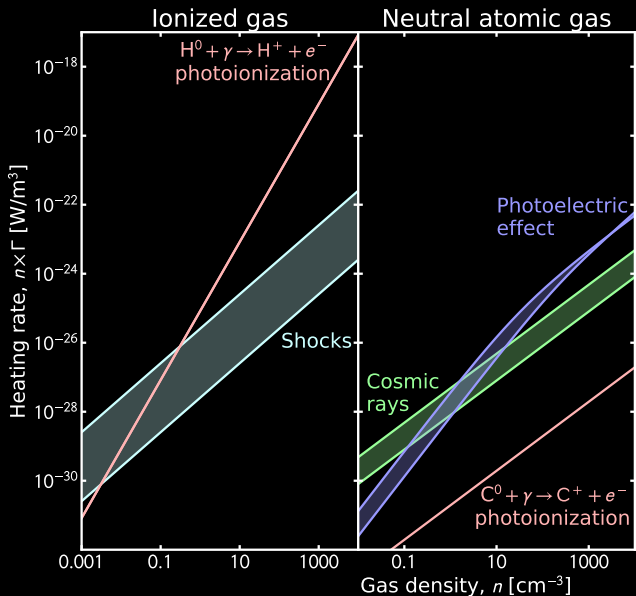
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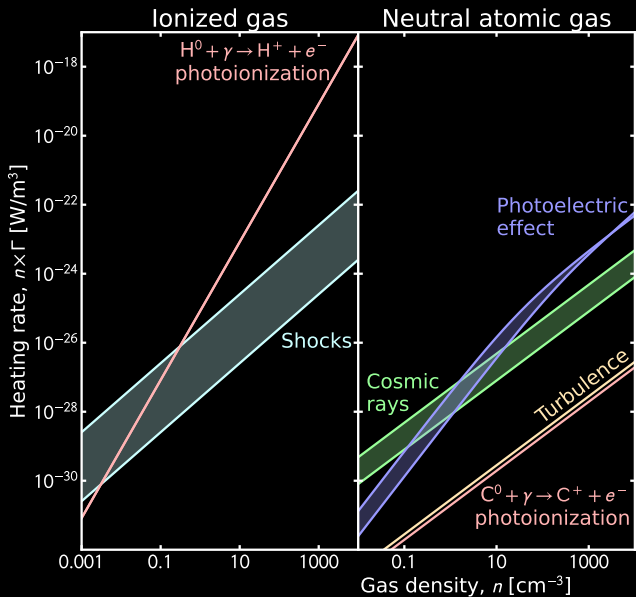
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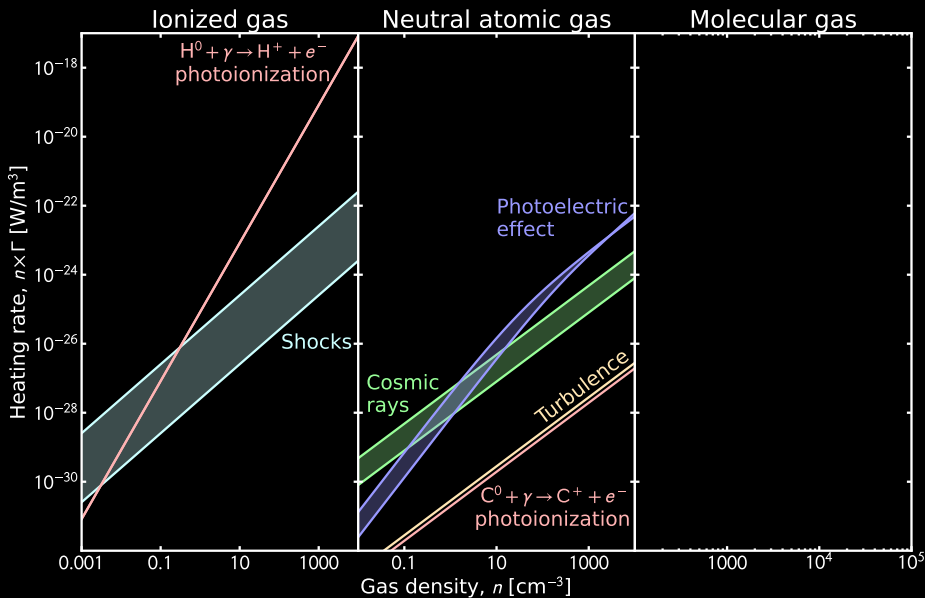


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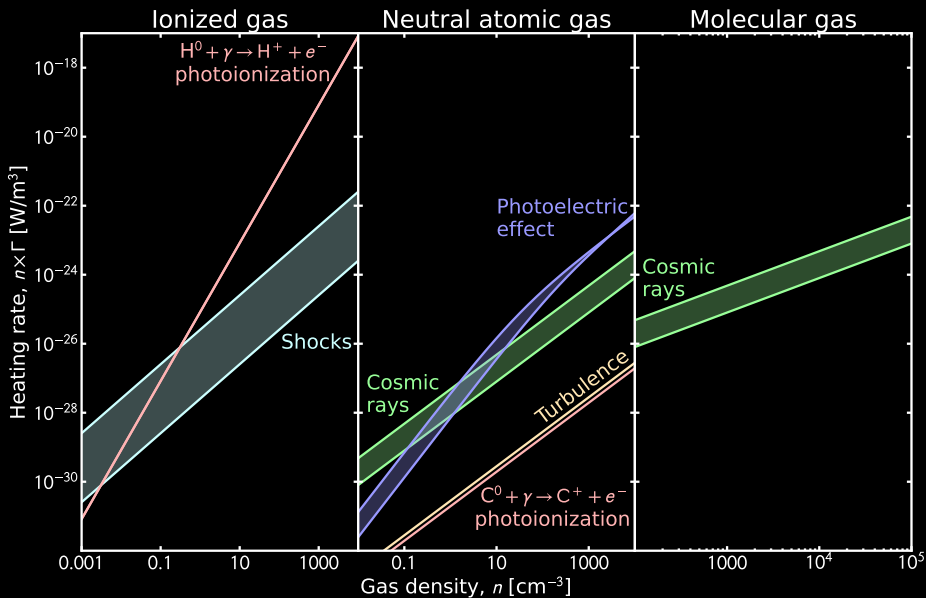




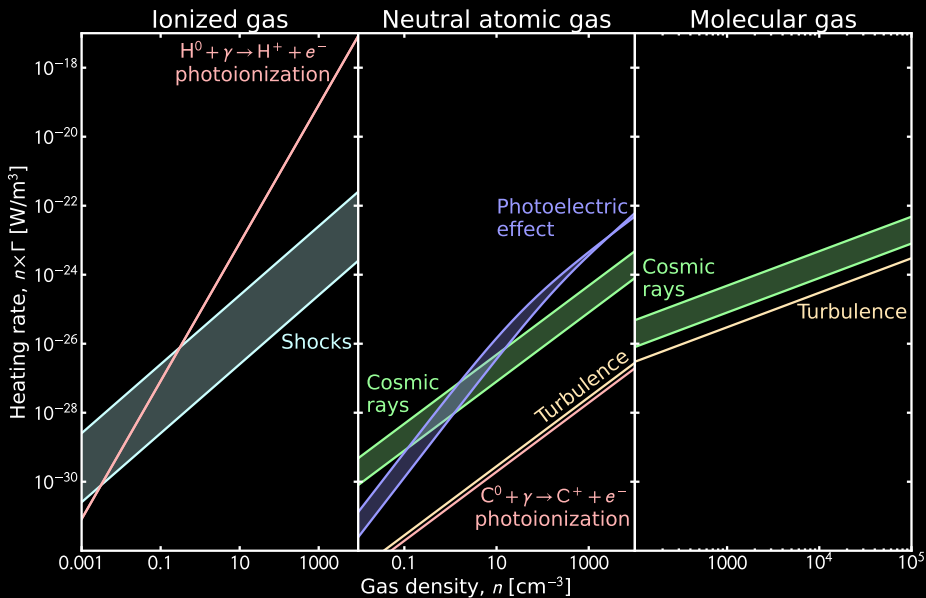
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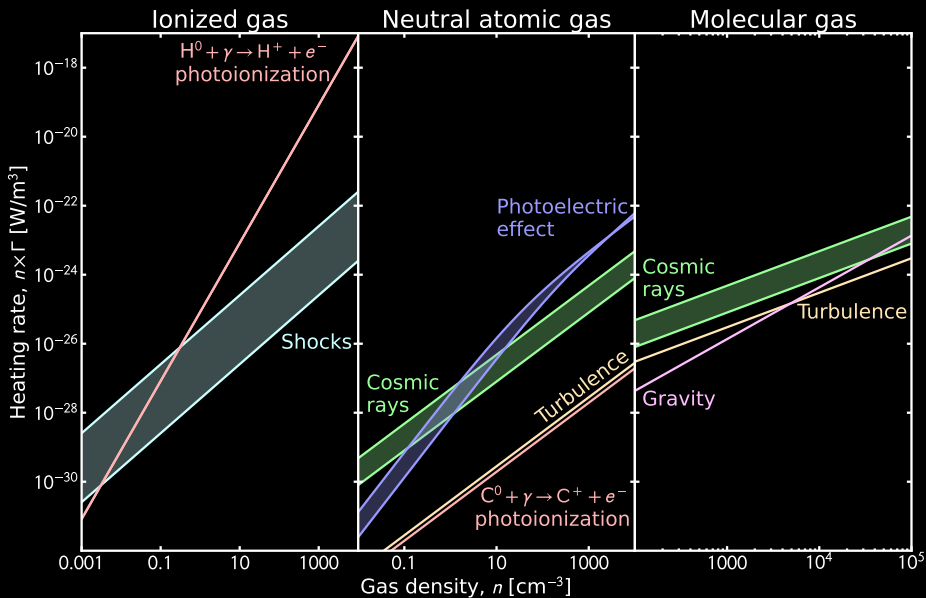
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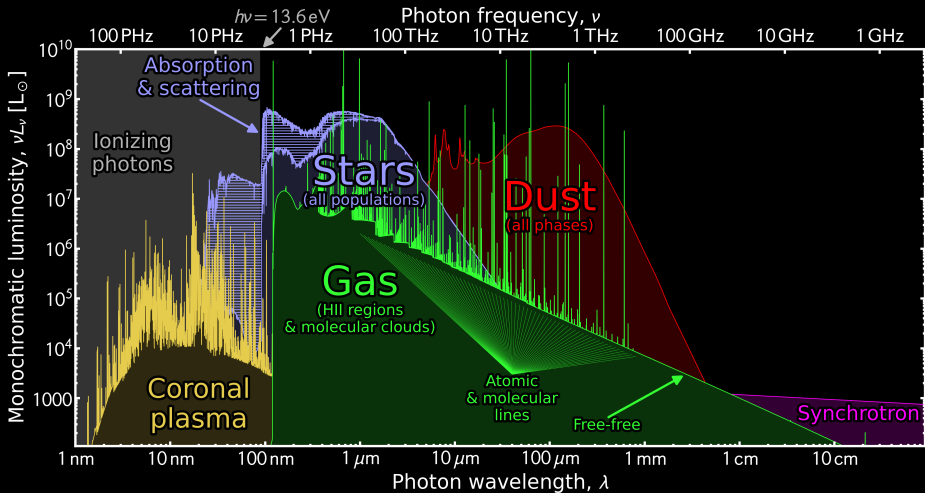


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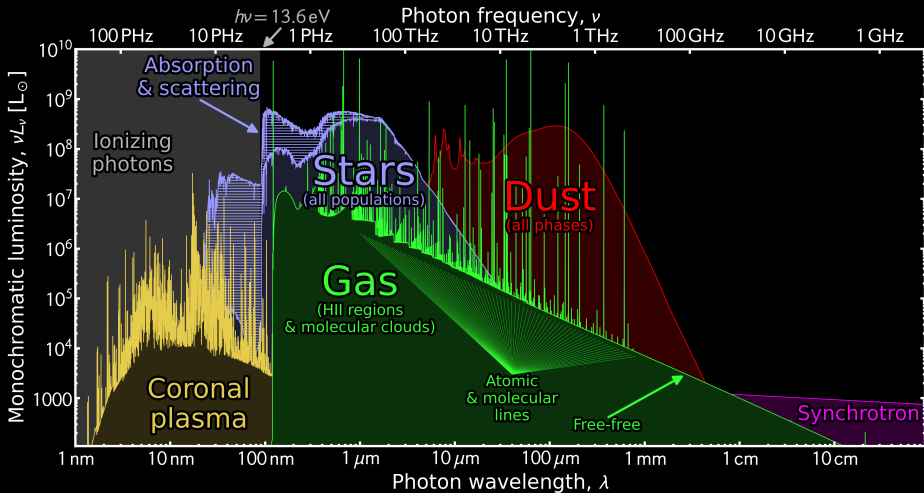


# Thermal Phases | Dust Cooling & Total ISM Cooling

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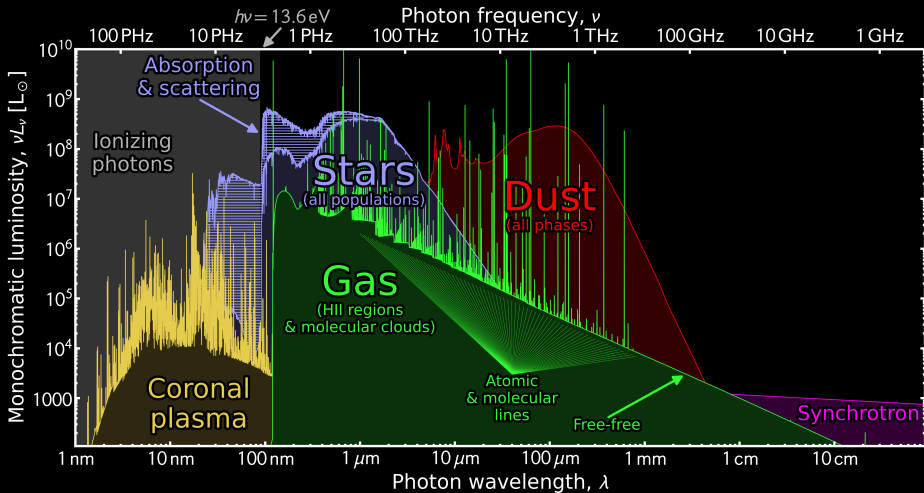


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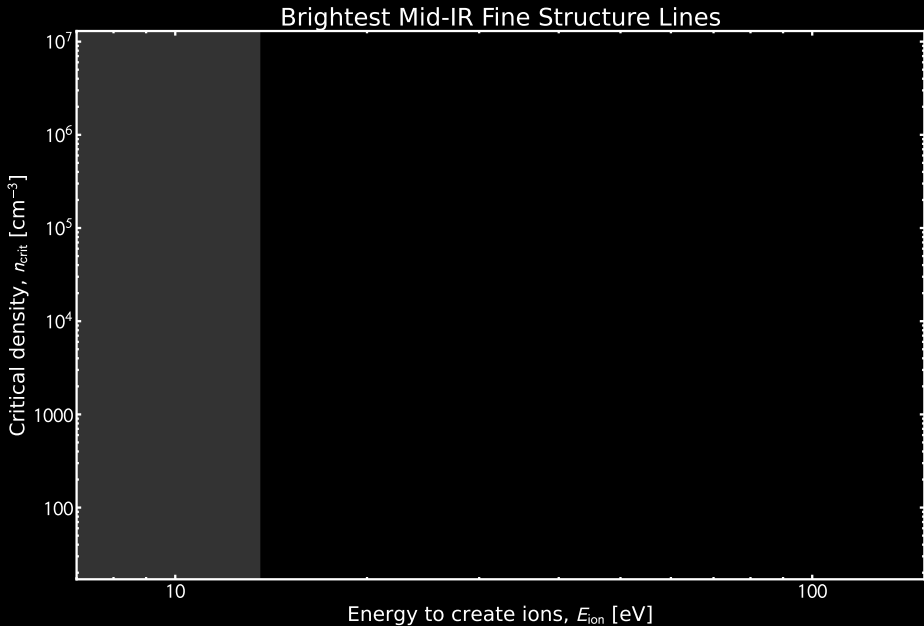
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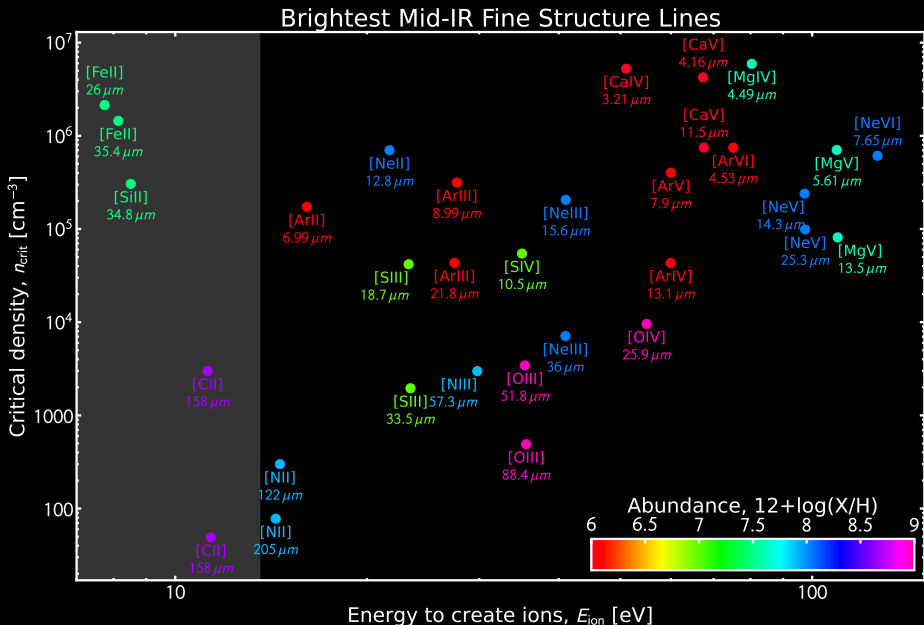
- Gas & dust are not thermalized (e.g.  $T_{\text{gas}}(\text{WNM}) \simeq 10^4 \text{ K}$  vs.  $T_{\text{dust}}(\text{WNM}) \simeq 18 \text{ K}$ ).
- Dust dominates the energetic balance of the ISM:  $L_{\text{dust}}^{\text{cool}} = L_{\text{dust}}^{\text{abs}} \simeq 30\% L_\star \Rightarrow L_{\text{gas}}^{\text{cool}} \simeq 1\% L_{\text{dust}}^{\text{cool}}$ .



# Thermal Phases | The Dominant Coolants of the ISM

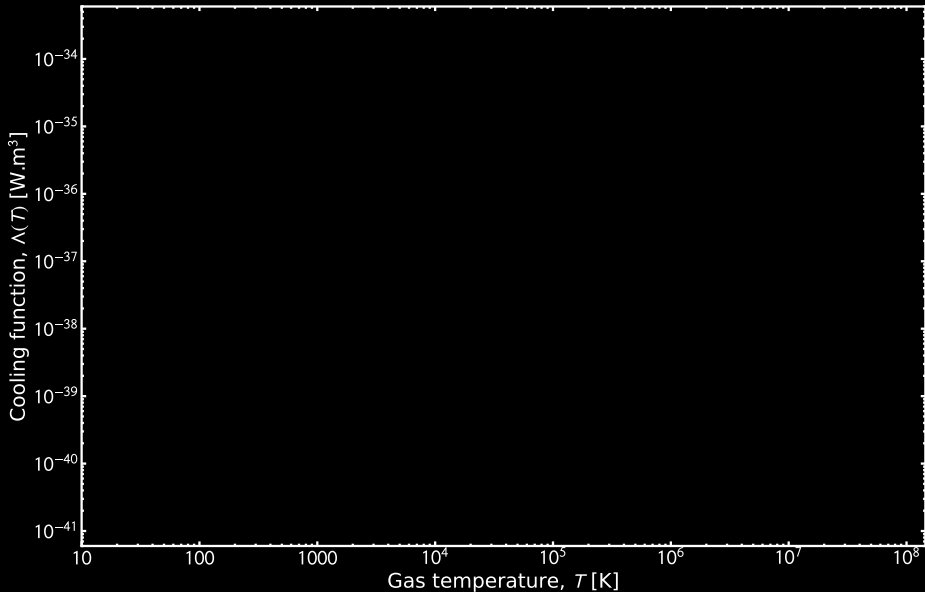


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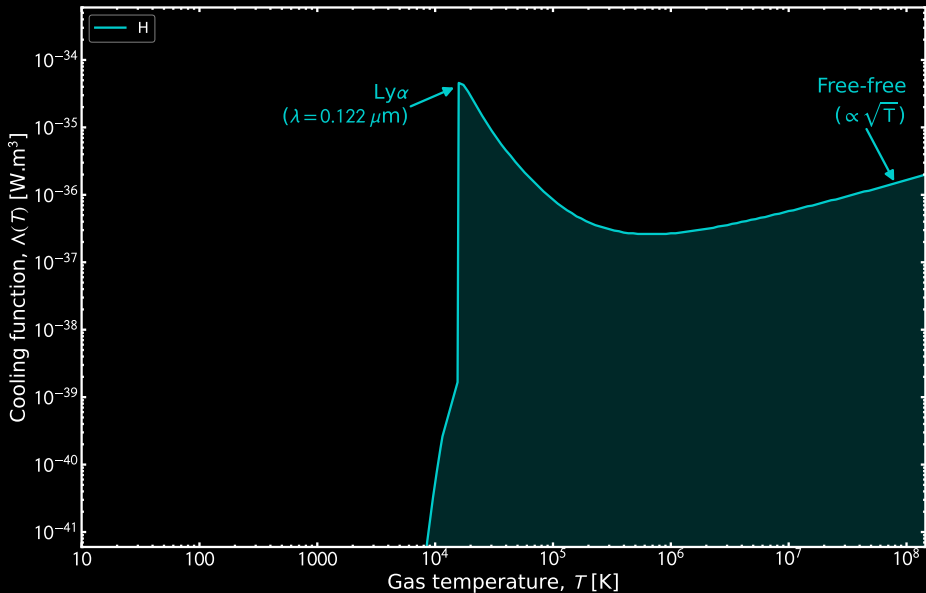


# Thermal Phases | The Interstellar Cooling Function

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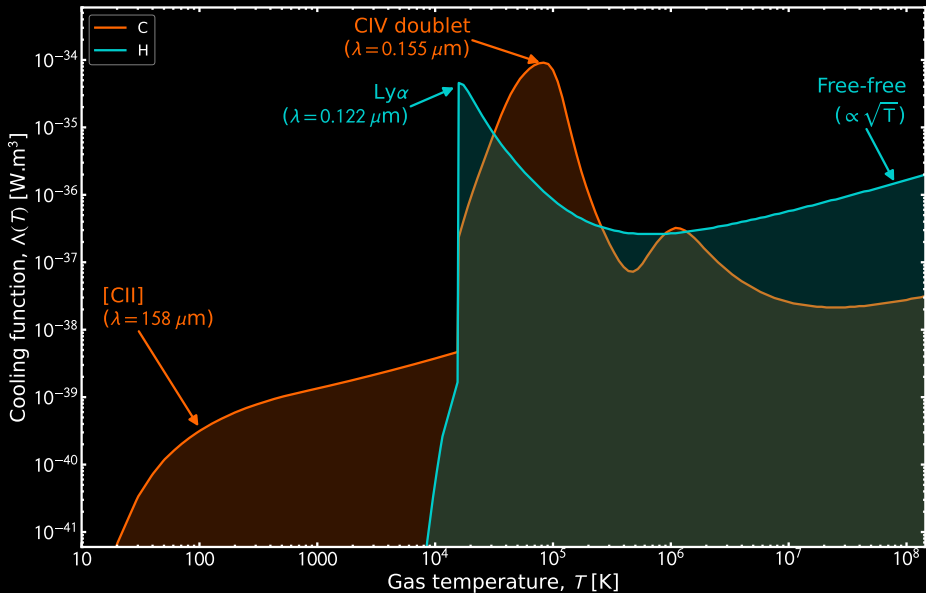


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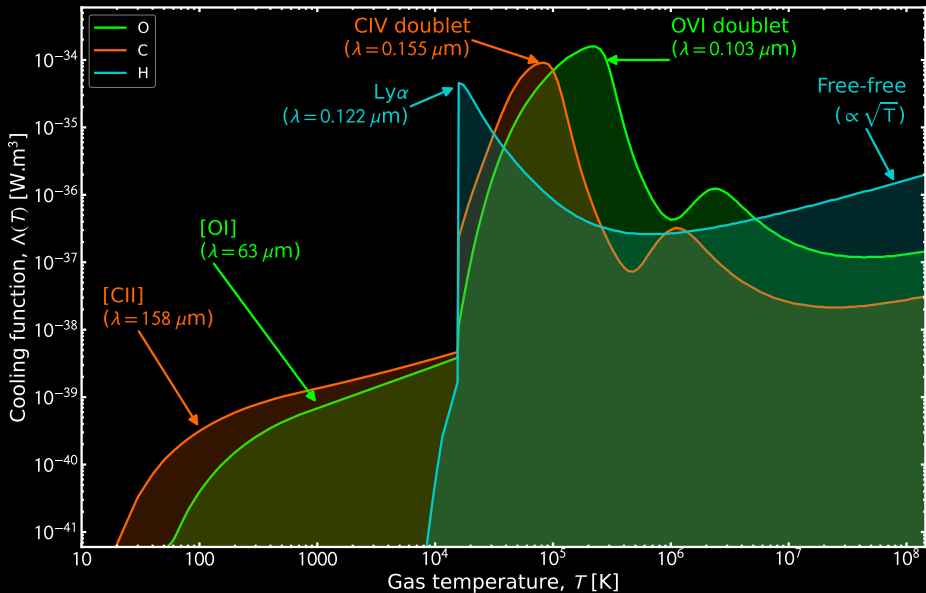
(Dalgarno & McCray, 1972; Schure et al., 2009; Wolfire et al., 1995, 2022)

