

Lecture #4

Stability and Protection

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Outline

- Stability
 - Cryostable vs. adiabatic windings
 - Current-sharing temperature; disturbances; energy margins
 - Acoustic emission (AE) technique
- Protection
 - Self-protecting magnet
 - Normal zone propagation (NZP) velocities
 - Active protection techniques
- Conclusions

Two Types of Stability: *Cryostable* & *Adiabatic*

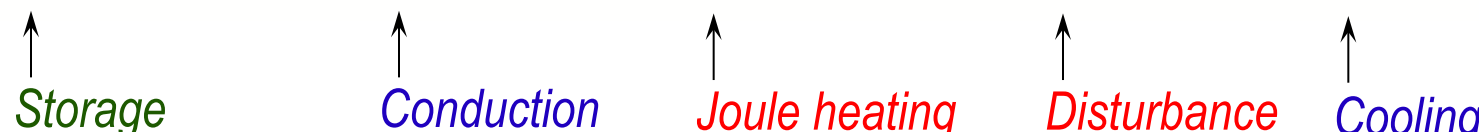
Cryostable

- Conductor over most of the winding **well-cooled** to enable **Cooling** to balance **Joule heating**

Adiabatic

- Conductor, except over the winding surface, **not exposed to cooling**

$$C_{cd}(T) \frac{\partial T}{\partial t} = \nabla \cdot [k_{cd}(T) \nabla T] + \rho_{cd}(T) J_{cd_o}^2(t) + g_d(t) - \left(\frac{f_p \mathcal{P}_D}{A_{cd}} \right) g_q(T)$$


Storage Conduction Joule heating Disturbance Cooling

Adiabatic (Also Known as High-Performance) Magnet

- Elimination of coolant within the winding:

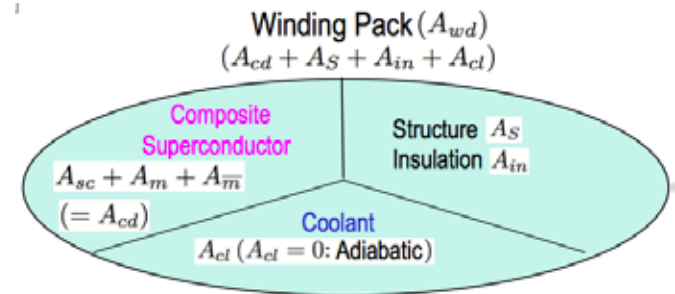
- Enhances the overall current density, λJ ;

$$\frac{I_{op}}{A_{wd}} = \frac{I_{op}}{A_{cd} + A_S + A_{in} + \cancel{A_{cl}}} \quad \uparrow$$

- Makes the winding pack structurally robust

- High-performance magnets: MRI; NMR; HEP

- Susceptible to quench, by a “minute” (but $> \Delta e_h$) disturbance energy



Why fusion magnets “cryostable,” i.e., $A_{cl} \neq 0$?

Huge mechanical reinforcement within the winding, $A_S \gg A_{cl}$:

A_{cl} little impact on λJ , i.e., a negligible sacrifice on magnet efficiency

Let's guarantee *stability* by making the winding *cryostable*, i.e., $A_{cl} \neq 0$

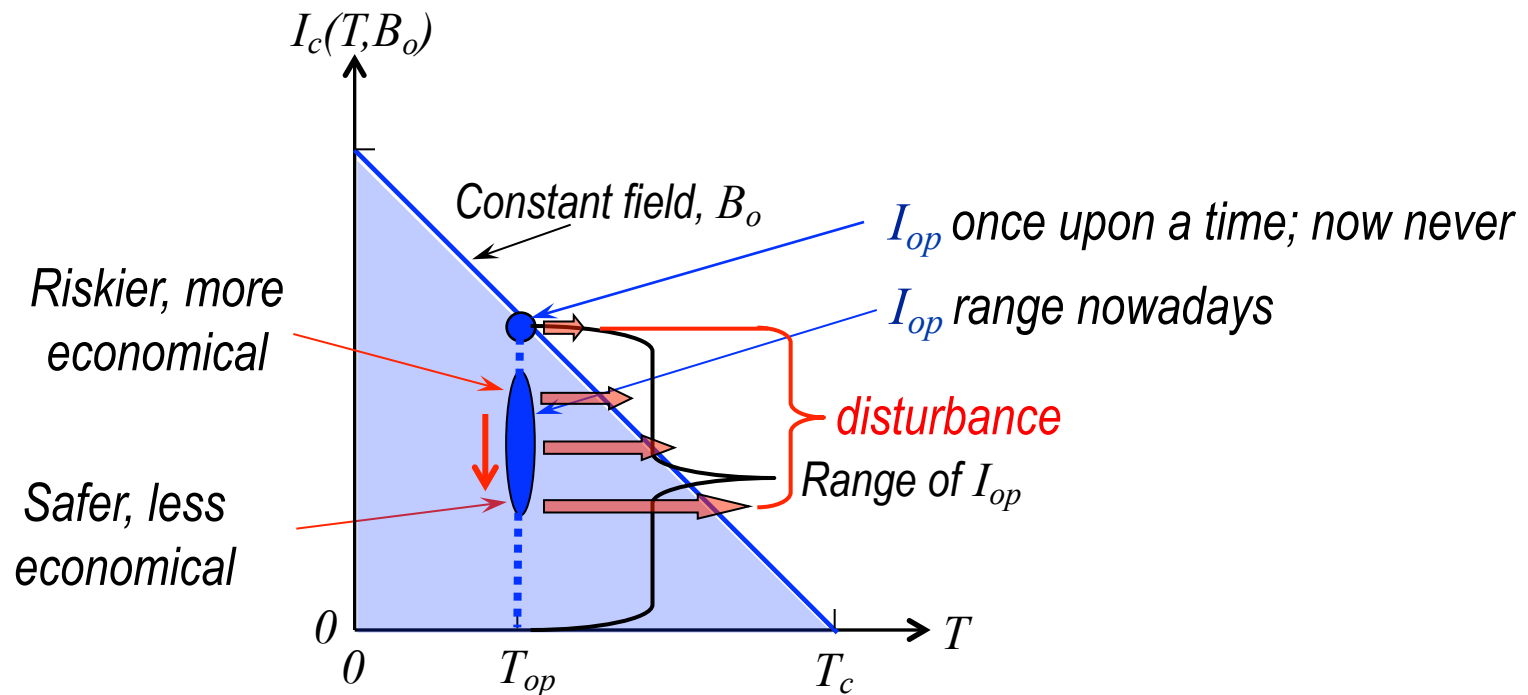
For “small” magnets like MRI, NMR, HEP,

$A_{cl} = 0$ enhances λJ enough to permit “reduced” stability

Stability

Stability (Operation Reliability)

Stable operation of a superconducting magnet in the **superconducting state** despite the presence of **disturbances** that may drive a section of or the whole magnet into the **normal state**

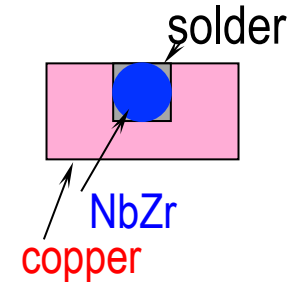


Composite Superconductor

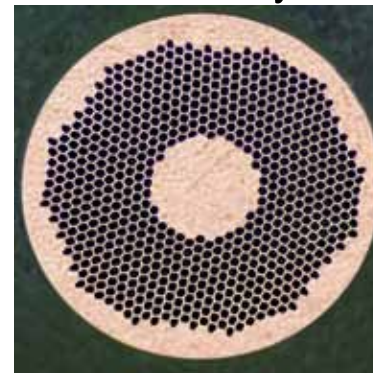
- First formulated and developed in 1964-1965 by Z. John Stekly:
because $\rho_{non-super} \gg \rho_{copper}$, **superconductor** shunted by electrically
conductive **normal metal** like copper

Material @4.2 K	Resistivity [$n\Omega$ m]
Copper	0.15
Stainless steel	540
NbTi (normal state)	600

Stekly (1964-1965)

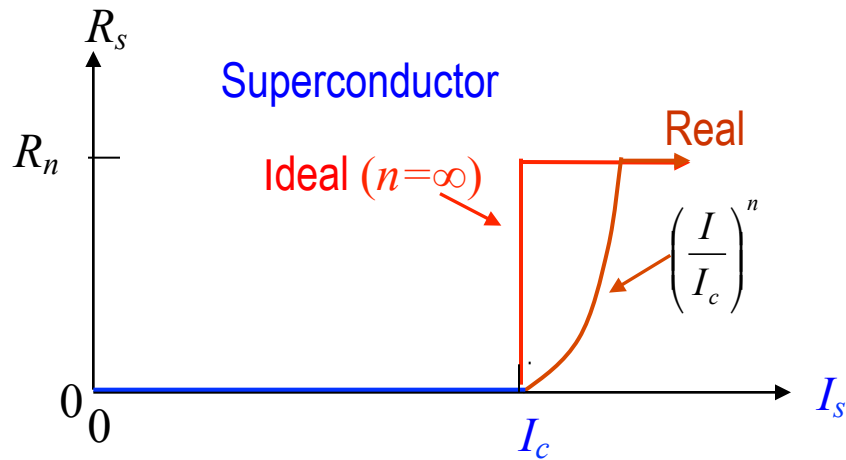


Multifilamentary **NbTi**



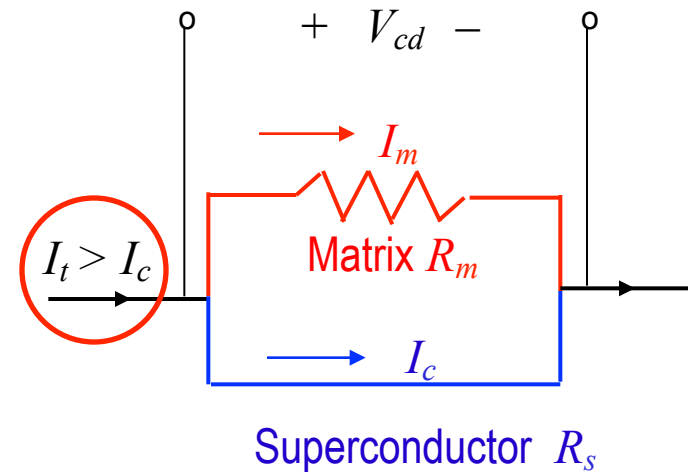
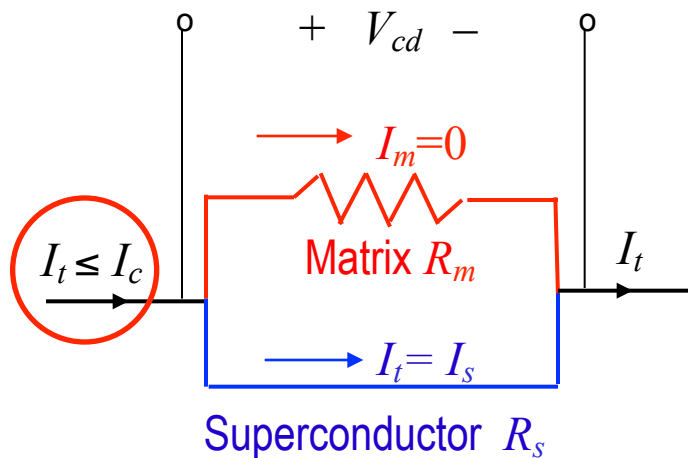
Diameter: 1.03 mm
 # Filaments: 642
 Filament dia.: 30 μ m
Cu/NbTi: 1.1

Circuit Models for Composite Superconductor

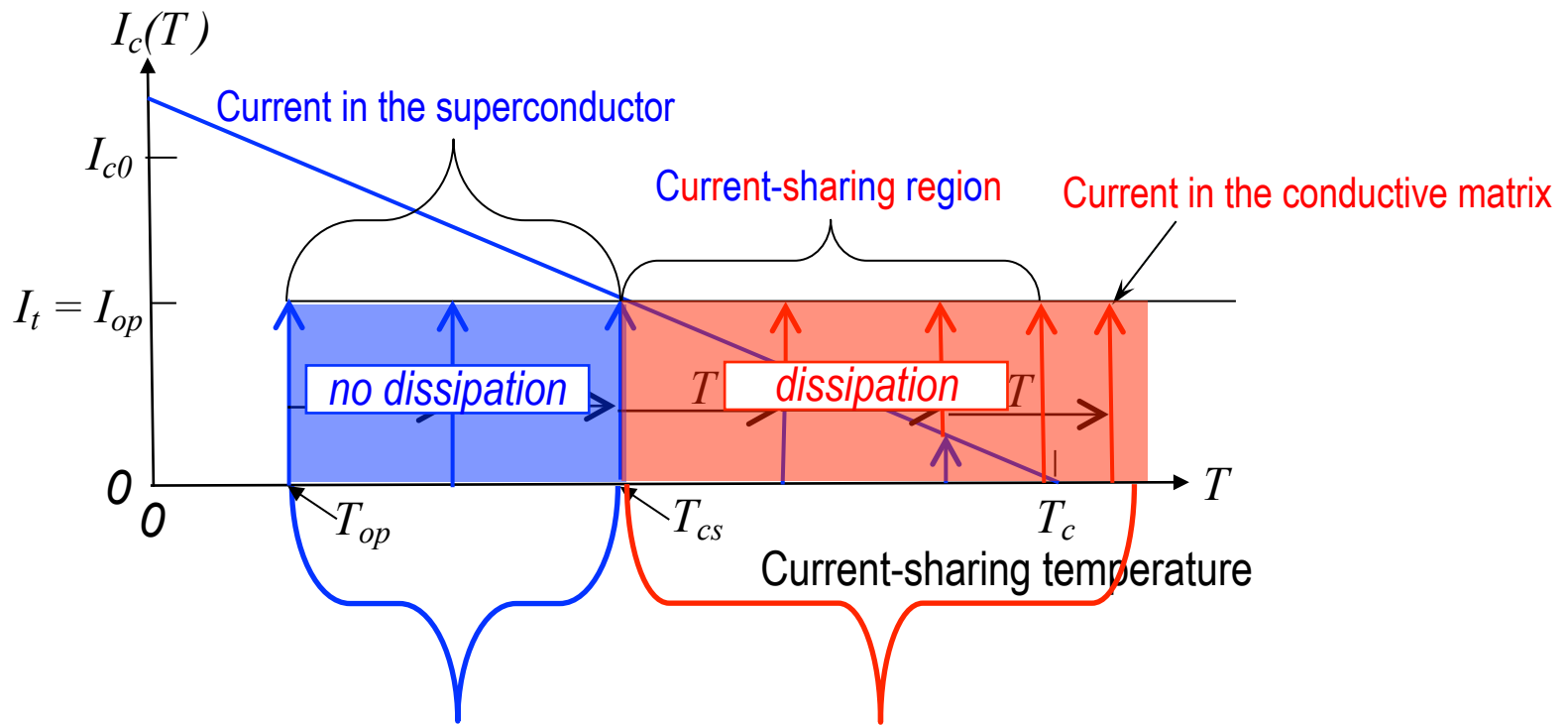


n : Index

- $n > 30$: LTS
- $n < 30$: HTS
- $n = \infty$: Ideal superconductor



Current Sharing in Composite Superconductor

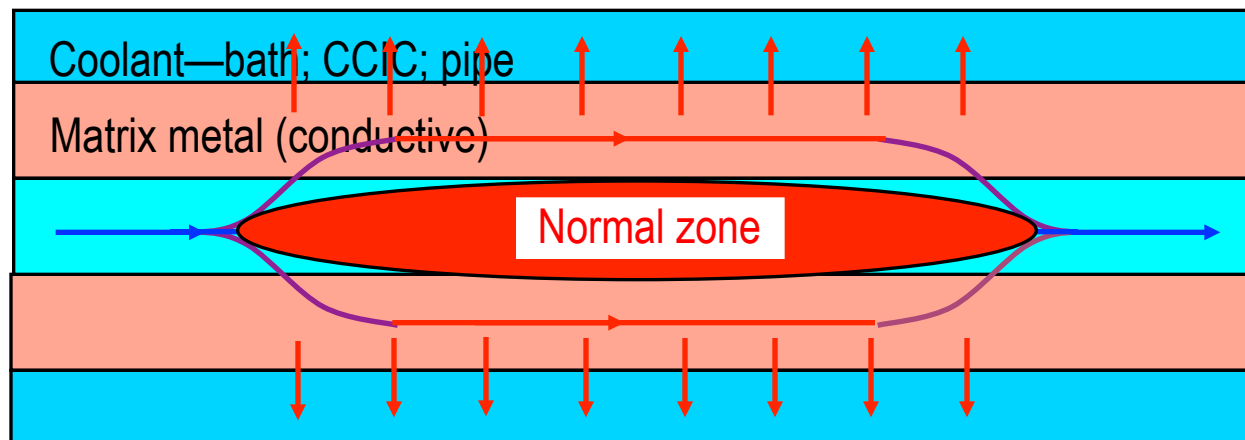
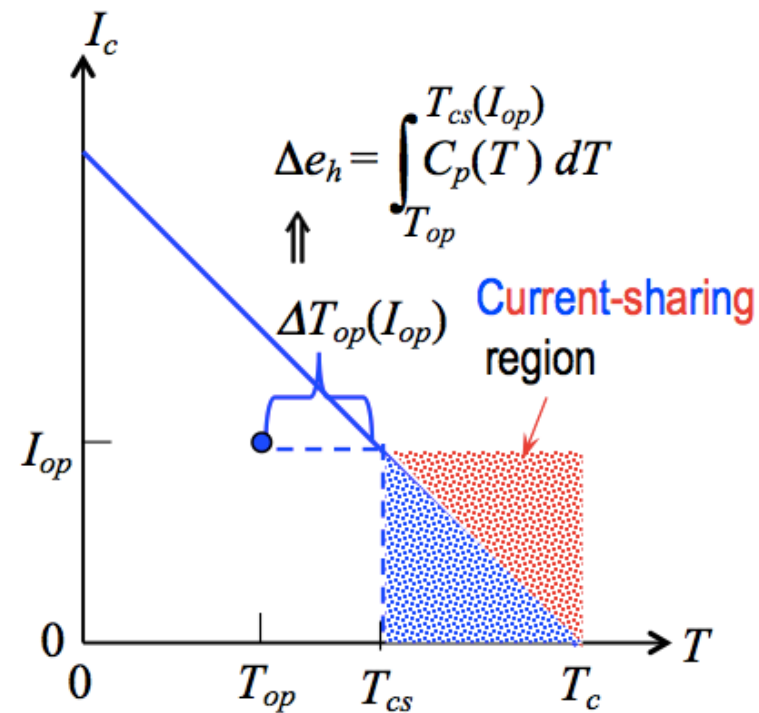


