

Measurement of $B(B_{(s)}^0 \rightarrow \mu^+ \mu^-)$ at LHC(b)

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Seminar at CEA Saclay

Monday, January 6th 2014

*CERN

Outlines

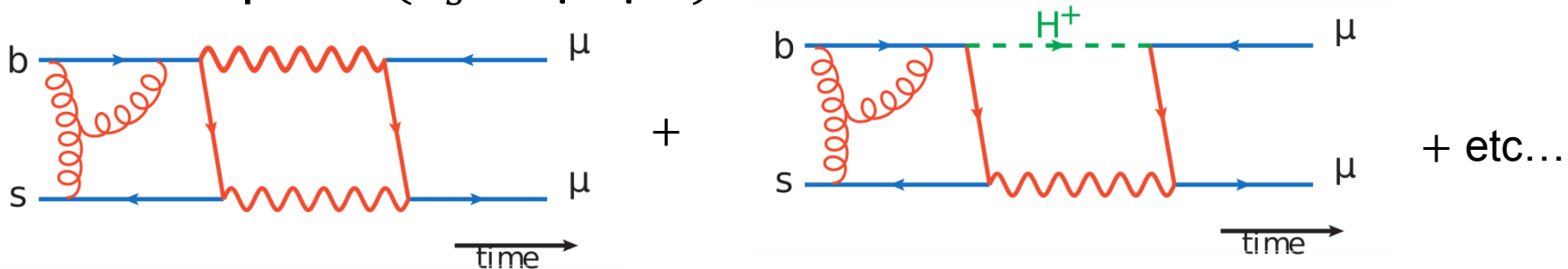
- Motivations to search for $B_{(s)}^0 \rightarrow \mu^+ \mu^-$
- Searching for $B_{(s)}^0 \rightarrow \mu^+ \mu^-$ at LHCb
- Combination with CMS
- Conclusions

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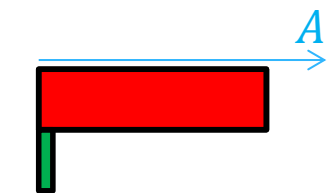
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Searching for NP with Flavour Physics

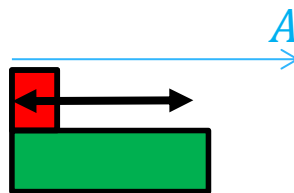
- Decay amplitude **sums SM and NP** (if any) contributions
- For example: $A(B_s^0 \rightarrow \mu^+ \mu^-) =$



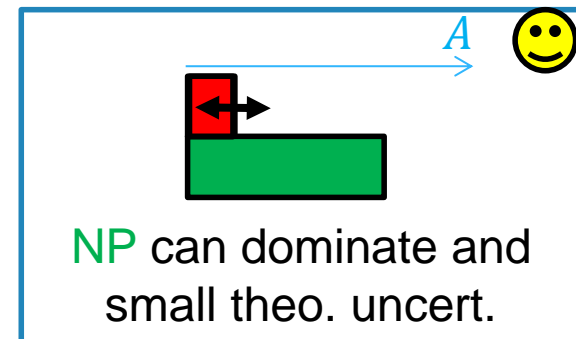
- Depending on the decay, several scenarios possible for A :



SM dominates



NP can dominate but
large theo. uncert.

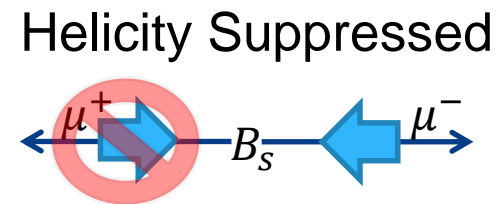


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- Golden channel = **rare decay in SM, precisely predicted**

The $B_{(s)}^0 \rightarrow \mu^+ \mu^-$ Case: Rare & Precise

- **Flavour Changing Neutral Current:**
 - No SM tree diagram, only higher order
 - Suppressed in SM
- Spin 0 weakly decaying into $\mu^+ \mu^-$:
 - **Helicity suppression** in SM $BR_{SM} \propto m_\mu$
- Main source of uncertainties: QCD
 - Here, **leptonic final** state and...
 - ...initial state **decay constant F_B well known:**
 F_B uncertainty strongly improved recently $20 \rightarrow 1.3\%^*$



Golden channel = **rare decay in SM, precisely predicted**

The $B_{(s)}^0 \rightarrow \mu^+ \mu^-$ Observables

- Simplest obs.: **untagged** time-integrated branching fraction:

$$BF = \frac{1}{2} \int dt \left[\Gamma(B_{(s)}^0(t) \rightarrow \mu^+ \mu^-) + \Gamma(\bar{B}_{(s)}^0(t) \rightarrow \mu^+ \mu^-) \right]$$

- Neutral B mesons oscillate in admixture of mass eigenstates:

$$\langle \Gamma(B_{(s)}^0(t) \rightarrow \mu^+ \mu^-) \rangle = R_H e^{-\Gamma_H^{(s)} t} + R_L e^{-\Gamma_L^{(s)} t}$$

- For $B^0 \rightarrow \mu^+ \mu^-$ the decay widths are similar, $\Gamma_H \sim \Gamma_L$ so:

$$\begin{aligned} BF(B^0 \rightarrow \mu^+ \mu^-) &= BF(B^0(t) \rightarrow \mu^+ \mu^-)_{t=0} \\ &= \frac{\tau_{B^0}}{2} (R_H + R_L) \end{aligned}$$

$$BF(B^0 \rightarrow \mu^+ \mu^-) \stackrel{\text{SM}}{=} \mathbf{1.07 \pm 0.10 \times 10^{-10}}$$

- For $B_s^0 \rightarrow \mu^+ \mu^-$ the decay widths are different, $\Gamma_H^S \neq \Gamma_L^S$, hence:

$$BF(B_s^0 \rightarrow \mu^+ \mu^-) = \underbrace{\frac{\tau_{B_s^0}}{2} (R_H + R_L)}_{BF(B_s^0(t) \rightarrow \mu^+ \mu^-)_{t=0}} \times \frac{1 + A_{\Delta\Gamma} y_s}{1 - y_s^2}$$

with:

$$A_{\Delta\Gamma} = \frac{R_H - R_L}{R_H + R_L} \in [-1; 1] \quad y_s = \frac{\Gamma_L - \Gamma_H}{\Gamma_L + \Gamma_H} \stackrel{\text{meas.}}{=} 0.0613 \pm 0.0059$$

- SM predictions


$$A_{\Delta\Gamma} \stackrel{\text{SM}}{=} 1$$

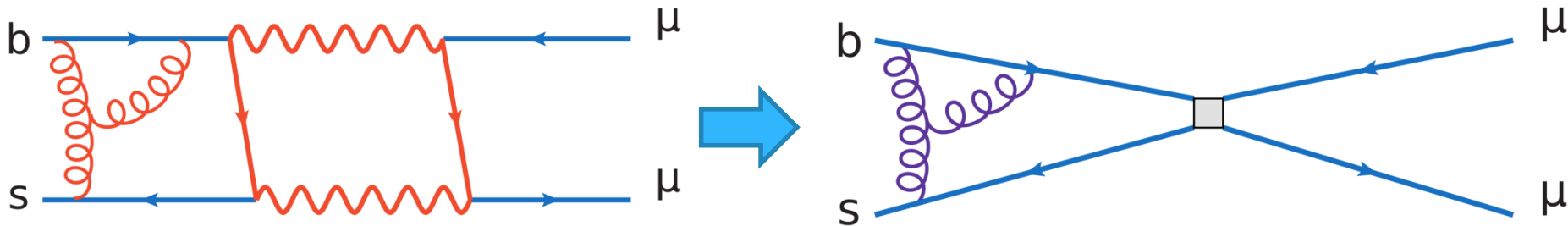
$$BF(B_s^0 \rightarrow \mu^+ \mu^-) \stackrel{\text{SM}}{=} 3.57 \pm 0.30 \times 10^{-9}$$

Uncertainty Budget	
F_{B_s}	72.5%
$ V_{tb}^* V_{ts} $	22.8%
m_t	3.7%
τ_{B_s} and y_s	1.1%

What About New Physics?

Model Independent Approach

- **Recall:** virtual particles are **off-shell**: $E^2 - p^2 \neq m_{shell}^2$
- Uncertainty principle, $\Delta t \propto 1 / \Delta E$: 
- **QCD** energy scale \ll **EW** energy scale, hence:



- **Energy scales separate** in amplitude expression:

$$A(I \rightarrow F) \propto \sum_i \langle F | Q_i | I \rangle \times C_i$$

Matrix elements:

- encode **low energy**


- Main source of uncertainty

Wilson coefficients:

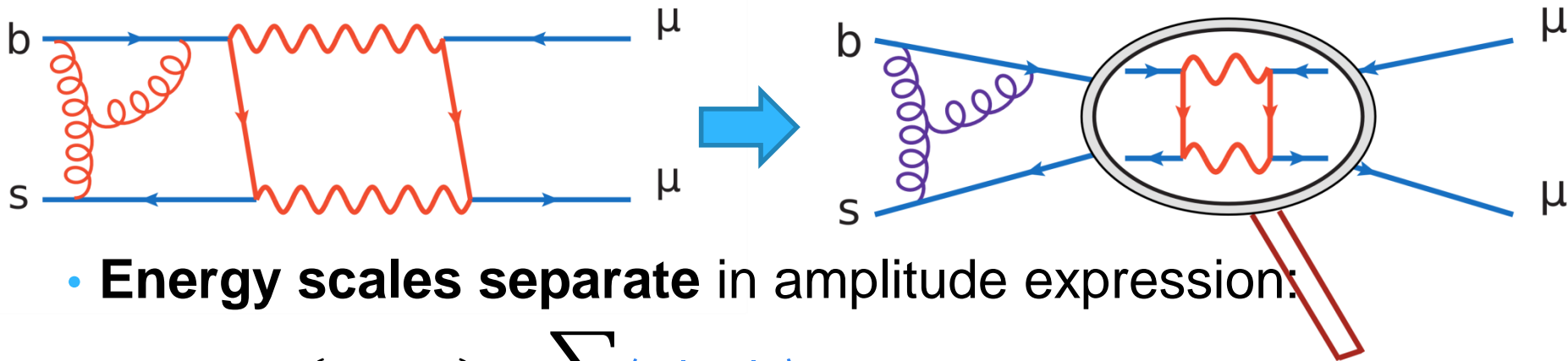
- 10 universal coefficients
- Encode **high energy**

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New Physics in $BF(B_{(s)}^0 \rightarrow \mu^+ \mu^-)_{t=0}$

$$BF(B_{(s)}^0(t) \rightarrow \mu^+ \mu^-)_{t=0}^*$$

$$\propto \left(1 - \frac{4m_\ell^2}{m_B^2}\right) |C_S - C'_S|^2 + \left| (C_P - C'_P) + 2 \frac{m_\mu}{m_B^2} (C_{10} - C'_{10}) \right|^2$$

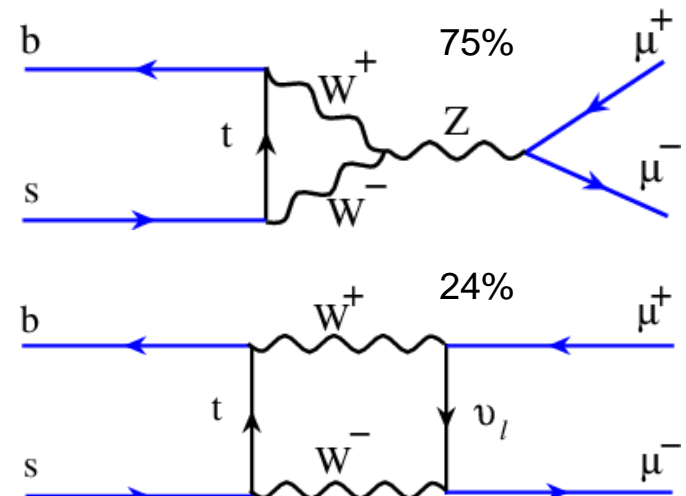
Helicity Supp.