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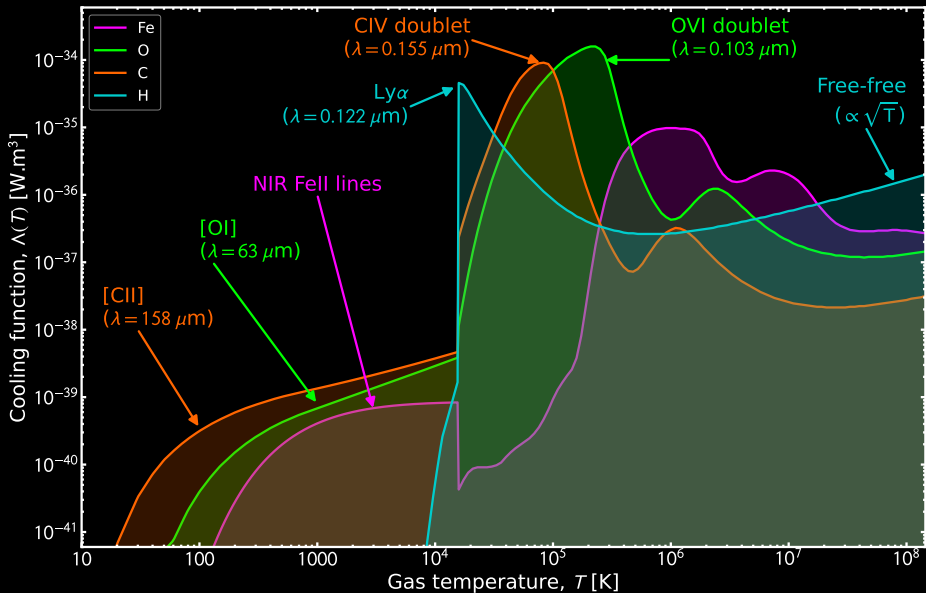
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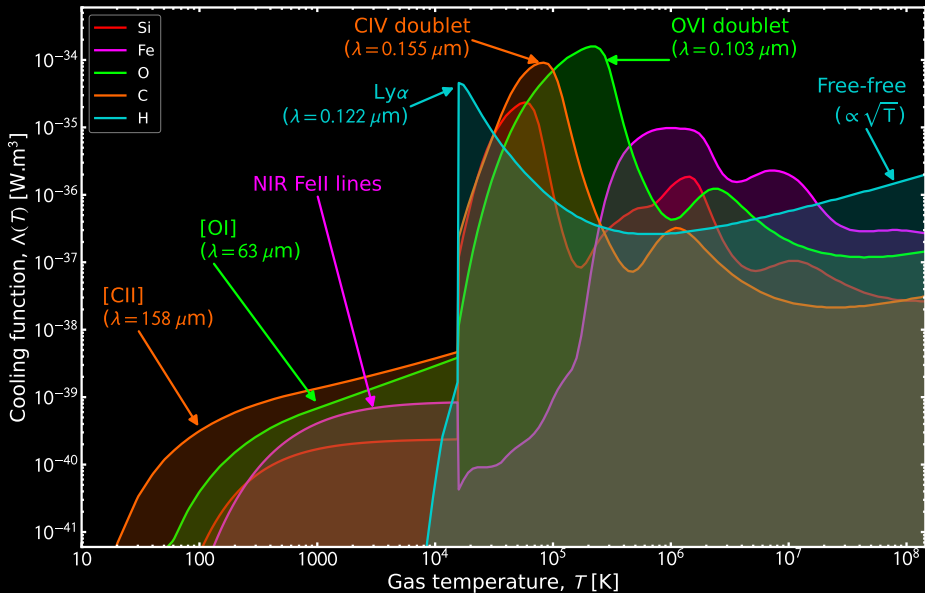


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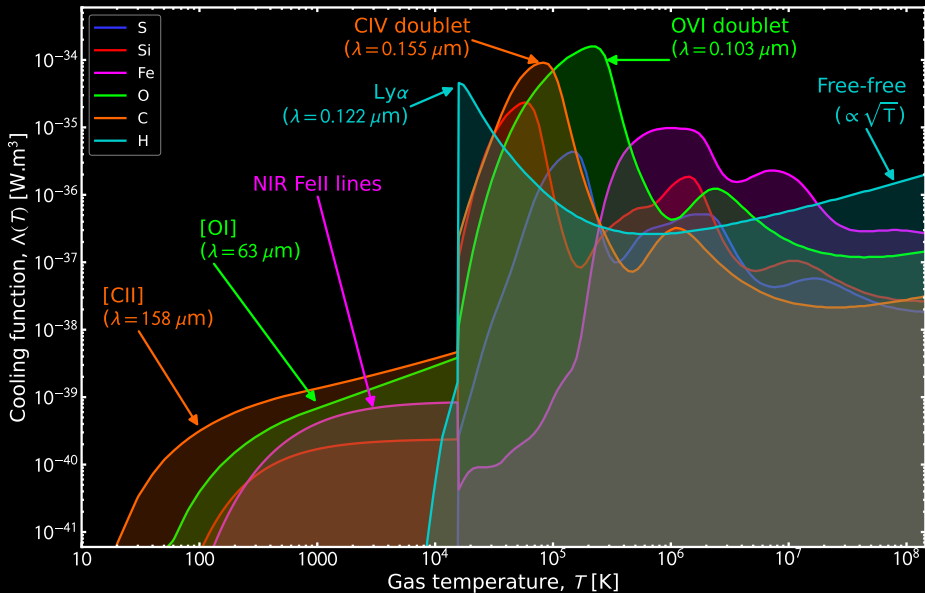
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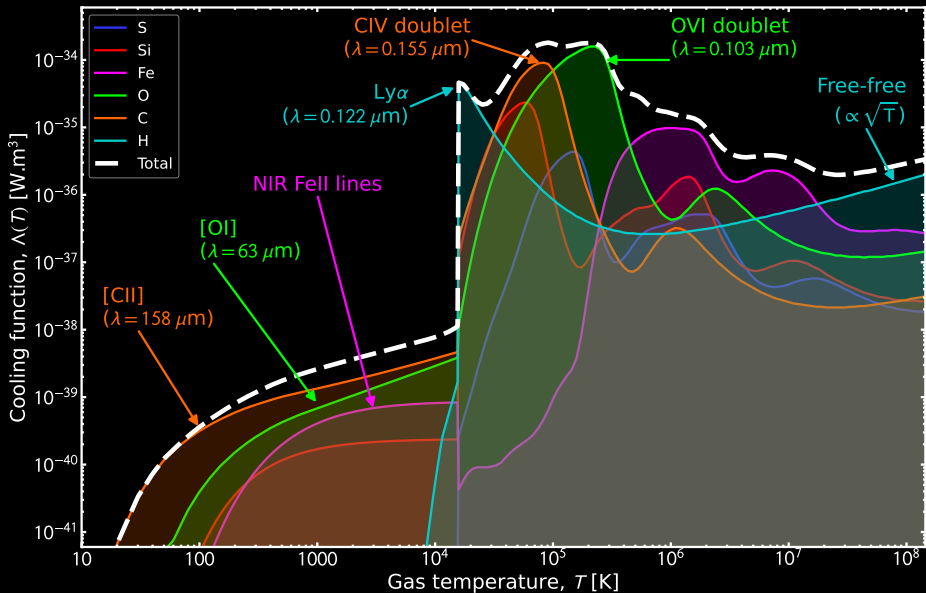
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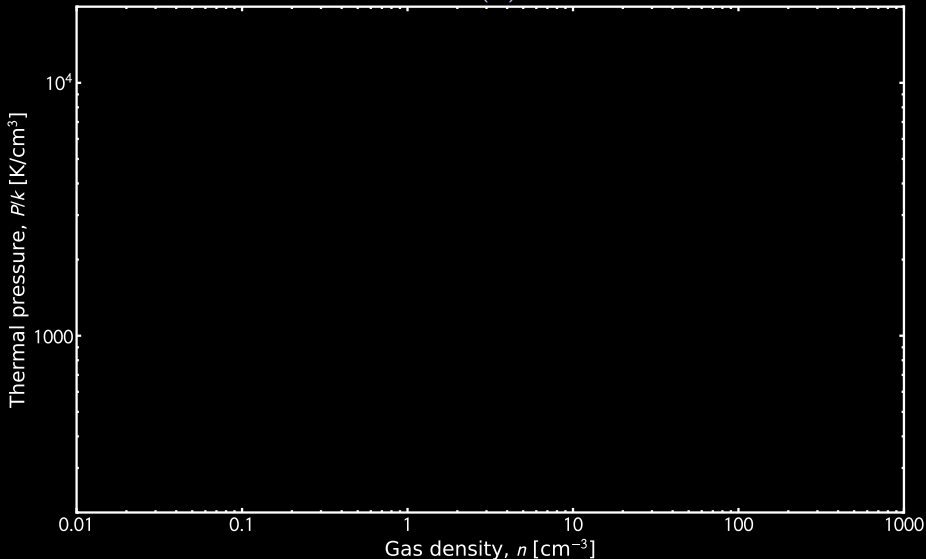
## Thermal Phases | The Two Neutral Atomic Phases of the ISM

Thermal balance:  $n \times \Gamma = n^2 \times \Lambda(T) \Rightarrow \frac{P}{k} = \frac{T \times \Gamma}{\Lambda(T)}$ . In the ISM:  $P/k \simeq 3000 \text{ K.cm}^{-3}$ .



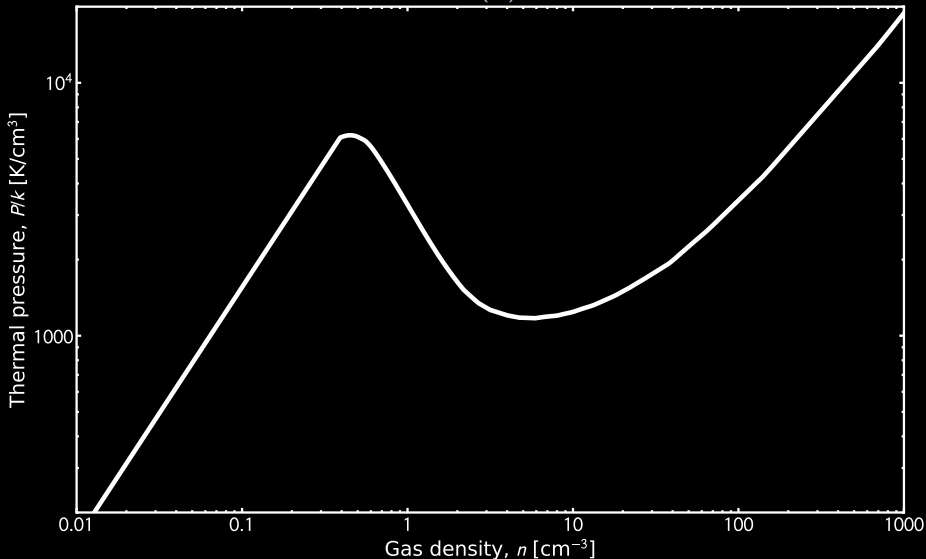
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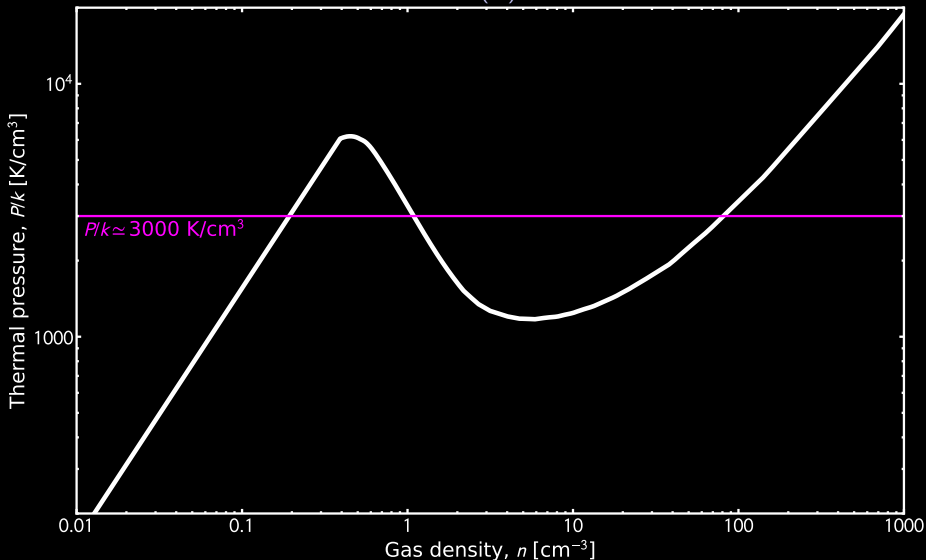
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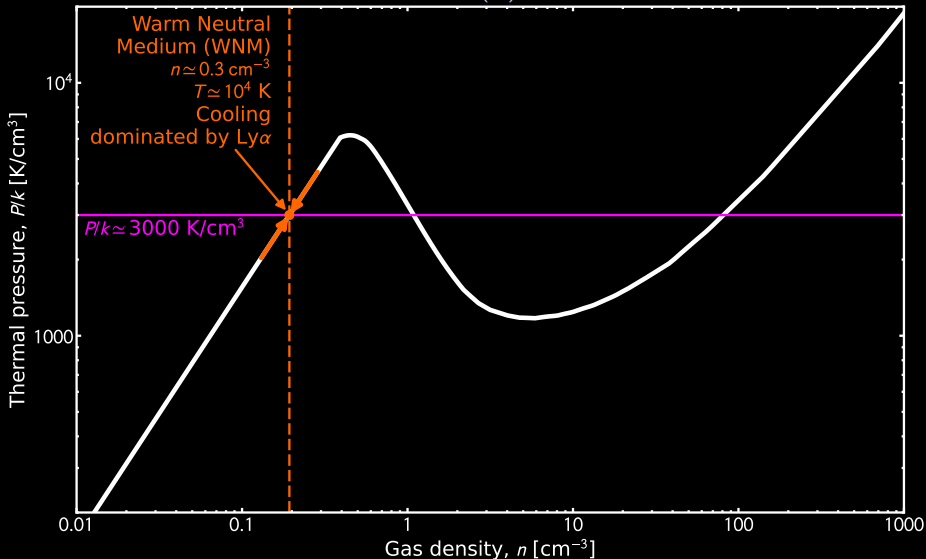
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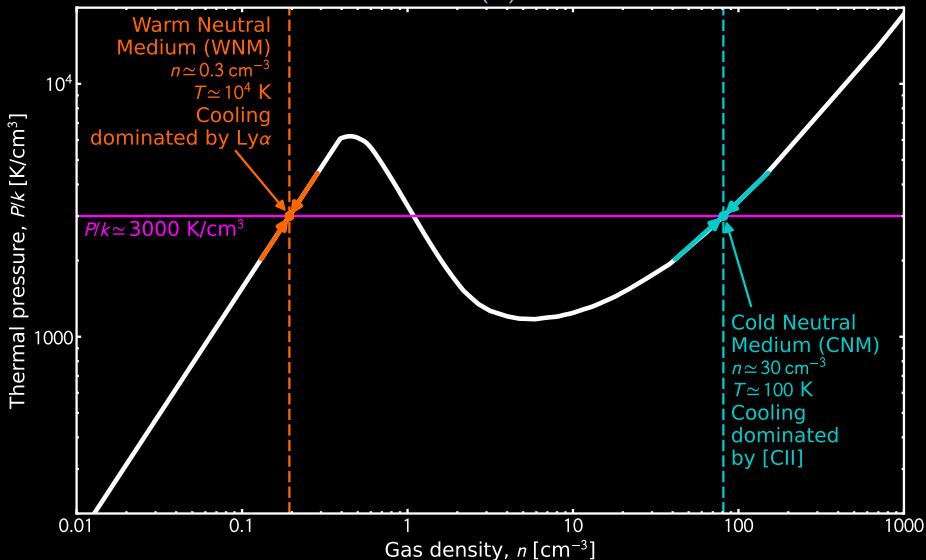
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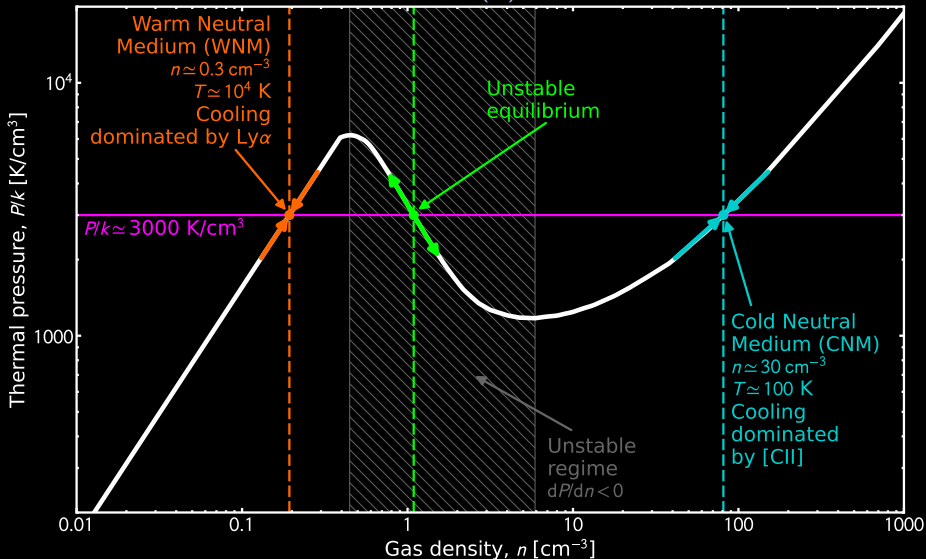
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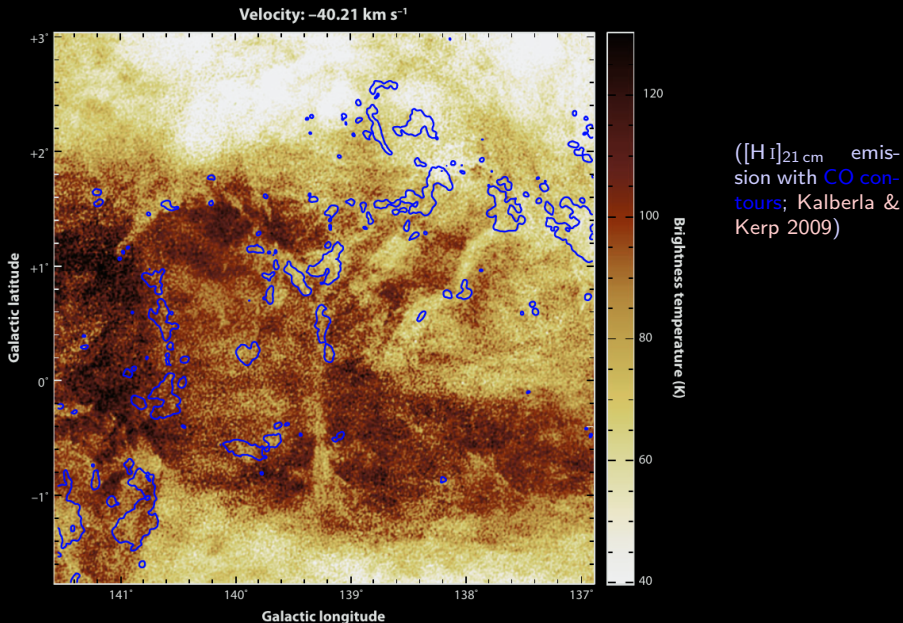
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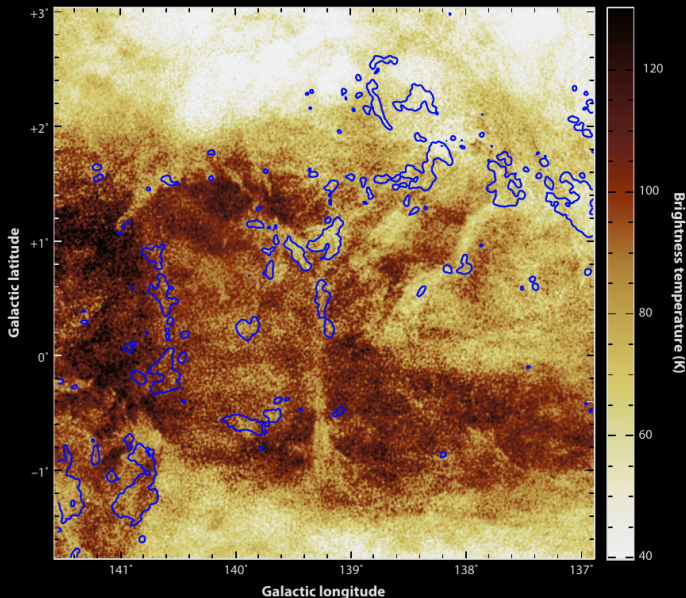
# Thermal Phases | Observations of the Bithermal Neutral Medium





# Thermal Phases | Observations of the Bithermal Neutral Medium

Velocity:  $-40.21 \text{ km s}^{-1}$



( $[\text{H I}]_{21 \text{ cm}}$  emission with CO contours; Kalberla & Kerp 2009)

⇒  $[\text{H I}]_{21 \text{ cm}}$  CNM absorption in front of WNM  $[\text{H I}]_{21 \text{ cm}}$  emission, without systematic association to CO.

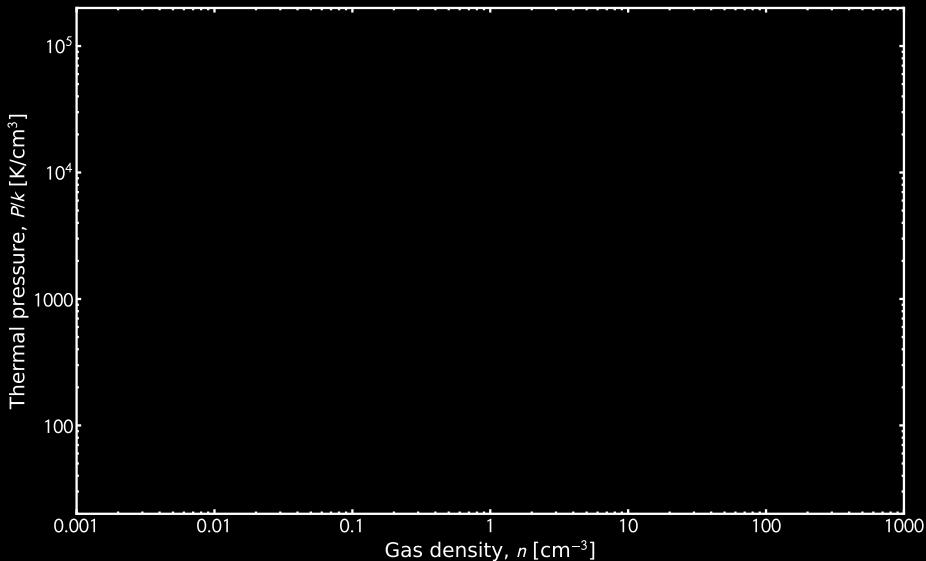
# Thermal Phases | The Two Ionized Phases of the ISM

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Accounting for heating by shock &  $H^0$  photoionization:

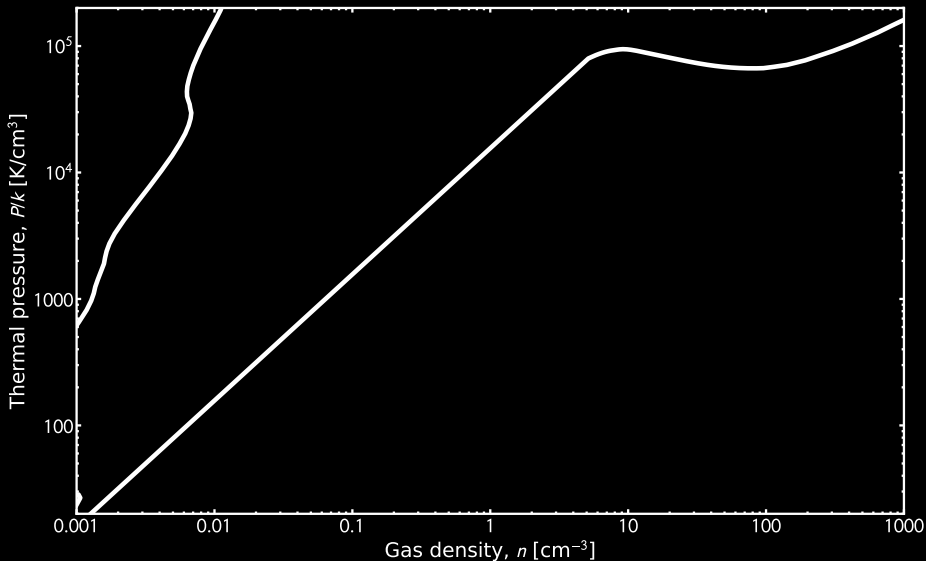
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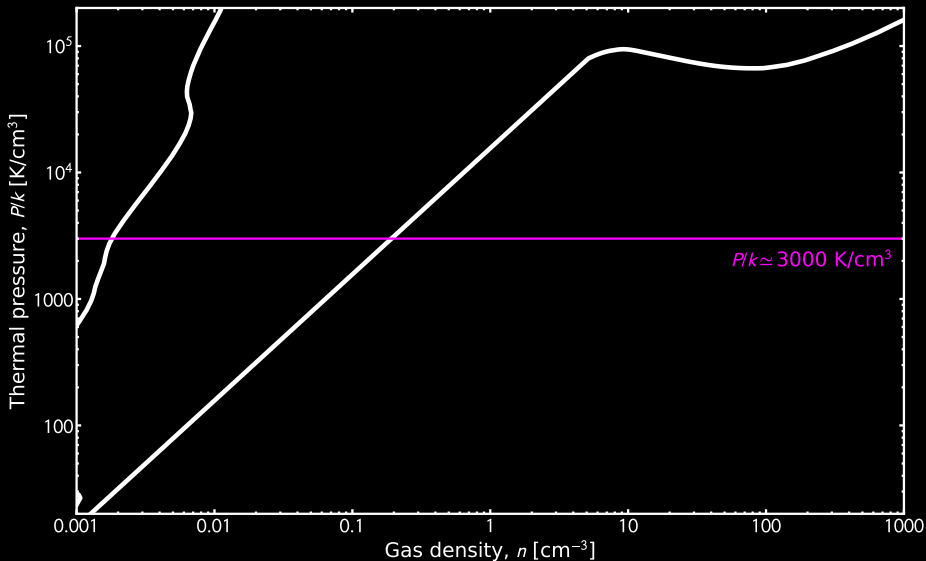
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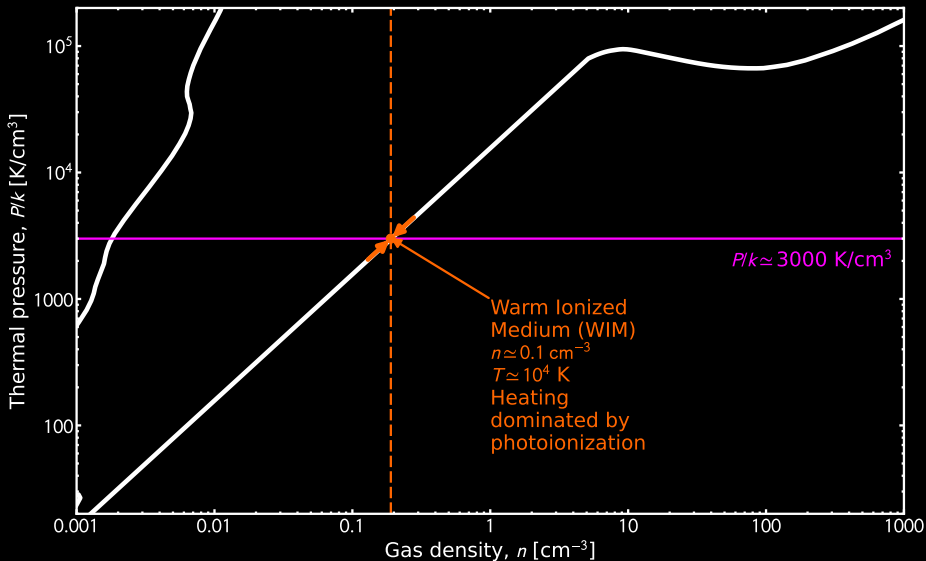
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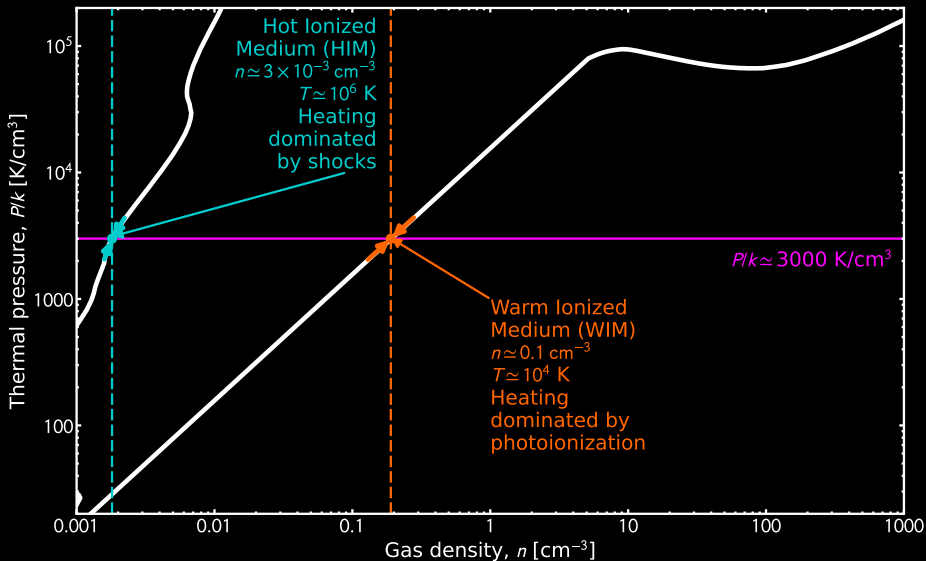
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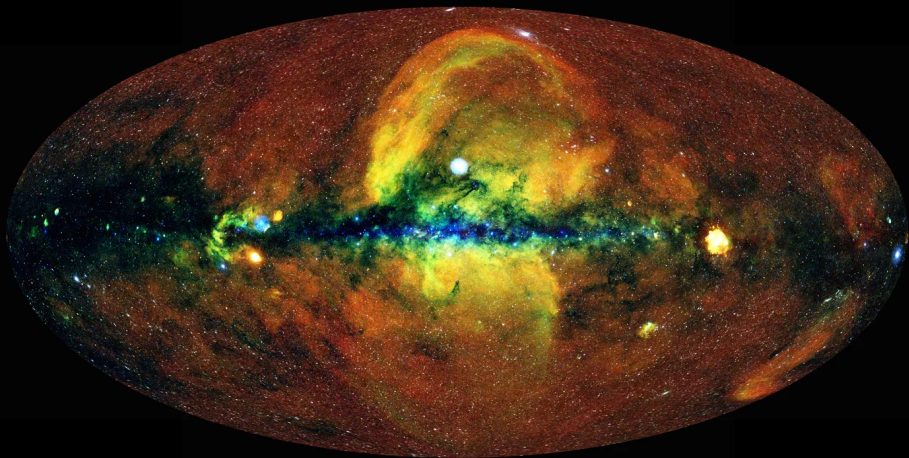
Accounting for heating by shock &  $H^0$  photoionization:







# Thermal Phases | Observations of the Hot Ionized Medium (HIM)



Credit: eRosita all-sky survey (0.3–0.6 keV / 0.6–1 keV / 1–2.3 keV); J. Sanders, H. Brunner & the eSASS team (MPE); E. Churazov, M. Gilfanov (on behalf of IKI).



Diffuse molecular clouds:  $n(\text{H}_2) = 10^2 - 10^3 \text{ cm}^{-3}$  &  $T = 40 - 100 \text{ K}$ .

## Thermal Phases | Molecular Clouds

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**Molecular cores:**  $n(\text{H}_2) = 10^6 - 10^7 \text{ cm}^{-3}$  &  $T = 10 - 20 \text{ K}$ .







# Thermal Phases | Summary of the Properties of the ISM Phases

Phase	Density [ $\text{cm}^{-3}$ ]	Temperature [K]	Volume filling factor	Main heating	Main cooling
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(Adapted from Tielens 2005 & Draine 2011)

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Hot Ionized Medium (HIM)	≈ 0.003	≈ 10 <sup>6</sup>	≈ 50 %	Shocks	Free-free

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Molecular clouds	10 <sup>2</sup> – 10 <sup>6</sup>	10 – 50	≈ 0.01 %	Cosmic rays	CO lines

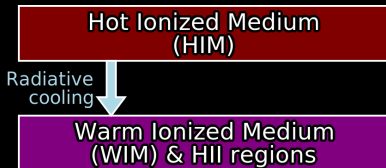
(Adapted from Tielens 2005 & Draine 2011)



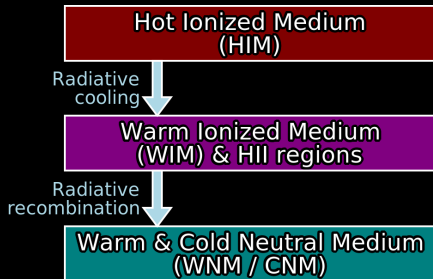
Hot Ionized Medium  
(HIM)

(adapted from P. van der Werf)

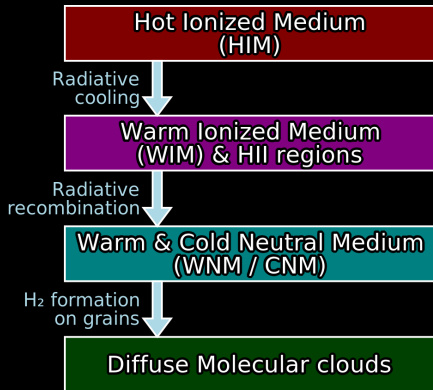




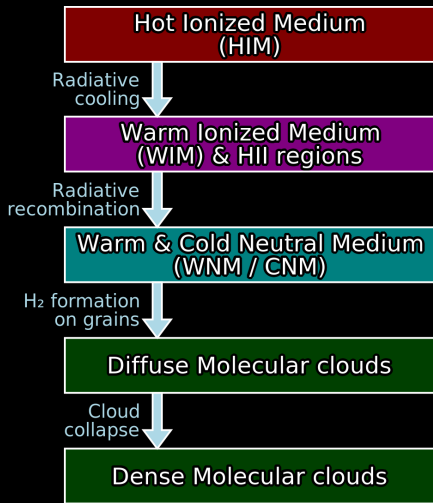
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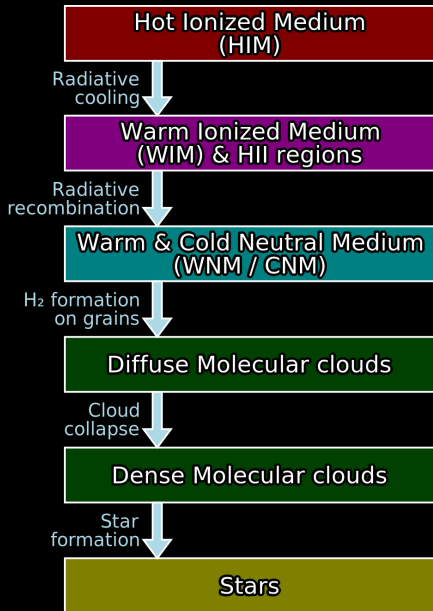
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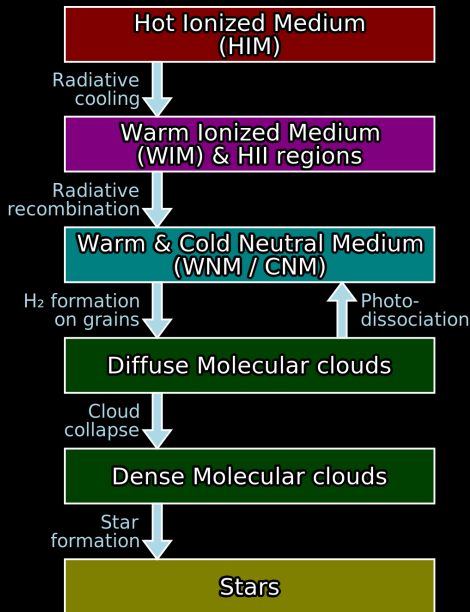
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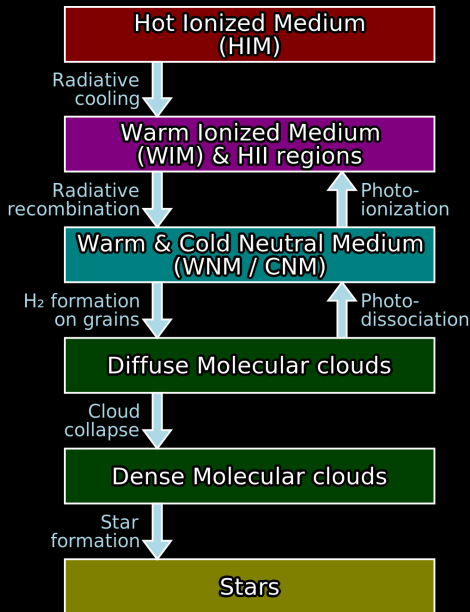


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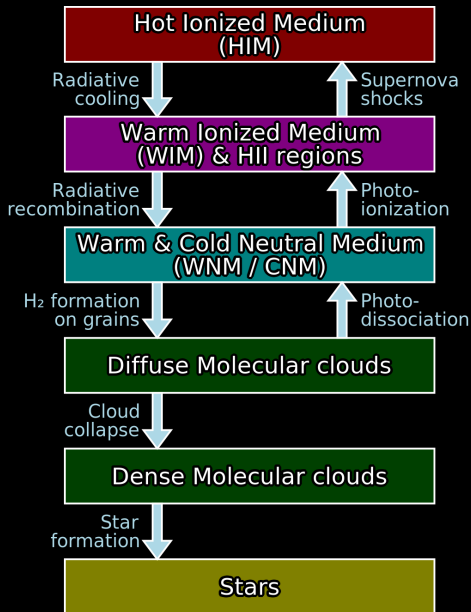
(adapted from P. van der Werf)

# Thermal Phases | The Multiphase Interstellar Dynamical Network



(adapted from P. van der Werf)

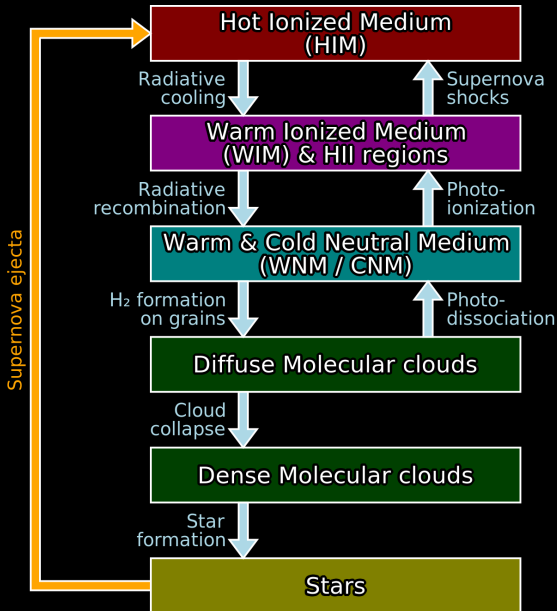
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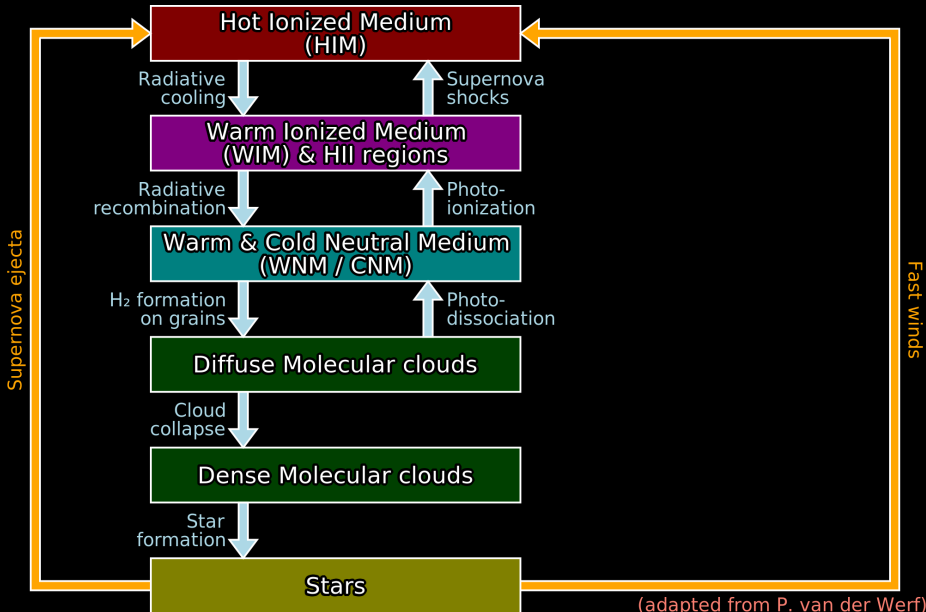


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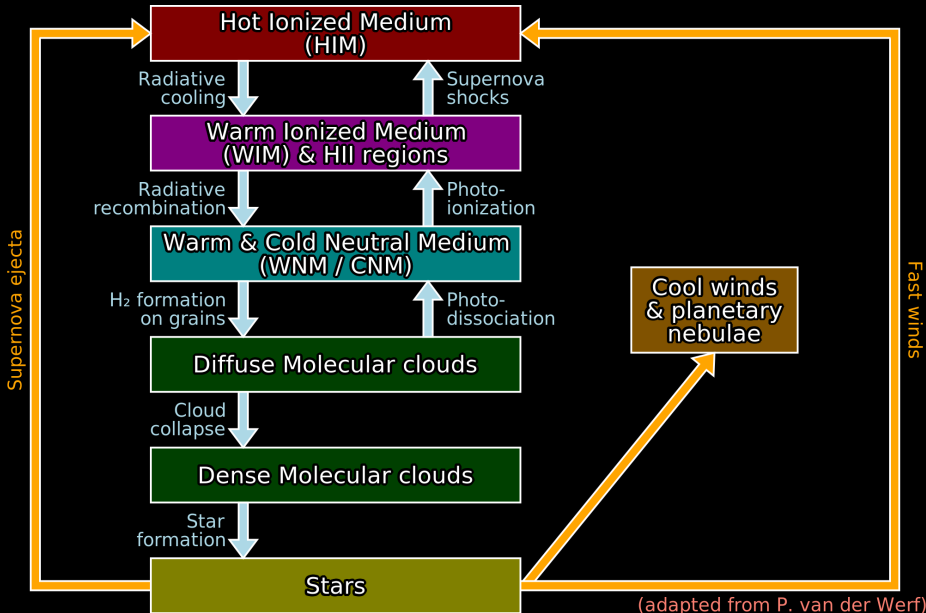


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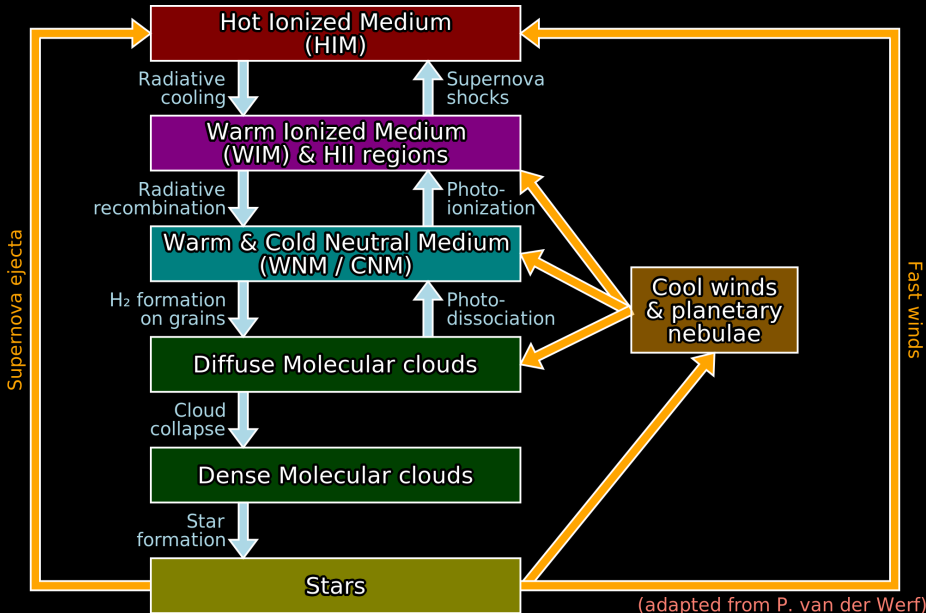
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## 1 COOLING & HEATING OF THE GAS

- The gas heating processes
- The gas cooling function
- The five thermal phases of the ISM

## 2 THE PRINCIPLES OF RADIATIVE TRANSFER

- The radiative transfer equation
- Solutions in simple cases
- Dust radiative transfer with more complex geometries

## 3 STAR-FORMING REGIONS

- The Structure of Star-Forming Regions
- H II regions
- PhotoDissociation Regions (PDRs)

## 4 CONCLUSION

- Take-away points
- References

# Transfer | The Specific Intensity & Its Moments (1/2)

Spherical coordinate reminder

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Solid angle:  $d\Omega = \sin\theta d\theta d\phi$ .



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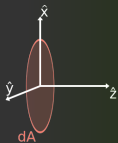
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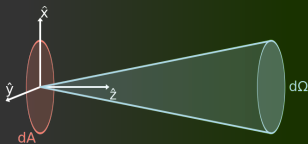
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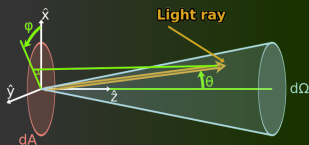
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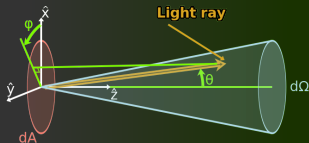
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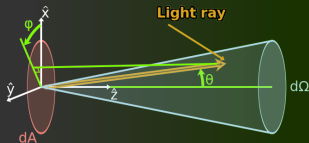
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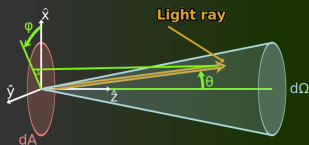
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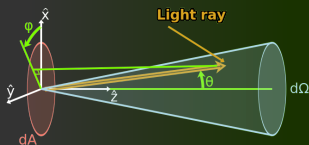
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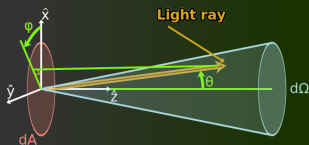
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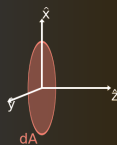
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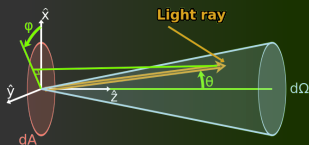
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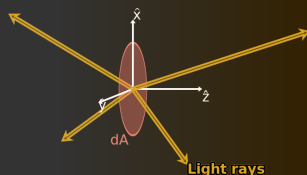
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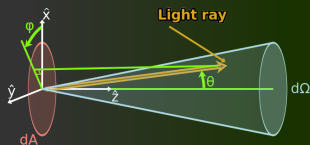
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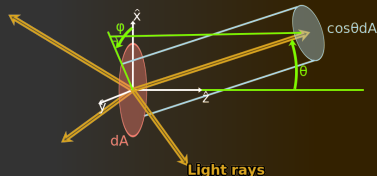
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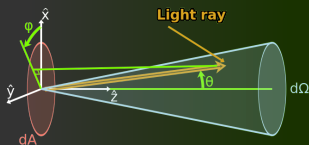
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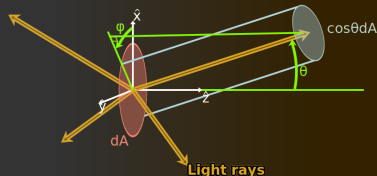
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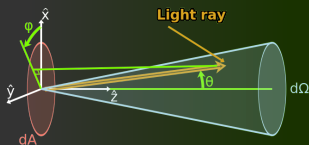
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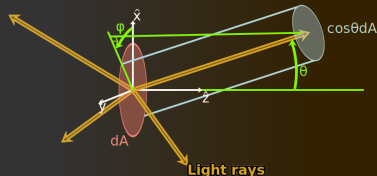
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Radiation pressure

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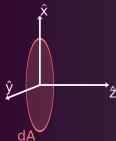
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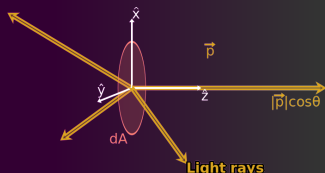
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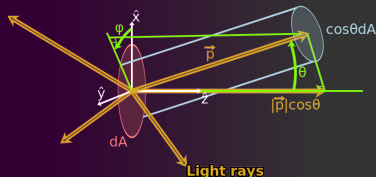
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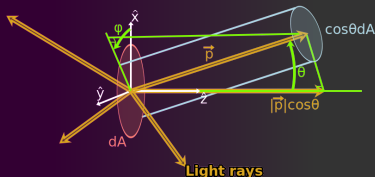
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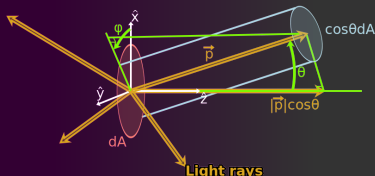
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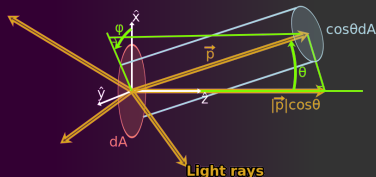
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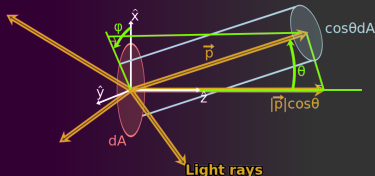
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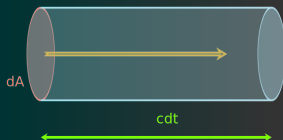
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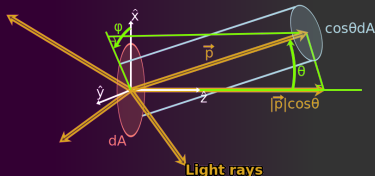
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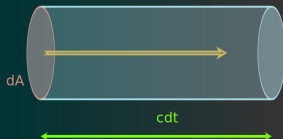
$$U_\nu(\nu, \vec{r}, \theta, \phi) \equiv \frac{dE}{dV d\Omega d\nu} = \frac{dE}{cdt dA d\Omega d\nu}$$

$$\Rightarrow U_\nu(\nu, \vec{r}, \theta, \phi) = \frac{I_\nu(\nu, \vec{r}, \theta, \phi)}{c}.$$