Permissible for any magnet,
even an “adiabatic” magnet

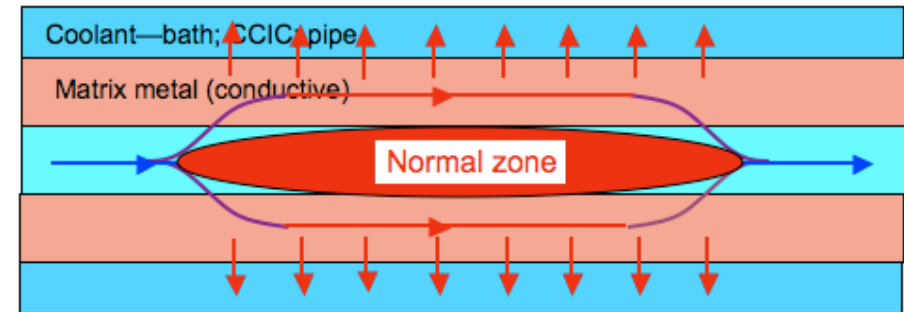
Permissible only for
“cryostable” magnets

Cryostable Magnet

- Disturbance energy density, $g_d(t)$, can exceed Δe_h



Key Issues for Cryostable Magnet



- **Dissipation (Joule heating) density:**
 - Matrix metal electrical resistivity, ρ_m : the lower the ρ_m the better
 - Matrix metal current density, $J_{mo} \Rightarrow A_m$: the greater the A_m the better
- **Cooling:**
 - Coolant, e.g., helium (ordinary; superfluid; supercritical)
 - Heat transfer data (natural or forced convection)
 - Conductor design, e.g., monolith; Rutherford; CICC

Cryostability

Stekly's cryostability

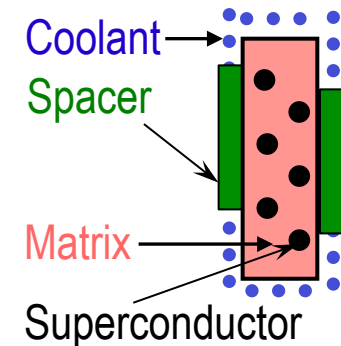
- Joule heating / unit length = cooling flux / unit length

$$\frac{\rho_m I_{m_o}^2}{A_m} = f_p \mathcal{P}_D q_{fm} = \rho_m A_m J_{m_o}^2$$

- ρ_m : matrix resistivity; A_m : matrix cross section
- f_p : fraction of \mathcal{P}_D , conductor perimeter exposed to cooling

$$[J_{m_o}]_{sk} = \sqrt{\frac{f_p \mathcal{P}_D q_{fm}}{\rho_m A_m}}$$

Cryostable operation, $[J_{m_o}]_{sk} \ll J_c$



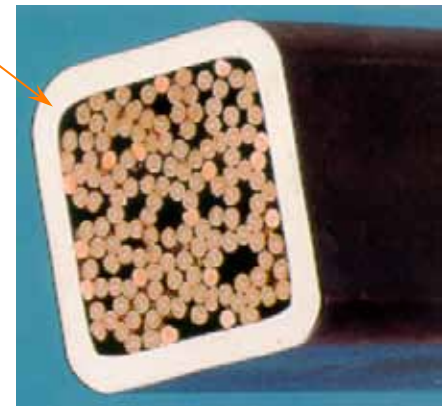
Cryostable Magnets

Key Features

- $[J_{m_0}]_{sk}$ determined by parameters other than J_c :

$$[J_{m_0}]_{sk} = \sqrt{\frac{f_p \mathcal{P}_D q_{fm}}{\rho_m A_m}}$$

- LHe within the winding makes the cryostable winding “spongy”
- CICC used for “large” magnets, e.g., ITER, requiring a robust winding
- For “large” magnets in which structural materials occupy a significant fraction of the winding pack, making the condition $[J_{m_0}]_{sk} \ll J_c$ not as important as for adiabatic magnets.

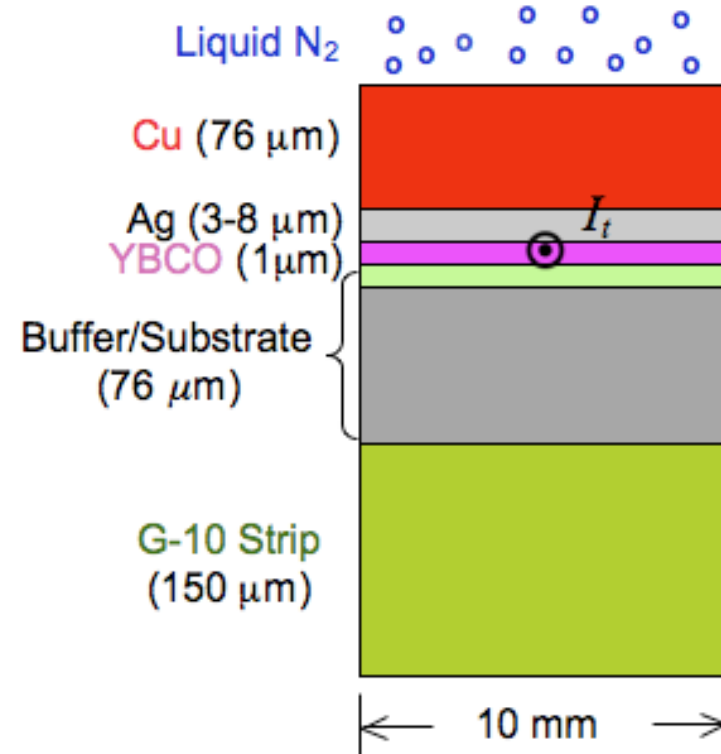
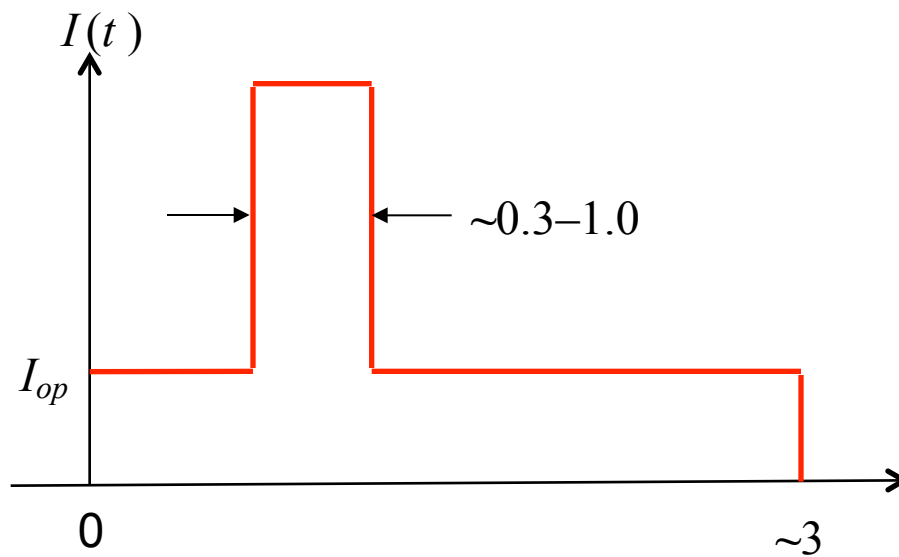


CIC conductor (CICC)

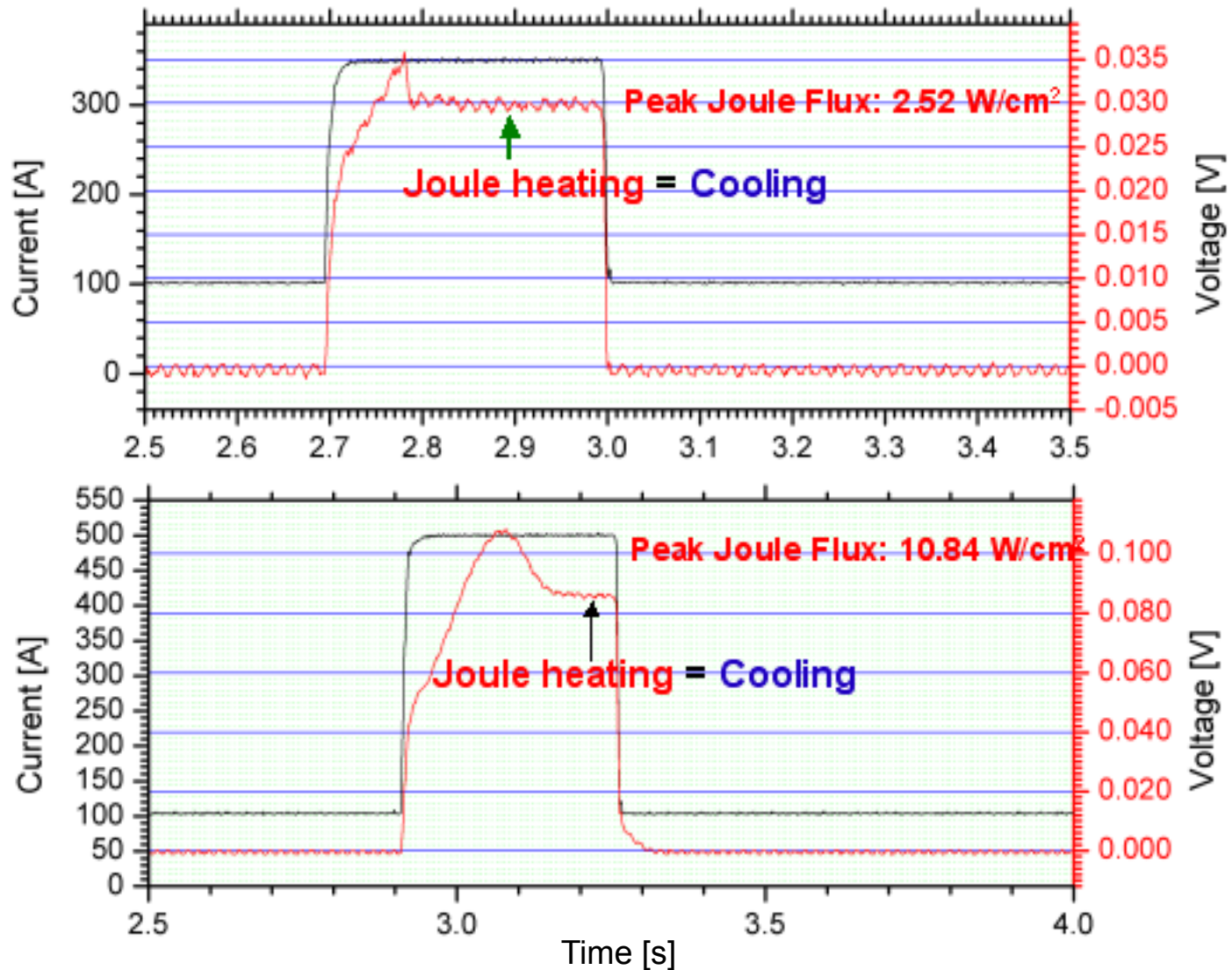
An Experimental Illustration of *Cryostability*

Experiment: *Liquid N₂ Cooled*, “Composite” YBCO Tape

- Composite YBCO, 10-cm long; I_c (77 K, self field): >110 A
- A current pulse ($3-5 \times I_c$) applied over a steady-state DC current ($\sim 0.9I_c$)

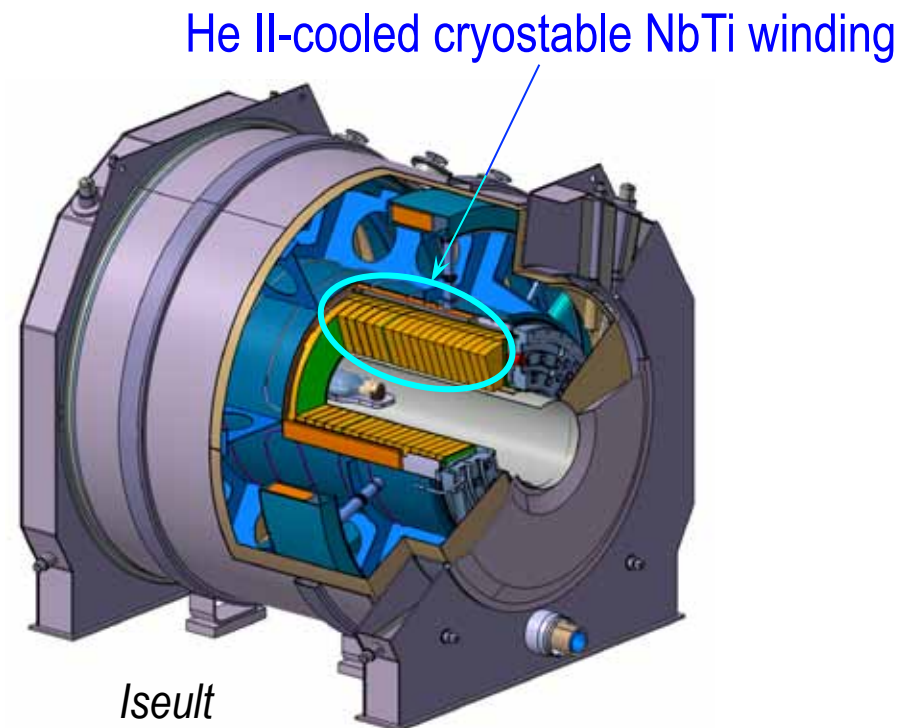


An Experimental Illustration of *Cryostability*



Cryostable Magnets: Current Trend

- Up to ~1980 magnets were mostly cryostable
 - *Success* much more important than *efficiency*
- Since ~1980, *cryostability* restricted to “large” magnets, e.g.,
 - ITER coils: forced supercritical helium through CICC
 - *Iseult*: a large MRI magnet (500 MHz/ 900 mm RT bore) nearly completed in France

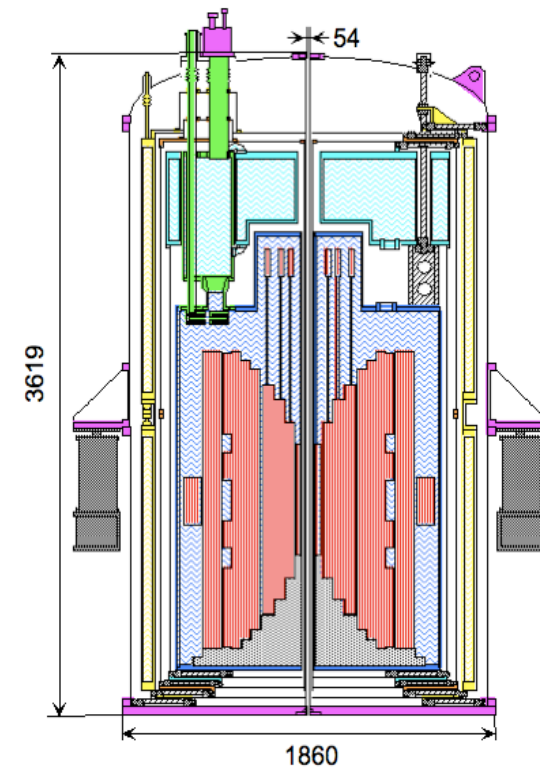


Adiabatic Magnets

- Since ~1980, adiabatic* (“high-performance”) magnets prominent chiefly because of efficiency (lower cost), e.g.,
 - Magnet *always* requires cooling but its winding not necessarily exposed directly to the coolant
 - HEP dipole and quadrupoles
 - NMR/MRI magnets
 - Most “research” magnets