Sensitive to (Pseudo-)Scalar NP

- Not affected by helicity supp.
- Scalar adds up with SM
- Pseudo-scalar can interfere destructively with SM

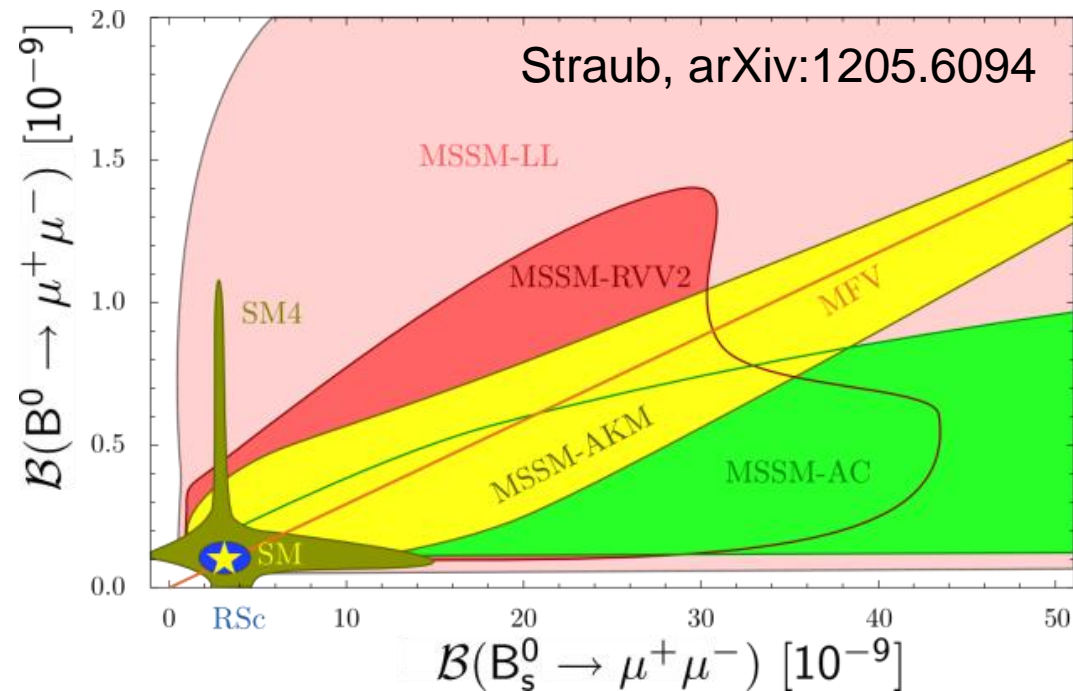
SM contributions:



* $A_{\Delta\Gamma}$ phenomenology not accounted for

Which Models are Probed?

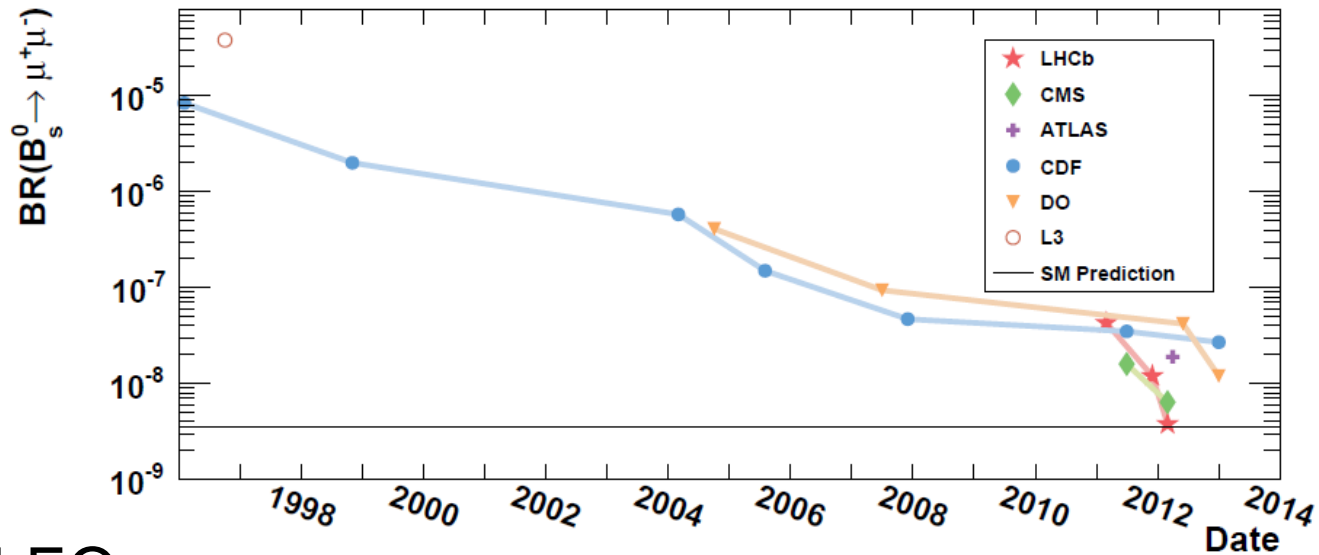
- $BF(B_s^0 \rightarrow \mu^+ \mu^-)$:
 - Models with extended Higgs sector, e.g SuperSymmetry with large $\tan \beta$ as $C_{S,P} \propto \tan^3 \beta$
 - Lepto-quarks
 - Z' models
- $BF(B^0 \rightarrow \mu^+ \mu^-)$:
 - MFV hypothesis
 - Fourth generation



Experimental Picture

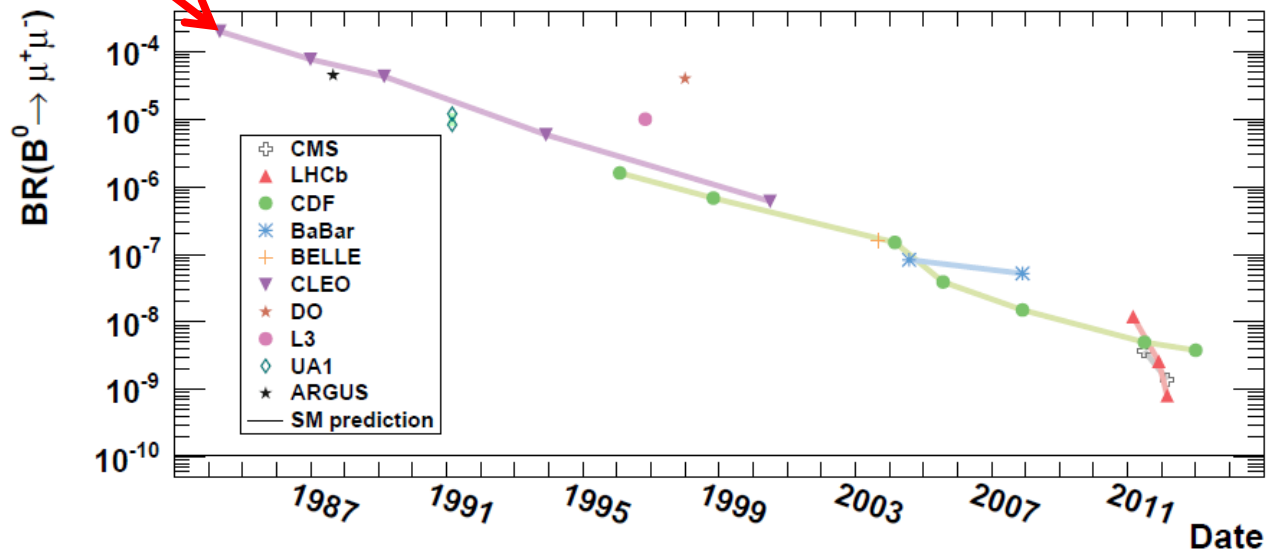
A long hunting...

90% C.L. Upper Limits



1984 CLEO

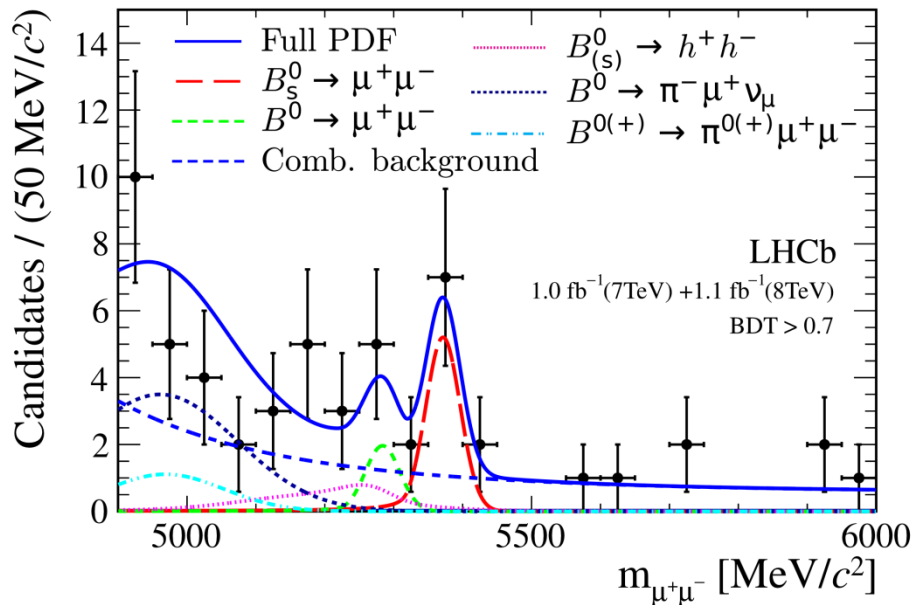
90% C.L. Upper Limits



...before the first evidence!

- Nov 2012 LHCb: First evidence with 1 (7 TeV) + 1 (8 TeV) fb^{-1}

PRL 110, 021801, 2013



$$B(B^0 \rightarrow \mu^+ \mu^-) < 9.4 \times 10^{-10} \text{ at } 95\% \text{CL}$$

$$B(B_s^0 \rightarrow \mu^+ \mu^-) = 3.2_{-1.2}^{+1.5} \times 10^{-9}$$

Significance of 3.5σ !