## Radiation pressure



## Energy density



## Emission & absorption coefficient

# Transfer | The Specific Intensity & Its Moments (2/2)

## Radiation pressure

**Momentum flux** carried by a photon of frequency  $\nu$ :  $p = h\nu/c$ .

**Radiation pressure:** (2<sup>nd</sup> order moment of  $I_\nu$ )

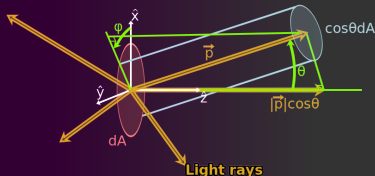
$$P_\nu \equiv \iint_{\Omega} I_\nu(\nu, \vec{r}, \theta, \phi) \cos^2 \theta \, d\Omega.$$

## Energy density

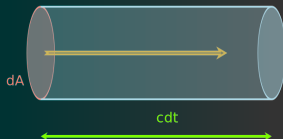
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### Radiation pressure



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## Emission & absorption coefficient

**Emission coefficient:**

$$j_\nu(\nu, \vec{r}, \theta, \phi) \equiv \frac{dE_{em}}{dt dV d\Omega d\nu}.$$

# Transfer | The Specific Intensity & Its Moments (2/2)

## Radiation pressure

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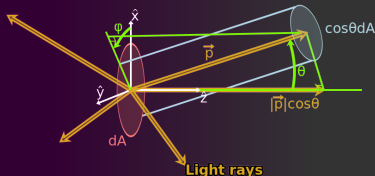
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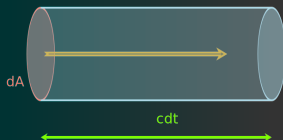
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## Emission & absorption coefficient

**Emission coefficient:**

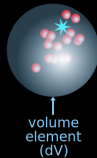
$$j_\nu(\nu, \vec{r}, \theta, \phi) \equiv \frac{dE_{em}}{dt dV d\Omega d\nu}.$$

**Extinction coefficient:**

$$\alpha(\vec{r}, \nu) = \rho(\vec{r}) \times \kappa(\vec{r}, \nu).$$

# Transfer | The Radiative Transfer Equation

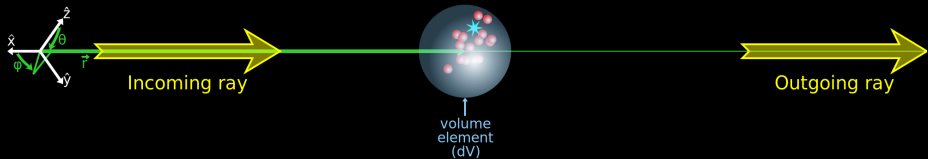
# Transfer | The Radiative Transfer Equation



(Rybicky & Lightman, 1979; Steinacker et al., 2013)



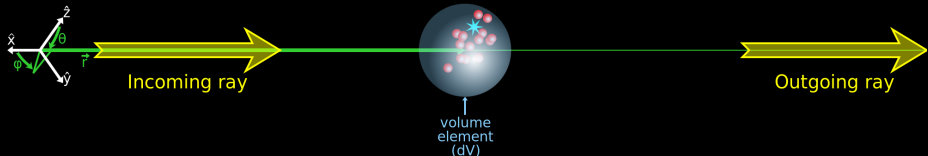
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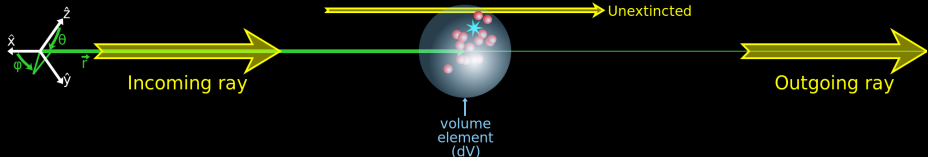
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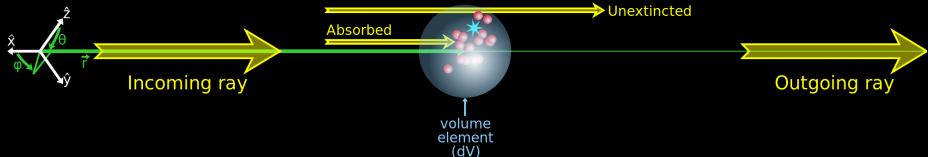
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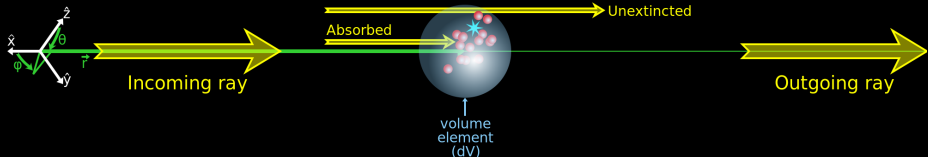
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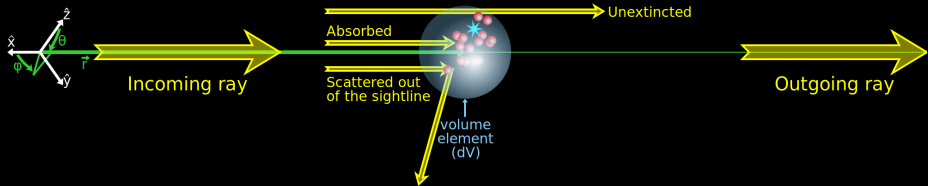
$$\frac{dl_\nu(\nu, \vec{r}, \theta, \phi)}{dl} = - \underbrace{\alpha_{\text{abs}}(\nu, \vec{r}) I_\nu(\nu, \vec{r}, \theta, \phi)}_{\text{absorption}}$$



(Rybicky & Lightman, 1979; Steinacker et al., 2013)

# Transfer | The Radiative Transfer Equation

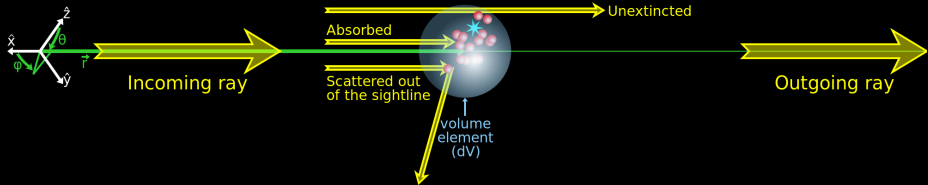
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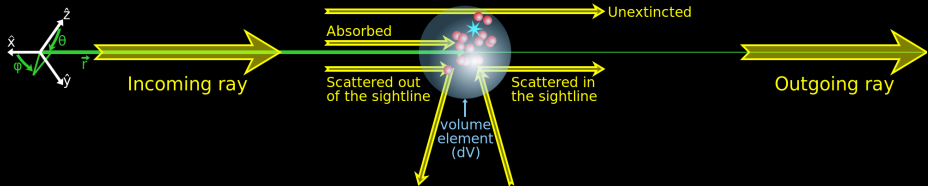
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(Rybicky & Lightman, 1979; Steinacker et al., 2013)

# Transfer | The Radiative Transfer Equation

$$\frac{dI_\nu(\nu, \vec{r}, \theta, \phi)}{dl} = - \underbrace{\alpha_{\text{abs}}(\nu, \vec{r}) I_\nu(\nu, \vec{r}, \theta, \phi)}_{\text{absorption}} - \underbrace{\alpha_{\text{sca}}(\nu, \vec{r}) I_\nu(\nu, \vec{r}, \theta, \phi)}_{\text{scattering out of the sightline}}$$

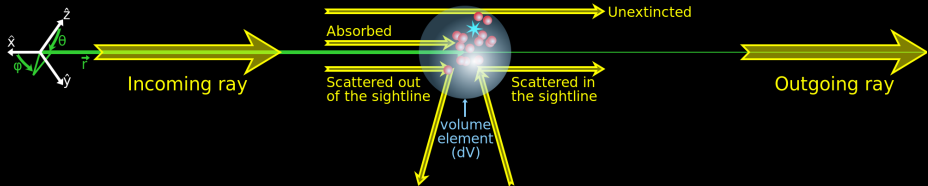


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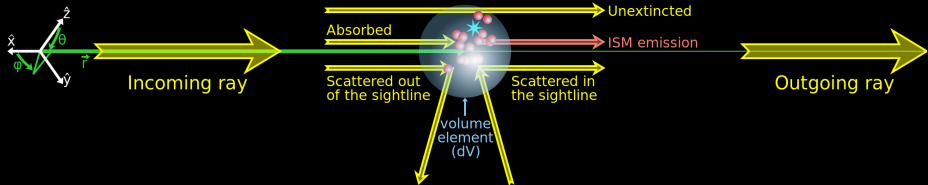
$$\frac{dl_\nu(\nu, \vec{r}, \theta, \phi)}{dl} = \underbrace{-\alpha_{\text{abs}}(\nu, \vec{r})l_\nu(\nu, \vec{r}, \theta, \phi)}_{\text{absorption}} - \underbrace{\alpha_{\text{sca}}(\nu, \vec{r})l_\nu(\nu, \vec{r}, \theta, \phi)}_{\text{scattering out of the sightline}} + \underbrace{\alpha_{\text{sca}}(\nu, \vec{r})2\pi \int_{-1}^1 \Phi(\cos \theta', \nu)l_\nu(\nu, \vec{r}, \theta(\theta'), \phi(\theta')) d \cos \theta'}_{\text{scattering in the sightline}}$$



(Rybicky & Lightman, 1979; Steinacker et al., 2013)

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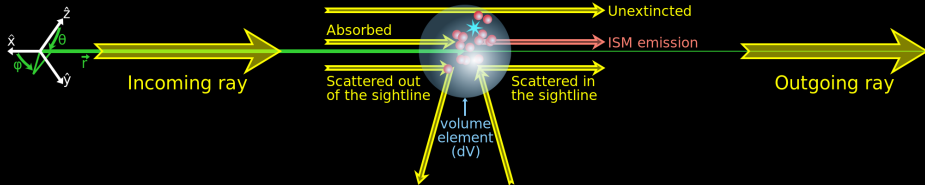
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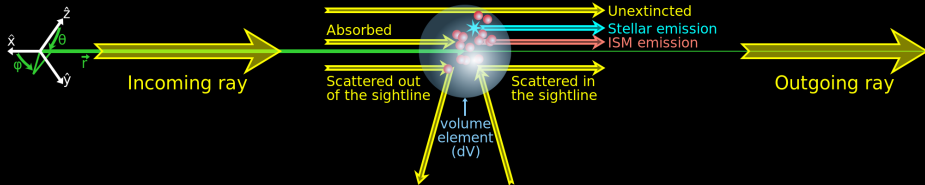
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(Rybicky & Lightman, 1979; Steinacker et al., 2013)

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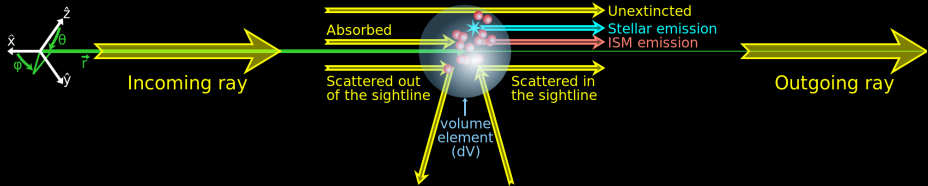
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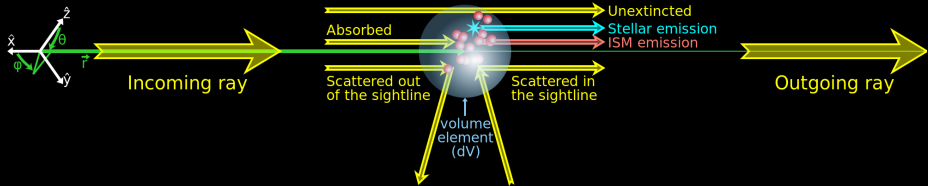
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(Rybicky & Lightman, 1979; Steinacker et al., 2013)

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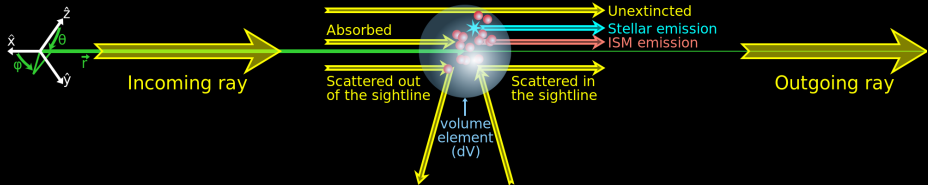


Solve this  $\forall \theta, \forall \phi, \forall \vec{r}, \forall \nu$

(Rybicky & Lightman, 1979; Steinacker et al., 2013)

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Solve this  $\forall \theta, \forall \phi, \forall \vec{r}, \forall \nu \Rightarrow$  numerically intensive.

(Rybicky & Lightman, 1979; Steinacker et al., 2013)

# Transfer | The Concept of Optical Depth



The optical depth along a sightline

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## The visible / near-IR mean free path for the different ISM phases

HIM	WNM	CNM	Molecular clouds
$n_{\text{H}} = 0.003 \text{ cm}^{-3}$	$n_{\text{H}} = 0.3 \text{ cm}^{-3}$	$n_{\text{H}} = 30 \text{ cm}^{-3}$	$n_{\text{H}} = 10^4 \text{ cm}^{-3}$

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$l_{\text{mean}}(U)$	139 kpc	1.39 kpc	13.9 pc	0.0417 pc

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$l_{\text{mean}}(V)$	223 kpc	2.23 kpc	22.3 pc	0.0669 pc

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$l_{\text{mean}}(U)$	139 kpc	1.39 kpc	13.9 pc	0.0417 pc
$l_{\text{mean}}(B)$	177 kpc	1.77 kpc	17.7 pc	0.0532 pc
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$l_{\text{mean}}(R)$	275 kpc	2.75 kpc	27.5 pc	0.0824 pc

# Transfer | The Concept of Optical Depth

## The optical depth along a sightline

Along a given sightline,  $l$ :

$$d\tau(\nu, l) = \alpha(\nu, l) dl = \underbrace{\rho(l)}_{\text{specific mass}} \times \underbrace{\kappa(\nu, l)}_{\text{opacity}} dl$$

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$$l_{\text{mean}}(\nu, \vec{r}) = \frac{1}{\alpha(\nu, \vec{r})} = \frac{1}{\rho(\vec{r})\kappa(\nu, \vec{r})}$$

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$l_{\text{mean}}(J)$	691 kpc	6.91 kpc	69.1 pc	0.207 pc
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(Rybicky & Lightman, 1979)



Transfer equation:  $\frac{dI_\nu}{dr} = 0$

(Rybicky & Lightman, 1979)



Transfer equation:  $\frac{dI_\nu}{dr} = 0 \Rightarrow I_\nu(R_*) = I_\nu(r) = B_\nu(T_*)$

(Rybicky & Lightman, 1979)

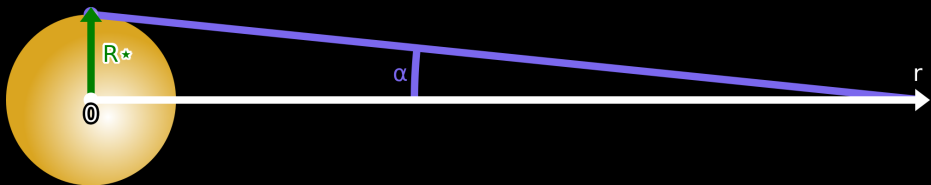


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(Rybicky & Lightman, 1979)

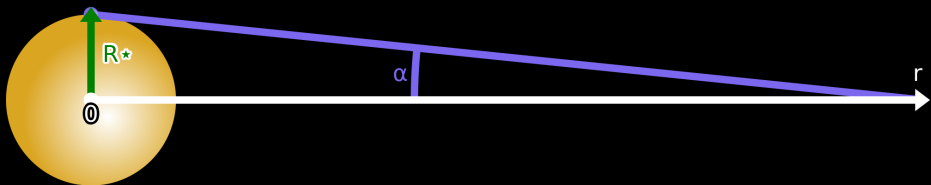


## Transfer | Analytical Solutions: Radiative Transfer in Vacuum



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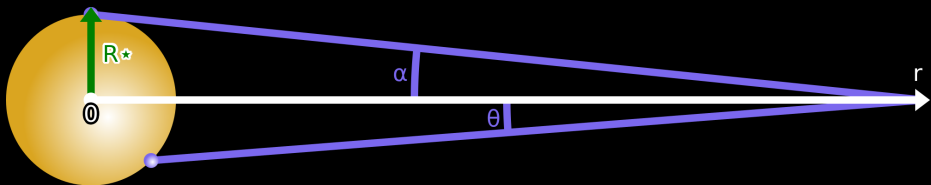


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**Angular size** at distance  $r$ :  $\sin \alpha = \frac{R_\star}{r}$ .

(Rybicky & Lightman, 1979)

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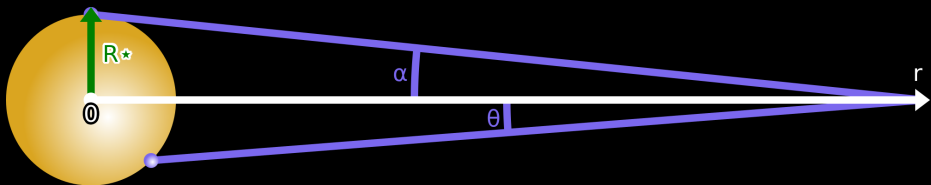


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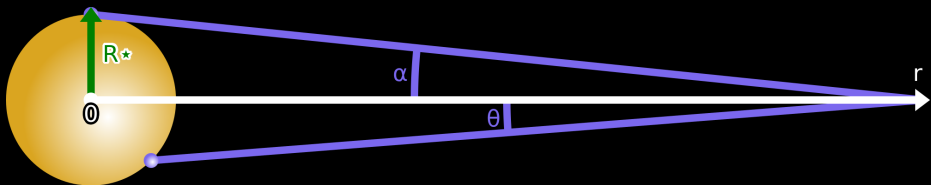
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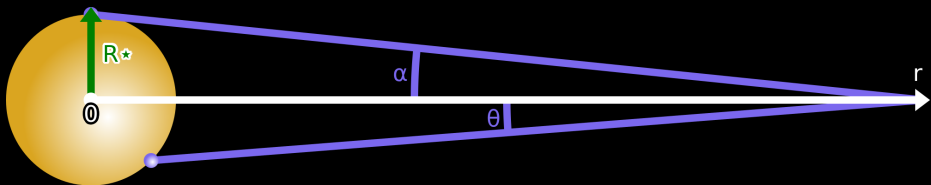
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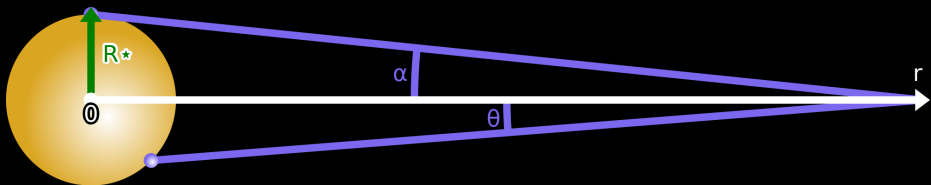
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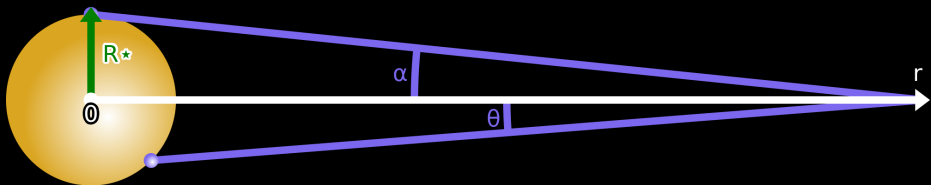
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**Consistency check:**  $F_\nu(R_\star) = \pi B_\nu(T_\star)$

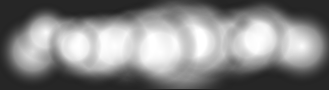
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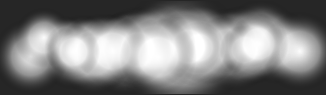


Emission only

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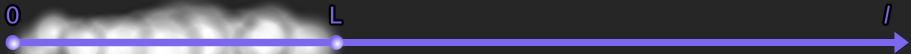


## Emission only



**Hypothesis:** homogeneous dust cloud of grains at thermal equilibrium,  $T = T_d$ , with opacity  $\kappa$ .

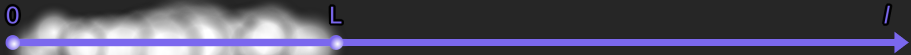
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# Transfer | Analytical Solutions: Emission or Absorption

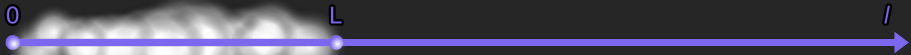
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## Emission only



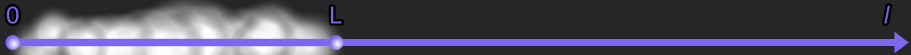
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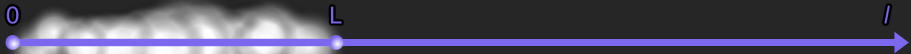
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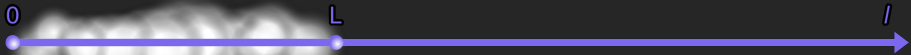
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## Absorption only

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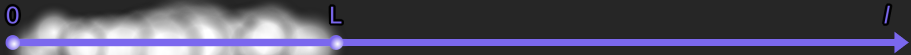
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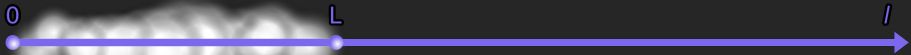
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**Hypothesis:** dust cloud, with opacity  $\kappa$ , in front of a star of specific intensity  $I_\nu^*$ .

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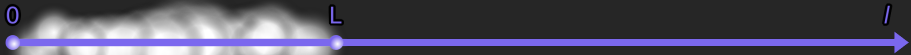
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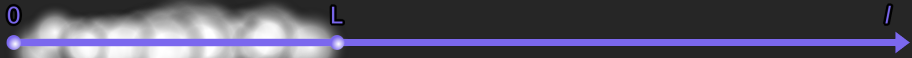


**Hypothesis:** dust cloud, with opacity  $\kappa$ , in front of a star of specific intensity  $I_\nu^*$ .

**Transfer equation:**  $\frac{dI_\nu}{dl} = -\alpha(l)I_\nu$

# Transfer | Analytical Solutions: Emission or Absorption

## Emission only

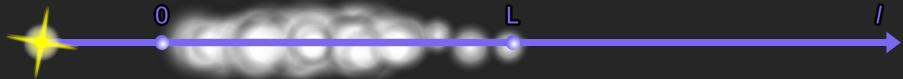


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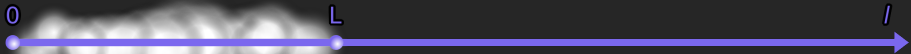


**Hypothesis:** dust cloud, with opacity  $\kappa$ , in front of a star of specific intensity  $I_\nu^*$ .

**Transfer equation:**  $\frac{dI_\nu}{dl} = -\alpha(l)I_\nu \Rightarrow I_\nu = I_\nu^* \exp \left[ -\kappa \int_0^L \alpha dl \right]$

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**Transfer equation:** can be simplified using  $\tau$  instead of  $l$  as a parameter:  $\frac{dI_\nu}{d\tau} = -I_\nu + S_\nu$ .

source function

## Transfer | Analytical Solutions: Emission & Absorption

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**Solution:**  $I_\nu(\tau) = I_\nu^* \exp(-\tau) + \int_0^\tau \exp(\tau' - \tau) \times S_\nu(\tau') d\tau'$

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$$\Rightarrow I_\nu = \underbrace{I_\nu^* \exp(-\tau)}_{\text{stellar extinction}} +$$

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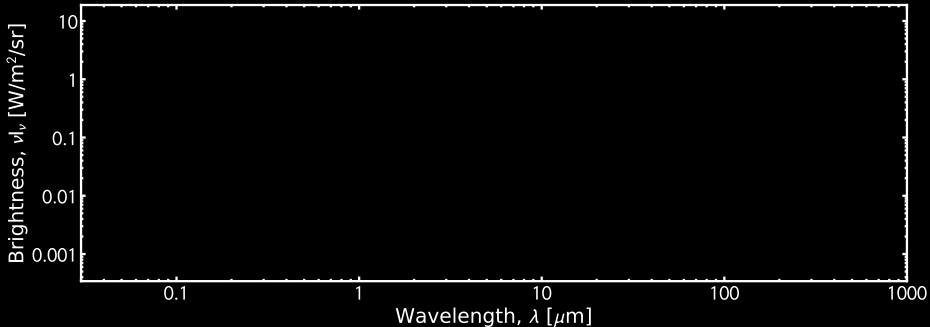
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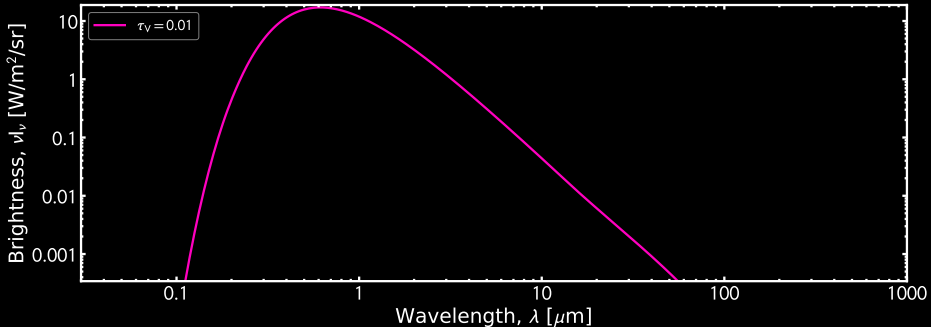
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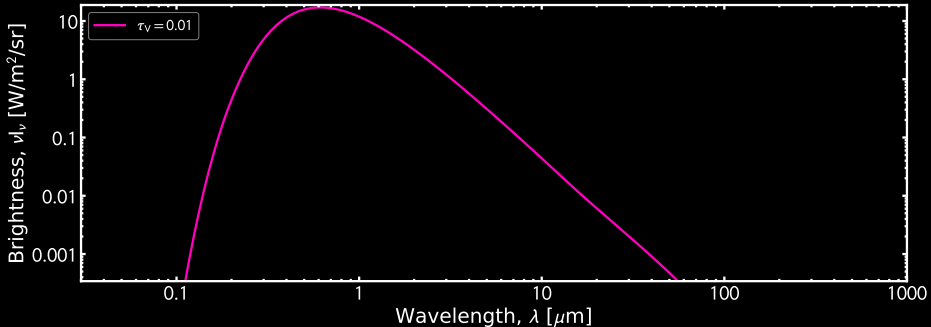