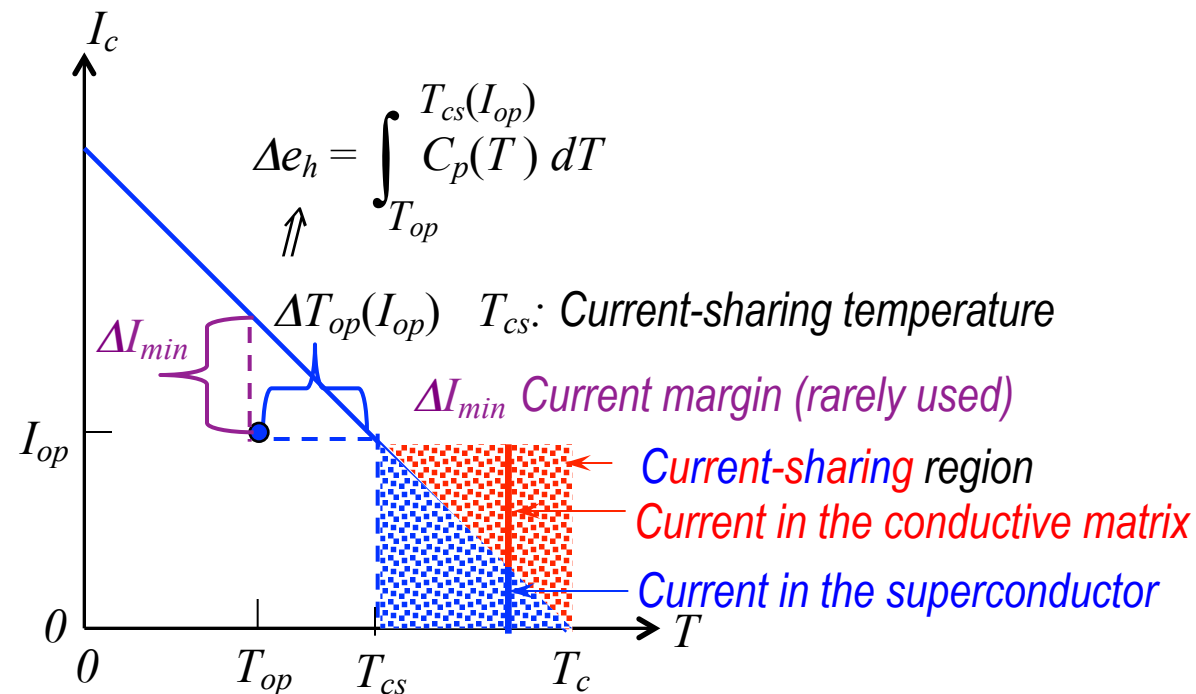
LHC dipole



920 MHz (21.6 T) NMR magnet

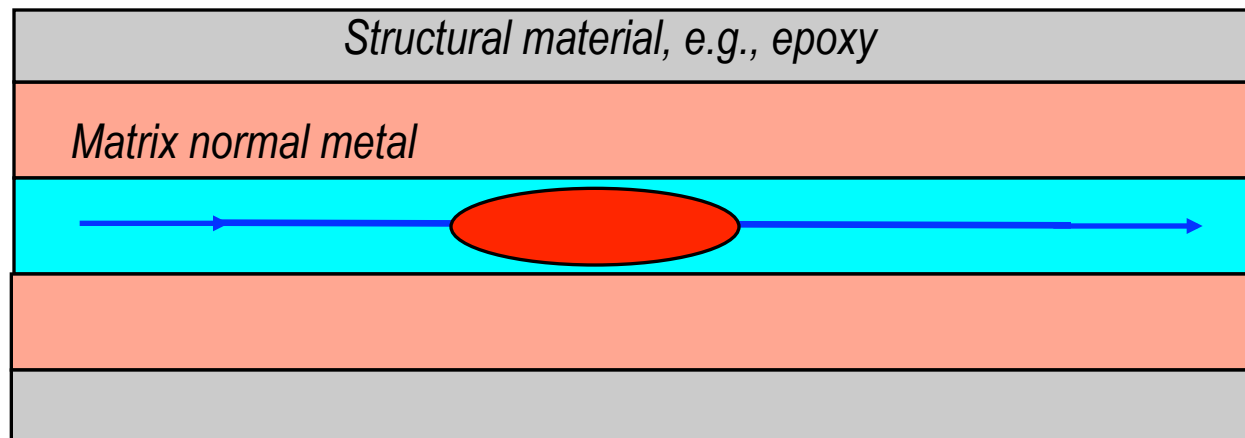
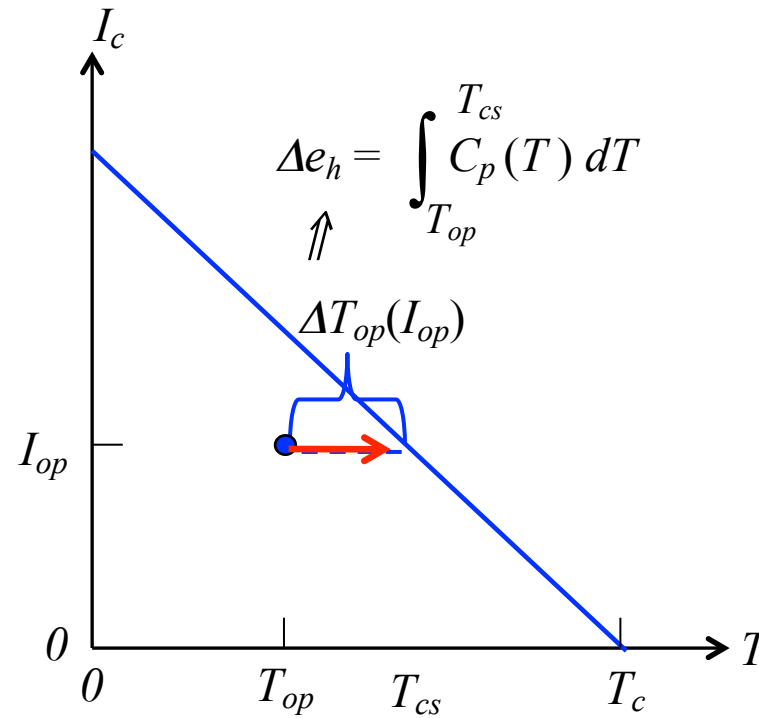
Stability Margin: Energy Δe_h or Temperature $\Delta T_{op}(I_{op})$

- Minimum energy density (or energy) or temperature rise that drives a part of the winding out of the superconducting state
- $\Delta T_{op}(I_{op})$ easier than Δe_h to quantify in the design stage;
 ΔI_{min} also easier than Δe_h but less used than $\Delta T_{op}(I_{op})$



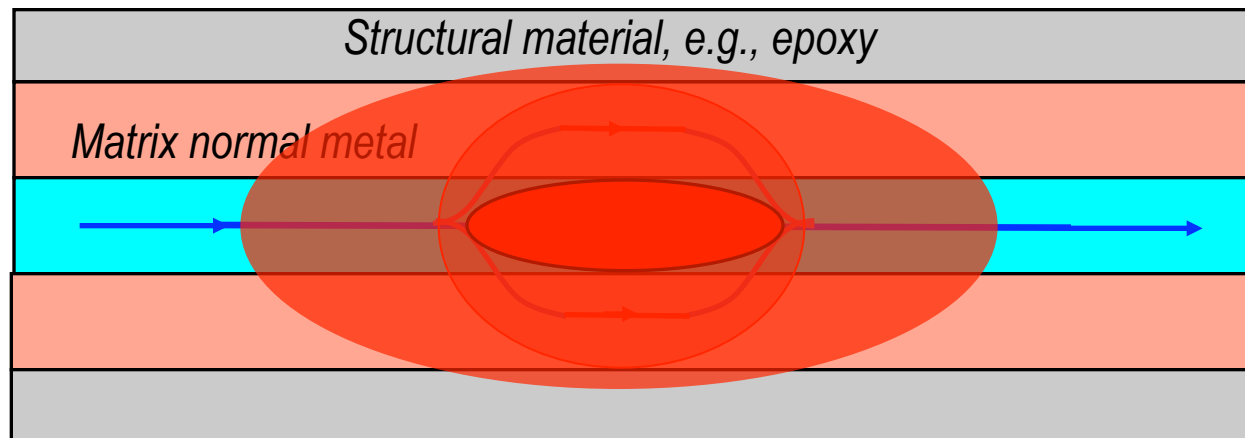
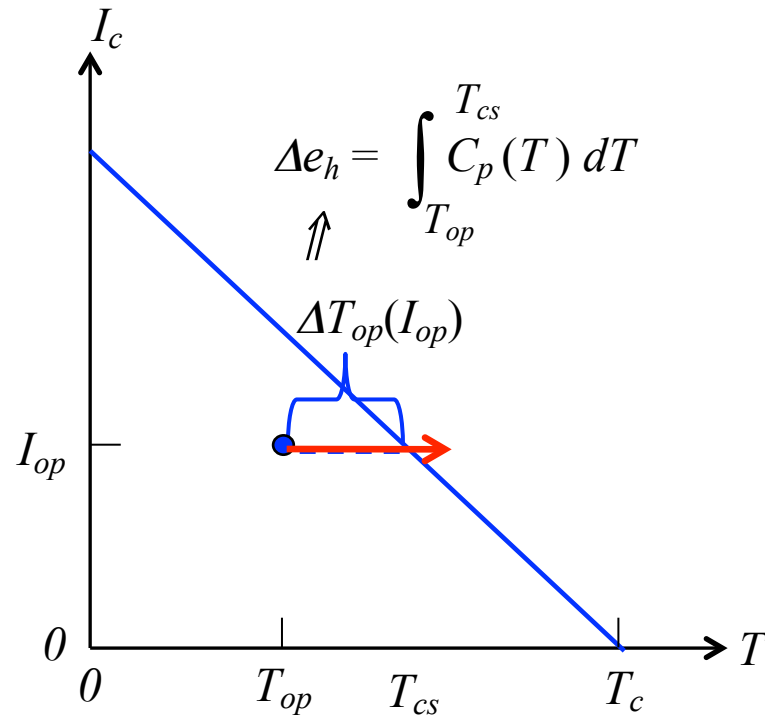
Adiabatic Magnet

- Disturbance energy density,
 $g_d(t) < \Delta e_h$



Adiabatic Magnet (cont.)

- $g_d(t) > \Delta e_h$: a quench



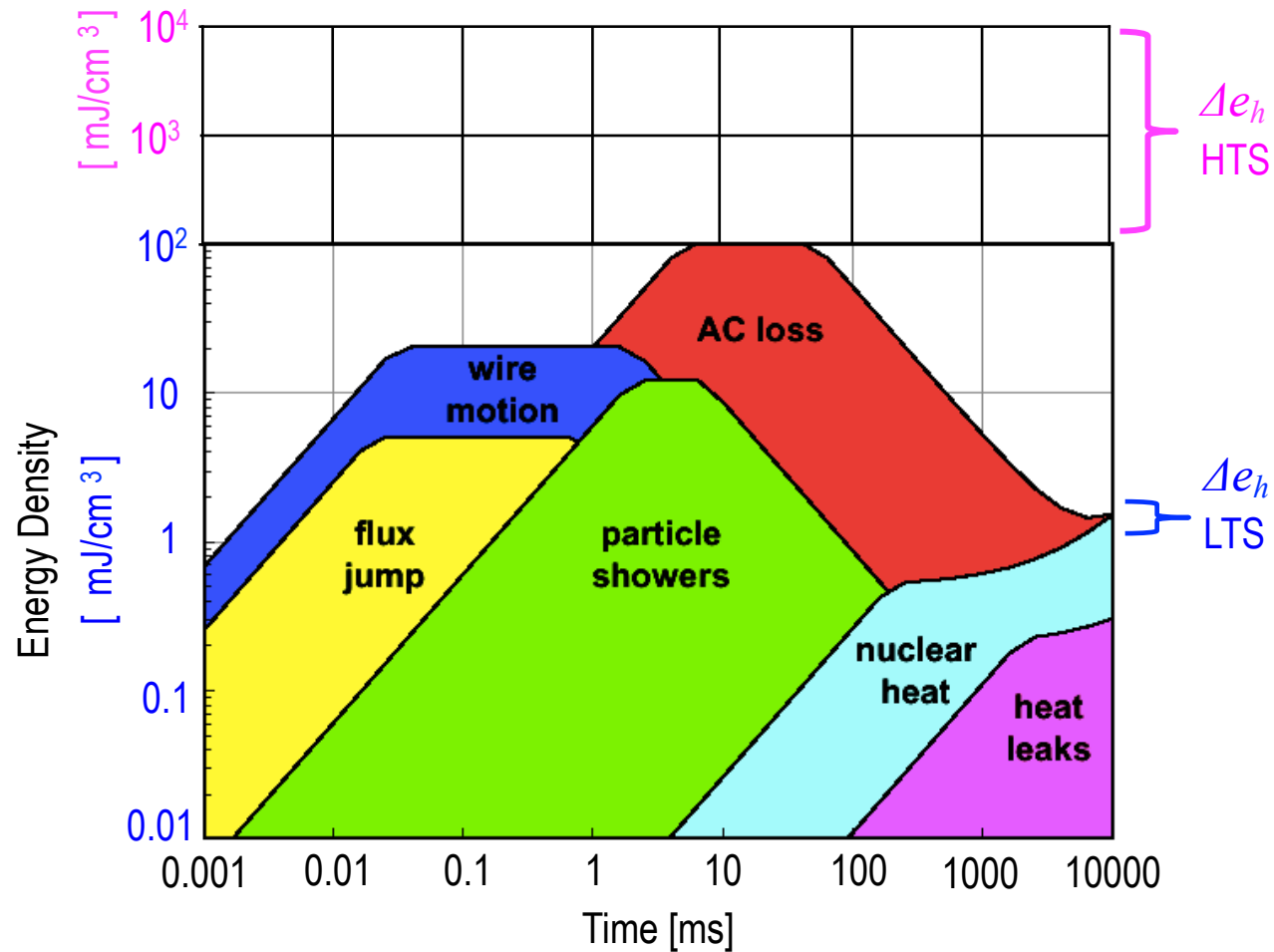
Sources of Disturbance

$$C_{cd}(T) \frac{\partial T}{\partial t} = \nabla \cdot [k_{cd}(T) \nabla T] + \rho_{cd}(T) J_{cd_o}^2(t) + g_d(t) - \left(\frac{f_p P_D}{A_{cd}} \right) g_q(T)$$

Storage
Conduction
Joule heating
Disturbance
Cooling

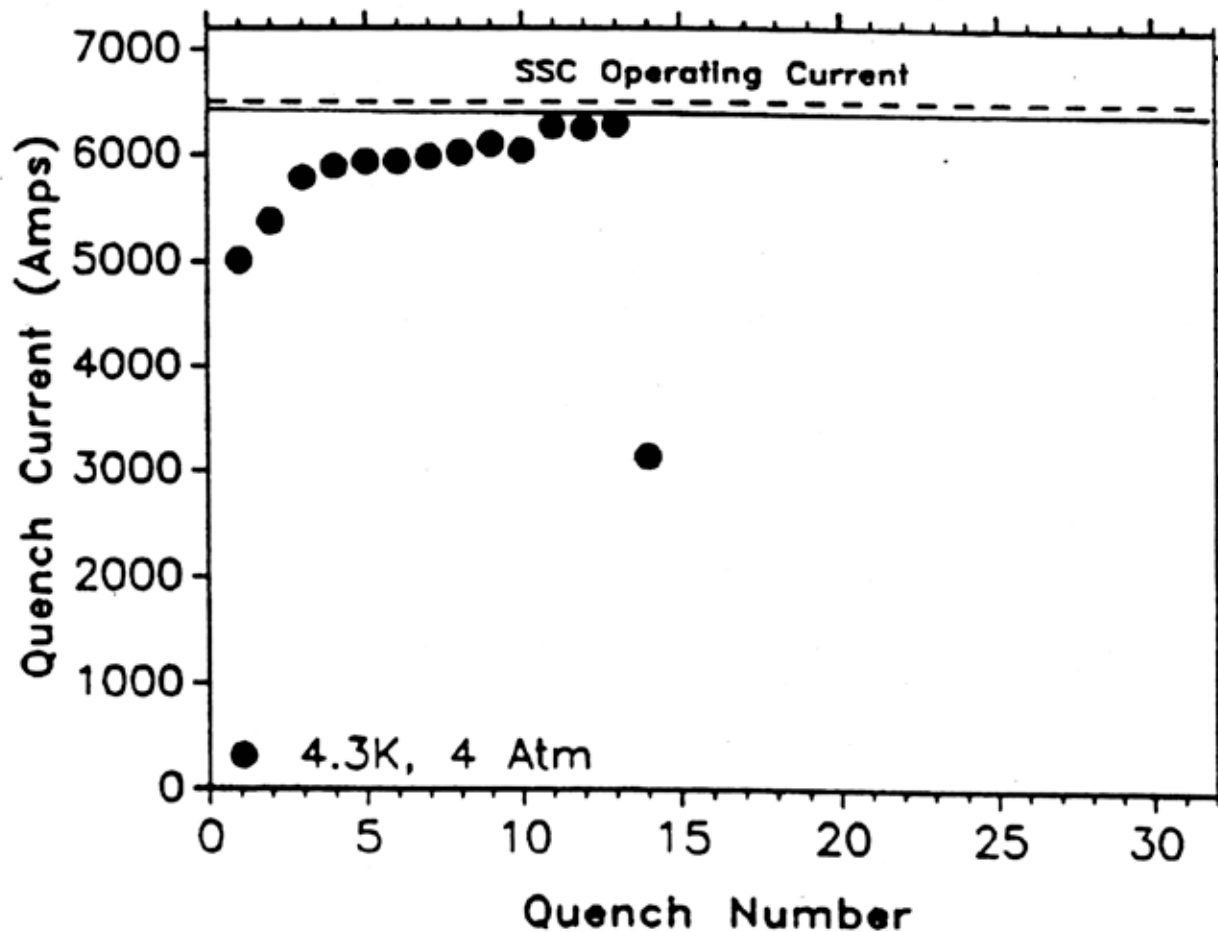
- Mechanical
 - Lorentz force; thermal contraction**
 - Wire motion / “micro-slip”
 - Remedy: Impregnate winding with epoxy or other filler
 - Structure deformation
 - Cracking epoxy; debonding
 - Wire motion remedy can become another disturbance
- Electrical/magnetic
 - Time-varying current/field**
 - Current transients, includes AC current
 - Flux motion, e.g., flux jump
 - Field transients, includes AC field
- Thermal
 - Conduction, through leads
 - Cooling blockage (poor ventilation)
- Nuclear radiation
 - Neutron flux in fusion machines
 - Particle showers in accelerators

Disturbance Energy Density Spectra



HTS magnets free of disturbances that afflict adiabatic **LTS** magnets

An Example of Training in an SSC* Dipole



* Superconducting Super Collider (US program launched in 1986 but canceled in 1993 because of cost overrun). SSC (vs. LHC): 20 TeV (7 TeV); 6.8 T/87 km (8.4 T/27 km)

[S. Ige (MIT ME Dept. Ph.D. Thesis, 1989)]