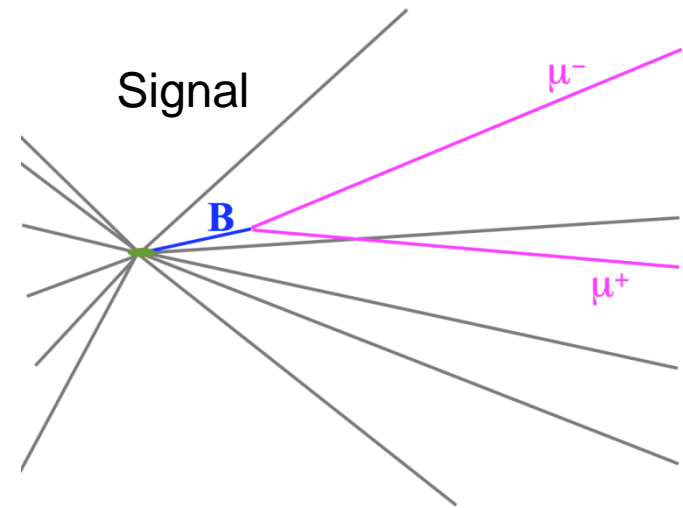
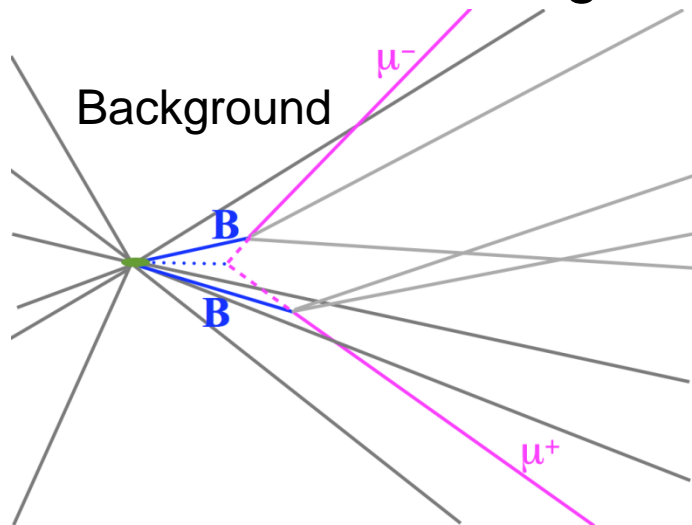
- **Today:** update with the **full dataset**: 1 (7 TeV) + 2 (8 TeV) fb^{-1}
- All data consistently **reprocessed**
- Data in $m(B_{(s)}^0) \pm 60 \text{ MeV}/c^2$ are **blind** til analysis completion.

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2 Key Points for $B_{(s)}^0 \rightarrow \mu^+ \mu^-$ with LHCb

1. **Production** of $B_{(s)}^0$ mesons: (x-section and trigger)
2. Separation **Signal/Background** (detector performance)
 - Combinatorial background: $b\bar{b} \rightarrow \mu\mu X$

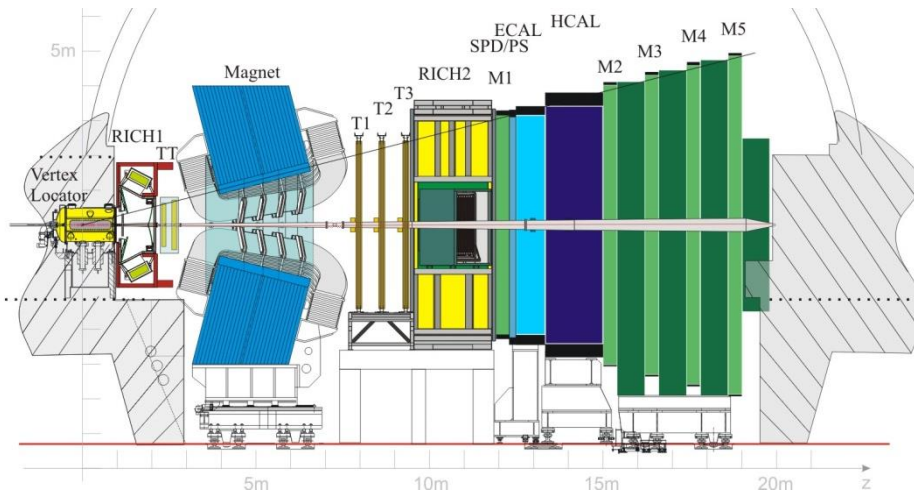
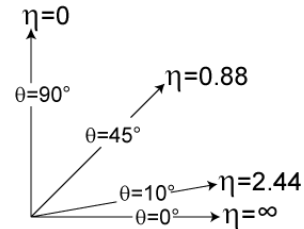


- Physical backgrounds:

e.g. $B \rightarrow K\pi, KK, \pi\pi$ where K, π decay in flight to μ

Key Point 1: $B_{(s)}^0$ production

- LHCb: a single arm forward spectrometer: $b\bar{b}$ are produced forward
- Instantaneous luminosity $4 \times 10^{32} \text{cm}^{-2} \text{s}^{-1}$



Exp.	Accept.	$\sigma_{b\bar{b}}$	$b\bar{b}$ pairs
ATLAS CMS	$ \eta < 2.2$	$\sim 75 \mu b$	$\sim 4 \times 10^{11}$
LHCb	$2 < \eta < 6$	$\sim 94 \mu b$	$\sim 9 \times 10^{10}$

Albrecht, arXiv:1207.4287

- Not all $p\bar{p}$ interactions produce B : $\sigma_{b\bar{b}} \approx 1\% \sigma_{tot}$
- Record only interesting events with a **trigger system**

Trigger

Trigger is a 2-level system:

- L0 Trigger:
 - Made with custom electronics
 - Use fast available sub-detectors information
 - Rate reduction: 40 MHz \rightarrow 1 MHz
- HLT Trigger
 - Software trigger
 - Refine selection based on partial reconstructions
 - Rate reduction : 1 MHz \rightarrow 2-6 kHz
- Trigger Efficiency for $B_s^0 \rightarrow \mu^+ \mu^-$: 90%

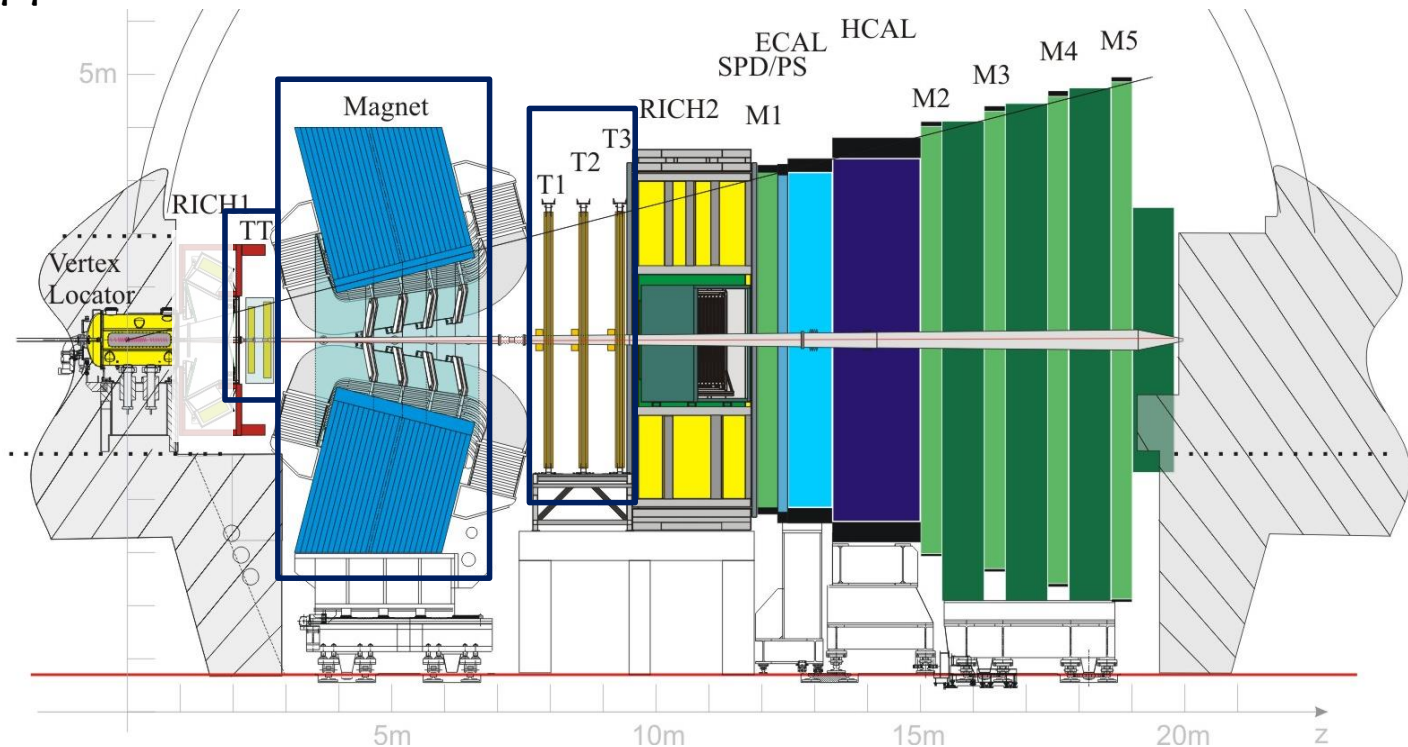
Key Point 2: Separation Sig/Bkg

Signal separated from combinatorial Bkg thanks to:

Mass and **momentum resolution** (magnet, tracking)

$$\frac{\delta p}{p} \sim 0.4 \rightarrow 0.6\% \text{ for } p = 5 \rightarrow 500 \text{ GeV}/c$$

$$\Delta m_{\mu\mu} \sim 25 \text{ MeV}/c^2 \text{ (2 [3-4] times better than CMS [ATLAS])}$$



