Time-varying data-driven modeling of solar active region and time-dependent solar wind background by SIP-CESE MHD Model

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In this talk, a time-dependent MHD modeling driven by the time-dependent observed magnetograms is introduced to study the dynamic evolution of both active region and solar wind background with the help of the 3D Solar-Interplanetary (SIP) adaptive mesh refinement (AMR) space-time conservation element and solution element (CESE) MHD model (SIP-AMR-CESE MHD Model).

A) The simulated evolution of the global solar wind ambient from 2008-07-01 to 2008-08-11 is compared with solar observations and solar wind measurements from both Ulysses and spacecraft near the Earth.

B) Using observed vector magnetogram (& a nonlinear force-free field extrapolation) prior to a sigmoid eruption in AR 11283 as the initial condition, we successfully simulate the realistic initiation process of the eruption event, as is confirmed by a remarkable resemblance to the SDO/AIA observations.

I. Solar-InterPlanetary AMR CESE Model (SIP-CESE MHD Model)

Feng et al., ApJ, 2007, JGR, 2009; Hu et al., 2008, JGR; Feng et al., APJ, 2010, 2011; Sol. Phys. 2012; Zhou and Feng, JGR, 2012,etc

Grid in the solar corona

►Numerical method: Space-Time conservation

$$\frac{\partial u_m}{\partial t} + \frac{\partial f_m}{\partial x} + \frac{\partial g_m}{\partial y} + \frac{\partial h_m}{\partial z} = \eta_m$$

By Gauss's divergence theorem on space-time conservation cell Vxyzt

$$\oint_{S(V)} \vec{q}_m \cdot d\vec{S} = \int_V \eta_m dV$$



S(V) is the boundary of a space time region Vxyzt

which leads to the implicit solver of nonlinear Newtonian equations.

Projection of spacetime cell onto space domain

CESE is different from routine FVM method in that

According to Reynolds transport theorem

$$\frac{\partial}{\partial t} \int_{V_{ijk}} u_m dv + \oint_{S(V_{ijk})} (f_m n_x + g_m n_y + h_m n_z) ds = \int_{V_{ijk}} \eta_m dv$$
$$\int_{V_{ijk}} u_m dv \left|_{t_1}^{t_2} = \int_{t_1}^{t_2} \left(-\oint_{S(V_{ijk})} (f_m n_x + g_m n_y + h_m n_z) ds + \int_{V_{ijk}} \eta_m dv \right)$$

The rate of change of the total amount of a substance contained in a fixed spatial control volume Vijk is equal to the combination of the two factors: (i) the flux of that substance across the boundary S(Vijk) of the control volume Vijk, and (ii) the integration of the source term over the fixed spatial domain.

$$\frac{d\mathbf{U}_{i,j,k}}{dt} = -\frac{1}{V_{i,j,k}} \sum_{m=1}^{N_f} \left(\vec{\mathbf{F}} \cdot \vec{n} \,\Delta A \right)_{i,j,k,m} + \bar{\mathbf{S}}_{i,j,k} + \bar{\mathbf{Q}}_{i,j,k} = \mathbf{R}_{i,j,k}(\mathbf{U}) \,,$$

The conventional finite volume methods concentrate on the evaluation of the right side. Time integration is usually obtained with Runge-Kutta.

OURS is the space-time 4D volume integration

$$\oint\limits_{S(V)}ec{q}_m\cdot dec{S}=\int\limits_V\eta_m dV$$

DII: Grid System from the Sun to Earth space (Feng et al., APJ, 2010; 2011, Solar Physics, 2012)



Feng et al., ApJ, 2007, JGR, 2009; Hu et al., 2008, JGR; Feng et al., APJ, 2010, 2011; Sol. Phys. 2012; Zhou and Feng, JGR, 2012

DII: AMR Polyhedron Grid—two methods with PARAMESH

Modified by some flux conservation.