AE Technique

Acoustic signals emitted by sudden *mechanical events* in a body *being* loaded or unloaded, e.g., a magnet being charged or discharged; useful for detection and location of a premature quench caused by *conductor motion* or *epoxy fracture* event in *adiabatic magnets*

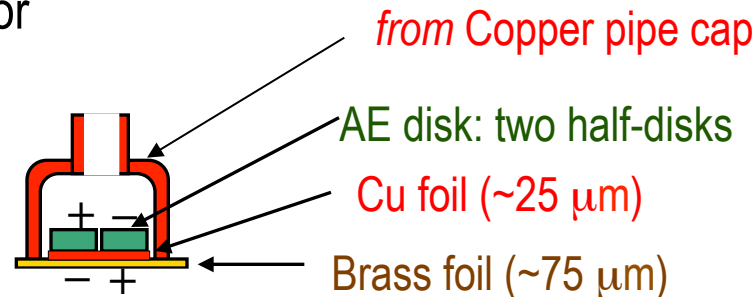
The technique used extensively in the 1980s at FBML to: 1) understand the nature of these disturbances; 2) develop a new technique to minimize the detrimental effects of these disturbance and improve magnet performance, i.e., minimize the *premature quenches*

Piezoelectric Effect: The coupling of mechanical and electric effects in which a strain in a certain class of crystals, e.g., quartz, induces an electric potential and vice versa; *discovered by P. Curie in 1880*

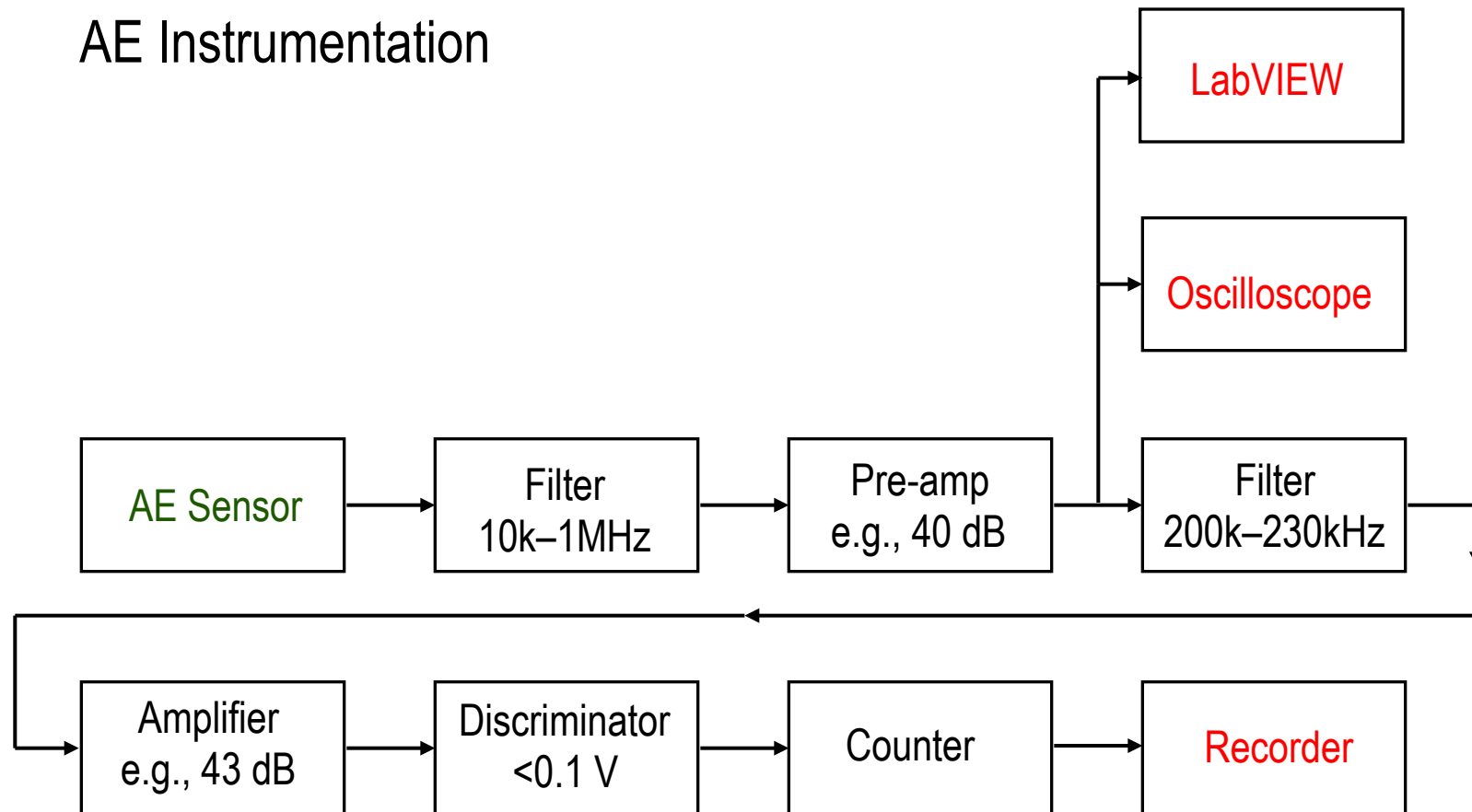
AE Sensor

- Commercially available sensor: expensive (\$500-\$2000); and even those built for use in “low temperature” generally fail
- Home-made (FBML) differential sensors: reasonable cost (~\$50/AE disk + labor); withstands 4.2 K - RT cycles.

Differential Sensor



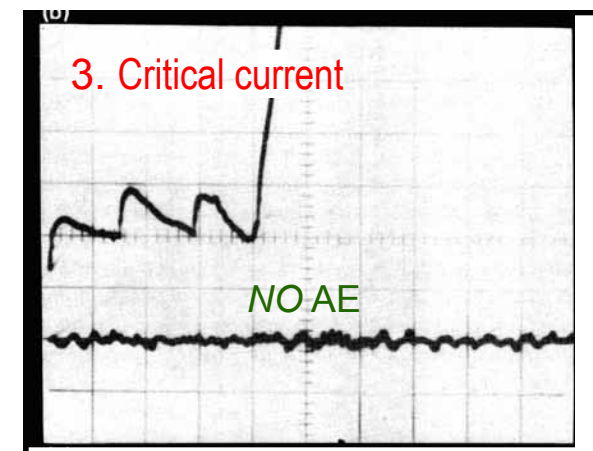
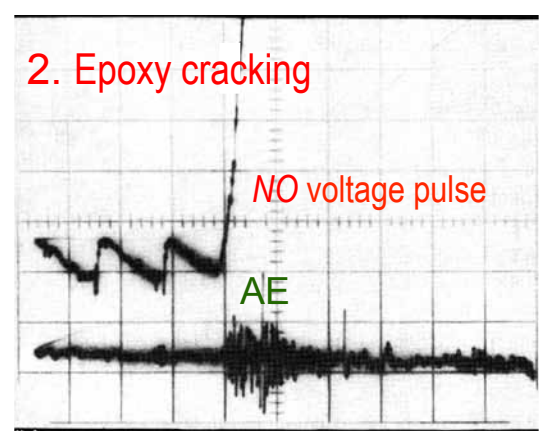
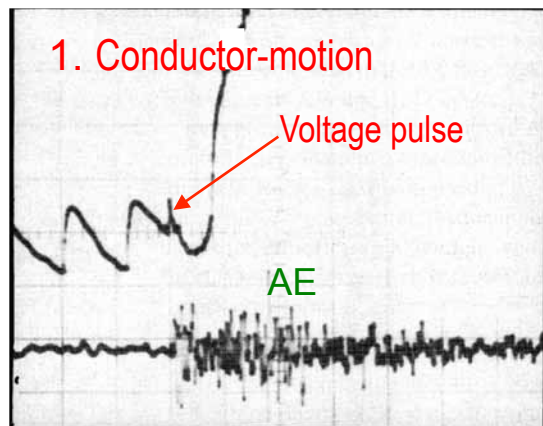
AE Instrumentation



Identification of Quench Causes by AE Technique

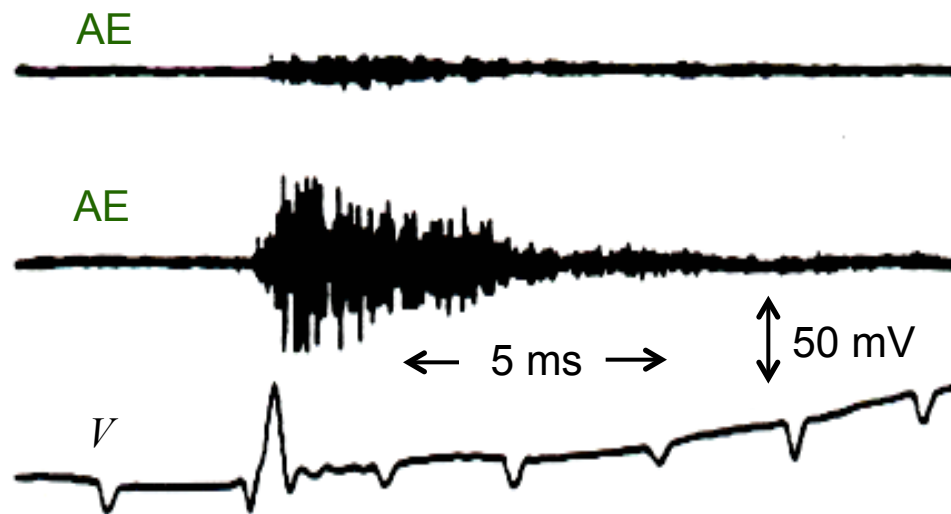
A combination of **voltage** & **AE** monitoring permits identification of 3 *distinguished* causes of a quench in **adiabatic** magnets

1. Conductor motion: a **voltage spike** & the start of **AE** signals
2. Epoxy fracture: **no voltage spike** but **AE** signals
3. Critical current: **no voltage spike nor AE** signals



[O. Tsukamoto, J.F. Maguire, E.S. Bobrov, and Y. Iwasa, *Appl. Phys. Lett.* **39**, 172 (1981)]

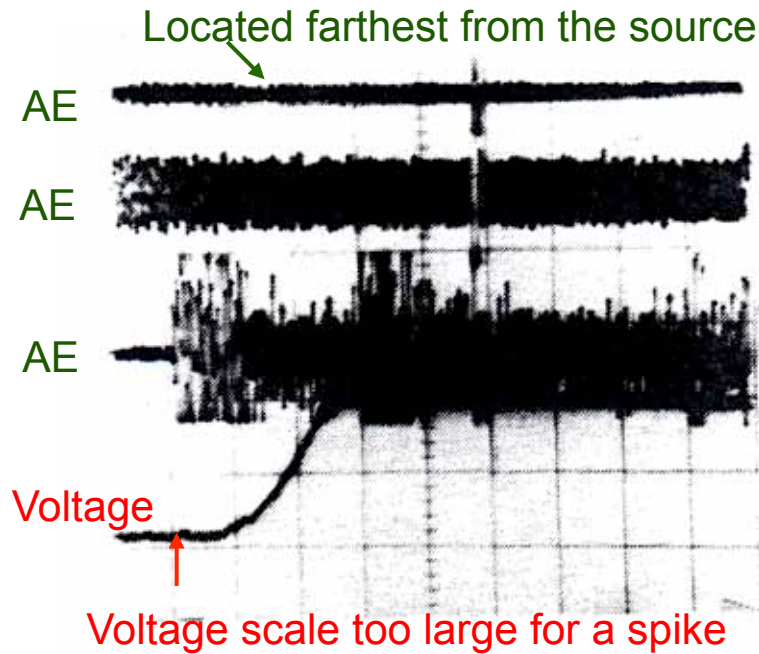
A Conductor-Motion Induced Quench — *Isabella Dipole* (BNL, c. 1981)



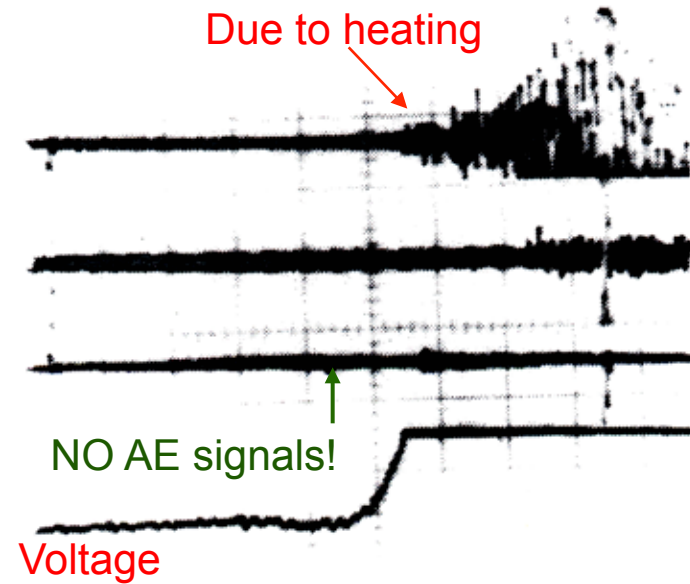
[O. Tsukamoto, M.W. Sinclair, M.F. Steinhoff, and Y. Iwasa, *App. Phys. Lett.* **38**, 718 (1981)]

Conductor-Motion Induced & Critical-Current Quenches

— An SSC Dipole



$$I_q = 6510 \text{ A}$$



$$I_c = 6828 \text{ A}$$

[S. Ige (MIT ME Dept. Ph.D. Thesis, 1989)]

Conductor Motion

- Frictional heating energy release, e_f , due to a Lorentz-force induced conductor motion (“slip”) of Δr_f :

$$e_f = \mu_f f_{Lr} \Delta r_f = \mu_f J_\theta B_z \Delta r_f$$

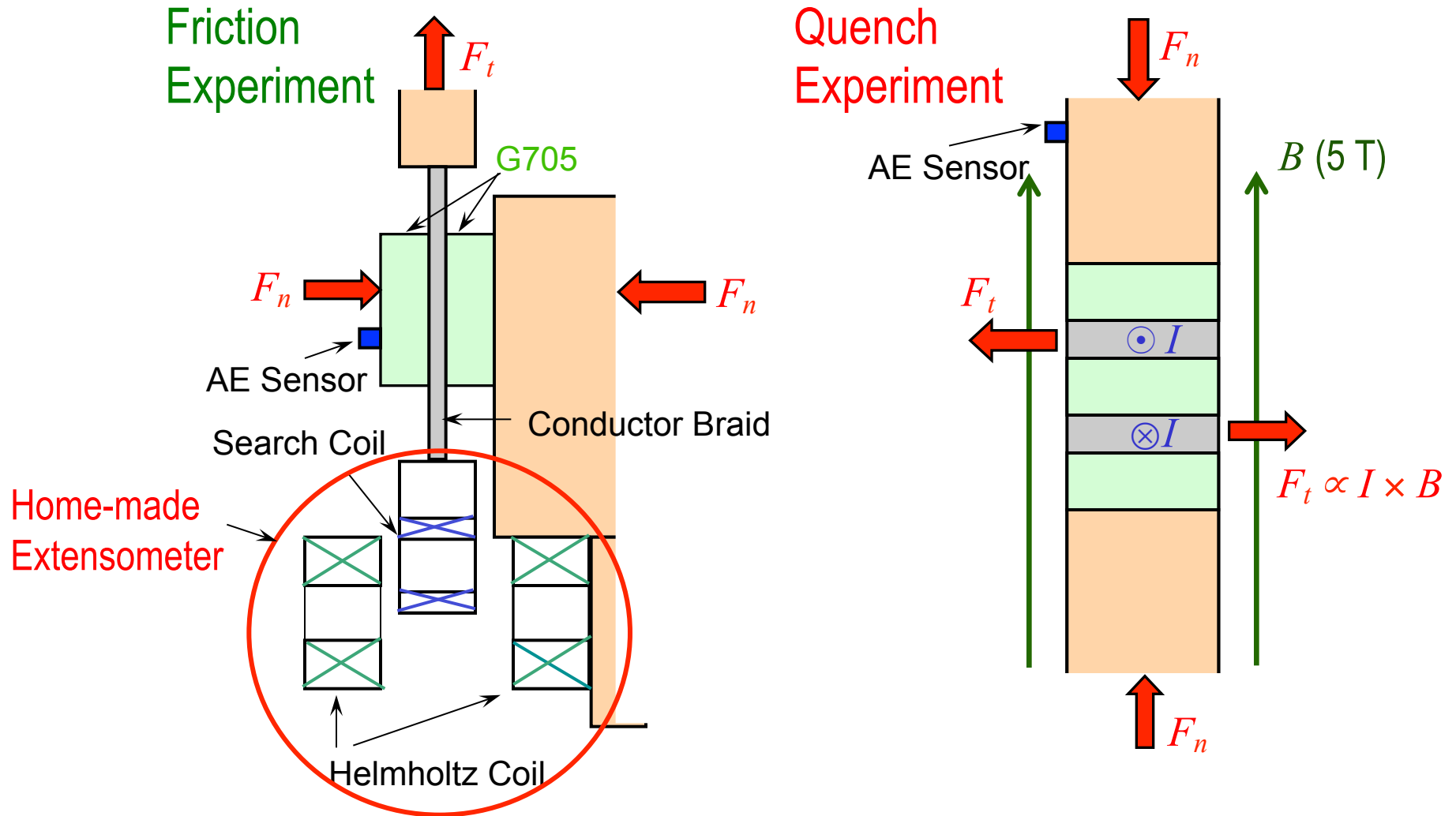
With $\mu_f = 0.3$, $J_\theta = 200 \times 10^6 \text{ A/m}^2$, $B_z = 5 \text{ T}$, and

$$e_f = h_{cu}(5.2\text{K}) - h_{cu}(4.2\text{K}) = 1300 \text{ J/m}^3 :$$

$$\Delta r_f = \frac{e_f}{\mu_f J_\theta B_z} = \frac{(1300 \text{ J/m}^3)}{(0.3)(200 \times 10^6 \text{ A/m}^2)(5 \text{ T})} \cong 20 \mu\text{m}$$