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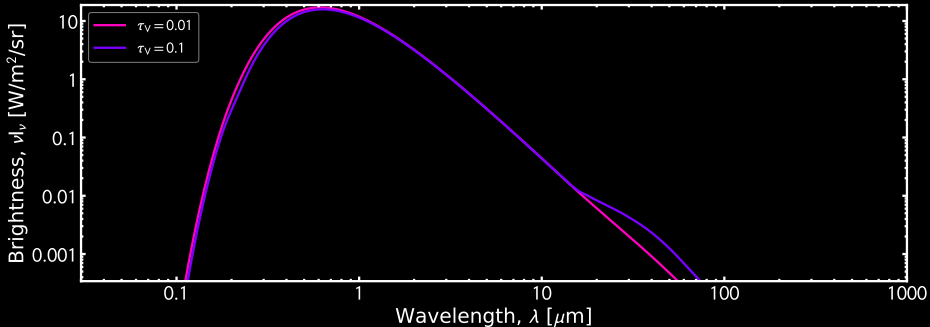


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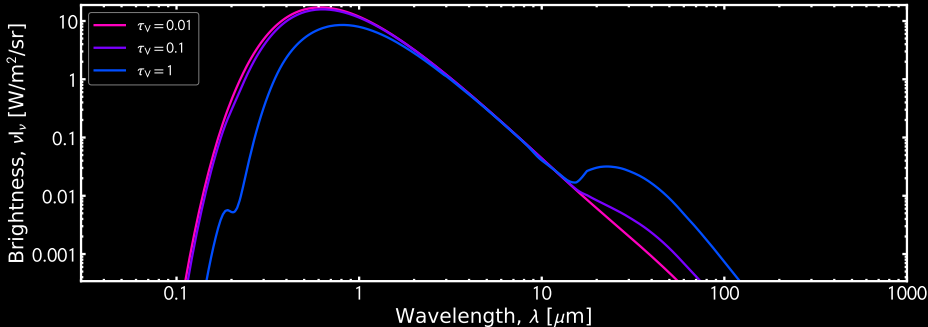


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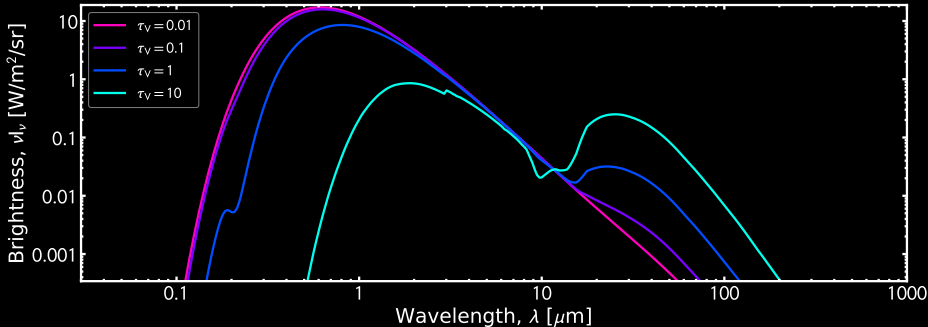
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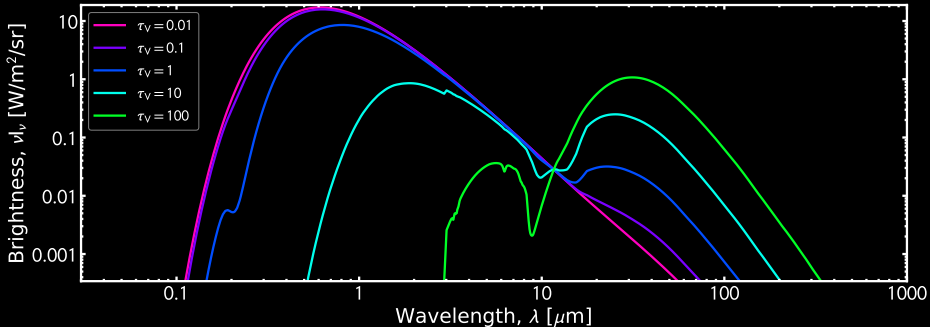
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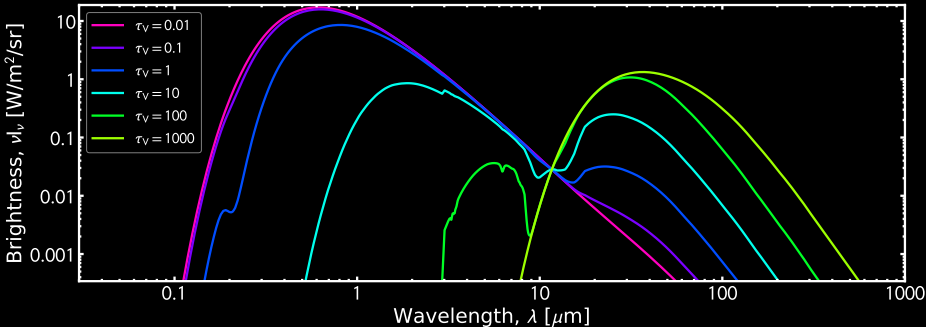
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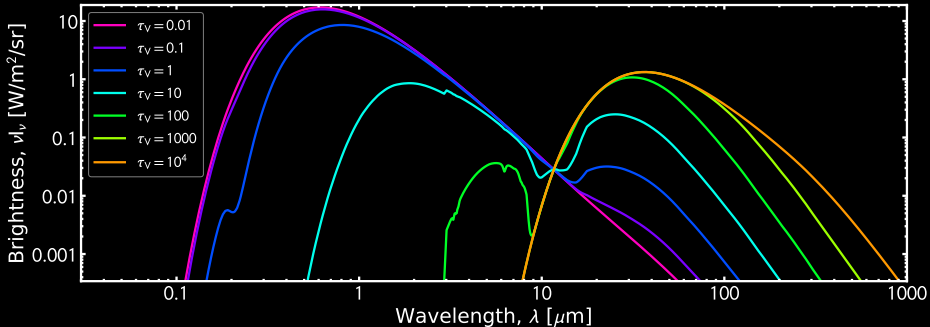
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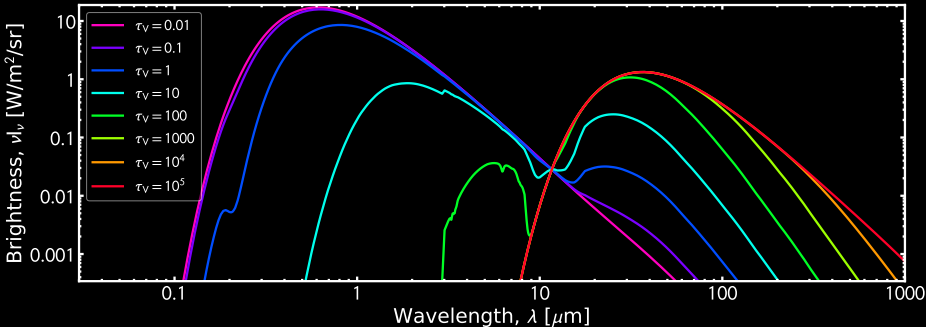
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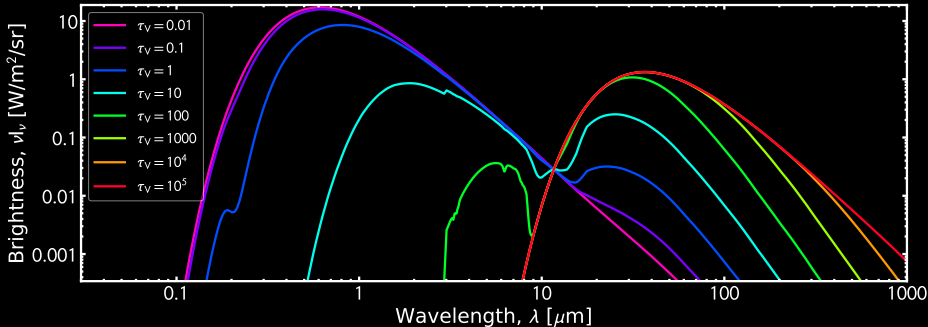
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# Transfer | Application to the 21 cm HI Line



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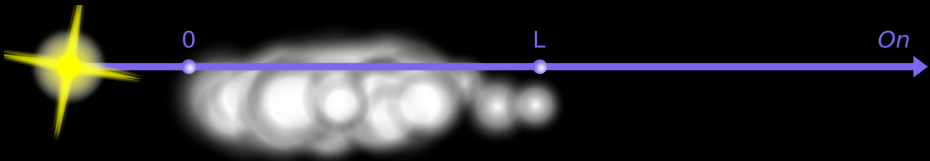
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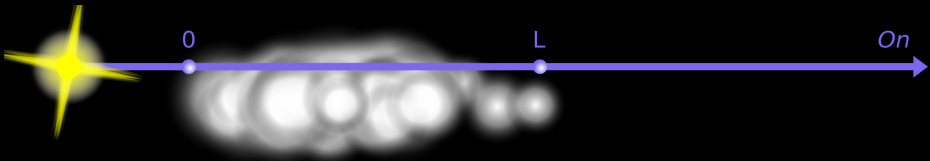
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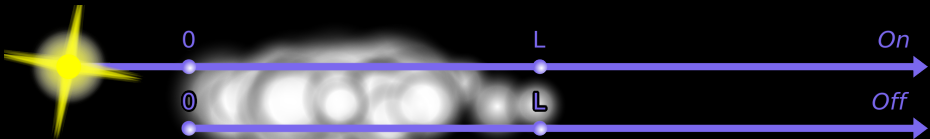
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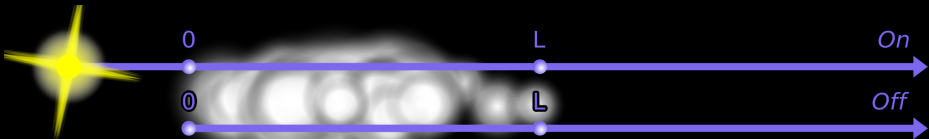
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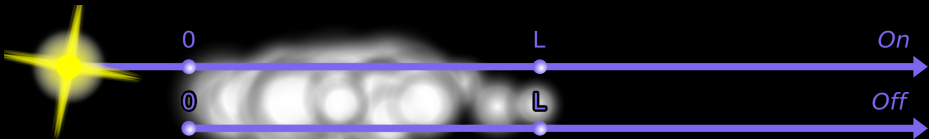
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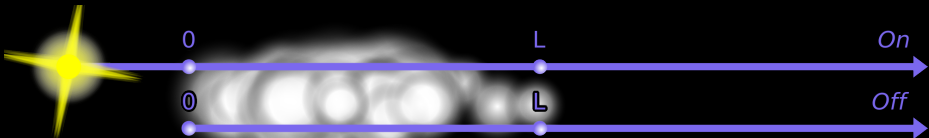
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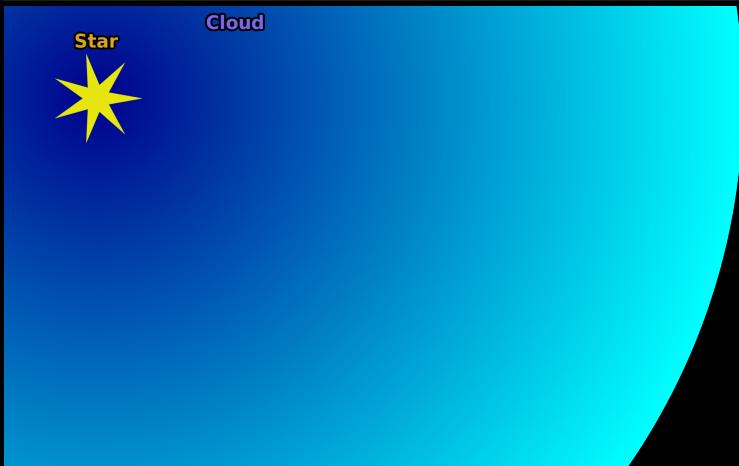
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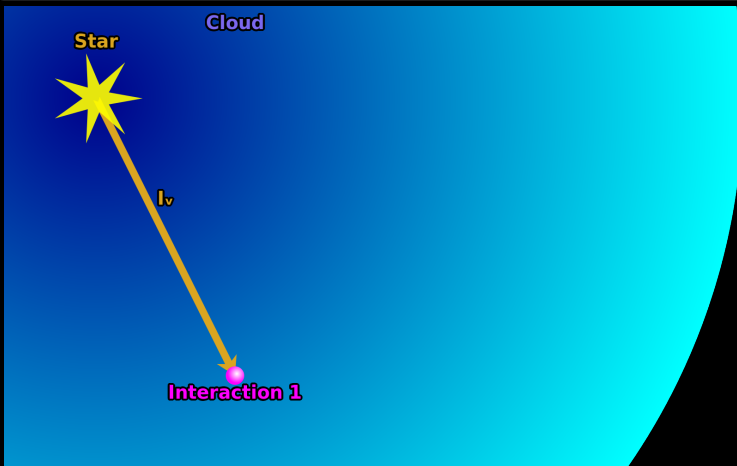


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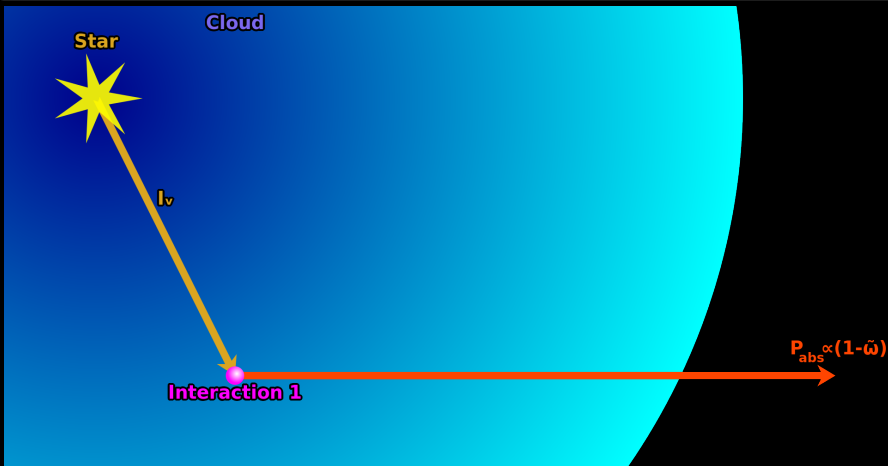


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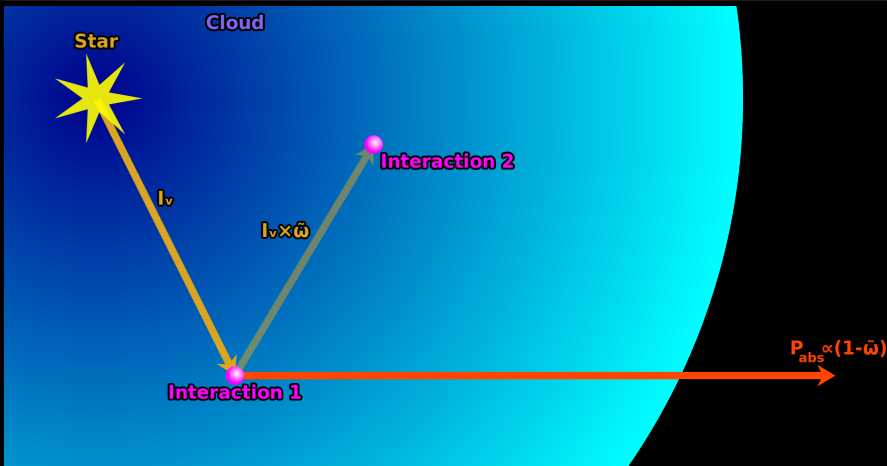


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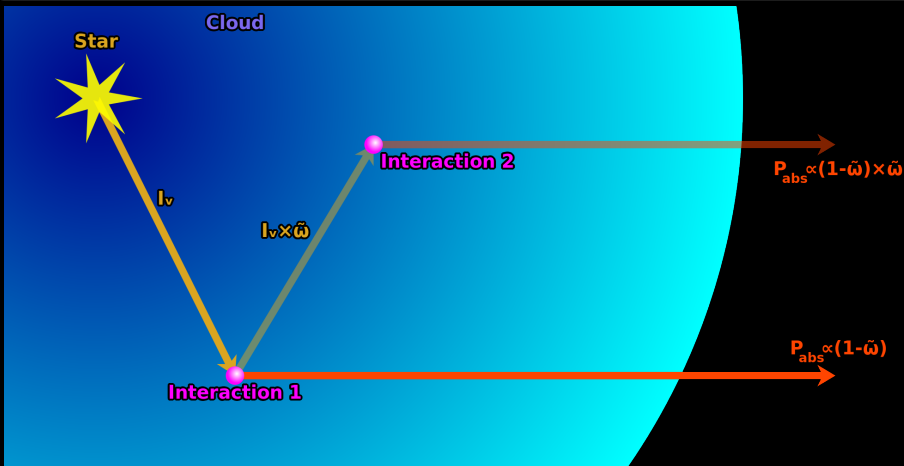
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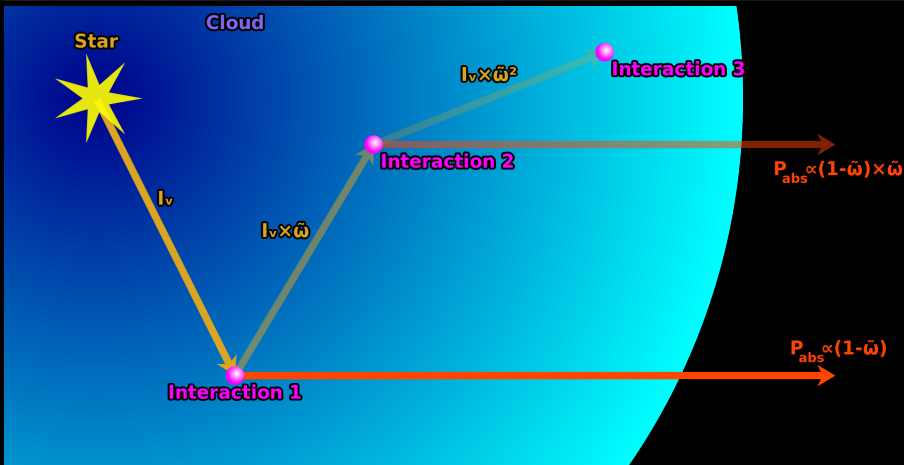


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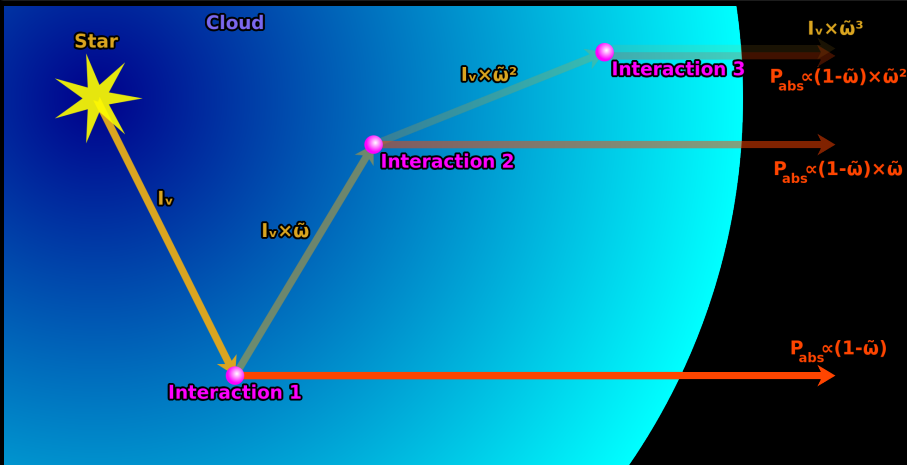


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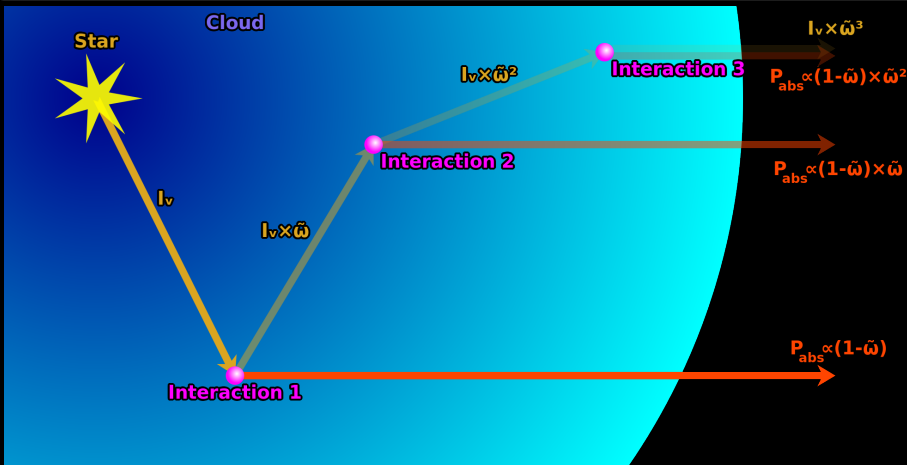
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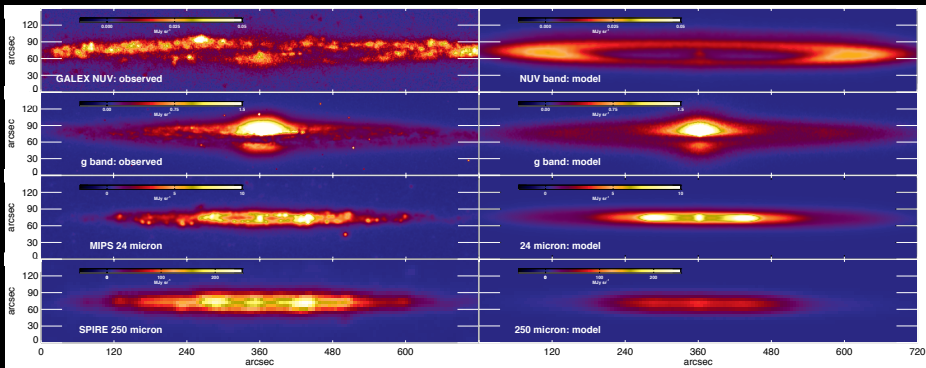
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**Iterative process** is required to compute atomic & molecular level populations & dust heating.





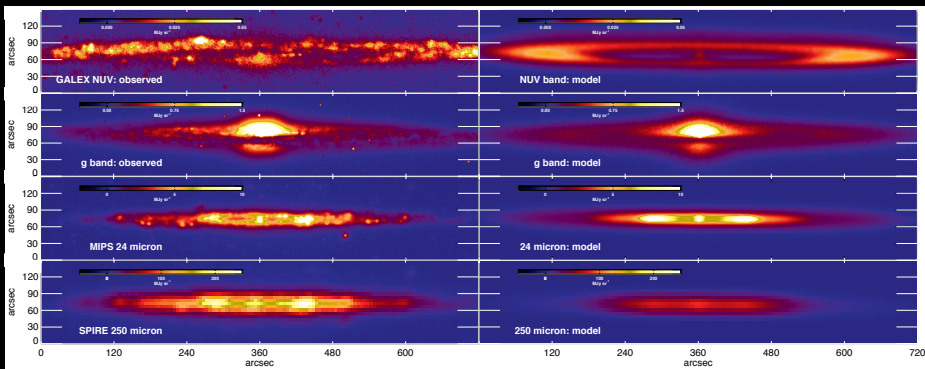
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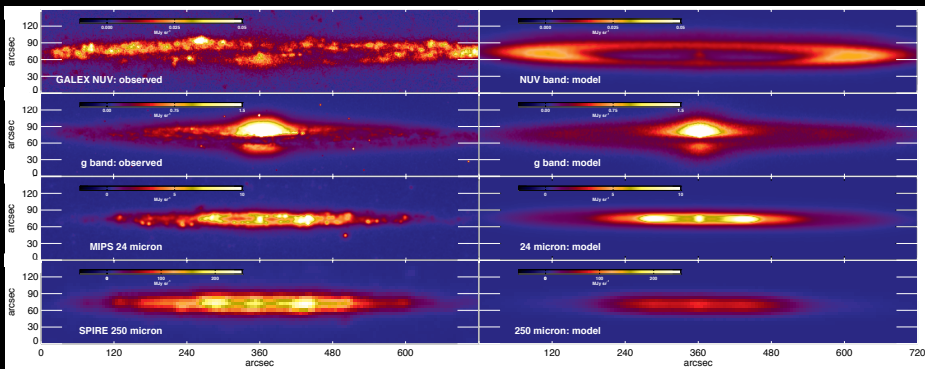
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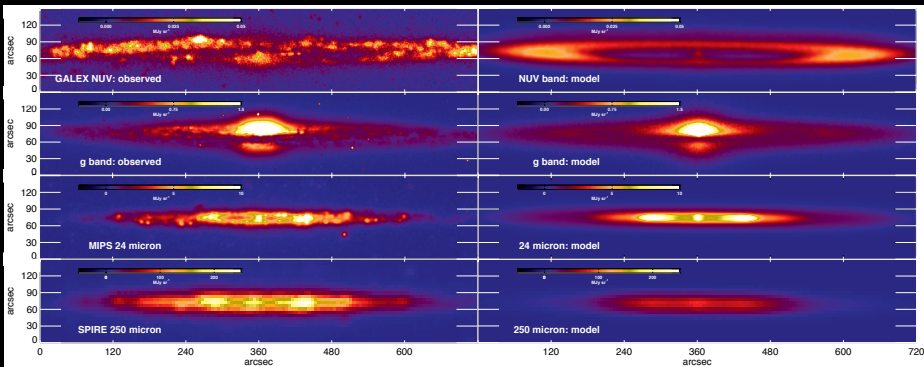


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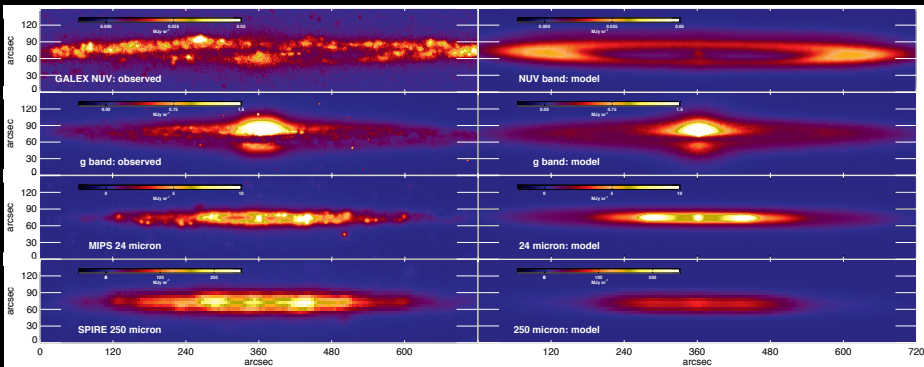


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## Simulations:

Monte Carlo radiative transfer models can also be used to post-process numerical simulations of star-forming regions or galaxies  $\Rightarrow$  synthetic observables.