I) Coordinate transform (Feng et al., Solar Physics, 2012)



Refinement criterion of the curl of magnetic field

II) Direct AMR by the following orientation







Berger–Oliger algorithm can be applied directly

DIV: Other merits includes

 C_a

Div(B) Error Cleaning Method by Fast AMR multigrid Poisson solver (Ricker, ApJS 176:293, 2008)

Positivity consideration

A negative pressure or thermal energy $e = p/(\gamma - 1)$ in the low- β or high speed regions (i.e., $e \ll E$) usually occurs. In such unsafe regions, instead of total energy equation we entropy equation $\frac{\partial e}{\partial t} + \nabla \cdot (eV) = -p\nabla \cdot V + Q_e$ for plasma β or e/E being very small.

If negative values still occur, we identify all cells (within the same grid block) that represent physical states surrounding a faulty cell in a rectangular zone up to n_{pos} cells away; and (2) for all but the magnetic field components, replace the faulty cell values by the average of surrounding physical state cells.

Heating/acceleration by empirically specifying the energy and momentum source heating term with the magnetic field expansion factor fS and the minimum angular separation θb (at the photosphere) between an open field foot point and its nearest coronal hole boundary.

$$Q_{\varepsilon} = Q_{1}C_{a}\exp(-\frac{r}{L_{Q_{1}}}) + Q_{2}C_{a}(\frac{r}{Rs} - 1)\exp(-\frac{r}{L_{Q_{2}}}) + \nabla(\xi T^{5/2}\frac{\nabla T \cdot B}{B^{2}}) \cdot B$$

$$S_{m} = M_{0}C_{a}(\frac{r}{Rs} - 1)\exp(-\frac{r}{L_{M}}) \quad \text{Wang-Sheeley model}$$

$$= Ca'/\text{Max}(Ca') \text{ with } Ca' = \frac{1}{(1+f_{s})^{2/7}}(5.8 - 1.6\exp[1 - (\frac{\theta_{b}}{8.5})^{3}])^{3.5}$$

DV: Time-dependent projected characteristic boundary condition is used at the subsonic region by limiting the mass flux escaping through the solar surface with Ulysses observations (e.g., Wu et al., ApJ, 2001; 2006; Hayashi APJ, 2005),



The projected characteristics method (Wang Hu, Wu, 1982; Wu et al. 2001, Hayashi, ApJS, 2005, Feng et al., ApJ, 2010; 2011; Solar Physics, 2011) is used to couple the surface flux transport (SFT) or time-dependent interpolation change or vector magnetogram with MHD models.

The compatibility equation must be used when updating the boundary variables if the corresponding eigenvalue is negative ($\lambda m < 0$, *i.e.*, the outgoing wave). While for the incoming waves ($\lambda m > 0$), since no observation is available to describe them, we just fix them.

II. Data-driven Solar Wind Model: From 1Rs to 1AU

Background & Motivation:

Global estimates of the solar photospheric magnetic field distribution are critical for space weather forecasting. These global maps are the essential data input for accurate modeling of the corona and solar wind, which is vital for gaining the basic understanding necessary to improve forecasting models needed for really realistic operations. We are now testing the global photospheric field maps generated by the solar surface flux **Transport (SFT) model for** long-interval synoptic data products or Time Interpolation for short-interval synoptic data products as input to the CESE-MHD coronal and solar wind model.

Result: Improved, high quality "snapshots" of the Sun's global magnetic field as the input to drive our 3D numerical global coronal AMR-CESE-MHD model

Here, we obtain snapshot of magnetic maps as input to drive our MHD model by the following two methods: Surface flux transport & Time-interpolation.

SFT Model



- Applied to long-interval synoptic data products WSO, MDI(1 Carrington rotation cycle, 27 days)
- Differential rotation $\Omega(\theta)$ & meridian flow $\nu(\theta)$

(1) **Differential rotation**

(2) Meridional flow

$\Omega(\theta) = 0.18 - 2.3\cos^2\theta - 1.62\cos^4\theta \,\deg\,\mathrm{day}^{-1} \quad v_\theta(\theta) = C\cos\left[\frac{\pi(\theta_{\mathrm{max}} + \theta_{\mathrm{min}} - 2\theta)}{2(\theta_{\mathrm{max}} - \theta_{\mathrm{min}})}\right]\cos\theta$

(3) Supergranular diffusion







The surface flux transport (SFT) model describes the radial component evolution of large-scale photospheric magnetic field with time by using the magnetic induction equation in spherical coordinates. The flux transport model (Yeates, ApJ, 2010) accounts for known flows in the solar photosphere by including diff rotation & meridian flow.