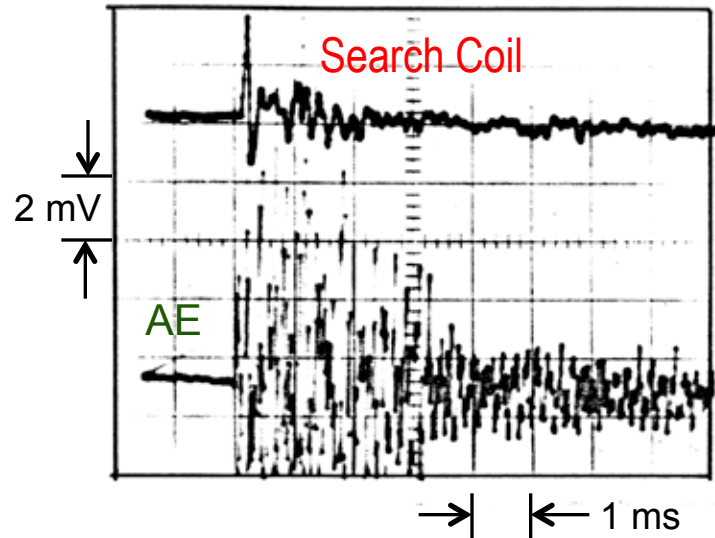
- Actually a conductor slip as small as $\sim 1 \mu\text{m}$ (“microslip”) can drive a short length of the conductor to the normal state, inducing a premature quench

Friction/Quench Experiments



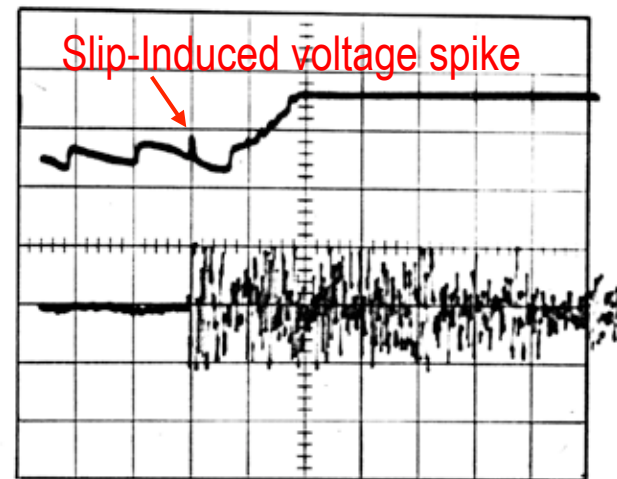
Based on O. Tsukamoto, H. Maeda, and Y. Iwasa, Appl. Phys. Lett. 39, 918 (1981)

Friction Experiment



Slip distance: $\sim 1 \mu\text{m}$
 Peak slip velocity: $\sim 1 \text{ cm/s}$
 $F_n = 2000 \text{ N}$; $F_t \sim 400 \text{ N}$

Quench Experiment

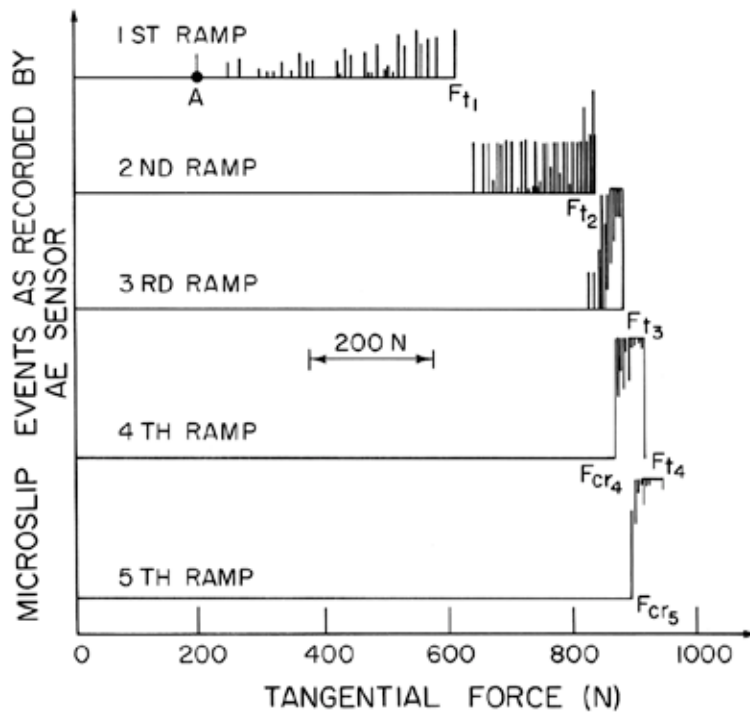


Slip distance: $\sim 1 \mu\text{m}$
 Peak slip velocity: $\sim 3 \text{ cm/s}$
 $F_n = 2000 \text{ N}$; $F_t = 500 \text{ N}$
 $[=(0.025 \text{ m})(4000 \text{ A})(5 \text{ T})]$

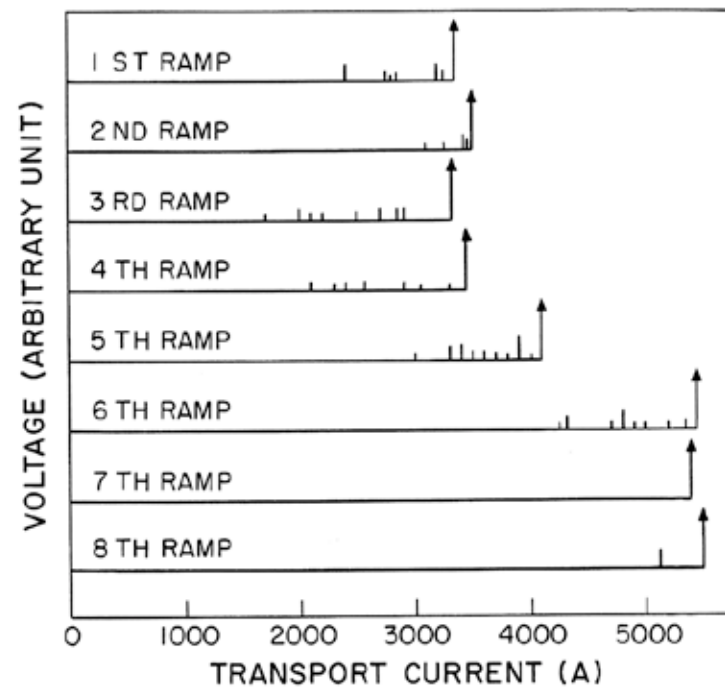
[O. Tsukamoto, H. Maeda, and Y. Iwasa, *Appl. Phys. Lett.* **39**, 918 (1981)]

Observation of Kaiser Effect, i.e., Training

Friction Experiment



Quench Experiment

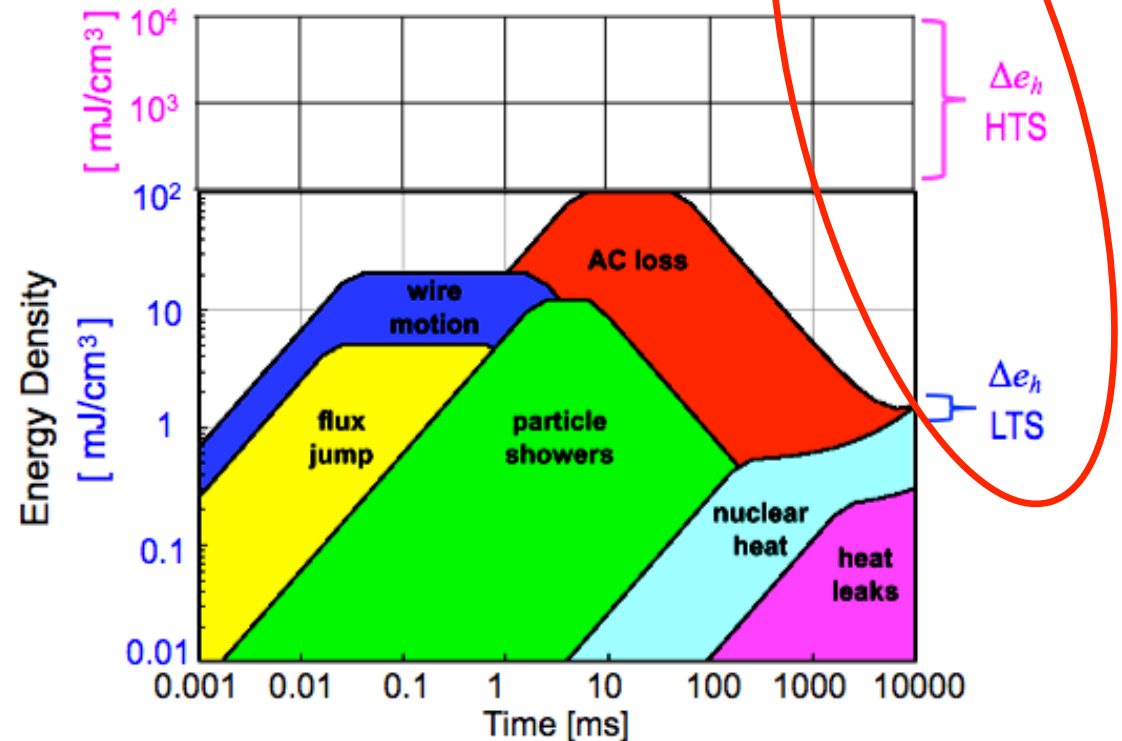
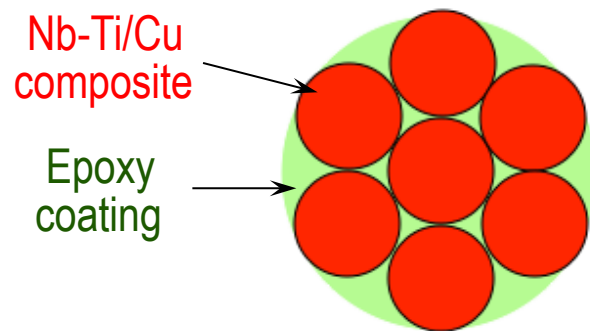


[H. Maeda, O. Tsukamoto, and Y. Iwasa, *Cryogenics* 22, 287 (1982)]

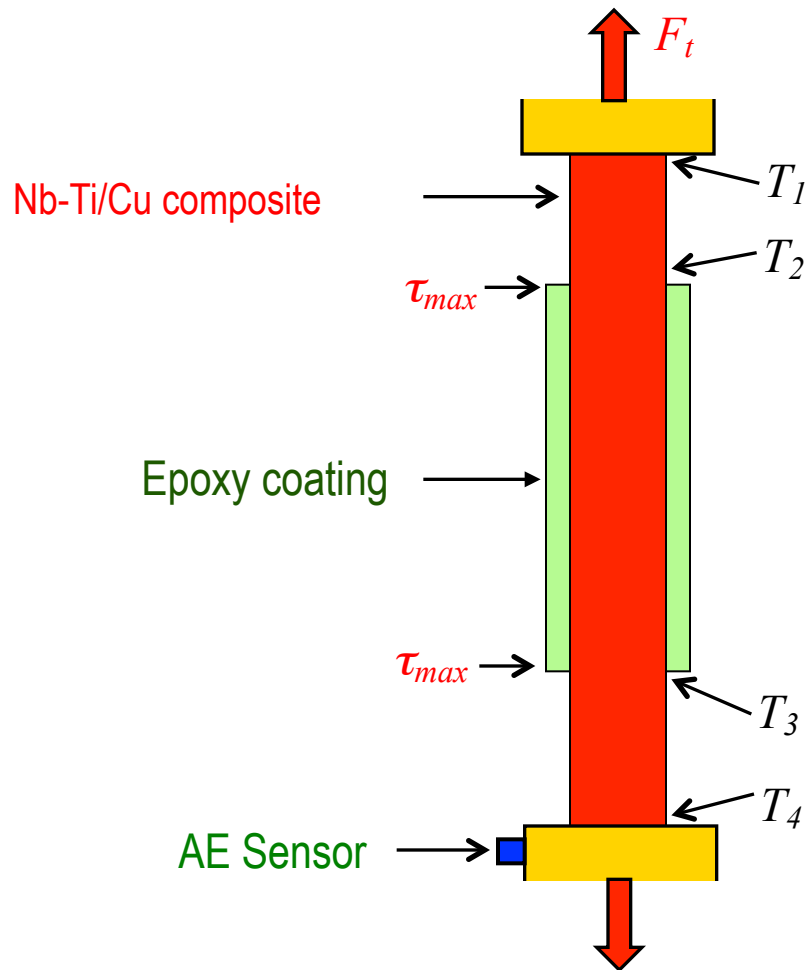
Epoxy Fracture Inducted Heating

Stored elastic energy density, ϵ_{el} , typical epoxy resin:

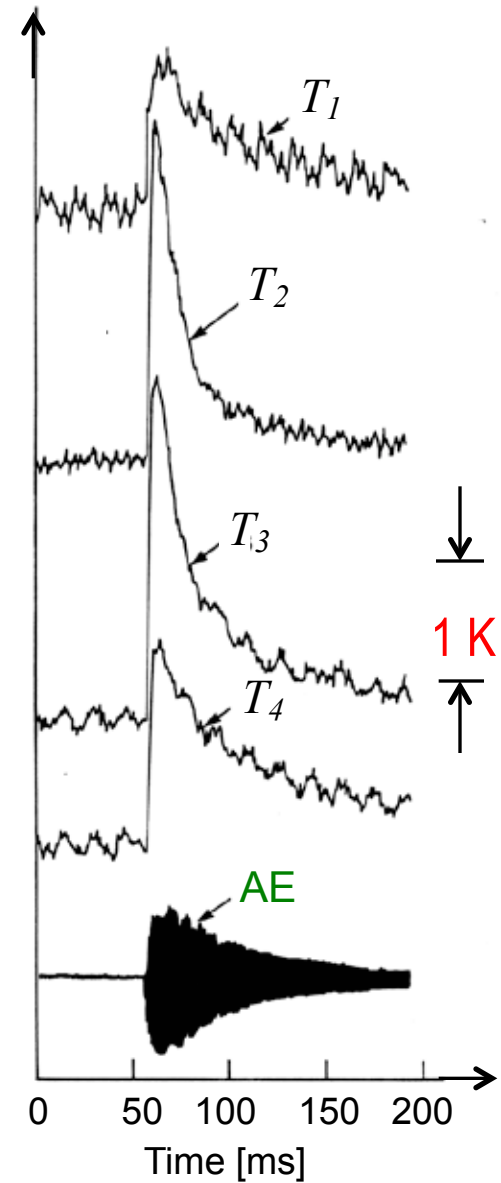
$$\epsilon_{el} = \frac{\sigma_{el}^2}{2E} \approx \frac{(15 \times 10^6 \text{ Pa})^2}{2(10 \times 10^9 \text{ Pa})} = 11,250 \text{ J/m}^3 \sim 10 \text{ mJ/m}^3 \gg [e_h]_{mx}$$



Epoxy Cracking Inducted Heating — Experimental Results



[Y. Yasaka and Y. Iwasa, *Cryogenics* **24**, 423 (1984)]



Properties (at 4.2 K) and Energy Densities of Selected Filler Materials:^{*}
 Epoxy, Cynate Ester, Vinyl Ester, Polyester, and Others

Manufacturer / Trade Name or #	E [GPa]	σ_{ul} [Mpa]	e [mJ/cm ³]
Hercules / 3502	9.5	66	229
Shell / 9310	9.5	86	389
Dow Chemical / Tactix 123	8.3	102	627
Composite Technology Development / 102	8.1	95	557
Ciba-Geigy / 179	7.5	85	482
Shell / DPL 862	7.0	128	1170
Rhone-Poulenc / REX-378	6.8	117	1007
ICI / 954-3	6.4	69	372
Composite Technology Development / X700	9.4	62	204
Composite Technology Development / X800	7.5	130	1127
Dow Chemical / Derakane 8084	5.8	139	1665
Owens Corning / 701	7.4	95	610
NHMFL 61**	7.5	141	1325
Paraffin+	(assume 6)	21	37

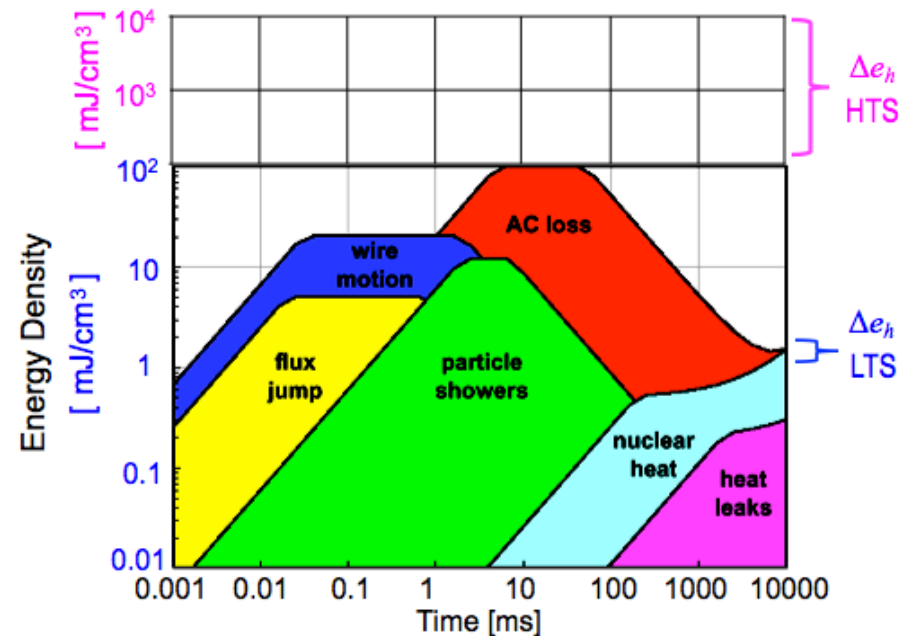
* [D. Evans and J.T. Morgan (Rutherford and Appleton Lab., early 1980s0)]