# Outline of the Lecture

## 1 COOLING & HEATING OF THE GAS

- The gas heating processes
- The gas cooling function
- The five thermal phases of the ISM

## 2 THE PRINCIPLES OF RADIATIVE TRANSFER

- The radiative transfer equation
- Solutions in simple cases
- Dust radiative transfer with more complex geometries

## 3 STAR-FORMING REGIONS

- The Structure of Star-Forming Regions
- H II regions
- PhotoDissociation Regions (PDRs)

## 4 CONCLUSION

- Take-away points
- References

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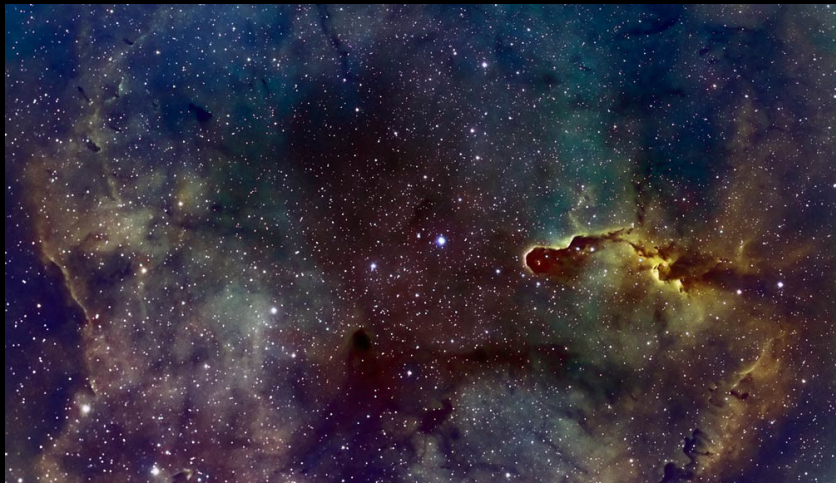
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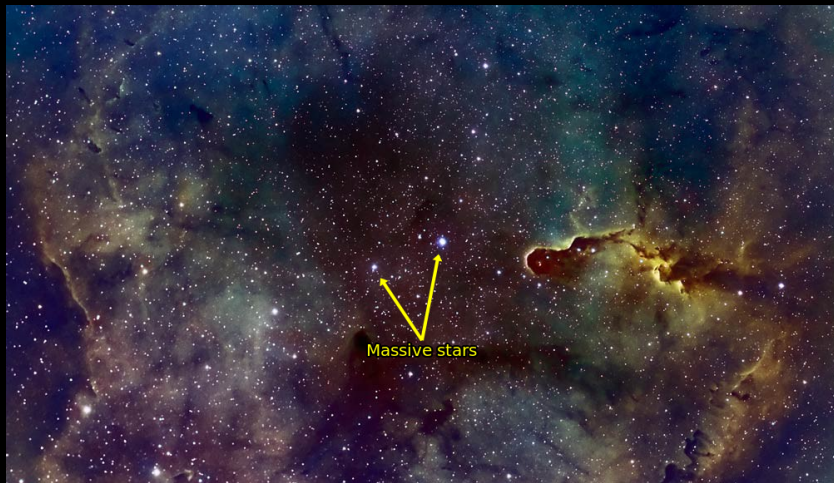


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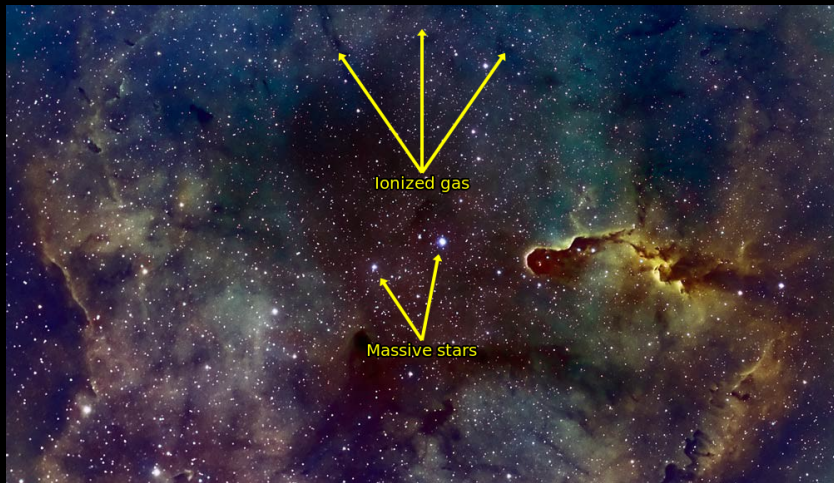


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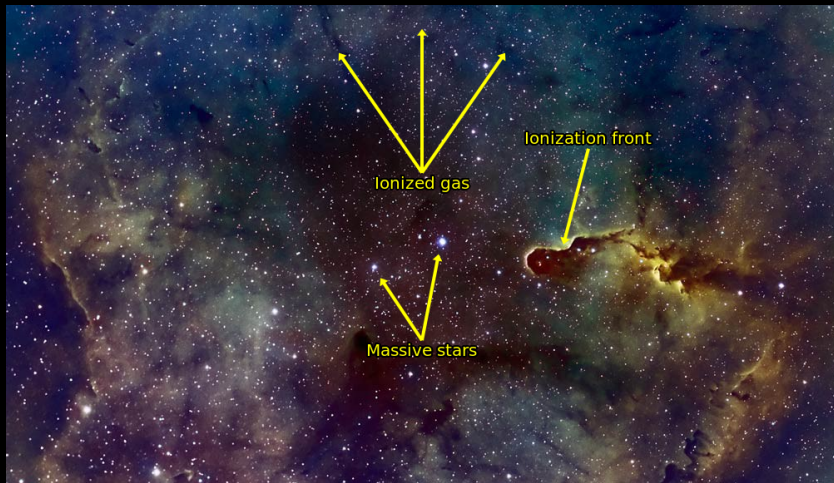


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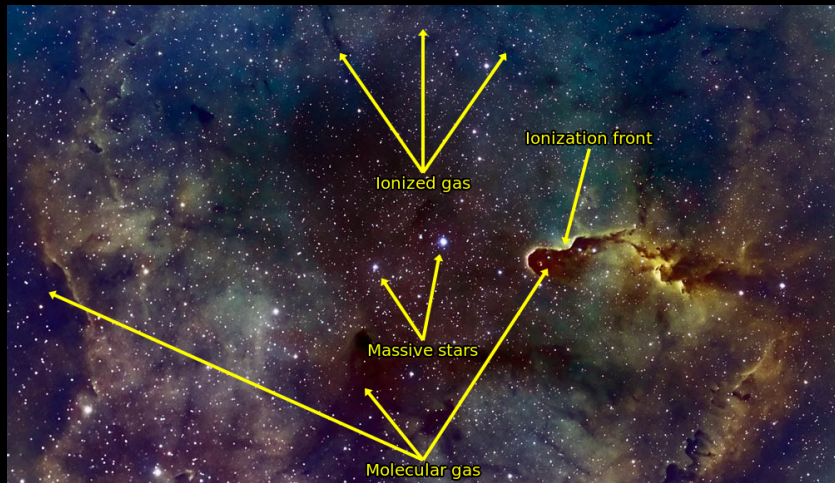


Credit: IC 1396 (Kallias IOANNIDIS).

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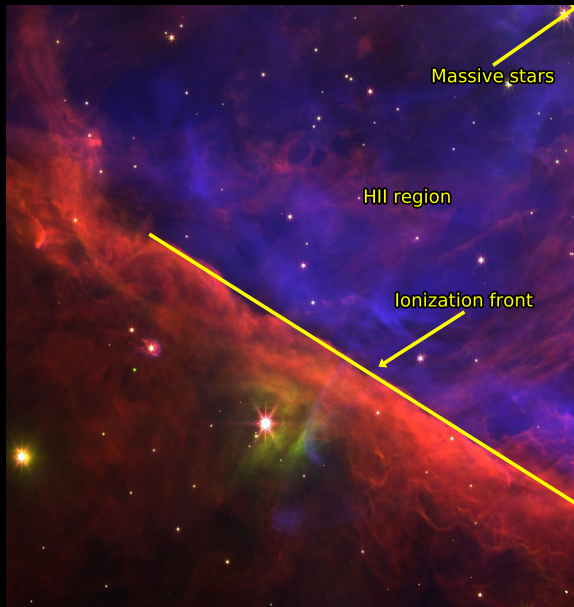


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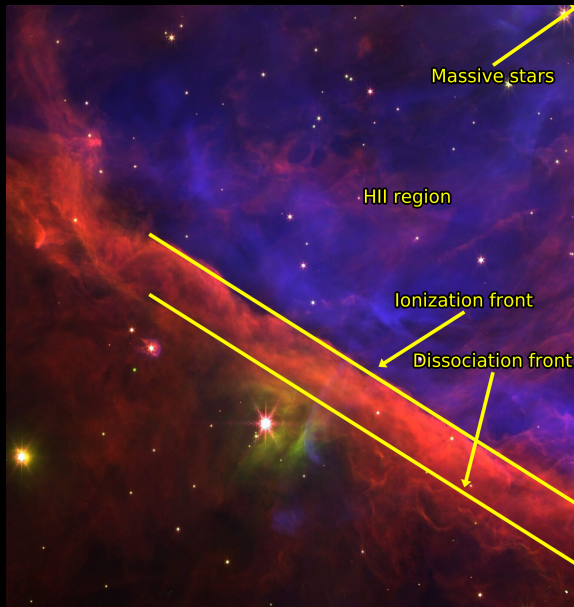
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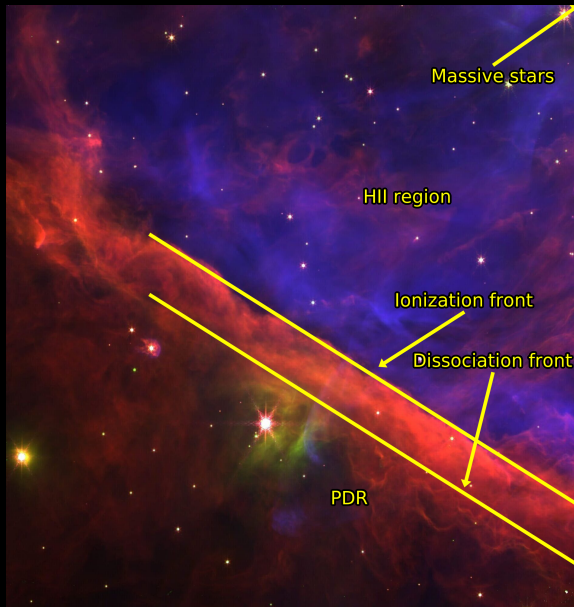
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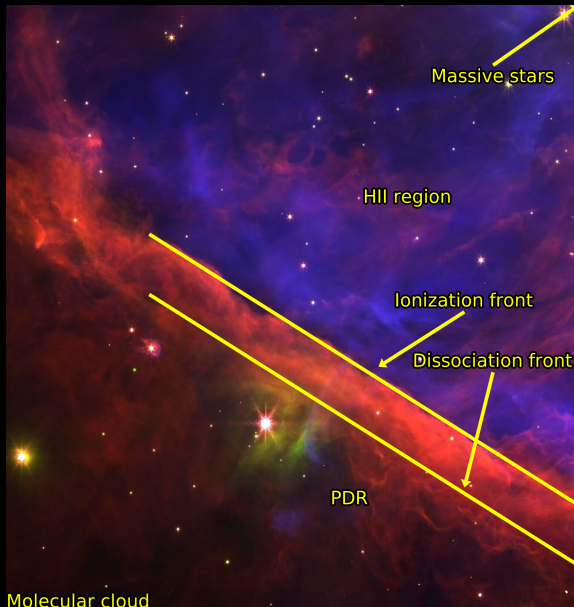
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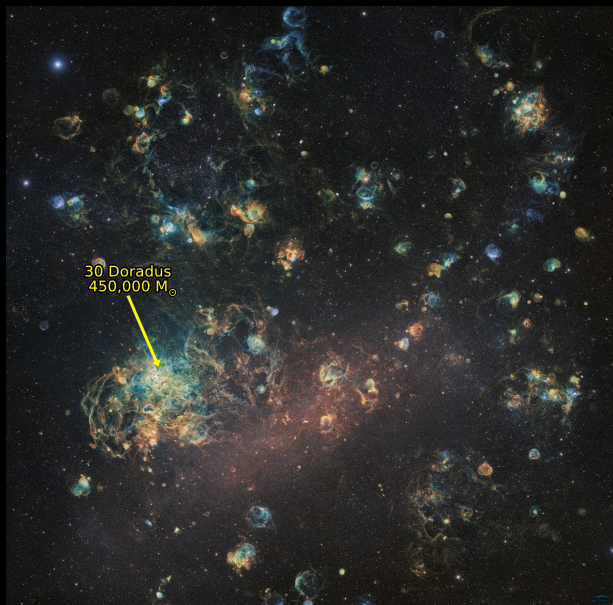
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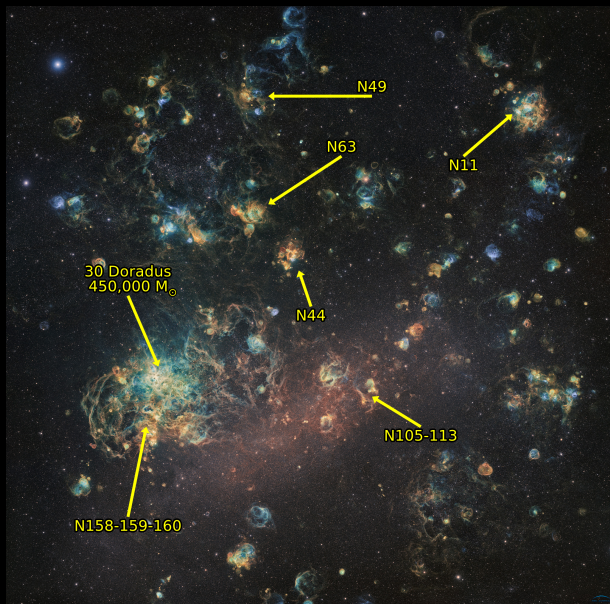
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Name	Scope	Reference	Download link
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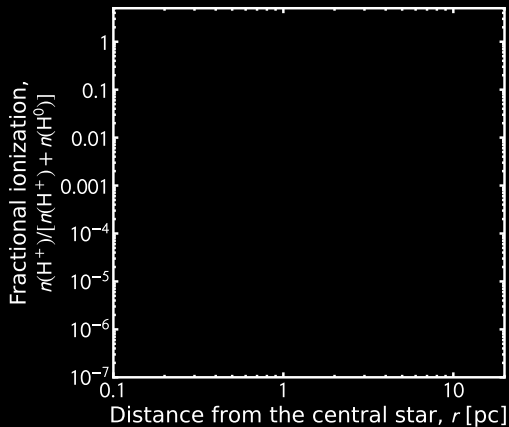
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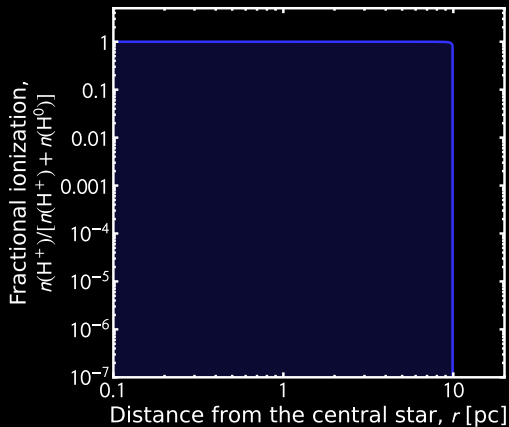
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UCL PDR	PDRs (3D)	Bell et al. (2005); Bisbas et al. (2012)	<a href="https://uclchem.github.io/">https://uclchem.github.io/</a>

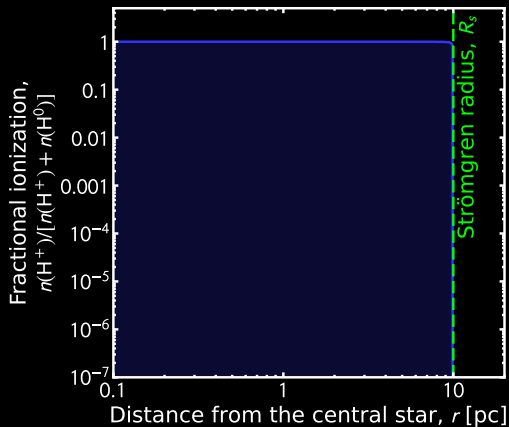
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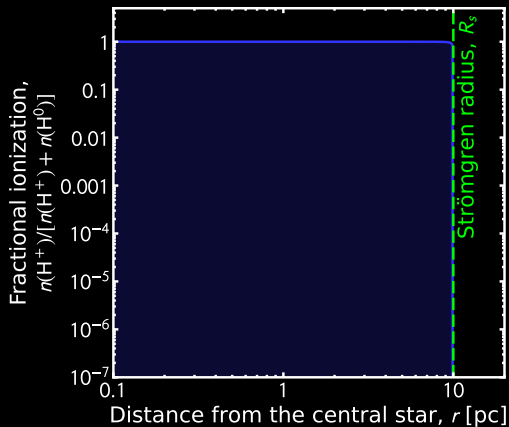


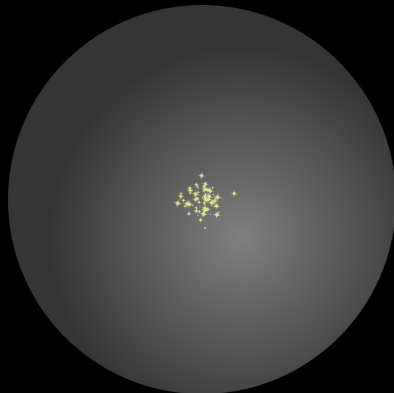
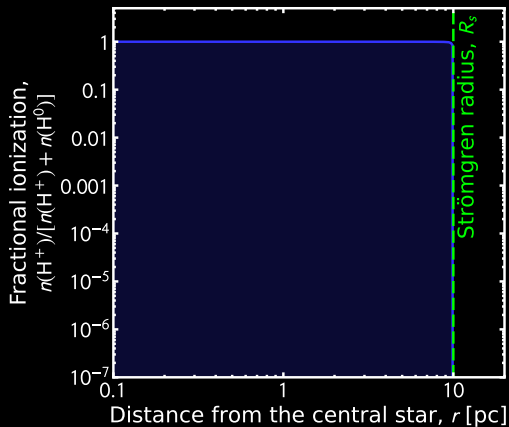




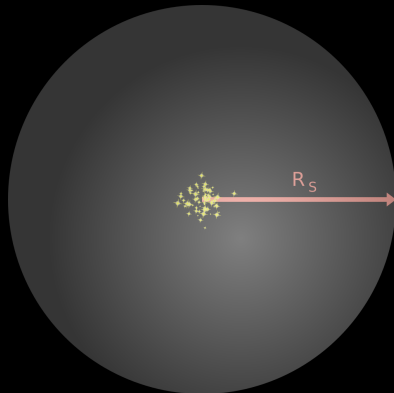
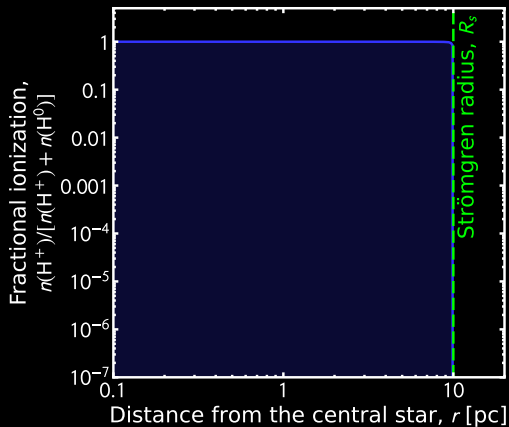


# SF regions | Photoionization Balance – The Strömgen Sphere

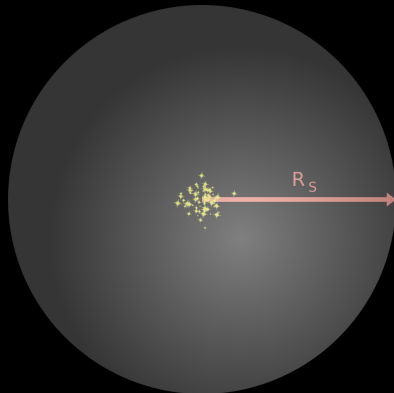
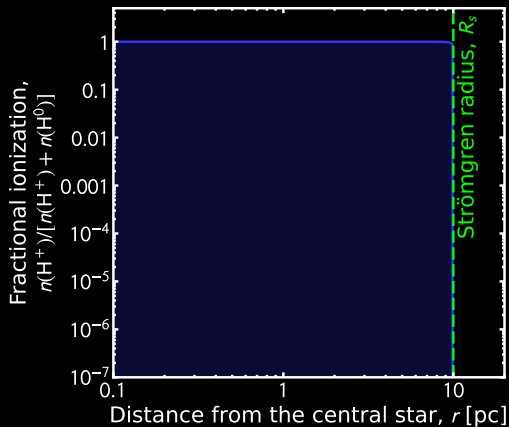




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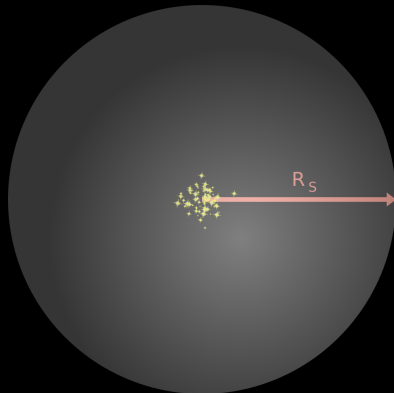
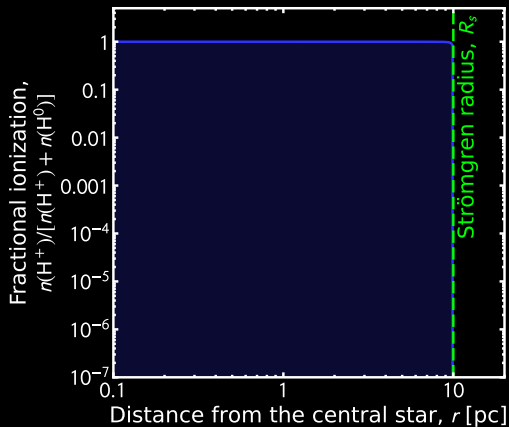
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The size of an H II region (Strömgen, 1939)