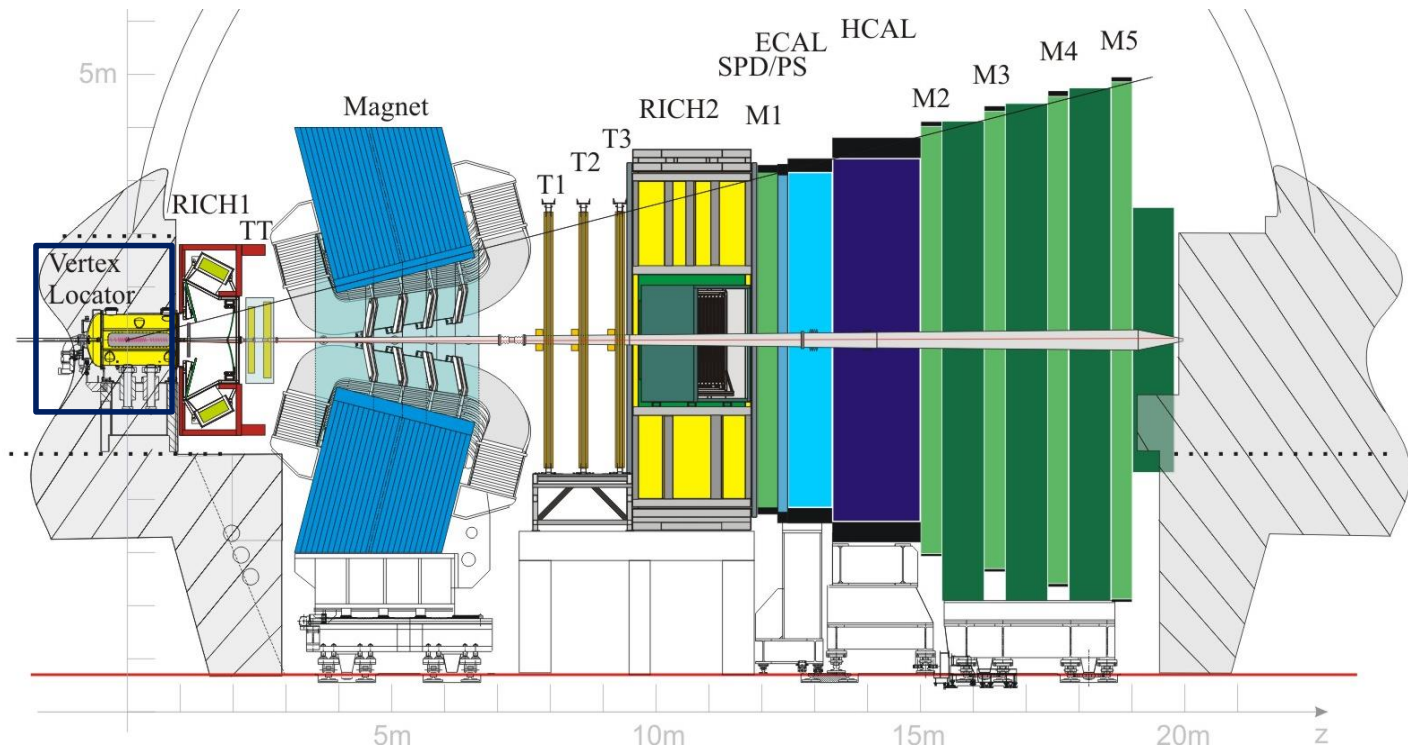
Key Point 2: Separation Sig/Bkg

Signal separated from combinatorial Bkg thanks to:

Secondary vertex resolution: (high boost and tracking)

B average flight distance 10 mm

$\sigma_{IP} = 25 \mu\text{m}$ at $p_t = 2 \text{ GeV}/c$



Key Point 2: Separation Sig/Bkg

Signal separated from physical Bkg thanks to:

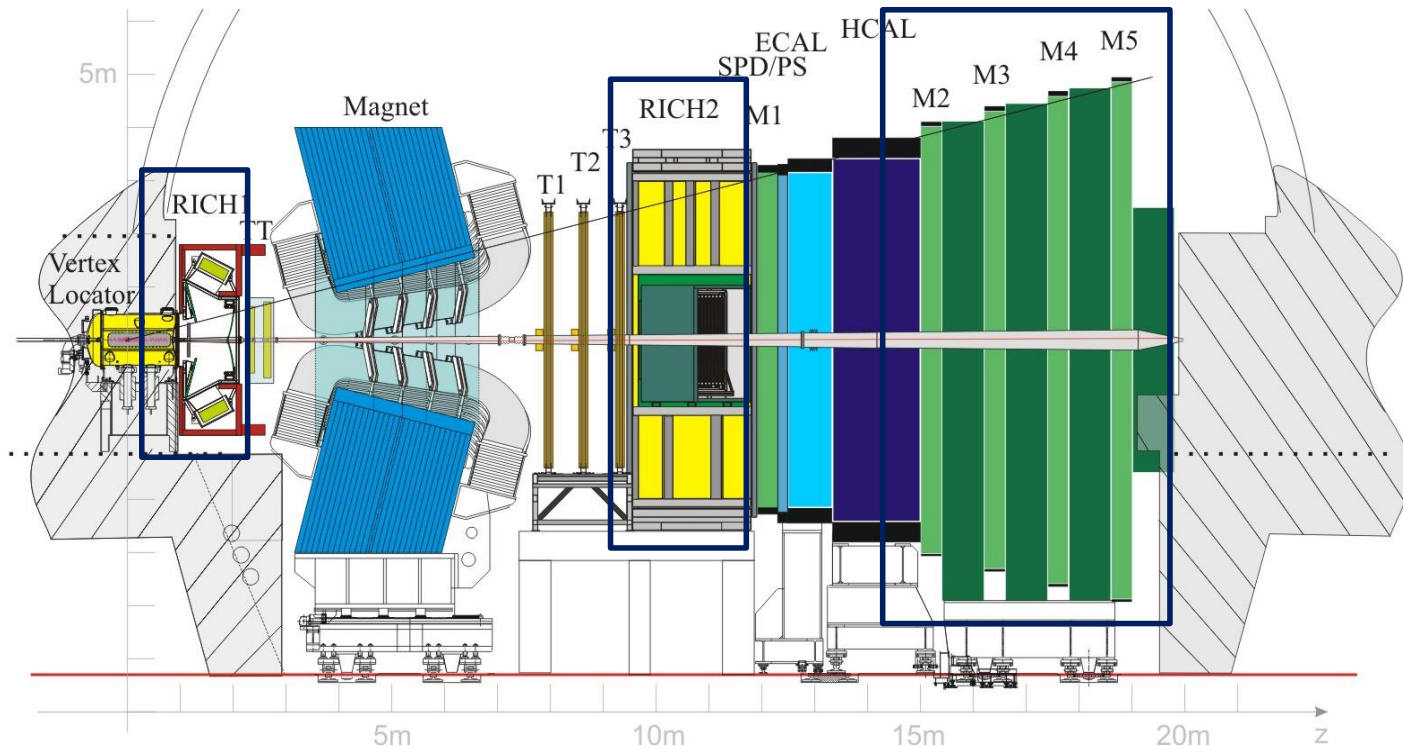
Particle identification info (RICH – muons chambers)

$$\epsilon(\mu \rightarrow \mu) \sim 98\%$$

$$\epsilon(K \rightarrow \mu) \sim 0.3\%$$

$$\epsilon(\pi \rightarrow \mu) \sim 0.6\%$$

$$\epsilon(p \rightarrow \mu) \sim 0.3\%$$



LHCb Analysis

Analysis Overview

- Answering the question:
 - Which BF is (in-)compatible with the observed data?**
- Observed data = $N(B_{(s)}^0 \rightarrow \mu^+ \mu^- + \mathbf{Bkg})$
 1. Increasing sensitivity:
 - Events **Selection and Classification** in categories
 2. Derive **Signal and Bkg expectations** from control channels
 3. Compare expectations with observation and infer about BF
 - **CLs method** and **Fitting** procedure if signal evidence

- **Data Set:**

2011	1.0 fb ⁻¹	7TeV	
2012	+1.1 fb ⁻¹	8TeV	PRL 110, 021801, 2013
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Selection and Classification

- After loose selection, classify evt based on $m_{\mu\mu}$ and geometry
- Train Boosted Decision Tree (BDT) to recognize signal from combinatorial background based on 12 geometrical variables

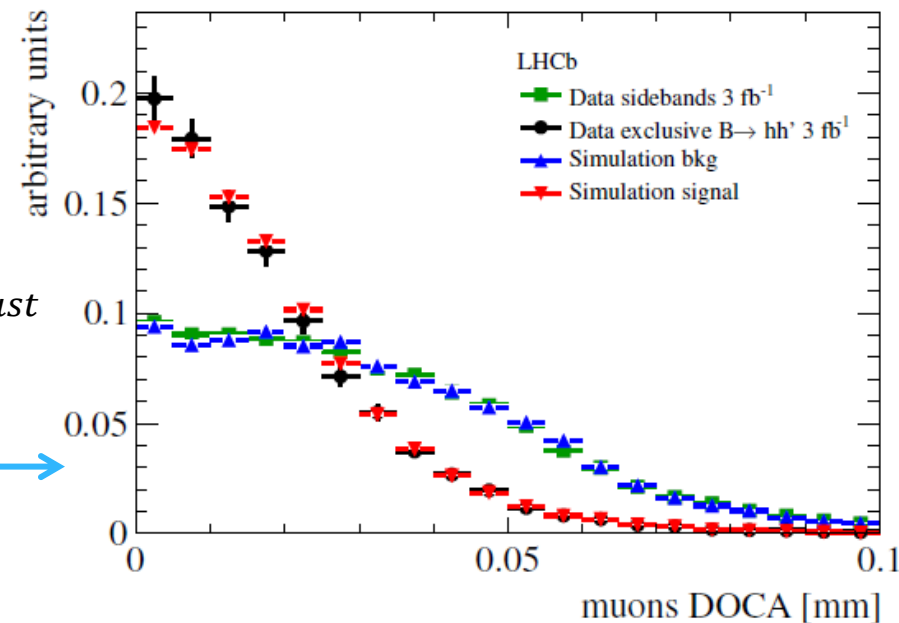
B candidate:

- proper time
- impact parameter
- transverse momentum
- B isolation
- Angle between \vec{p}_B and \vec{p}_{thrust}
- Angle in B rest frame between p_{μ^+} and \vec{p}_{thrust}

Muons:

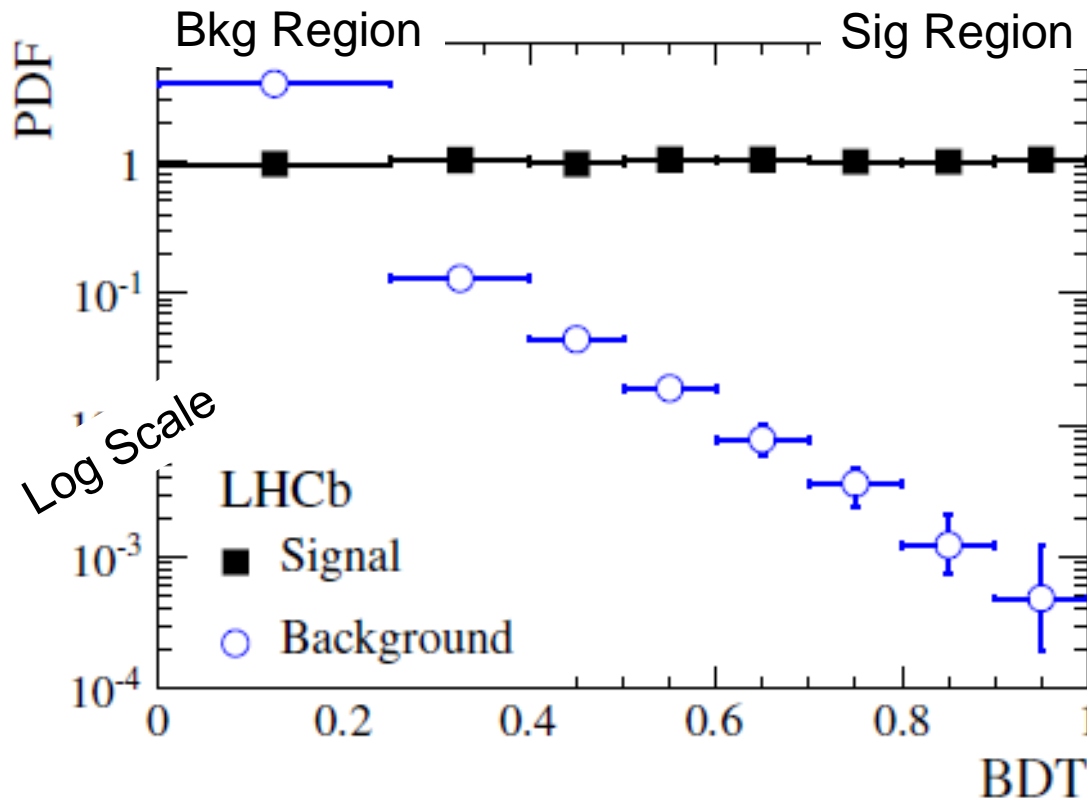
- min IP significance
- distance of closest approach
- muon isolation
- polarisation angle
- $|\eta(\mu_1) - \eta(\mu_2)|$
- $|\varphi(\mu_1) - \varphi(\mu_2)|$