** [W.D. Markiewicz, I.R. Dixon, J.L. Dougherty, K.W. Pickard, and A.B. Brennan (ICMC/CEC, 1997)]

+ [P.F. Smith and B. Colyer, *Cryogenics* 15, 201 (1975)]

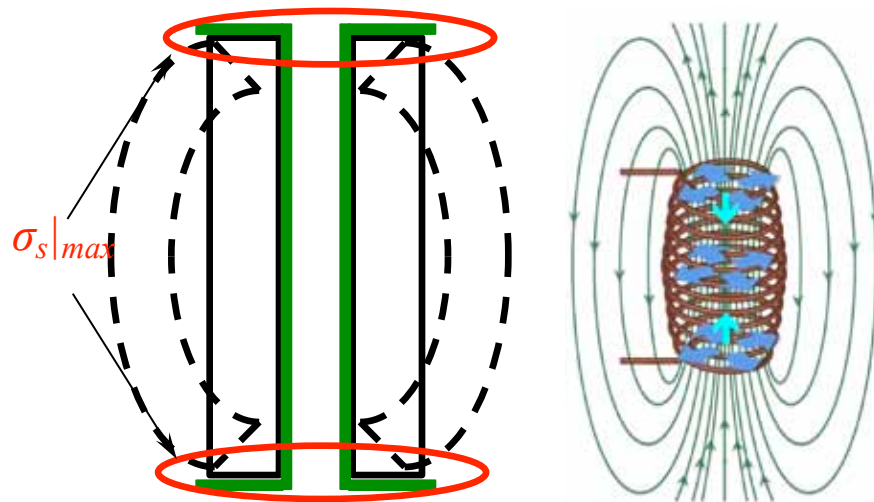
Observations on Filler Materials

- Filler materials generally release a fracture energy density ($> 200 \text{ mJ/cm}^3$)
 - A fracture incident likely to cause a premature quench in *LTS* magnets
 - Still, paraffin-filled magnets suffer least incidents of premature quench
- *HTS* magnets unlikely to suffer from filler fracture
- *HTS* magnets unlikely to suffer from conductor motion
 - Filler material *not* required to prevent conductor motion

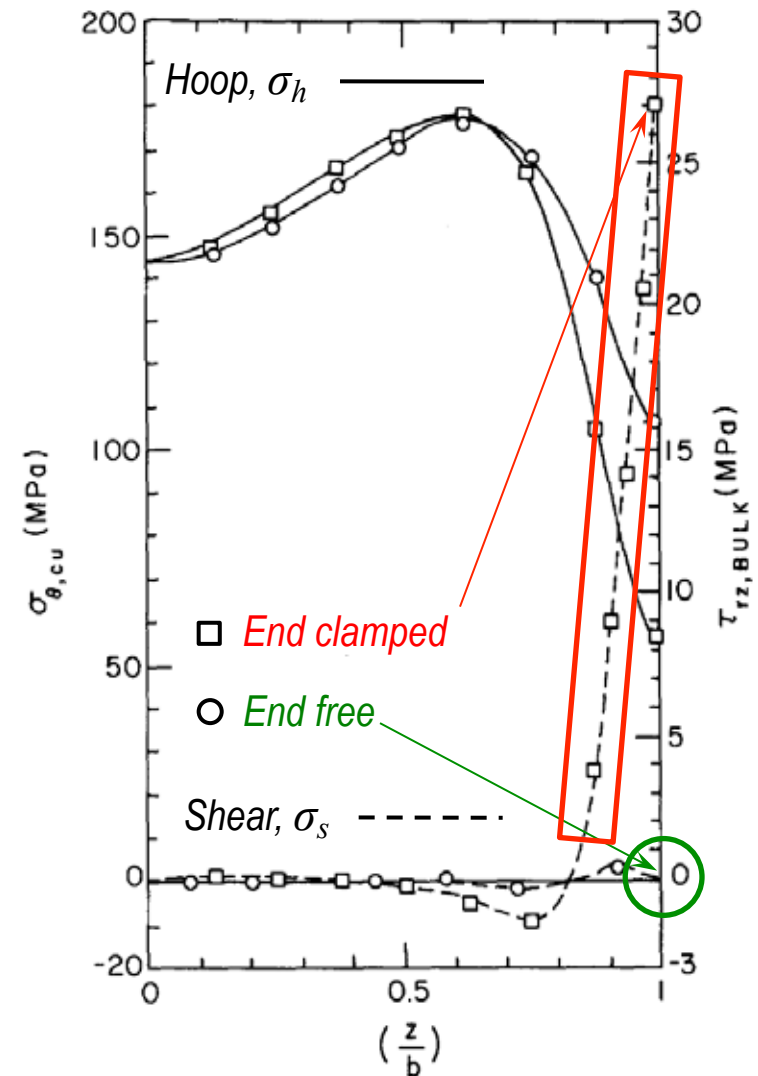


Epoxy-Fracture-Inducted Heating

- Epoxy-impregnated winding anchored to the coil form at both ends by epoxy
- When energized, the winding becomes barrel-shaped
- Large shear stresses appear at the coil ends, causing epoxy fracture, which in turn induces premature quenching

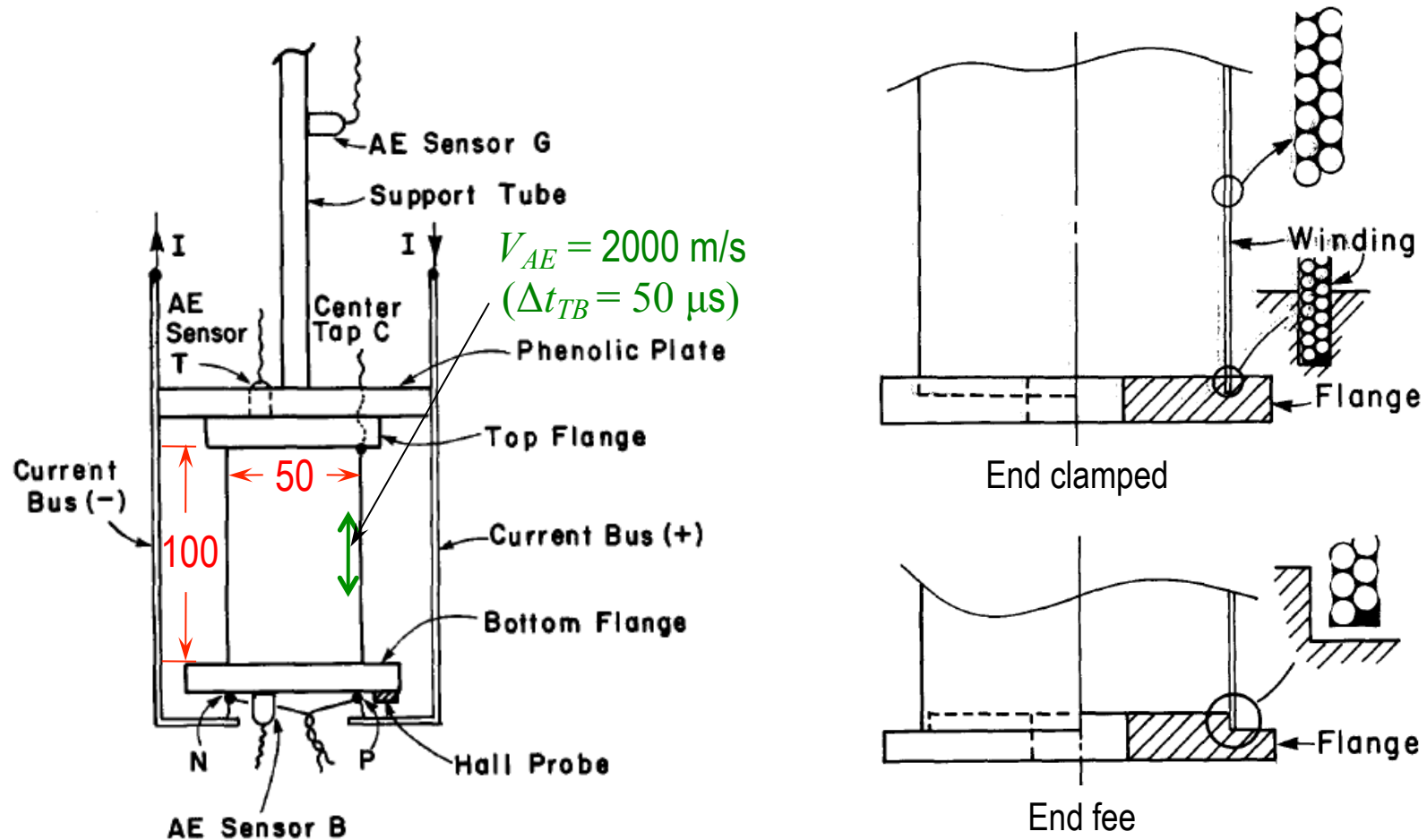


Barrel-shaped (Overly exaggerated)



[E.S. Bobrov, J.E.C. Williams, and Y. Iwasa, Cryogenics 25, 307 (1985)]

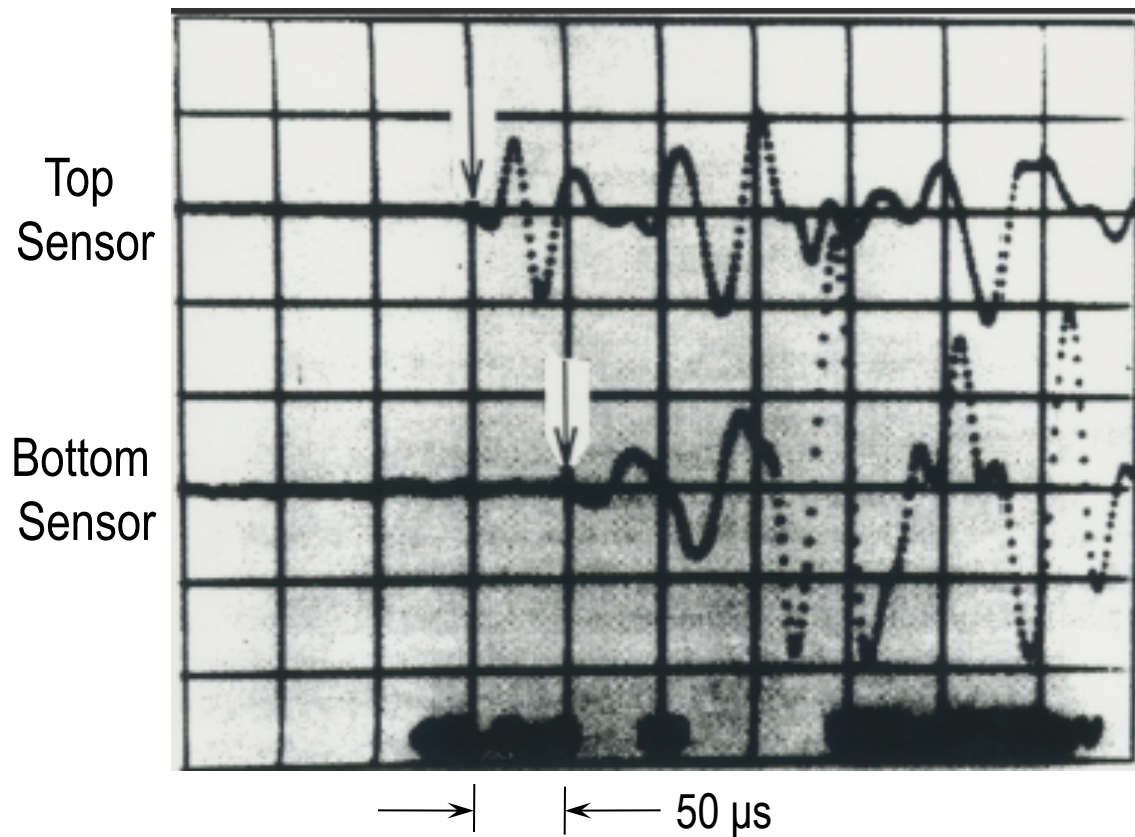
An Experimental Confirmation of Shear-Stress Induced Epoxy Fracture



[Y. Iwasa, E.S. Bobrov, O. Tsukamoto, T. Takaghi, and H. Fujita, *Cryogenics* **25**, 317 (1985)]

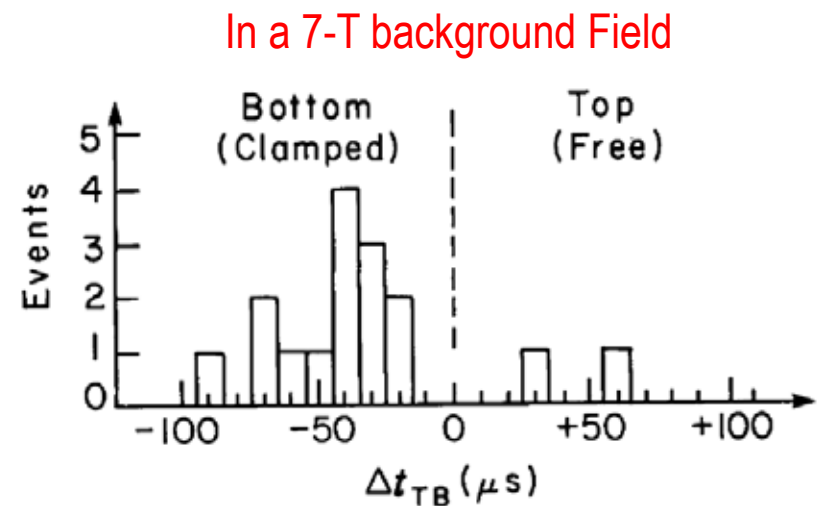
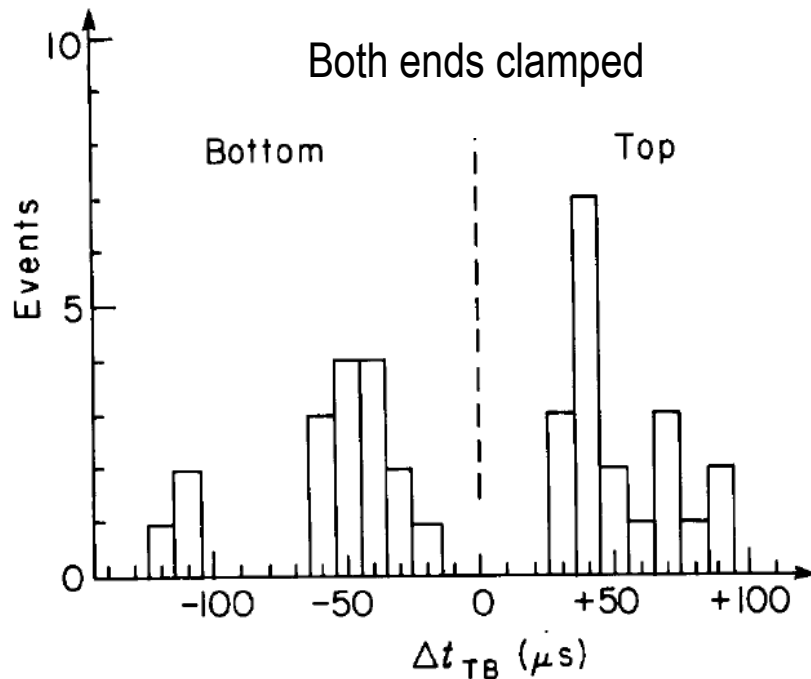
An Experimental Confirmation of Shear-Stress Induced Epoxy Fracture (cont.)