Applied to short-interval synoptic data products
 GONG(6-hour), SDO-HMI(1-day)

Using three synoptic maps to achieve third-order interpolation

$$B_{r}(t) = \frac{(t-t_{2})(t-t_{3})}{(t_{1}-t_{2})(t_{1}-t_{3})}B_{r,1} + \frac{(t-t_{1})(t-t_{3})}{(t_{2}-t_{1})(t_{2}-t_{3})}B_{r,2} + \frac{(t-t_{1})(t-t_{2})}{(t_{3}-t_{1})(t_{3}-t_{2})}B_{r,3}$$



This data processing method is aimed to provide snapshot of magnetic maps

Roadmap









Obtain background solar wind • Fixed synoptic map(t=0) Fixed boundary condition Evolves(relaxes) until it reaches a steady state Based this steady-state, our data-driven procedure starts! Data-driven Solar Wind Initialized with background solar wind obtained above • Evolving synoptic maps (SFT or time interpolation) for specific period (such as 2008-07-01 to 2008-08-11 below) Projected characteristic boundary conditions at 1Rs

(Feng et al, ASTRONUM 2011; Feng et al, APJ, 2012; Yang et al., JGR, 2012)



GONG 6-hour synoptic maps
Third-order time interpolation
From 2008-07-01 to 2008-08-11
Can be continued with more synoptic map input



Iso-surface of Br=0





Corona Magnetic Field



3D Magnetic field on July 01, 08, 16, 23 and August 01, 08, 2008





Contours at 2.5Rs



Number density

radial speed



Temperature



Br

Contours at 0.1AU



Number density

radial speed



Temperature



Br

Contours at 1AU



Number density

radial speed



Temperature



Br

Compared with OMNI Data at 1AU



Radial speed

Number density



Temperature

В



Equatorial plane



Radial speed

Mass flux $\rho V_r r^2$







Meridian plane(YZ plane)



Radial speed



Mass flux $\rho V_r r^2$





Meridian Plane (XZ plane)



Radial speed



Mass flux $\rho V_r r^2$





Corona Brightness



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Summary

- With observed magnetic field data as input, this model can be able to simulate long-term evolution of solar wind (several Carrington rotations or even longer).
- This model is able to give solar wind parameters from corona to 1AU, which shows obvious time-dependent structures of the solar wind.
- Higher resolution magnetic data will achieve more agreement with observation

III. Data-Driven Numerical Modeling for Active Region Evolutions and Eruptions



- Understanding how the solar coronal magnetic fields evolve and why the coronal fields erupt to produce flares and coronal mass ejections (CMEs), is a fundamental question of solar physics and it is crucial in forecasting space weather.
- We have developed a suite of numerical models for the magnetic evolution of the corona, including a unified and extremely fast code GLFFF for computing the global potential and linear force-free fields, a general nonlinear force-free extrapolation code CESE-MHD-NLFFF for both the local active regions and global corona, and a data-driven CESE-MHD model for simulating the magnetic evolution prior to and during eruptions.
- Based on these models & the booming data provided by SDO, a realistic 3D magnetic evolution for an eruption event from all over its formation to disruption can be achieved.

These lead to understanding how the eruptive core field is built up, the favorable magnetic topology is formed, and how the eruptions are triggered and driven.







Data-Driven Numerical Models for the Evolution and Eruption of Solar Coronal Magnetic Field



Note:

GLFFF: A very fast way for computing the global potential and linear force-free (LFFF) fields. Jiang & Feng (2012), Solar Physics
 CESE-MHD-NLFFF: A new implementation of the MHD-relaxation method for nonlinear force-free field (NLFFF) extrapolation Jiang & Feng, ApJ, 2012a, 2012b, 2013; Solar physics, 2013
 CESE-MHD: A data-driven MHD model for AR's magnetic evolution Jiang & Feng et al 2012, ApJ, 2013, ApJL.



As an example, using a nonlinear force-free field extrapolation prior to a sigmoid eruption in AR 11283 as the initial condition in a MHD model, we successfully simulate the realistic initiation process of the eruption event, as is confirmed by a remarkable resemblance to the SDO/AIA observations.