\vec{p}_{thrust} is the sum of momenta of all tracks consistent with originating from the decay of the other b hadron

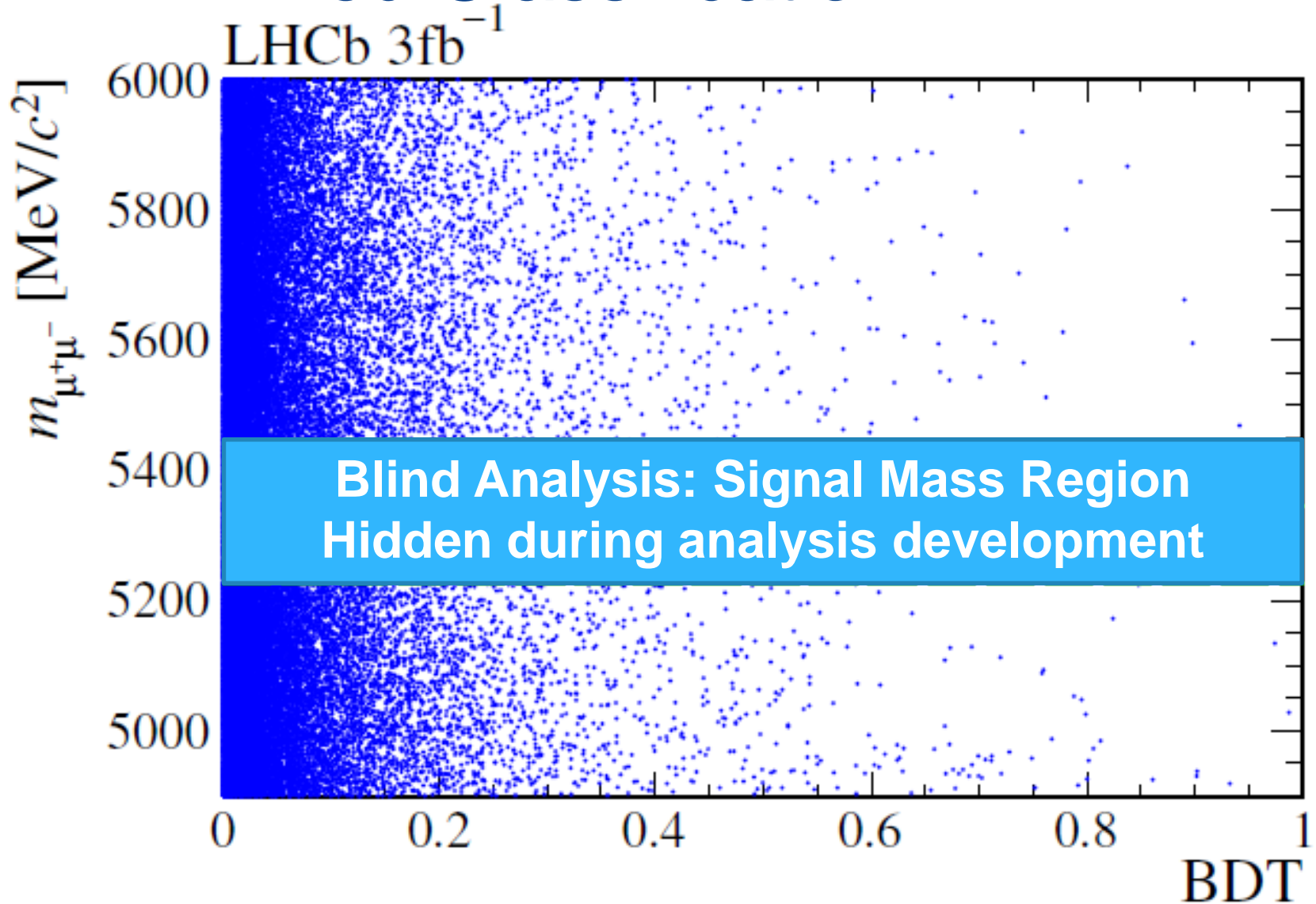


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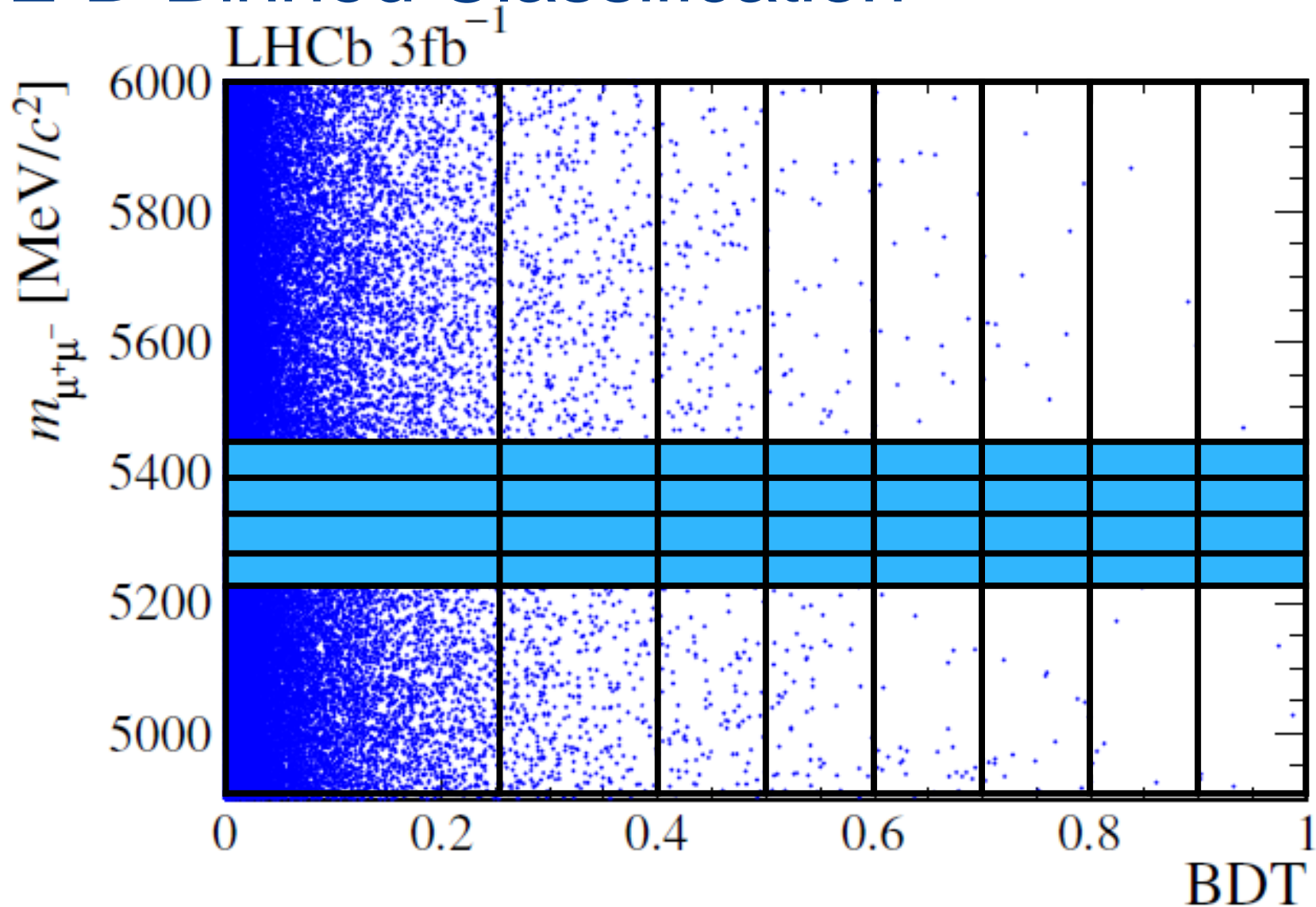
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Bkg Expectations

- Extrapolate Bkg from side-bands
- Fit components:

- Combinatorial
- MisId

$$B_s^0 \rightarrow h^+ h'^-$$

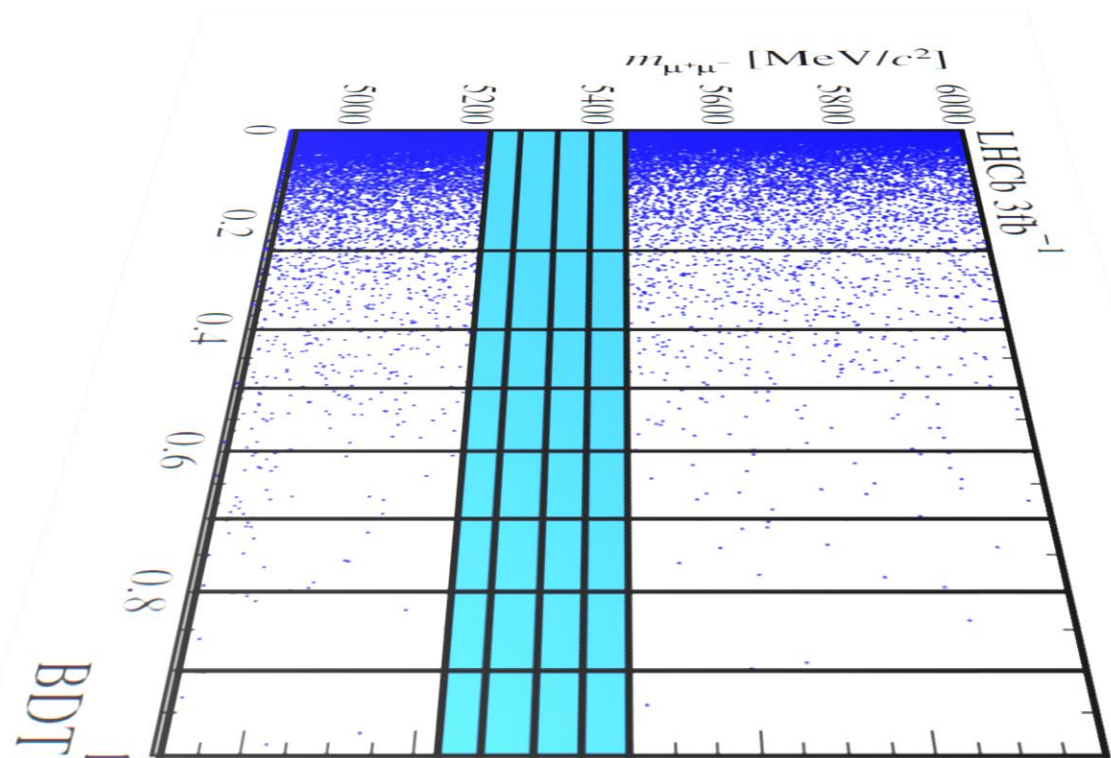
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- Partially Reco