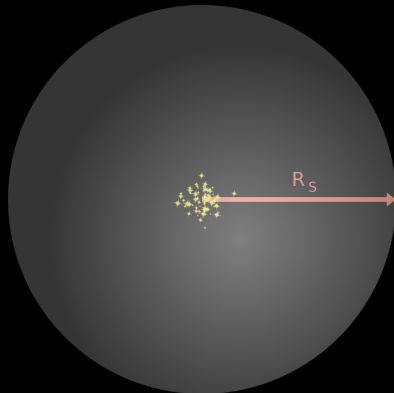
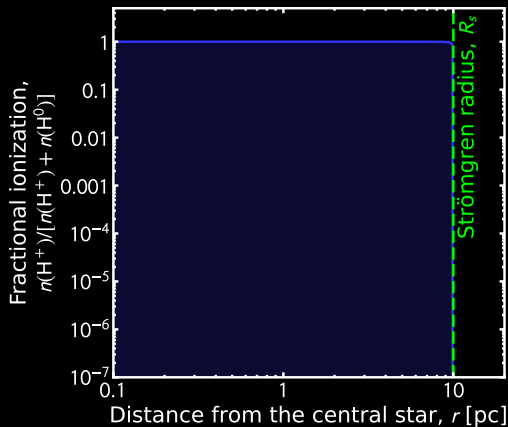
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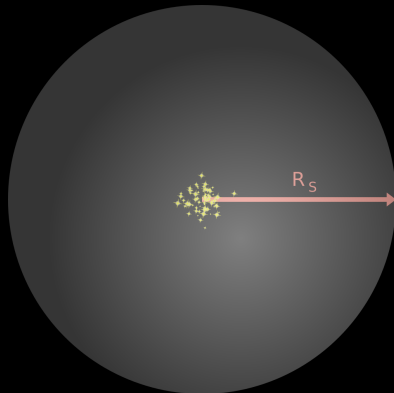
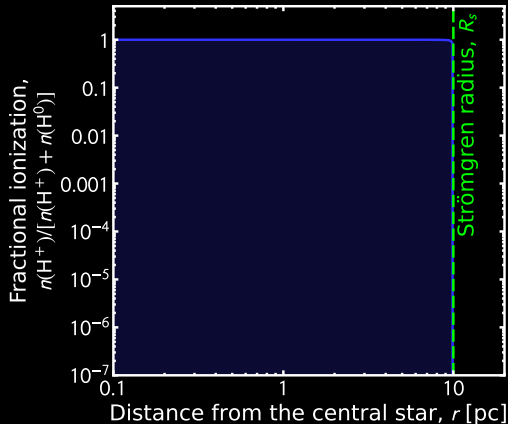
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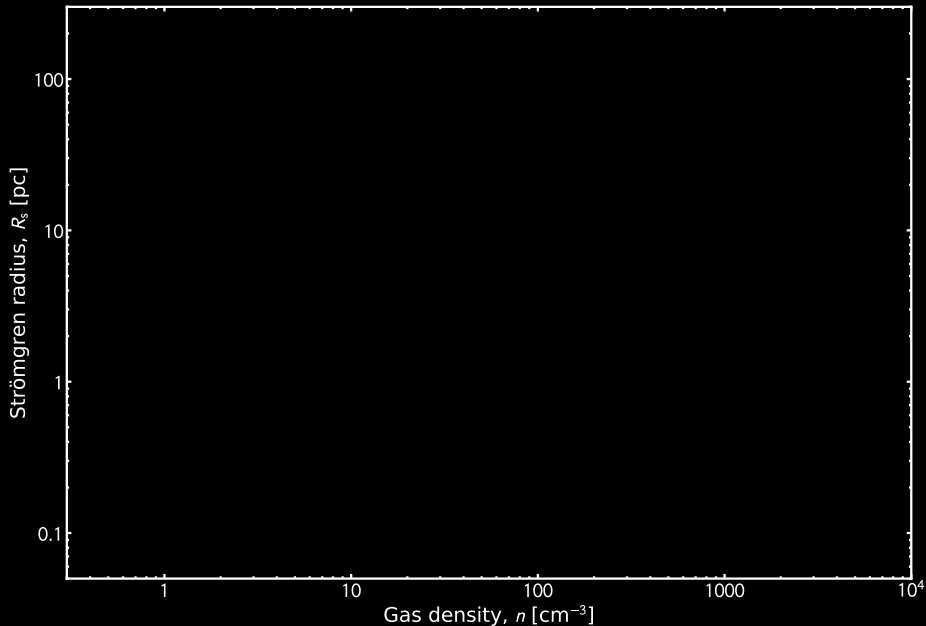
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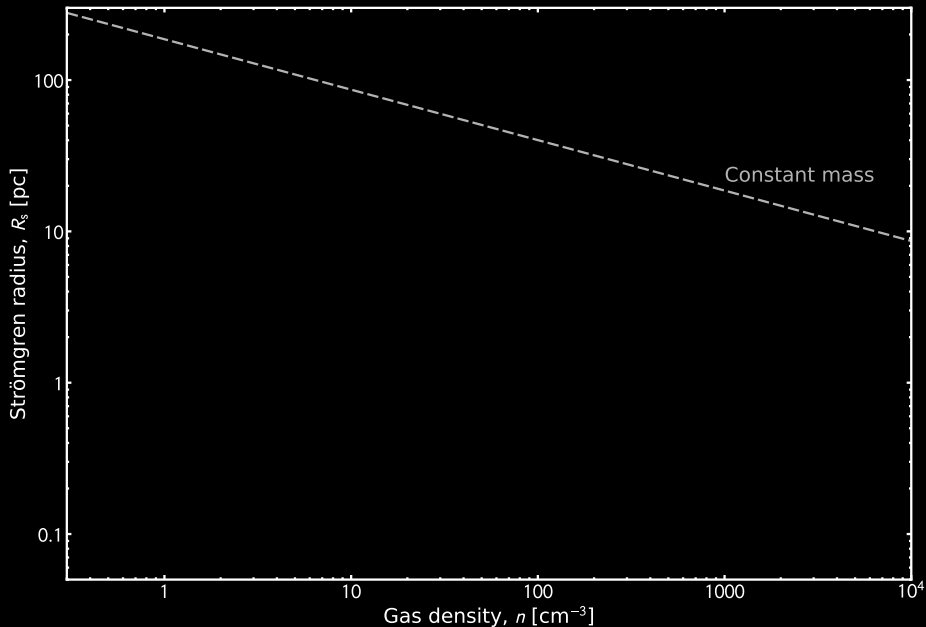


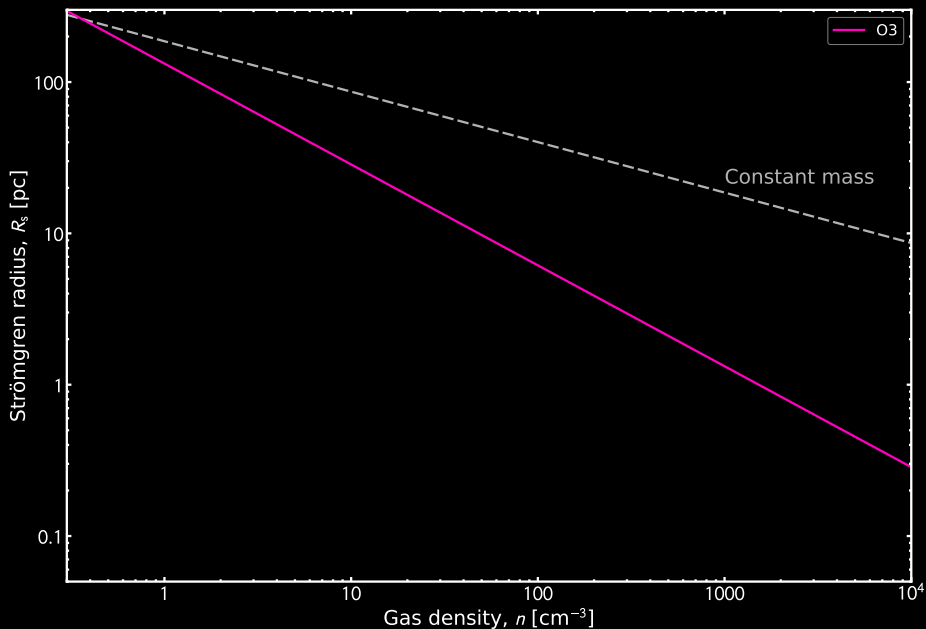
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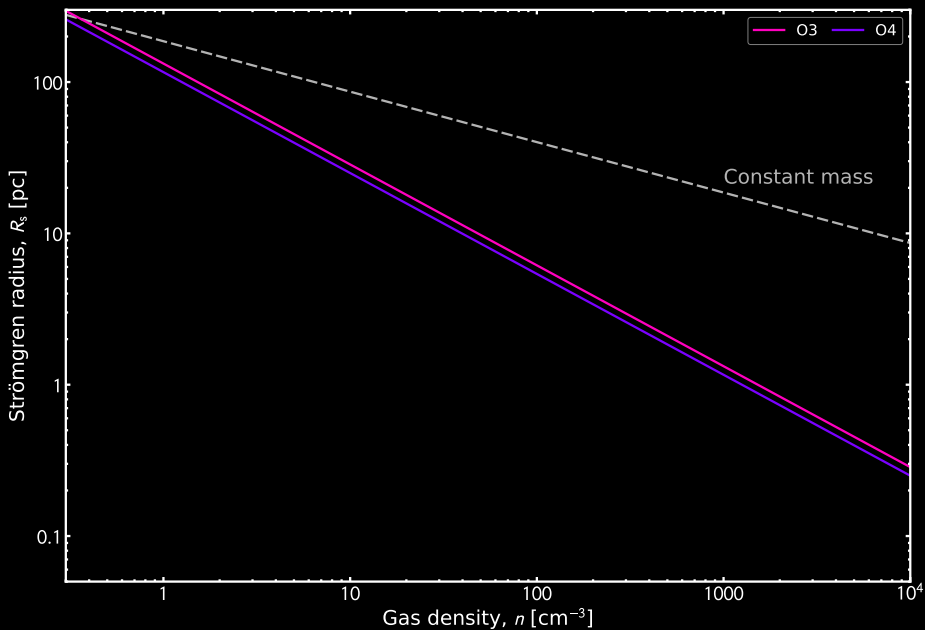






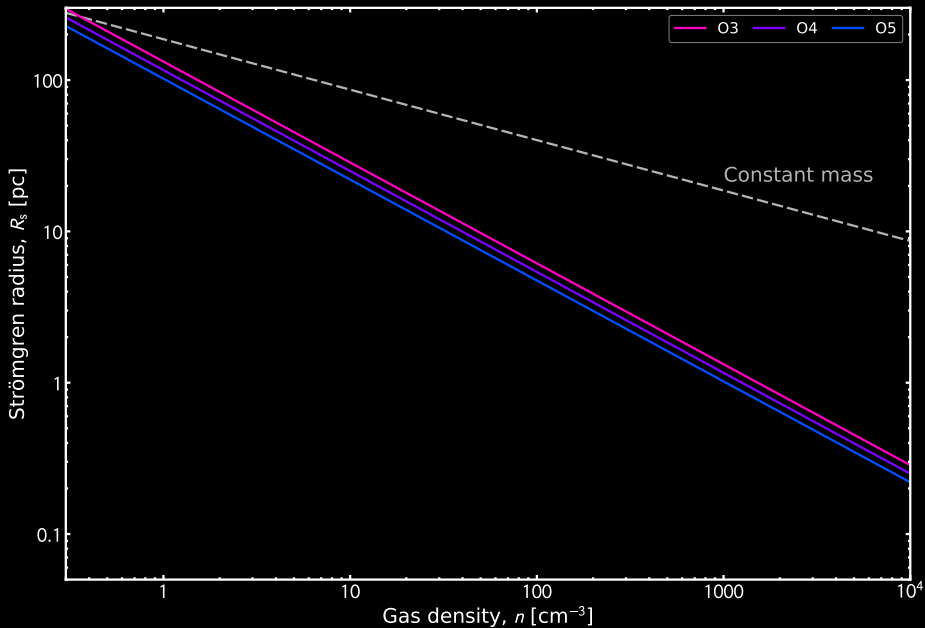


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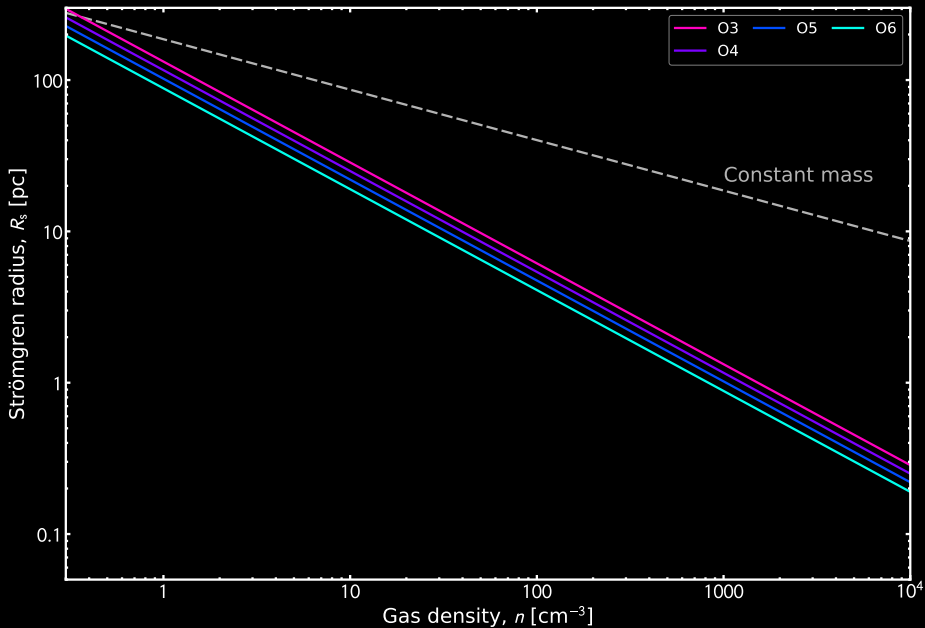




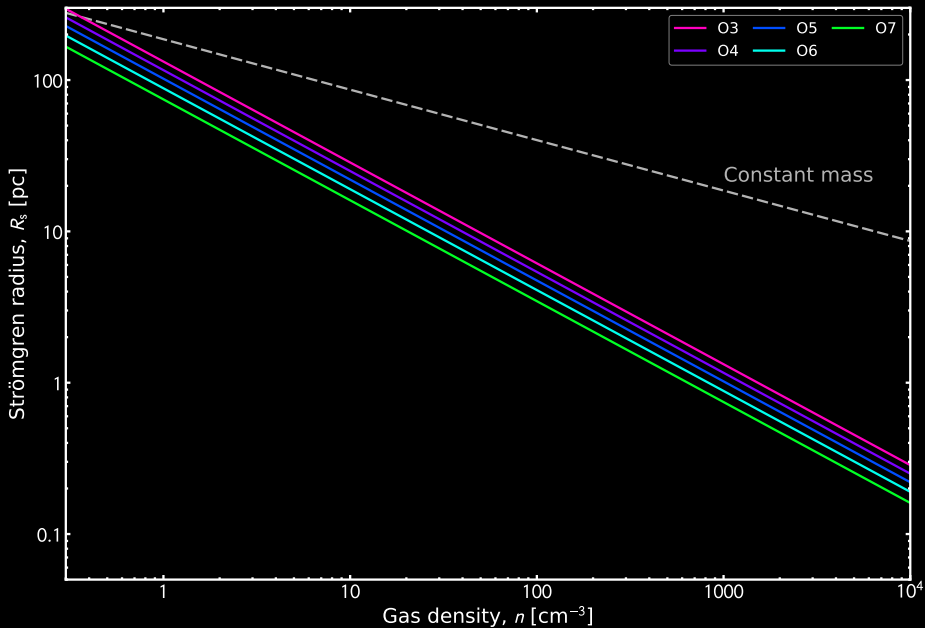
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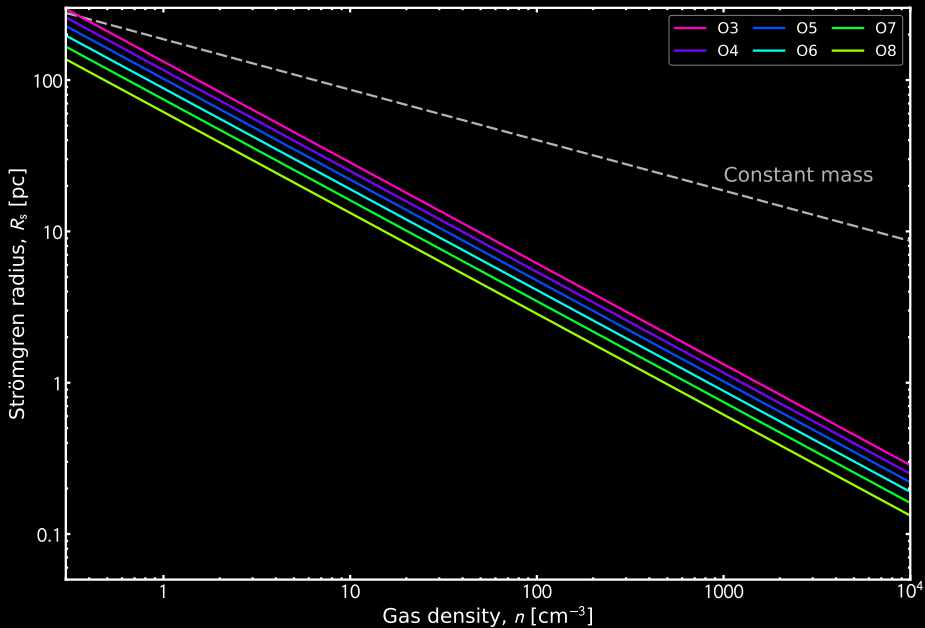
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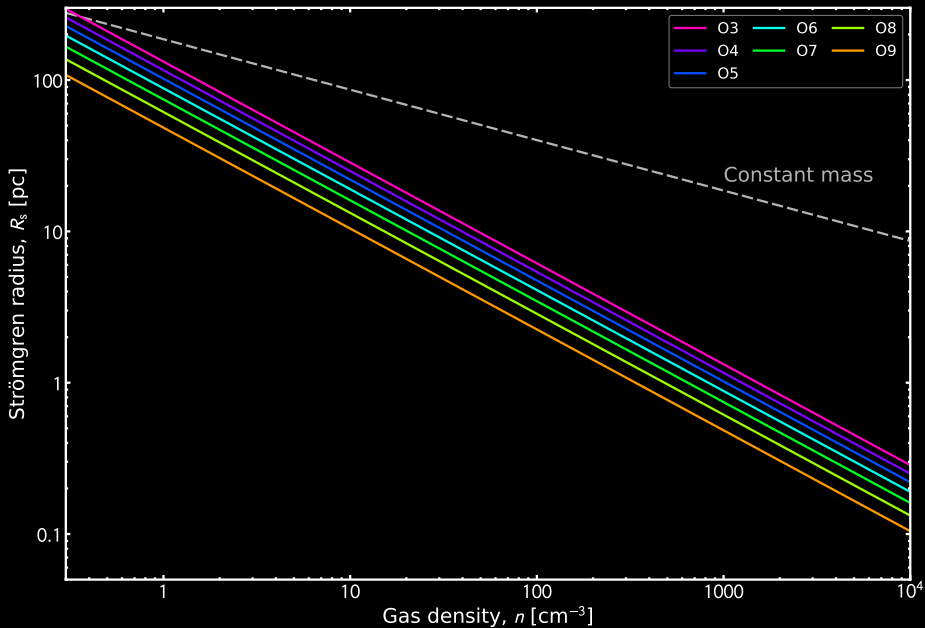
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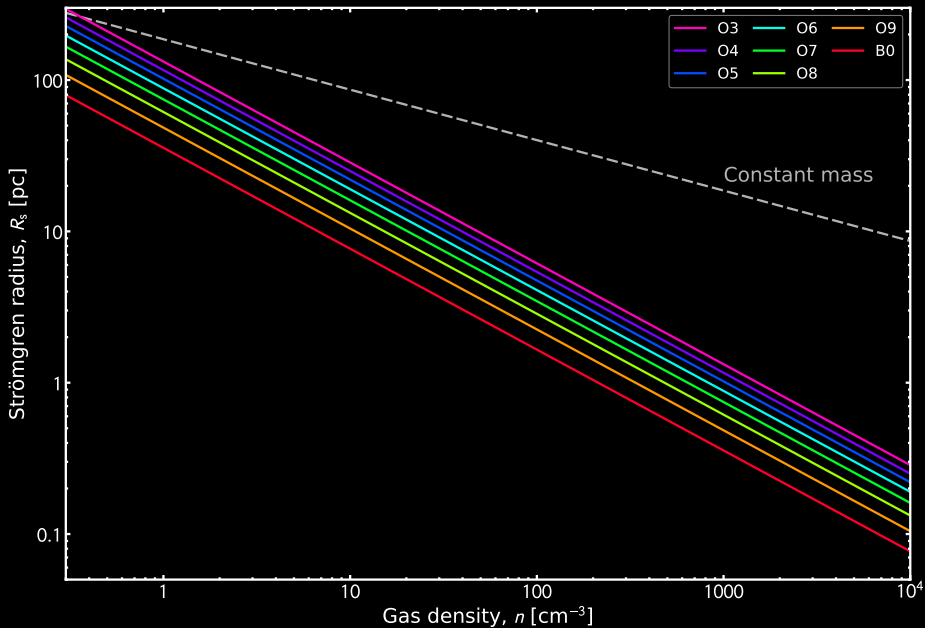
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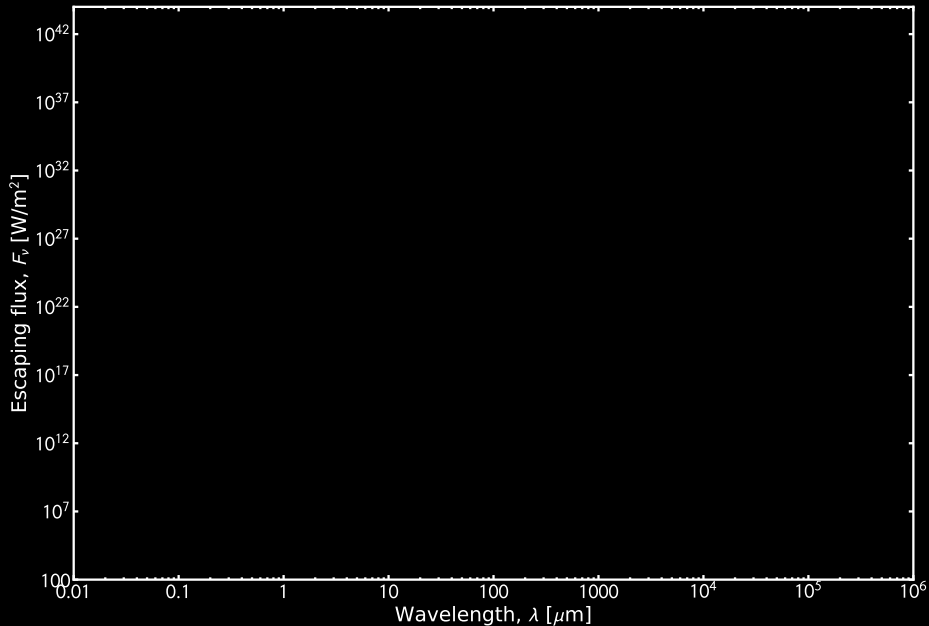


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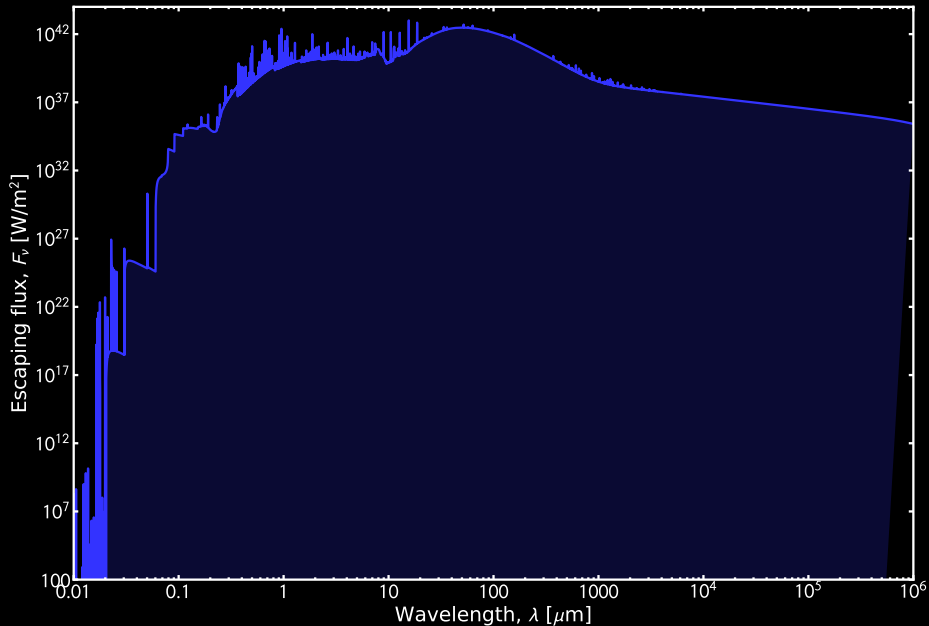
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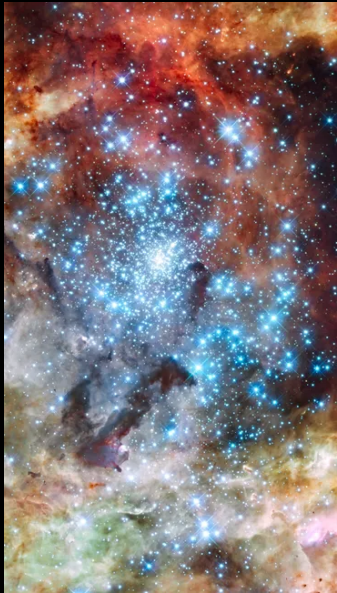


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Using Dust Emission



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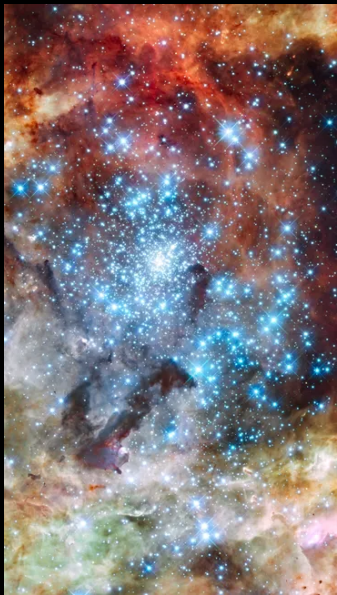
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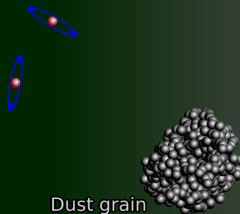
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## LANGMUIR-HINSHELWOOD



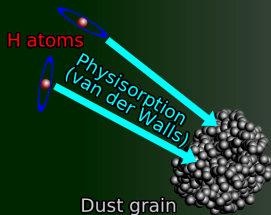
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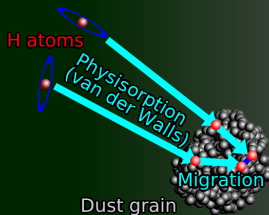


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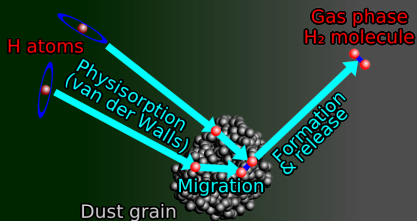


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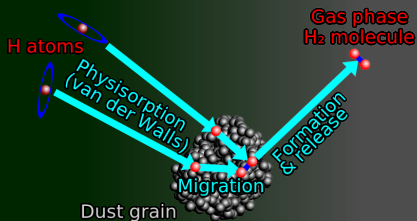


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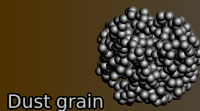
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### LANGMUIR-HINSHELWOOD



### ELEY-RIDEAL

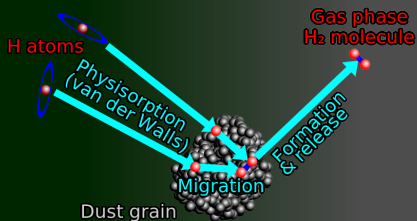


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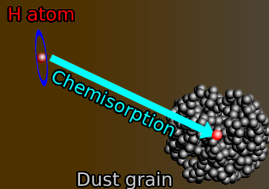
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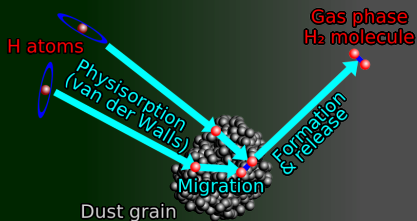


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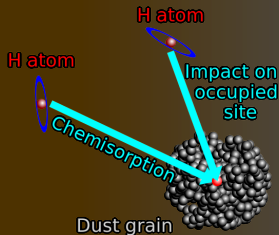
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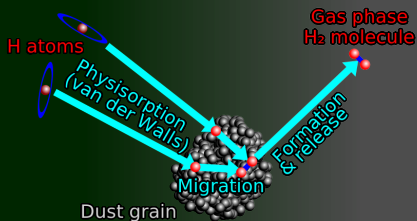


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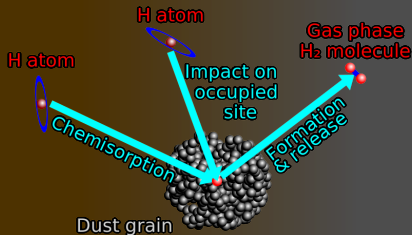
## The relevance of PDRs

- PDRs: continuation of H II regions where all ionizing photons have been absorbed  $\Rightarrow$  H<sup>0</sup>.
- PDR  $\Leftrightarrow$  UV-illuminated edges of molecular clouds. Broader nomenclature: most neutral & molecular clouds bathed with UV photons are PDRs.
- They harbor a rich variety of chemical reactions  $\rightarrow$  H<sub>2</sub>.