Analysis of the pre-eruption field reveals that the envelope flux of the sigmoidal core contains a coronal null and furthermore the flux rope is prone to a torus instability, as suggested by observations. This kind of simulation demonstrates the capability of modeling the realistic solar eruptions to provide the initiation process.



CESE-MHD-NLFFF extrapolation (Jiang & Feng, ApJ, 2013, 769, 144)



Main Equation (modified magneto-frictional model in the magnetic splitting form)

$$\begin{aligned} \frac{\partial \rho \mathbf{v}}{\partial t} &= (\nabla \times \mathbf{B}_1) \times \mathbf{B} - (\nabla \cdot \mathbf{B}_1) \mathbf{B} - \nu \rho \mathbf{v}, \\ \frac{\partial \mathbf{B}_1}{\partial t} &= \nabla \times (\mathbf{v} \times \mathbf{B}) + \nabla (\mu \nabla \cdot \mathbf{B}_1) - \mathbf{v} \nabla \cdot \mathbf{B}_1, \\ \rho &= |\mathbf{B}|^2 + \rho_0, \ \mathbf{B} = \mathbf{B}_0 + \mathbf{B}_1. \end{aligned}$$

Extrapolation test of the van Ballegooijen (2004) flux rope model (Jiang & Feng, ApJ 2012a)





Highest resolution match the magnetogram (e.g., 0.5 arcsec for HMI data); coarsest resolution ~4 arcsec

Model	C	C_{CS}	E'	E'	$E/E_{\rm net}$	CWsin	$\langle f_i \rangle$
	~ vec	- 05	n	2 m	2 / 2 pot		(J1)
For $z \in [2, 225]$							
Reference	1.000	1.000	1.000	1.000	1.343	0.107	1.02×10^{-1}
Our result	0.995	0.978	0.885	0.734	1.337	0.133	1.11×10^{-1}
$Wiegelmann^*$	1.00	0.99	0.89	0.73	1.34	0.11	
Wheatland [*]	0.95	0.98	0.79	0.70	1.21	0.15	
Valori*	0.98	0.98	0.84	0.71	1.25	0.15	
Potential	0.852	0.952	0.687	0.665	1.000		



AIA observation of the emergence and eruption



AR 11283 (2011/09/04-06)

 From 2011/09/04:
 New flux emergence into a bipolar active region

AIA 171, 335, 304

AIA 094





 2011/09/06:
 Sigmoid eruption at 22:17UT,
 Developed to a CME,
 associated with
 a X2.1 flare



- Photospheric flux emergence
 - Before 2011-09-04: Simple mature, bipolar (P0/N0) AR.
 - After 2011-09-04: New bipolar (P1/N1) emergence



Evolution of the photoshperic field observed

Field of view: 300*256 arcsec^2 (res=0.5arcsec)

250



- Photospheric signal of energy building up process
 - Apparent new flux injection occurred mostly on the first day (09/04).
 - Non-potentiality increased mostly on the second day (09/05), resulted by photospheric shear and rotation.

Total unsigned flux $\Phi = \int_{S} |Bz| ds$; Unsigned current $I = \int_{S} |Jz| ds$; (LSS=length of strong magnetic shear (>45°) with strong transverse field (> 300 G)]









BPSS model of sigmoid (TD1999,

Gibson2006).

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Magnetic topology of the Sigmoid







Formation of the basic topology and the sigmoidal flux rope

09.04 12:00







Cross section of the 3D NLFFF data.

An X point (coronal null in 3D) forms above the new polarity P1 and lift up

A flux rope forms above the polarity inversion line (PIL) of P1/N0

Photospheric shear change potential arcade to double-J shaped loop system;

➢ S-shaped flux rope formed from the double-J loops by tether-cutting reconnection (Moore et al. 2001).

≻Flux rope disappeared after eruption

Eruption mechanism





The flux rope—overlying flux system is prone to the Torus instability (TI, Kliem & Torok, 2006)



➢ Magnetic reconnection at the null cuts some overlying tethers (evidence: circular flare ribbon and overlying closed loops opened)→
 Flux rope expand slightly→
 TI is triggered →Fast eruption



Decay speed of envelope flux defined decay index $decay index = -\frac{r}{B} \frac{\partial B}{\partial r}$

horizontal line at 1.5, a critical threshold for torus instability (Torok & Kliem 2007; Aulanier et al. 2009). Note that the flux rope reaches almost 20 arcsec (left Figure 11), a height with decay index > 1.5.