$$B^{0,+} \rightarrow \pi^{0,+} \mu^+ \mu^-$$

$$\Lambda_b^0 \rightarrow p \mu^- \bar{\nu}_\mu$$

- Total



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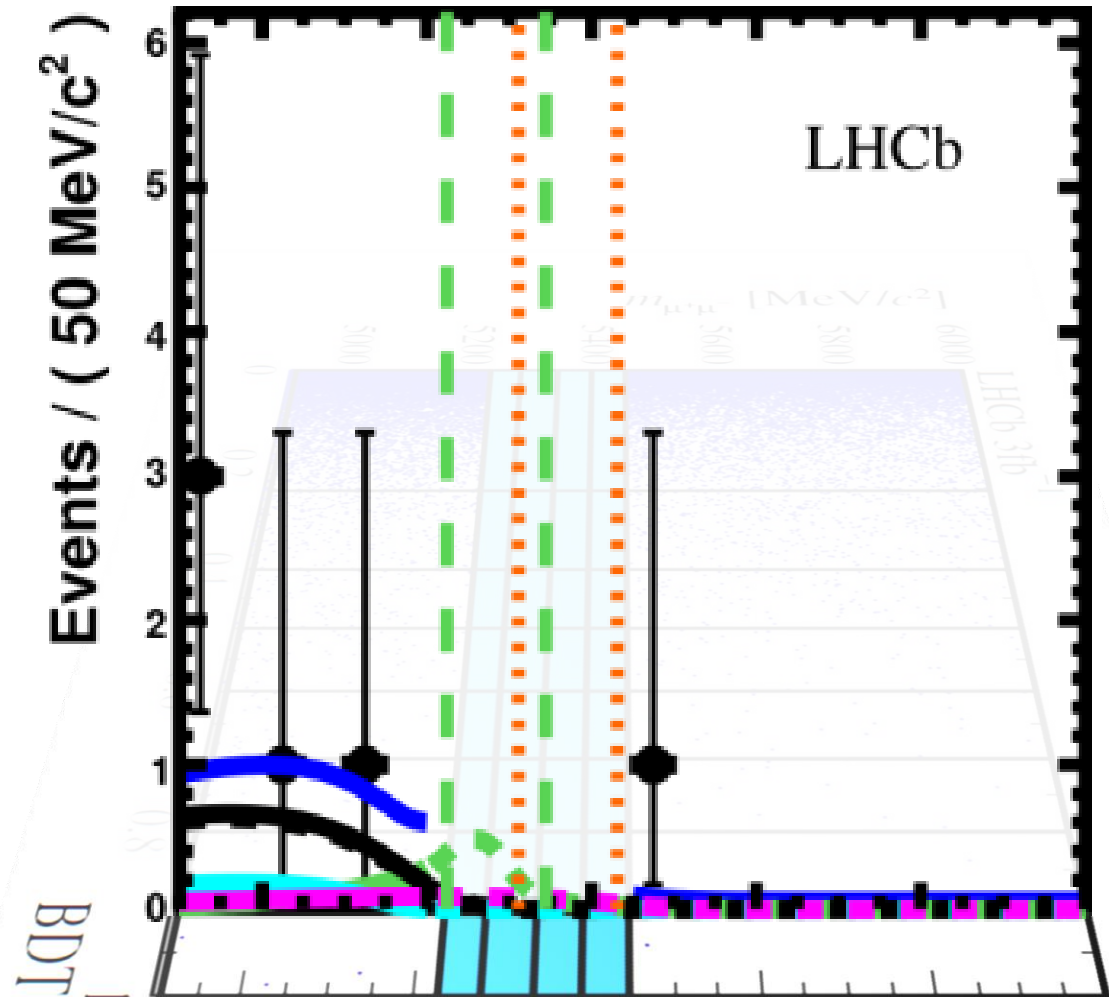
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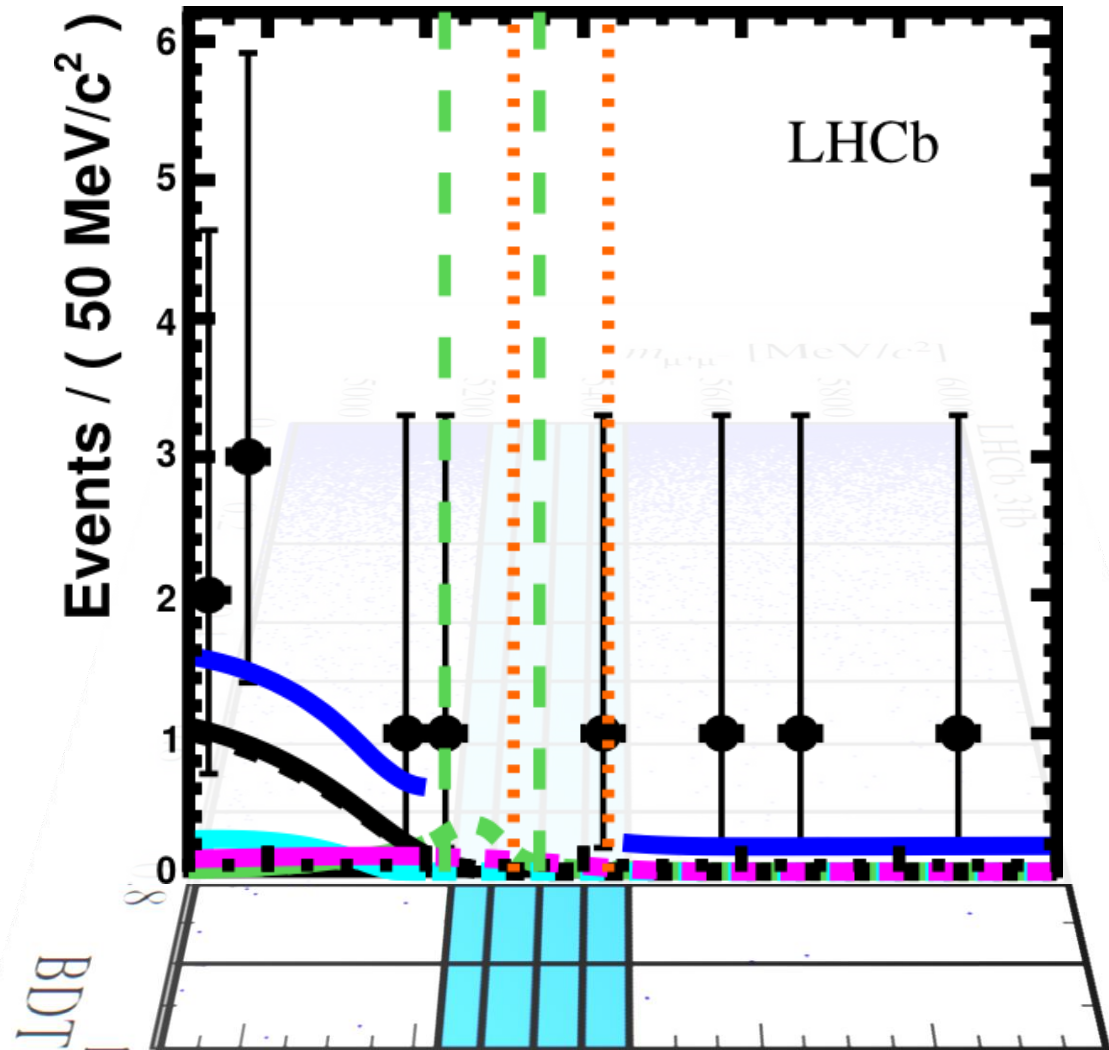
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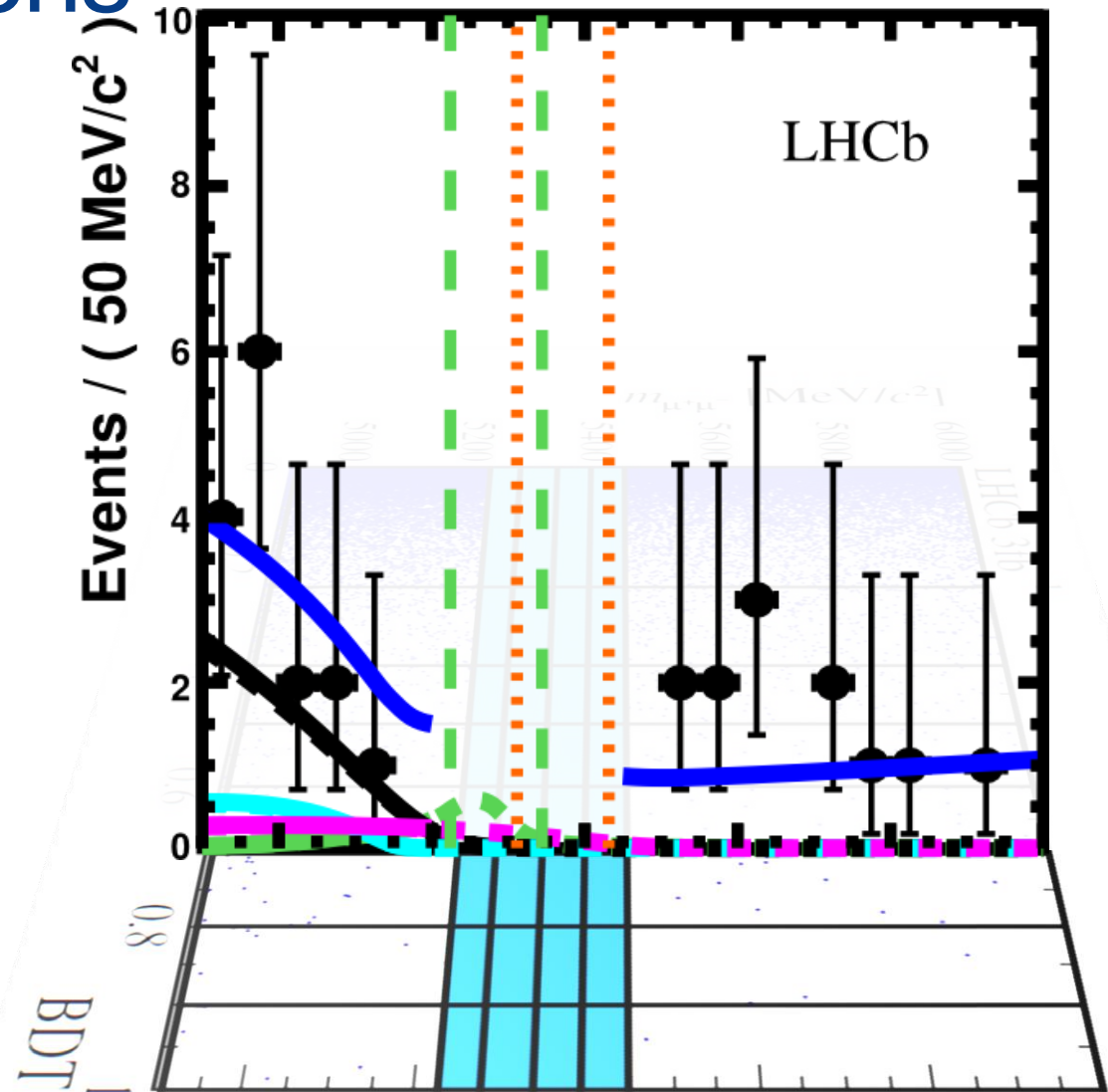
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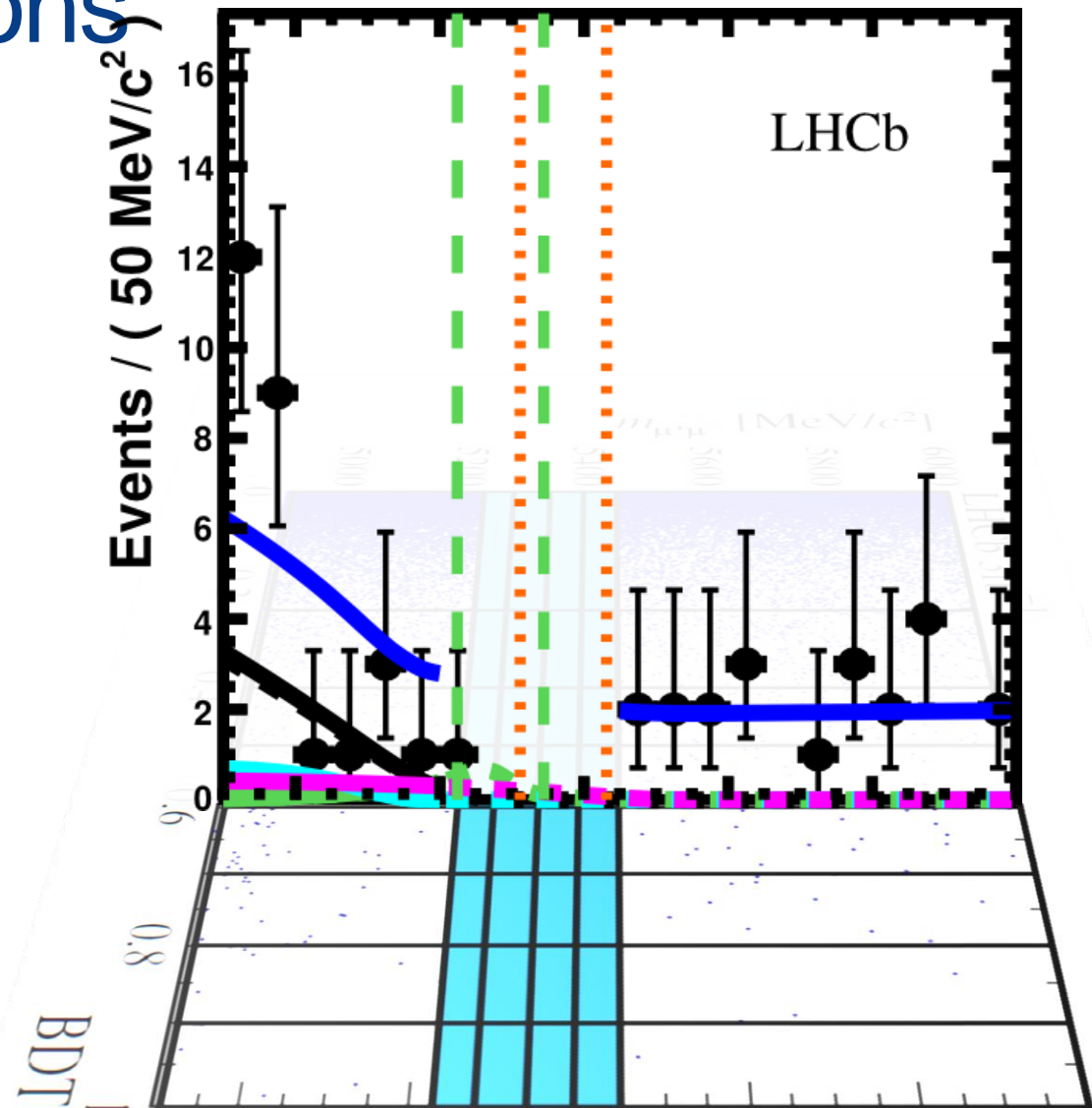