Oscillogram from Top and Bottom AE Sensors

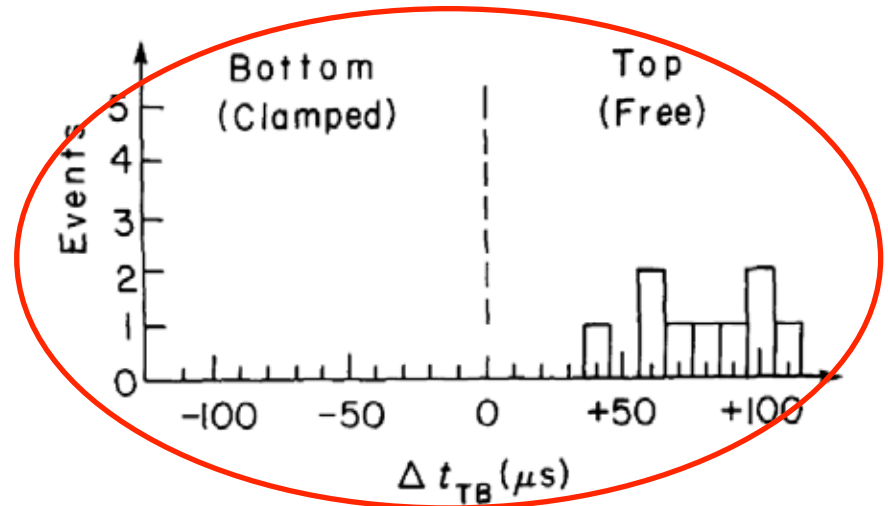


[H. Fujita, T. Takaghi, and Y. Iwasa, *Cryogenics* 25, 325 (1985)]

An Experimental Confirmation of Shear-Stress Induced Epoxy Fracture



The test coil positioned slightly below the magnet midplane; when the test coil was gradually energized, the coil moved upward and the winding rubbed against the free end, creating non-quench (current still too low) mechanical events picked up by the upper AE sensor



[H. Fujita, T. Takaghi, and Y. Iwasa, *Cryogenics* 25, 325 (1985)]

“Floating” Coil Winding Technique

- Developed at FBML in the 1980s to minimize epoxy (or more broadly filler) fracture induced premature quenches
- The technique now widely, if not universally, used for MRI magnets, which for commercially made, are all **LTS**-based
- The technique proven successful *most* of the time but *not always*, particularly when the winding is impregnated with a high-strength filling material (for winding reinforcement)

Summary on Stability

LTS Magnet

- **Cryostable**: Disturbance energy can exceed Δe_h

➤ **Joule dissipation** \cong **Cooling**

Goal: Maximum stability, i.e., reliability, that money can buy

- **Adiabatic**: Disturbance energy cannot exceed Δe_h

➤ **Dissipation energy within the winding** $\cong 0$ ($\leq \Delta e_h$)

Goal: Efficiency (↘ cost)

HTS Magnet

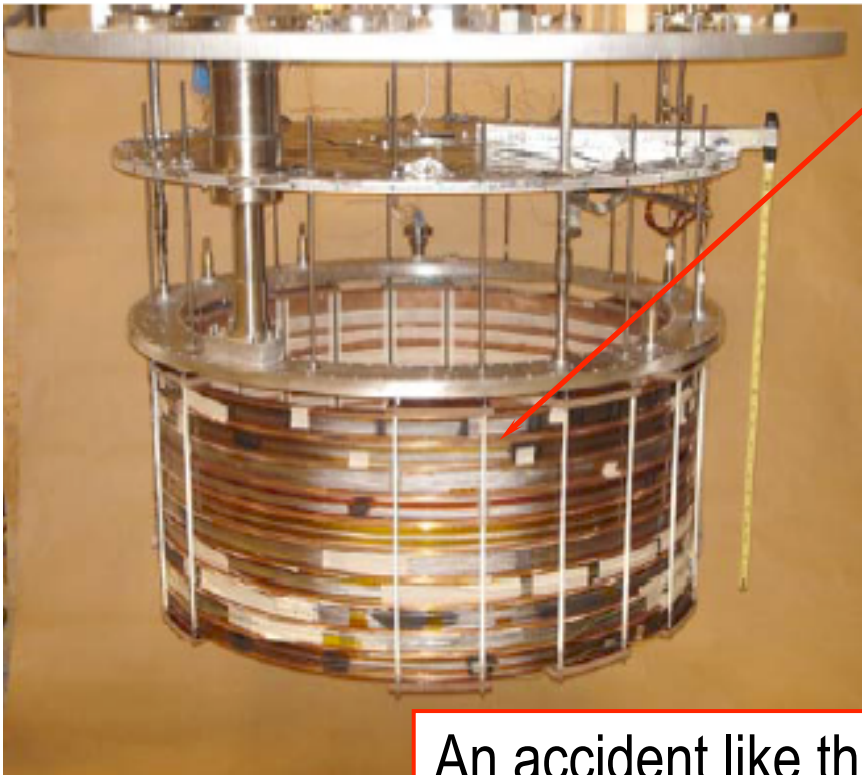
- Stability not a key issue

All **HTS** magnets should be **adiabatic**

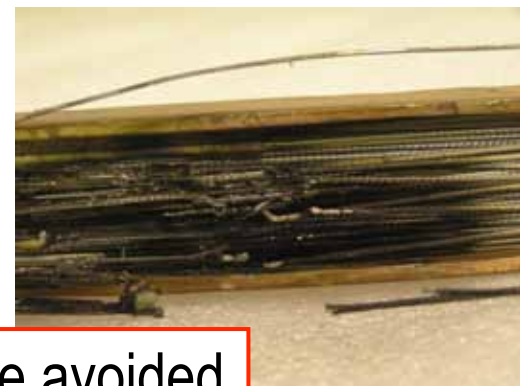
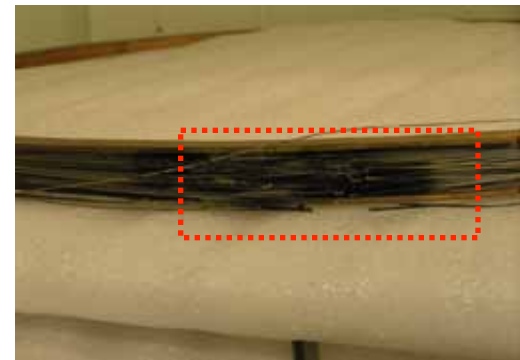
Protection

Objective: To **protect** the magnet from **permanent damage** in the event of an unscheduled **quench**

A 0.5 T / 773-mm Cold Bore MgB_2 Magnet
(FBML, 2007)



An unscheduled **quench** (top coil)
 \Rightarrow **Permanent damage**



An accident like this must be avoided

[W. Yao, J. Bascuñán, W-S Kim, S. Hahn, H. Lee, and Y. Iwasa, *IEEE Trans. Appl. Supercond.* **18**, 912 (2008)]

Two Approaches to Protection

Passive: applicable to “self-protecting” magnets, like **LTS** MRI;
critically dependent on normal zone propagation (NZP)

- Single coil: relies solely on NZP \Rightarrow size limitation
- Multiple coils: shunt resistors across each coil
 - Transfer of magnetic energy between coils, reducing the energy dissipated in the *hot spot*
 - Built-in heater energized by the magnet itself, rather than by an external source — “passive-activate-the-heater”

Active: applicable to non-self-protecting magnets

Protection

Sources of damage

- Overheating
- High voltage
- Overstress (and overstrains)
- Over pressure, in a system with liquid cryogen

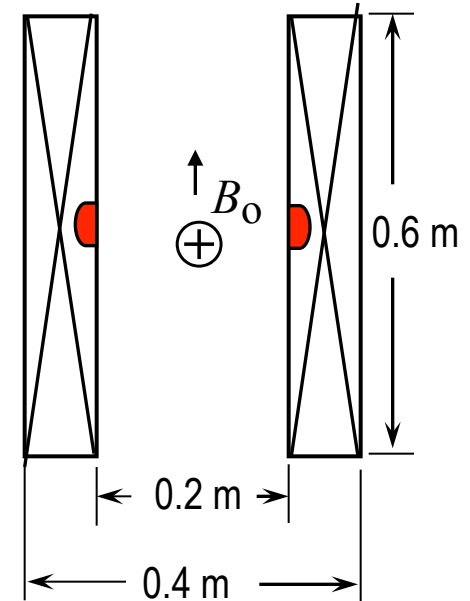
Best Protection Approach: Minimize **quench** events

Overheating

Example

- $B_o = 8 \text{ T}$; $E_{mg} = 10^6 \text{ J}$
- Winding volume = 0.06 m^3

Winding % Absorbing E_{mg}	T_f [K]	Remarks
100	55	Well below 100 K
50	70	< 100 K
10	130	Barely acceptable
1	580	Unacceptable



- “Fast” Normal Zone Propagation (NZIP) velocity required to spread out normal (i.e., energy absorbing) zone within the winding
- Self-protecting magnet relies on fast NZIP velocities

Normal Zone Propagation (NZP) Velocity

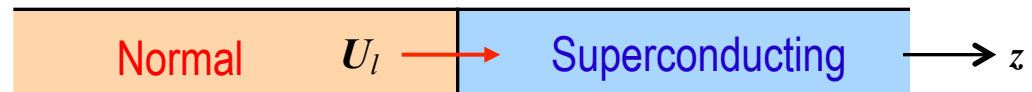
Along conductor axis (longitudinal)—No matrix

$$C_n(T) \frac{\partial T_n}{\partial t} = \frac{\partial}{\partial x} \left[k_n(T) \frac{\partial T_n}{\partial x} \right] + \rho_n(T) J^2 \quad (\text{normal})$$

$$C_s(T) \frac{\partial T_s}{\partial t} = \frac{\partial}{\partial x} \left[k_s(T) \frac{\partial T_s}{\partial x} \right] \quad (\text{superconducting})$$

$$\frac{\partial T_n}{\partial t} = \frac{\partial T}{\partial z} \frac{\partial z}{\partial t} = -U_\ell \frac{dT}{dz} \quad (U_\ell: \text{longitudinal velocity})$$

$$U_\ell = J \sqrt{\frac{\rho_n k_n}{C_n C_s (T_t - T_{op})}}$$



$$U_\ell = J \sqrt{\frac{\rho_n(T_t) k_n(T_t)}{\left[C_n(T_t) - \frac{1}{k_n(T_t)} \frac{dk_n}{dT} \Big|_{T_t} \int_{T_{op}}^{T_t} C_s(T) dT \right] \int_{T_{op}}^{T_t} C_s(T) dT}}$$

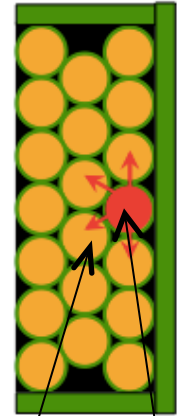
Protection & Normal Zone Propagation (NZP)

- “Small” **LTS** magnets rely on “fast” *NZP* velocity to spread out the normal zone to keep the “hot spot” from overheating
- “Large” **LTS** magnets rely on “subdivision” (by shunt resistors), but the subdivision technique too relies on “fast” *NZP* velocity
- In **HTS** magnets, *NZP* velocities (U_l , longitudinal & U_t , transverse) very slow, compared with those in **LTS** magnets: if relied only on *NZP*, an **HTS** hot spot overheated

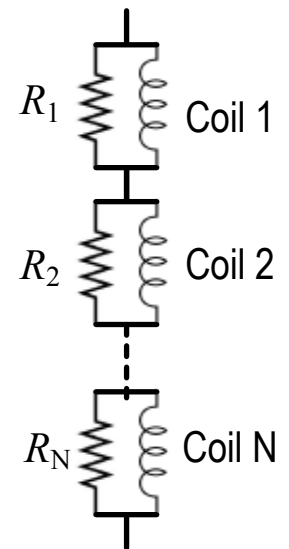
$$U_l(T) = \frac{J_m}{C_{cd}(T)} \sqrt{\frac{\rho_m(T)k_m(T)}{(T_{cs} - T_{op})}}$$

for **HTS** $C_{cd}(T)$ very large $\Rightarrow U_{lHTS} \ll U_{lLTS}$

Also for **HTS**, $U_t(T) < 0.1 U_l(T)$



NZP “Hot spot”



Protection & Normal Zone Propagation (NZP)

Selected Measured Longitudinal NZP Velocities (U_l)

Superconductor	B_{op} [T]	T_{op} [K]	J_m [A/cm ²]	U_l [mm/s]	Group (Year)
Nb ₃ Sn	0	12	70,300	511	MIT (1993)
	5	5.5	46,875	526	MIT (1993)
Bi2223	0	40	22,700	1.9	MIT (1993)
YBCO	0	46	1,000–1500	2–8	ORNL (2002)
	0	77	300–1500	3–10	NHMFL (2002)
	5	60	20,000	1	Waseda (2004)
	8	10	28,570	45	Grenoble-Saclay(2013)

HTS magnet must rely on active protection or
be a self-protecting assembly of NI coils*

* No-insulation (NI) winding technique—not discussed here

See, S. Hahn, D.K. Park, J. Voccio, J. Bascuñan, and Y. Iwasa, *IEEE Trans. Appl. Supercond.* **22**, 430405 (2012)

Hot-Spot Temperature (T_f)

$$\underbrace{C_{cd}(T) \frac{\partial T}{\partial t}}_{\text{Storage}} = \underbrace{\nabla \cdot [k_{cd}(T) \nabla T]}_{\text{Conduction}} + \underbrace{\rho_{cd}(T) J_{cd_o}^2(t)}_{\text{Joule heating}} + \underbrace{g_d(t)}_{\text{Disturbance}} - \underbrace{\left(\frac{f_p P_D}{A_{cd}} \right)}_{\text{Cooling}} g_q(T)$$

Compute T_f under adiabatic condition & other assumptions

$$A_{cd} C_{cd}(T) \frac{dT}{dt} = \frac{\rho_m(T)}{A_m} I_{op}^2(t) \quad [\text{W/m}]$$

$$I_{op}/A_m = J_{m_o} \quad C_{sc}(T) \approx C_{\bar{m}}(T) \approx C_m(T) \quad \gamma_{m/s} \equiv A_m / (A_{sc} + A_{\bar{m}})$$

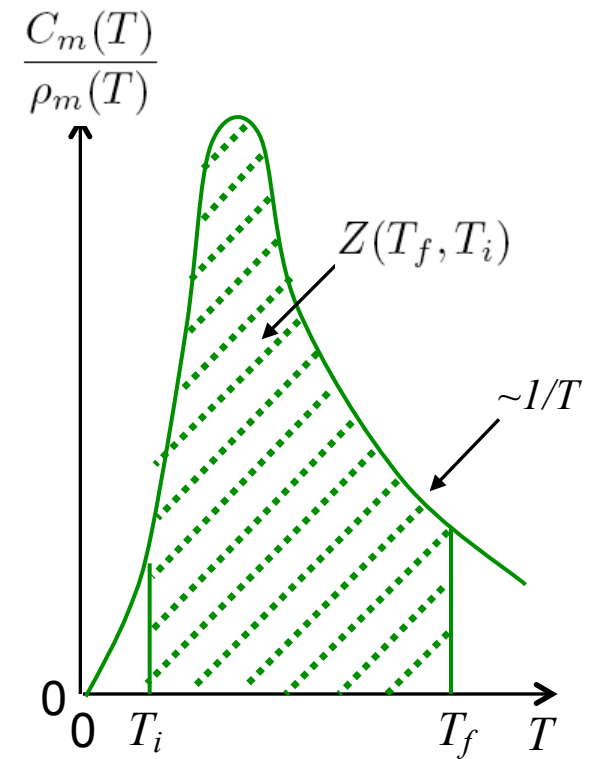
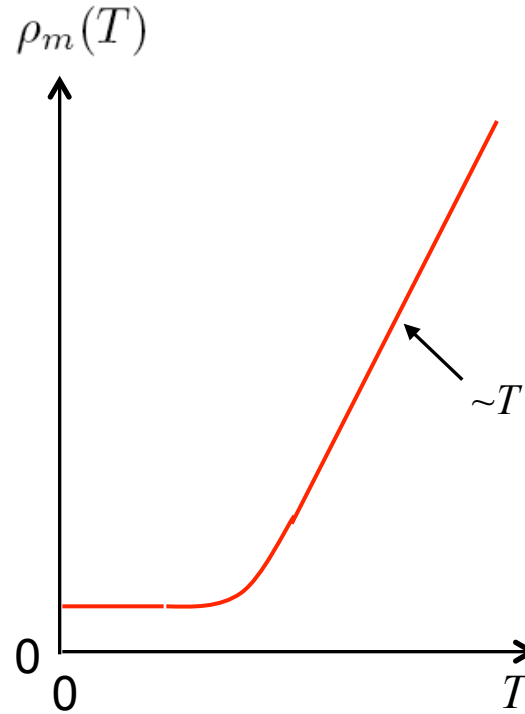
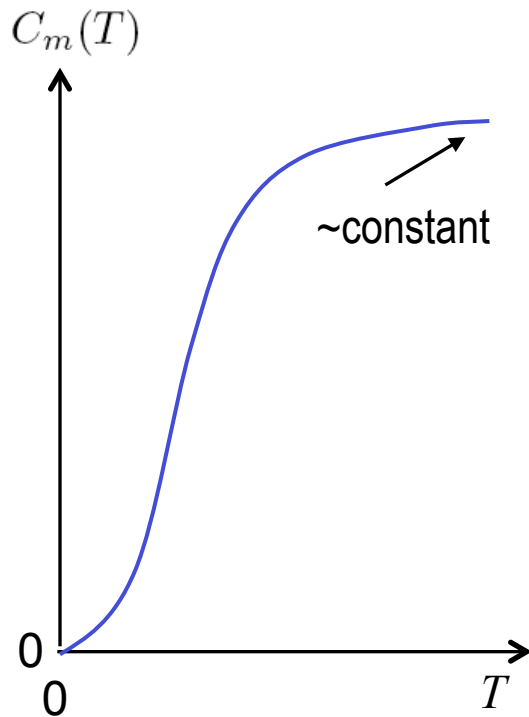
$$C_m(T) \frac{dT}{dt} = \left(\frac{A_m}{A_{cd}} \right) \rho_m(T) J_{m_o}^2 = \left(\frac{\gamma_{m/s}}{1 + \gamma_{m/s}} \right) \rho_m(T) J_{m_o}^2$$

$$\int_{T_i}^{T_f} \frac{C_m(T)}{\rho_m(T)} dT = \left(\frac{A_m}{A_{cd}} \right) J_{m_o}^2 \tau_{ah} = \left(\frac{\gamma_{m/s}}{1 + \gamma_{m/s}} \right) J_{m_o}^2 \tau_{ah}$$

Hot-Spot Temperature

Z Function

$$Z(T_f, T_i) \equiv \int_{T_i}^{T_f} \frac{C_m(T)}{\rho_m(T)} dT$$



Hot-Spot Temperature (continuation)

- For a given combination of T_i (e.g., 4.2 K) & T_f (e.g., 200 K), and matrix material (e.g., copper of RRR100), $Z(T_f, T_i)$ is determined:

$$Z(200 \text{ K}, 4.2 \text{ K}) = 12.5 \times 10^{16} \text{ A}^2 \text{ s/m}^4$$