### LANGMUIR-HINSHELWOOD



### ELEY-RIDEAL

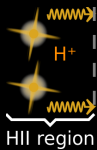


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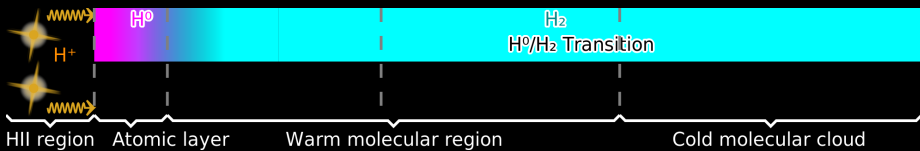
# SF regions | The $H^0/H_2$ Transition



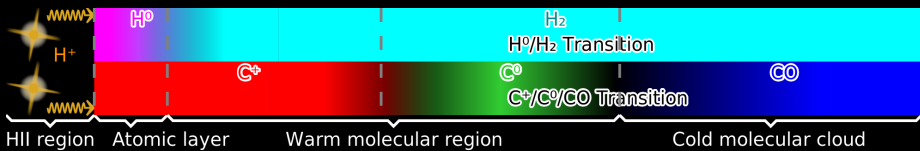
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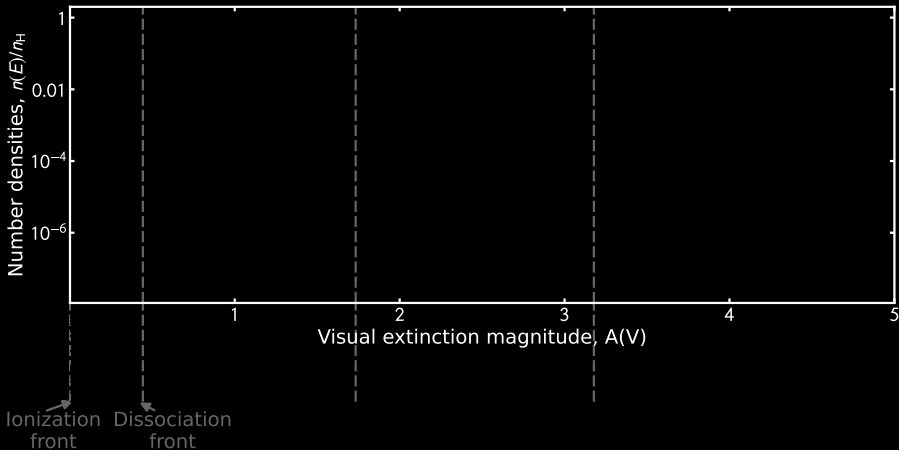
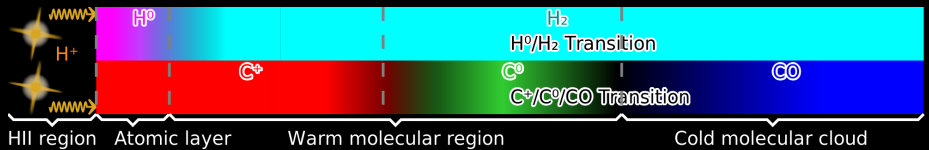
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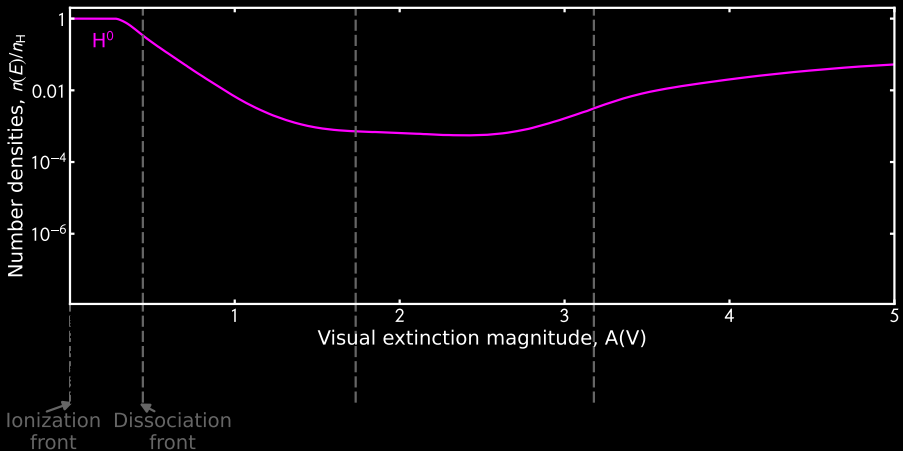
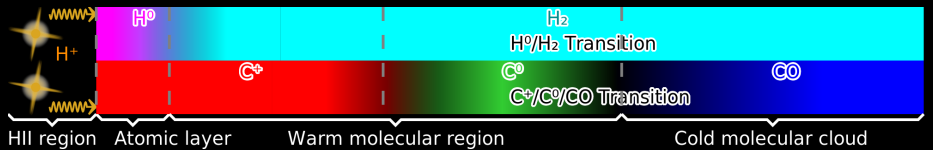
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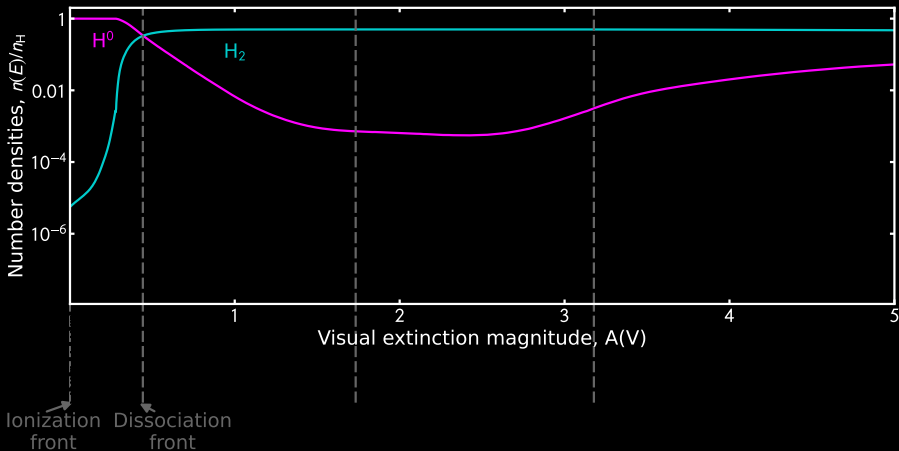
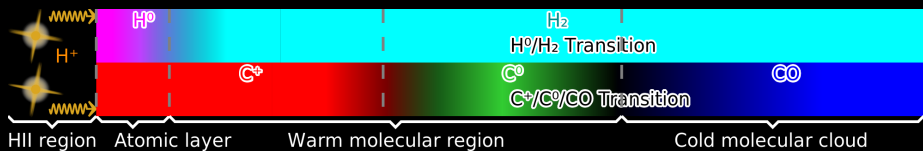
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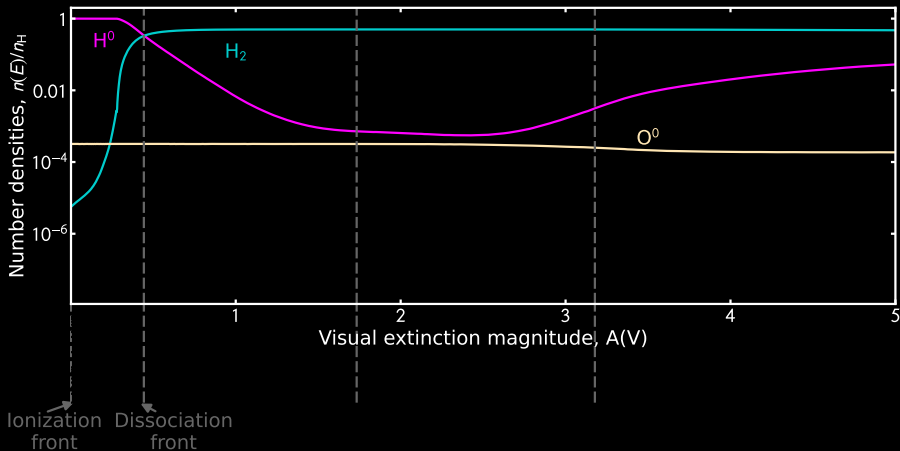
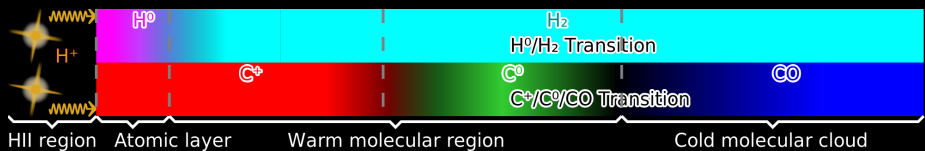
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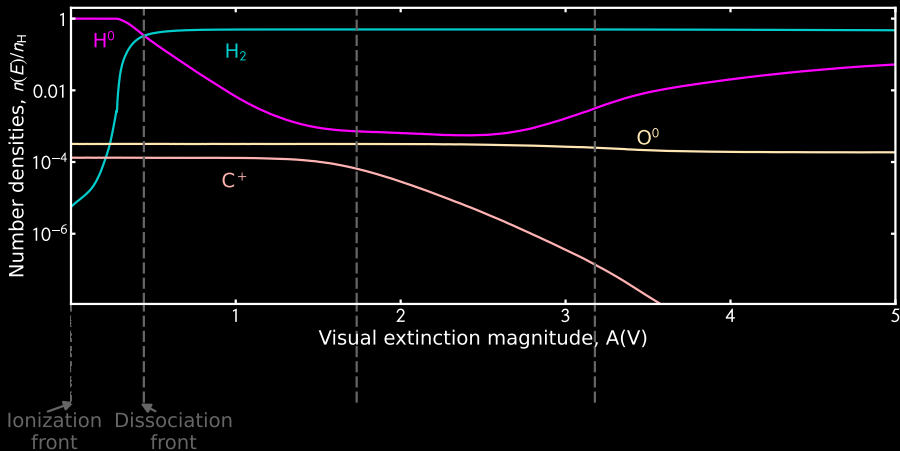
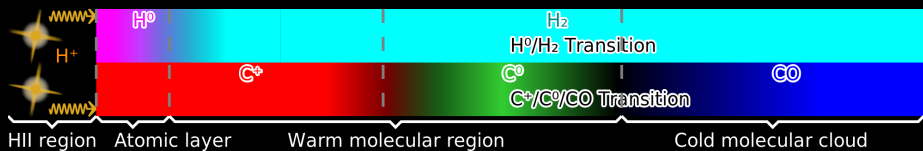
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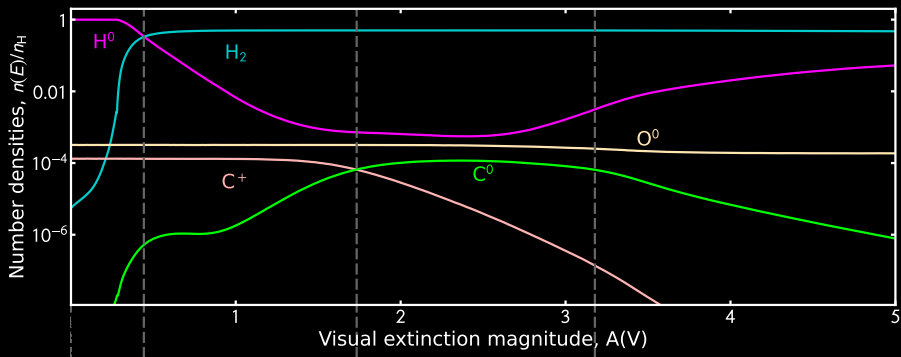
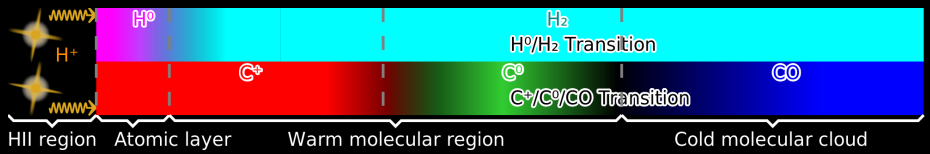


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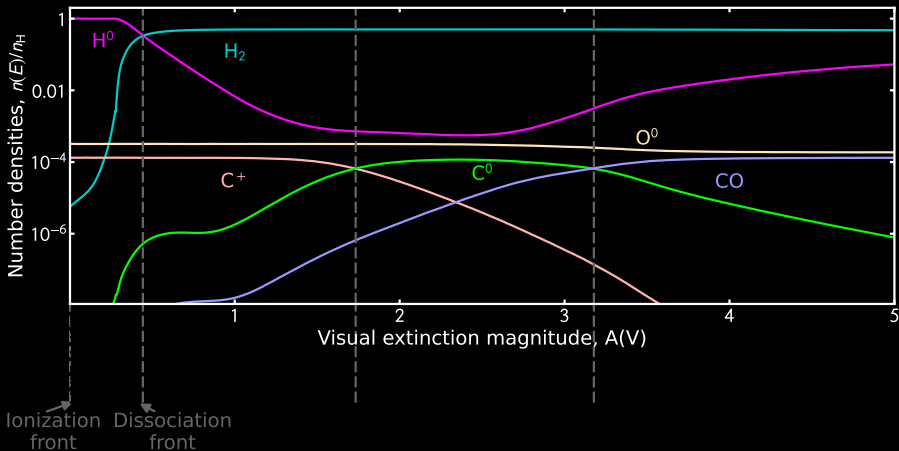
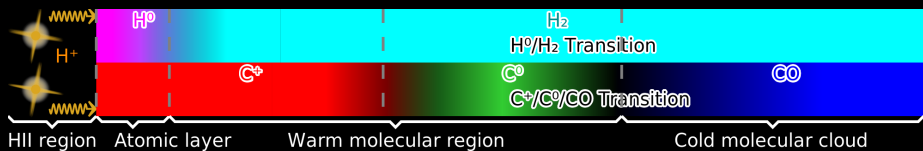


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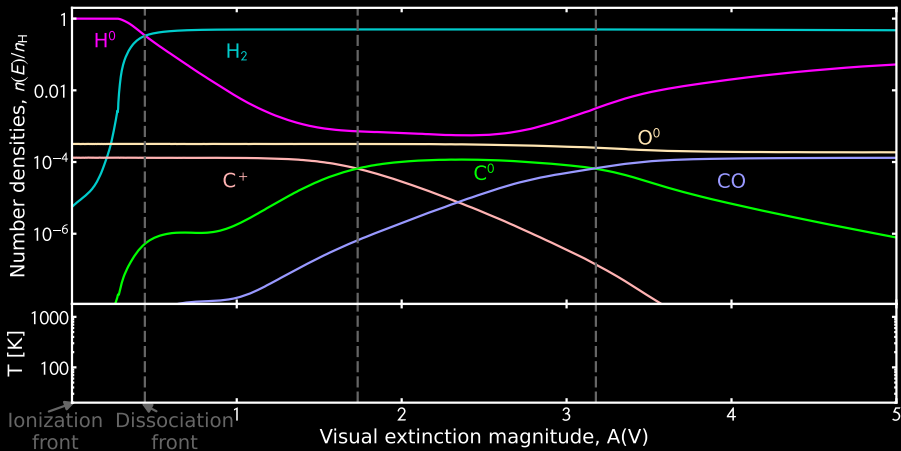
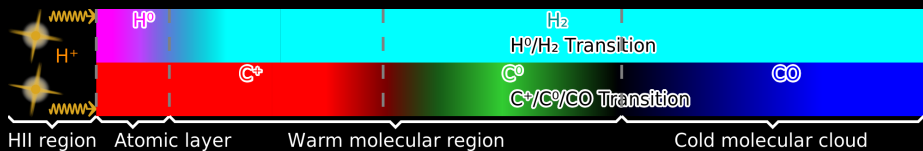


Ionization front    Dissociation front

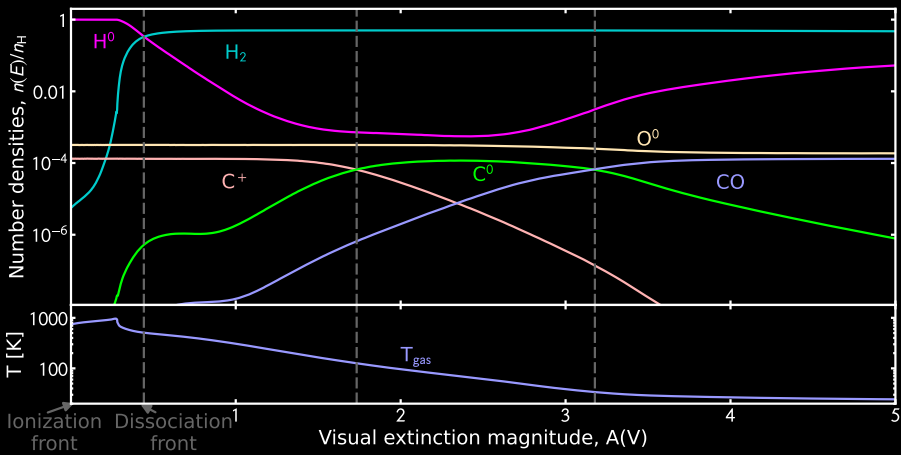
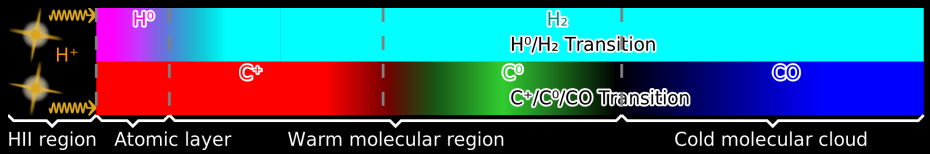
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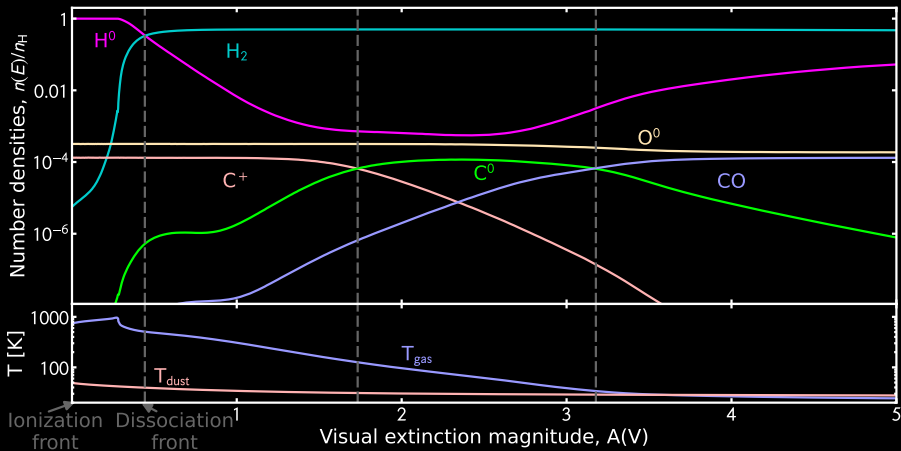
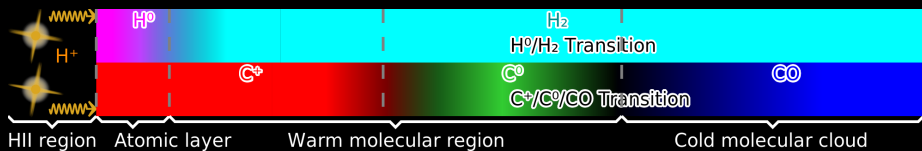
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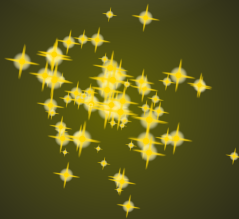
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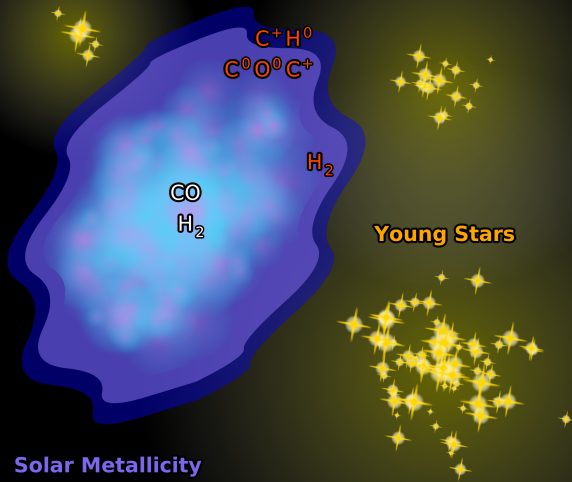


## Young Stars



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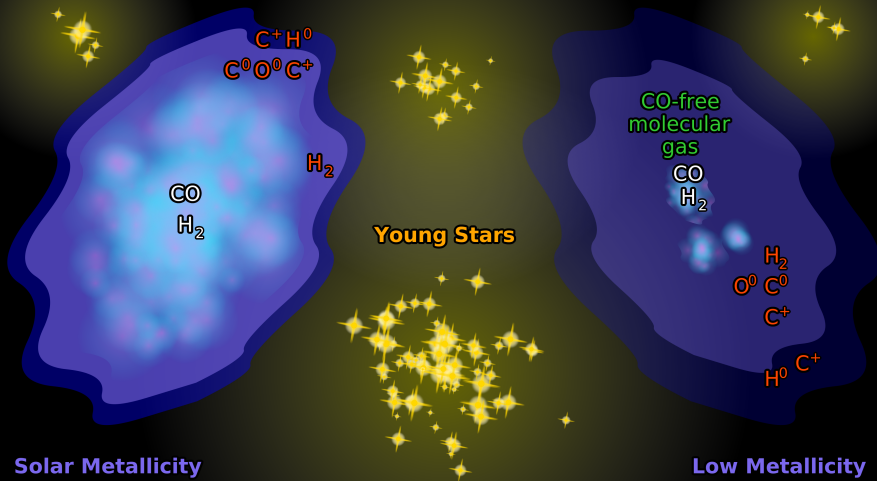


Solar Metallicity

# SF regions | The CO-Dark Gas

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# Outline of the Lecture

## 1 COOLING & HEATING OF THE GAS

- The gas heating processes
- The gas cooling function
- The five thermal phases of the ISM

## 2 THE PRINCIPLES OF RADIATIVE TRANSFER

- The radiative transfer equation
- Solutions in simple cases
- Dust radiative transfer with more complex geometries

## 3 STAR-FORMING REGIONS

- The Structure of Star-Forming Regions
- H II regions
- PhotoDissociation Regions (PDRs)

## 4 CONCLUSION

- Take-away points
- References

# Conclusion | Take-Away Points

Balance between gas heating & cooling – the phases of the ISM



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