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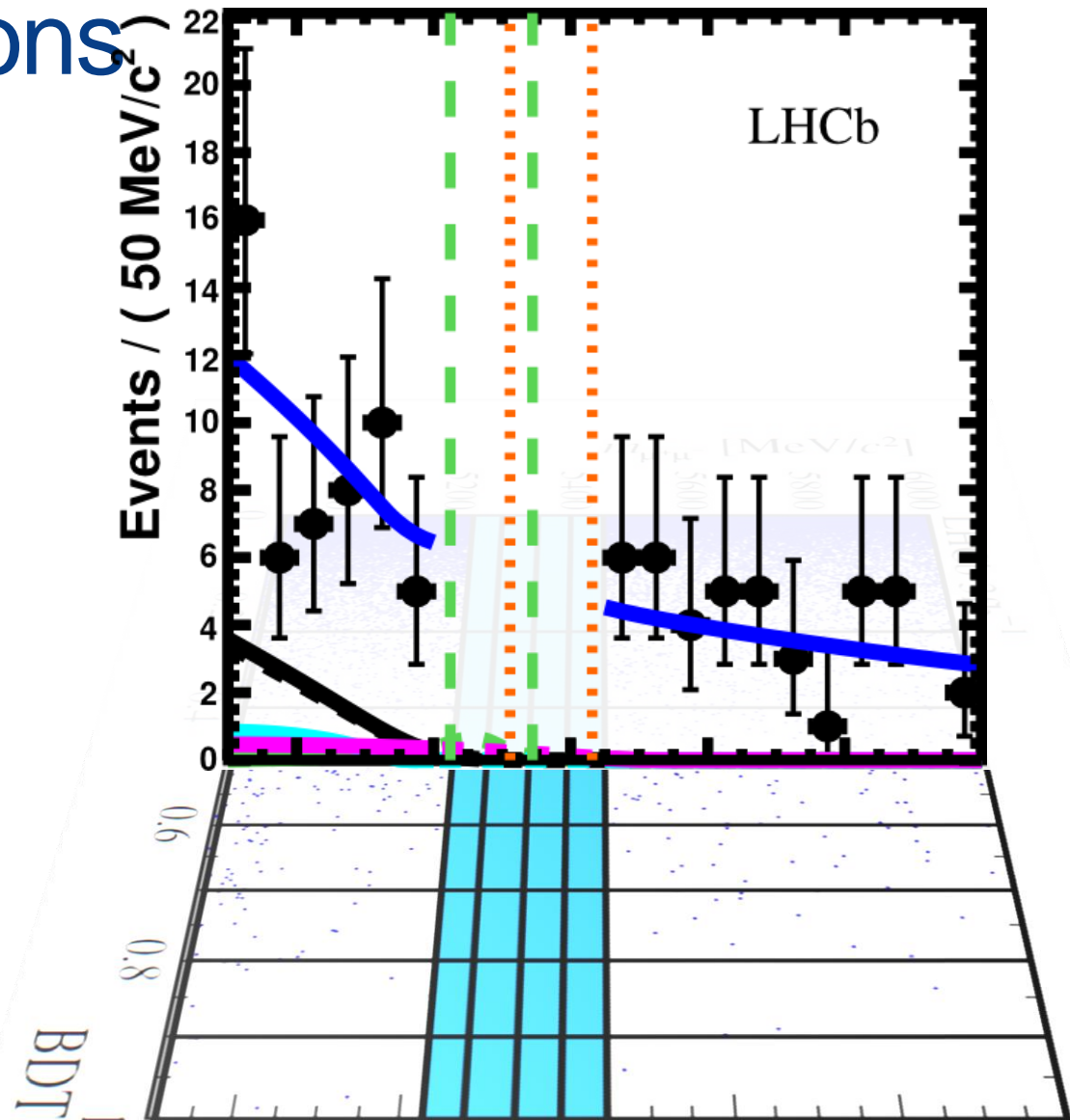
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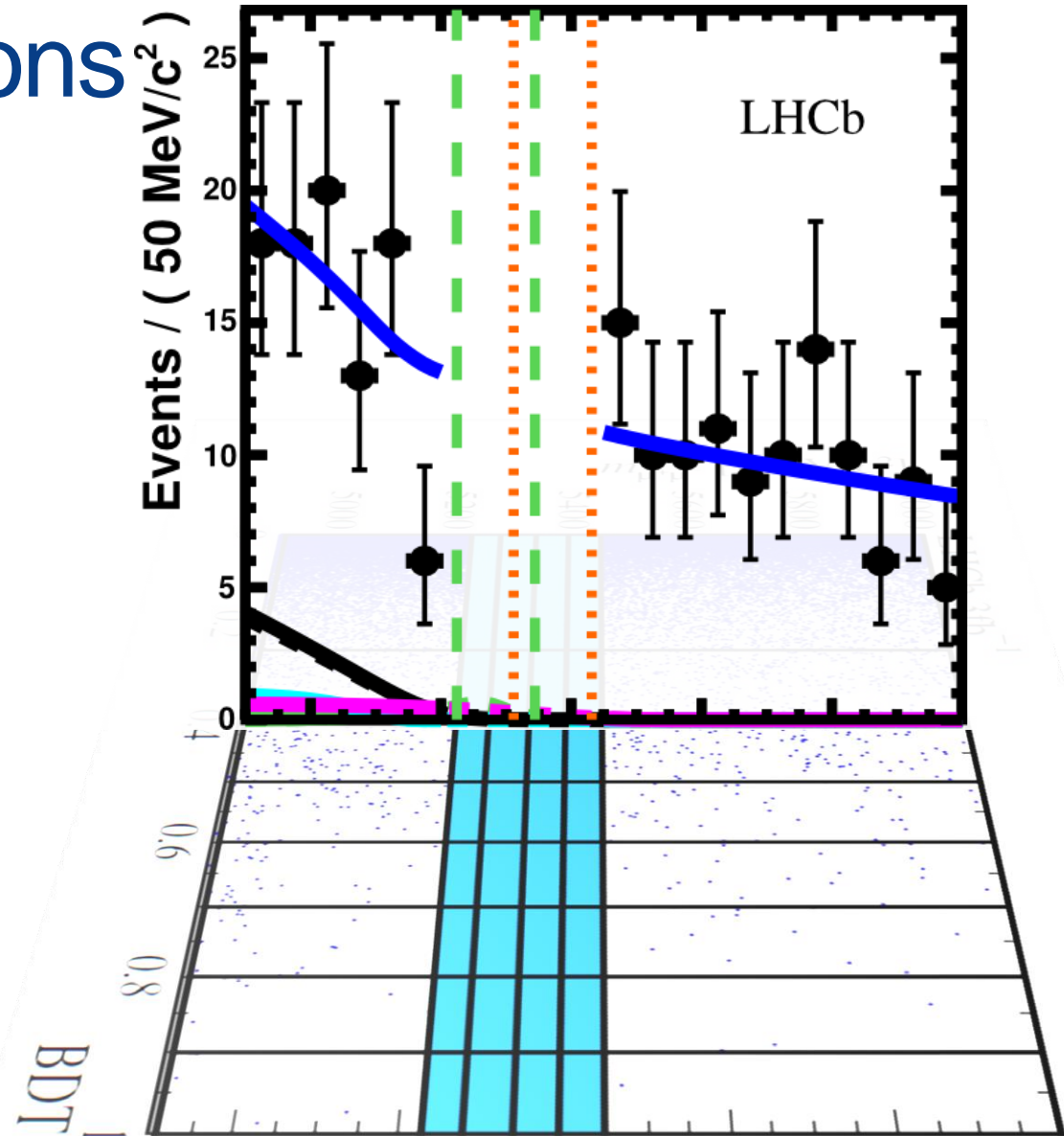
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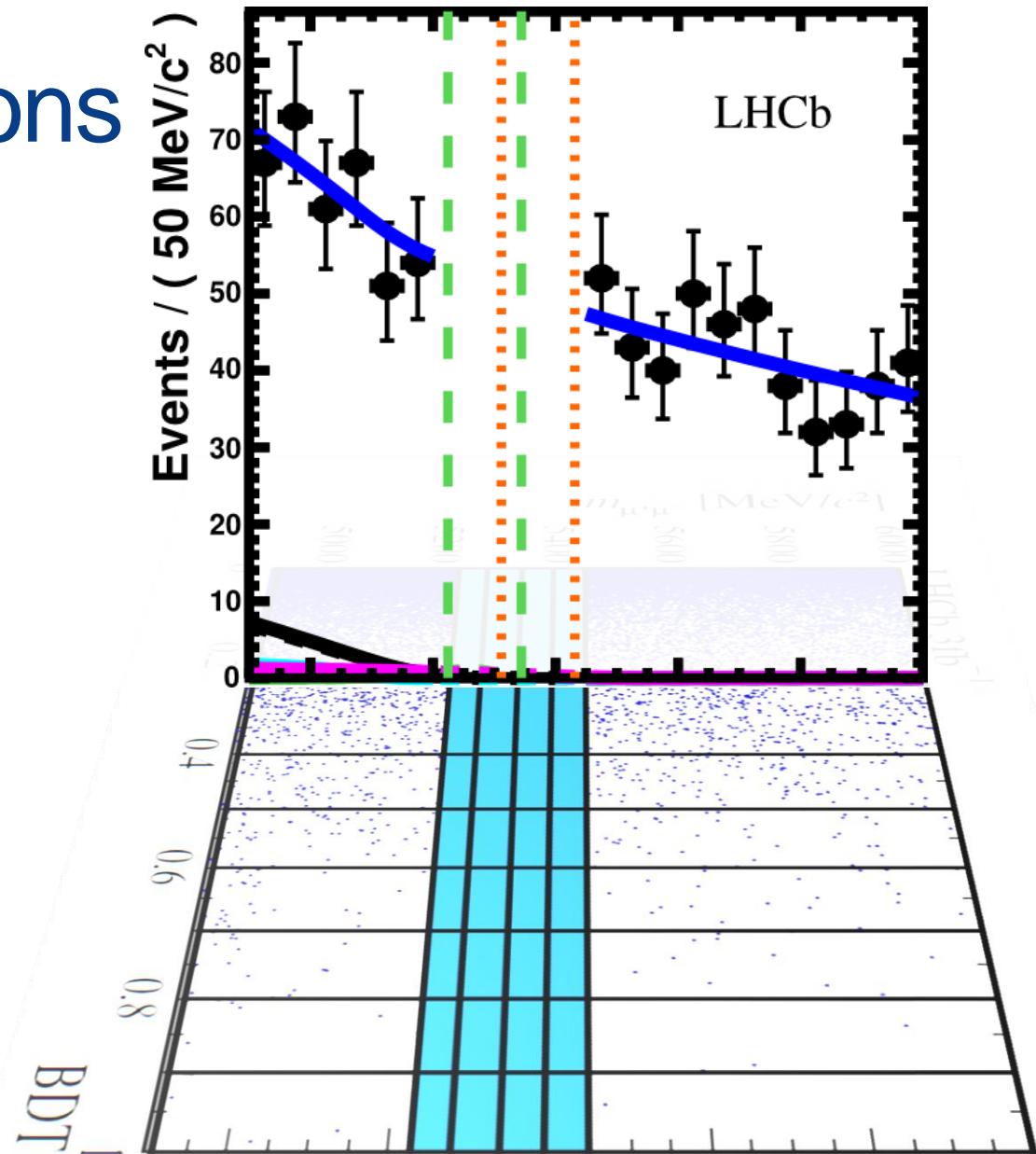
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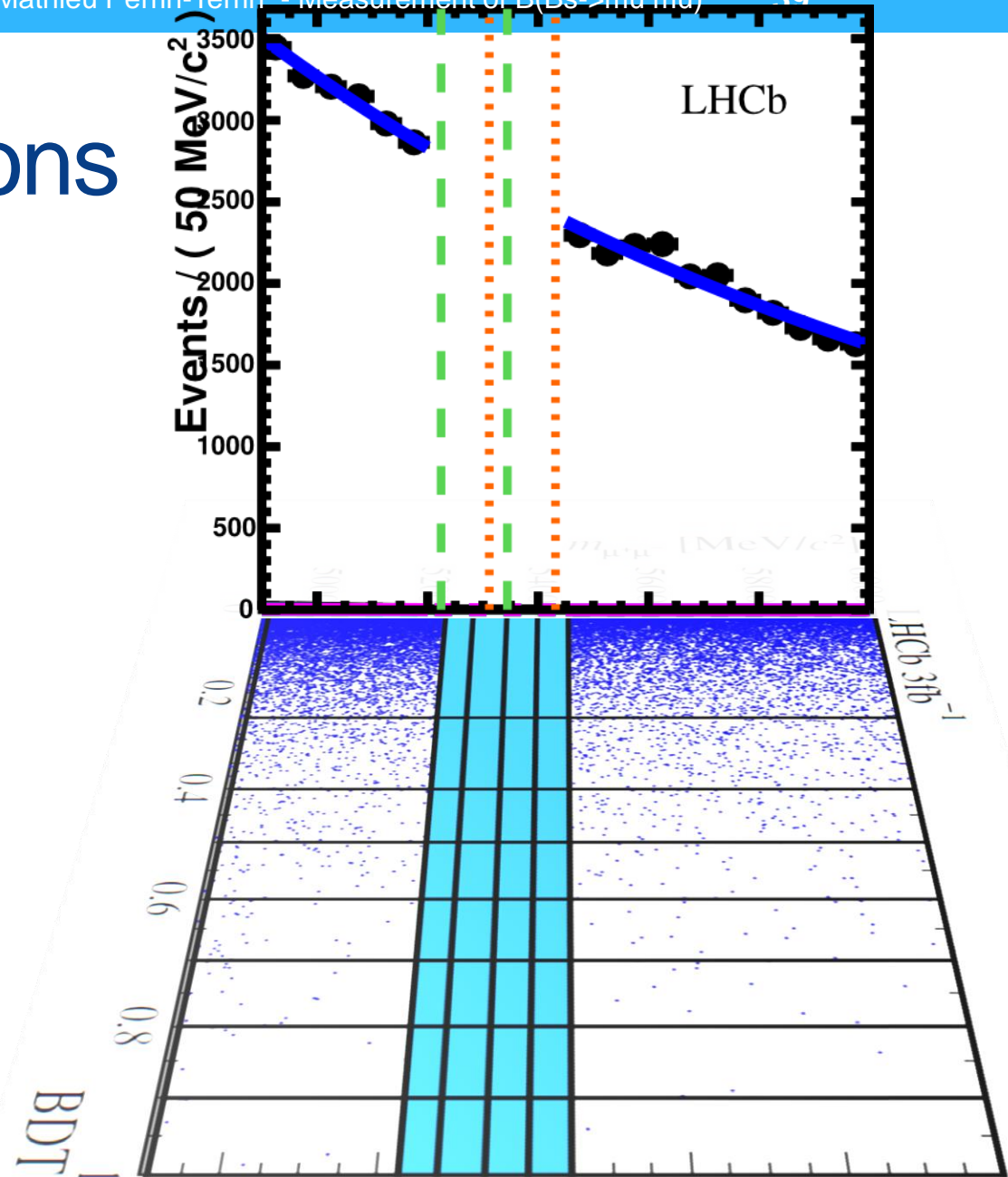
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Misidentified Backgrounds - $B_{(s)}^0 \rightarrow h^+ h'^-$