- Then for a given $\gamma_{m/s}$ the product $J_{m_0}^2 \tau_{ah}$ is fixed

Example 1

$$\gamma_{m/s} = 1$$

$$J_{m_0} = 100 \text{ A/mm}^2 = 10^8 \text{ A/m}^2$$

$$\tau_{ah} = 25 \text{ s} \Rightarrow \text{plenty of time}$$

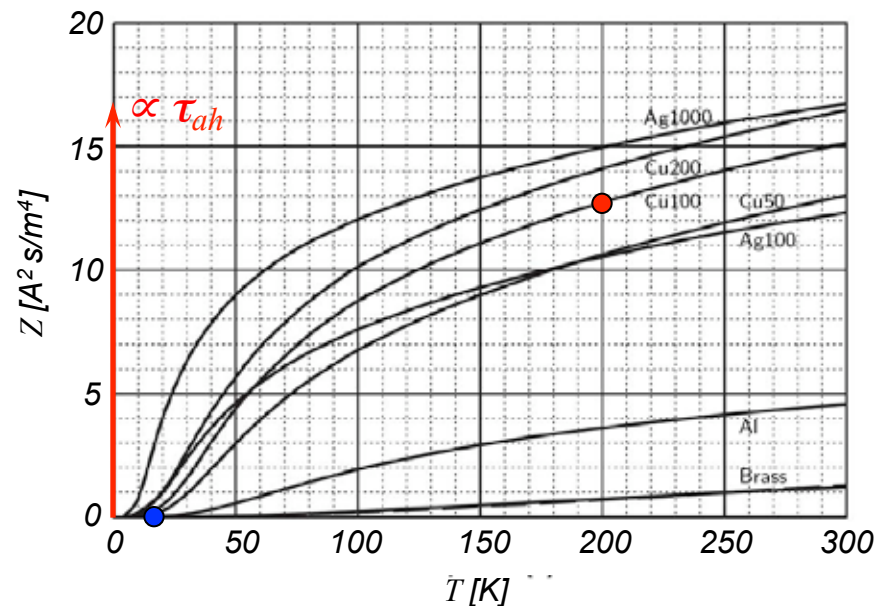
Example 2

$$\gamma_{m/s} = 1$$

$$J_{m_0} = 1000 \text{ A/mm}^2 = 10^9 \text{ A/m}^2$$

$$\tau_{ah} = 250 \text{ ms} \Rightarrow \text{too short}$$

$$Z(T_f, T_i) \equiv \int_{T_i}^{T_f} \frac{C_m(T)}{\rho_m(T)} dT = \left(\frac{\gamma_{m/s}}{1 + \gamma_{m/s}} \right) J_{m_0}^2 \tau_{ah}$$



Active Protection

Generally applied to “large” magnets, mostly driven, but also isolated (persistent-mode)

Active Protection Techniques

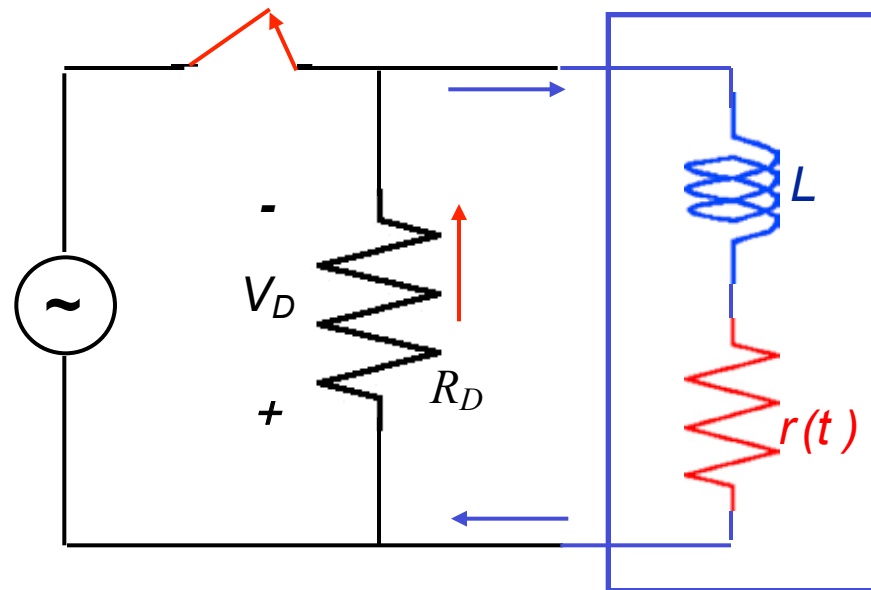
- Detect-and-Dump
- Detect-and-Activate-the-Heater or *Detect-and-Heat*

Key Issues

- Quench detection
- Time delays

Detect-and-Dump

- Dissipates most of the stored magnet energy into a “dump resistor” R_D
- **Hot spot** heated only for a “brief” period
- Leads to another criterion for operating current density



Detect-and-Dump

J_m criterion from Detect-and-Dump protection

$$J_{m_0}^D = \frac{A_{cd} V_D Z(T_f, T_i)}{E_m}$$

This J_m criterion is *different* from Stekly cryostability

Let us estimate $J_{m_0}^D$ for ITER TF magnet

$$V_D \approx 25 \text{ kV}; E_m = 41 \text{ GJ}; A_{cd} \approx 25 \text{ cm}^2 = 0.0025 \text{ m}^2;$$

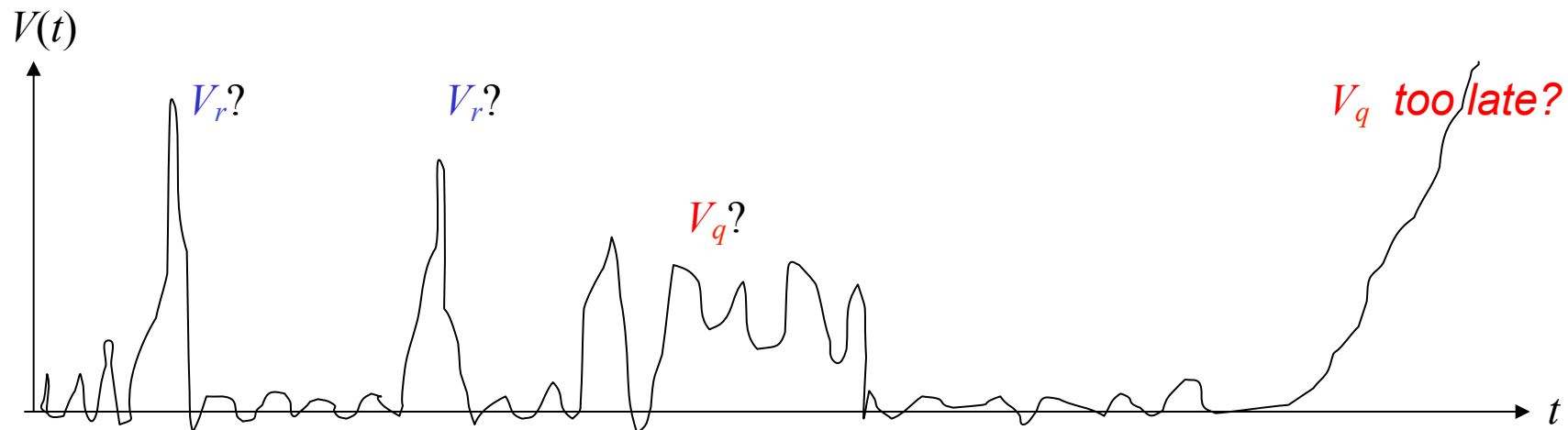
$$Z(200 \text{ K}, 4.2 \text{ K}) = 14 \times 10^{16} \text{ A}^2 \text{ s/m}^4:$$

$$J_{m_0}^D \approx 2 \times 10^8 \text{ A/m}^2 = 200 \text{ A/mm}^2 \quad \Rightarrow \text{reasonable(?)}$$

Quench Detection

Voltage

- Most directly related to a quench; quickest detection
- Often difficult to distinguish between a *recovering-quench voltage*, V_r , (i.e., *no dump required*), and a *genuine quench voltage*, V_q (i.e., *dump required*)



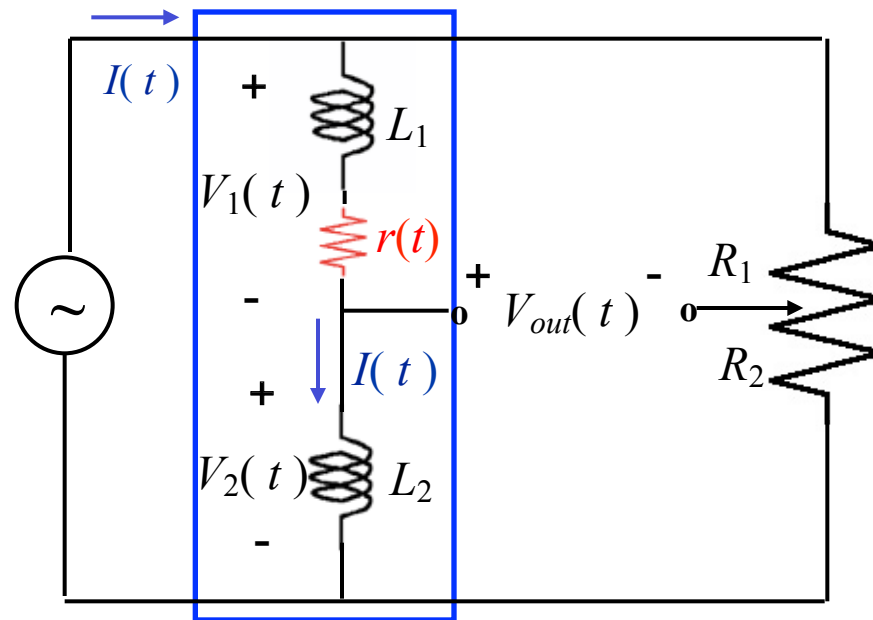
- Sometimes a criterion, $\int V(t) dt > \text{threshold value}$, used

Basics of Voltage Method

$$V_1(t) = L_1 \frac{dI(t)}{dt} + r(t)I(t) \quad V_2(t) = L_2 \frac{dI(t)}{dt}$$

$$V_{out}(t) = V_2(t) - V_1(t)$$

$$R_2 L_1 = R_1 L_1 \Rightarrow V_{out}(t) = - \left(\frac{R_2}{R_1 + R_2} \right) r(t) I(t)$$



A Critical Issue in Quench Detection for Detect-and-Dump

- Time delay, τ_{dl} , between Quench Initiation ($t = 0$) and Quench Detection, and finally opening of the Switch at ($t = \tau_{dl}$)

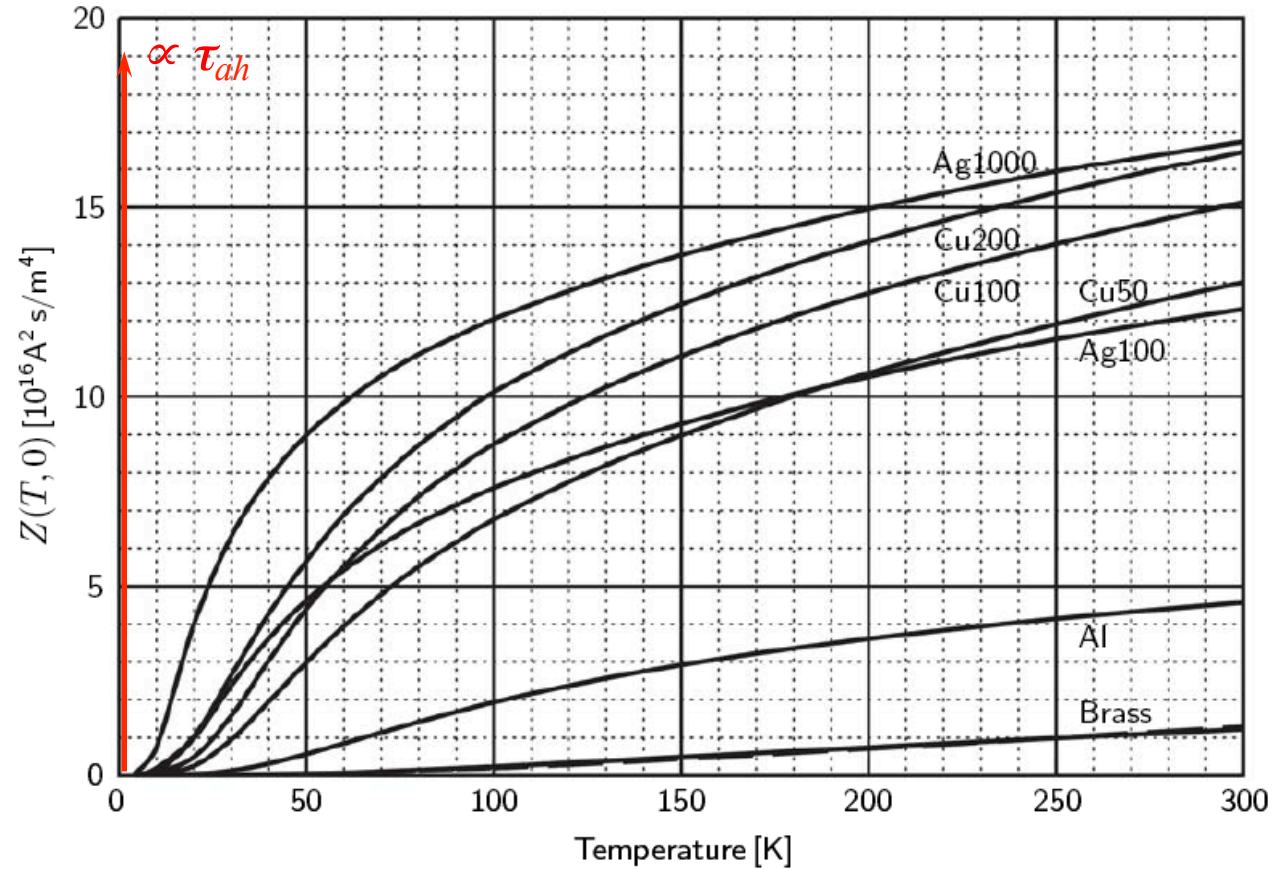
$$Z(T_f, T_i) = \left(\frac{A_m}{A_{cd}} \right) (J_{m_o}^2 \tau_{dl} + \frac{1}{2} J_{m_o}^2 \tau_{dg})$$

Constant-current heating

- The greater the time delay, the smaller will be the matrix current density
 \Rightarrow smaller $\lambda J \Rightarrow$ *less efficient magnet*

$t(T)$ from $Z(T)$ Function

$$Z(T) = \left(\frac{A_m}{A_{cd}}\right) J_{m_o}^2 \times t$$



$$t(T) - t(T_i) = \frac{Z(T, T_i)}{(A_m/A_{cd}) J_{m_o}^2} = \frac{Z(T, T_i) A_{cd}}{I_{op} J_{m_o}} \propto \frac{1}{J_{m_o}}$$

Lower the matrix current density, it takes longer to reach T

Quench Detection

Temperature

- T sensor must be at or vicinity of the *hot spot*
 - Otherwise, its response time may be “slow”

Pressure

- $T_{hot-spot}$ must reach LHe through “nonconductive” winding
 - Its response time may generally be “slow”
 - Not applicable to “dry” (no liquid) magnets

Neither a primary method but may complement V method

Quench Detection

Field

- *Mutual coupling effects* (more than one coil) may keep $B_{center} \cong \text{constnat}$ during the *critical initial* period

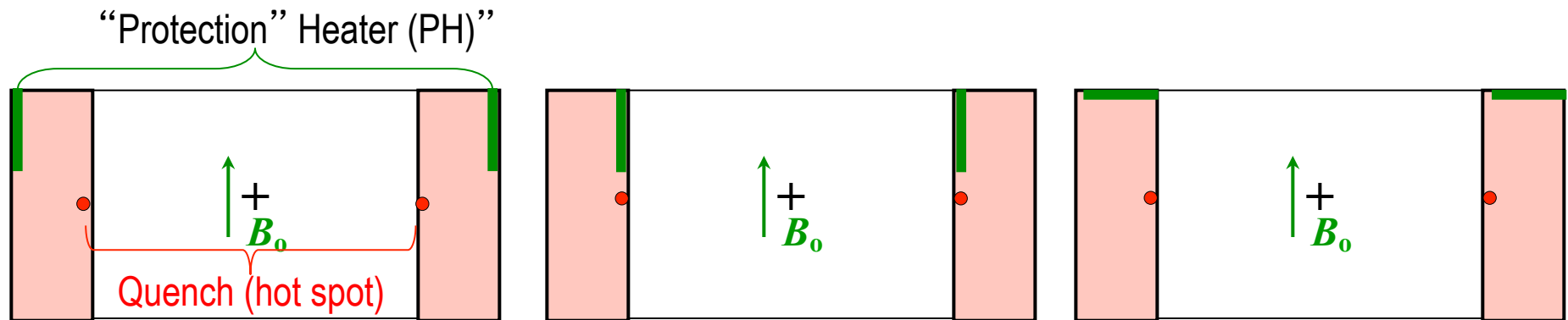
Current

- In a *driven-mode* magnet, the supply may keep $I_{op} \cong \text{constant}$ during the *critical initial* period
- In a *persistent-mode* magnet, the PCS may keep $I_{op} \cong \text{constant}$ during the *critical initial* period
 - Thus, the response time of each method may be “slow”

Neither a primary method but may complement V method

Detect-and-Heat (DAH)

- Activate a heater (“protection” heater) to drive the *minimum winding volume normal* to keep $T_f \leq \sim 300$ K
 - “Protection” heater needs not cover the entire winding
 - Heater size *independent* of the hot-spot size
- “Protection” heater location *not* critical
 - Place the heater at “convenient” locations



- DAH suitable for HTS magnets (slow NZP)
- Also, for “large” LTS magnets, e.g., NMR, dipoles

Conclusions

- Stability continues to be a critical issue for **LTS** magnets;
*Non-issue for **HTS** magnets*
- Protection well-established for **LTS** magnets;
*A huge challenge for **HTS** magnets*
 - NI (for “DC”) winding technique promising for **HTS** magnets
- Mechanical issue perhaps the greatest issue for high-field magnets,
LTS and **HTS**

Rendez-vous demain!