A vertical cross section cutting through the coronal null and the middle of the sigmoid, thus roughly parallel to the direction of eruption as observed. The thick solid and dashed lines with arrows denotes two directions (started from near the PIL on the bottom) in which the decay indexes of the field strength are plotted in right Figure. The solid one is radial and the dashed roughly the eruption direction modeled by the MHD simulation.

Data-Driven CESE-MHD Model









Figure 2. Typical configurations of the magnetic field strength *B*, the Alfvén speed V_A , and the plasma β along a vertical line through the computation volume.





MHD simulation of the eruption process

- Full 3D time-dependent MHD model with solar gravity
- Initiated by the NLFFF solutions; residual Lorentz force as perturbation of the unstable system.
- No explicit resistivity included, reconnection allowed by numerical diffusion of thin current sheet.
- Sufficient kinematic viscosity for numerical stability (may reduce the eruption speed)
- Modeling box: a sub-volume from the NLFFF box; size of
 224×256×256 arcsec³ with the eruption region at the center of the box.
- Adaptive grid: highest resolution ~0.5 arcsec in the sunspot region and coarsest resolution ~4arcsec near the side BCs.
- Fixed BCs on the bottom & non-reflecting BCs for numerical boundaries.



Formation and Eruption of a Sigmoid in AR 11283 (ApJL, 2013, 771:L30) SDO(AIA-171 2011-09-06T22:00:01.34Z

MHD simulation

Perfect resemblance of the simulation with AIA observations!

➢ Simulation confirms the eruption mechanism: overlying closed flux (the white lines) reconnected and opened, followed by the rapid rising of the sigmoidal flux rope

Slipping movement of the flux rope footpoint can be both seen in the observation and simulation (slip-running reconnection, Aulanier et al. 2006).

The south leg becomes faint because the field twist is weaker and the plasma can easily flow back down by gravity





Related Papers



- [1] Jiang, C. W., Wu, S. T., Feng, X. S., and Hu, Q. (2013), Formation and Eruption of a AR Sigmoid: NLFFF Modeling and Data-Driven MHD Simulation, ApJ, to be Submitted.
- [2] Jiang, C. W., Feng, X. S., Wu, S. T., and Hu, Q. (2013), MHD Simulation of a Sigmoid Eruption of Active Region 11283, ApJL, 771:L30.
- [3] Jiang, C. W. and Feng, X. S. (2013), Preprocess the Photospheric Vector Magnetograms for NLFFF Extrapolation using a Potential Field Model and a Optimization Method, Solar Physics, In press.
- [4] Jiang, C. W. and Feng, X. S. (2013), Extrapolation of the Solar Coronal Magnetic Field from SDO/HMI Magnetogram By A CESE–MHD–NLFFF Code, ApJ, 769, 144.
- [5] Jiang, C. W., Feng, X. S., S. T. Wu, and Hu, Q. (2012), Study of the Three-dimensional Coronal Magnetic Field of Active Region 11117 around the Time of a Confined Flare Using a Data-Driven CESE-MHD Model, ApJ, 759, 85.
- [6] Jiang, C. W. and Feng, X. S. (2012), A New Implementation Of The Magnetohydrodynamics-Relaxation Method For Nonlinear Force-Free Field Extrapolation In The Solar Corona, ApJ, 749, 135.
- [7] Jiang, C. W., Feng, X. S., and Xiang, C. Q. (2012) A New Code For Nonlinear Force-Free Field Extrapolation Of The Global Corona, ApJ, 755, 62.
- [8] Jiang, C. W. and Feng, X. S. (2012), A Unified and Very Fast Way for Computing the Global Potential and Linear Force-Free Fields, Solar Physics, 281(2), 621.



IV: Future Avenue



• Further improve and perfect our continuously data-driven time-dependent solar wind background and active region modeling suite

• Use the time-dependent numerical results for active regions as initiation to drive the CME from the Sun to Earth

Speed up the model's calculation and data visualization study

Thanks & Merci