1. MisID probabilities measured on data **in bins of p and p_T**
 - $\pi \rightarrow \mu$ and $K \rightarrow \mu$ measured with $D^0 \rightarrow K^+ \pi^-$ from $D^{*+} \rightarrow D^0 \pi^+$,
 - $p \rightarrow \mu$ measured with $\Lambda \rightarrow p \pi^-$
2. Probabilities then convoluted with $B_{(s)}^0 \rightarrow h^+ h'^-$ MC spectra to get the average double misID efficiency $\epsilon_{\mu\mu \rightarrow hh}$ ($\sim 10^{-5}$)
3. Rate obtained applying $\epsilon_{\mu\mu \rightarrow hh}$ to the $B_{(s)}^0 \rightarrow h^+ h'^-$ yield
4. Mass shape is evaluated from MC
5. $B_{(s)}^0 \rightarrow h^+ h'^-$ **included as fit component with rate constrained to expected yield**

Other exclusive backgrounds

- Yields obtained by normalising to $B^+ \rightarrow J/\psi K^+$

	Yield in full BDT range	Fraction with BDT > 0.7 [%]
$B_{(s)}^0 \rightarrow h^+ h'^-$	15 ± 1	28
$B^0 \rightarrow \pi^- \mu^+ \nu_\mu$	115 ± 6	15
$B_s^0 \rightarrow K^- \mu^+ \nu_\mu$	10 ± 4	21
$B^{0(+)} \rightarrow \pi^{0(+)} \mu^+ \mu^-$	28 ± 8	15
$\Lambda_b^0 \rightarrow p \mu^- \bar{\nu}_\mu$	70 ± 30	11

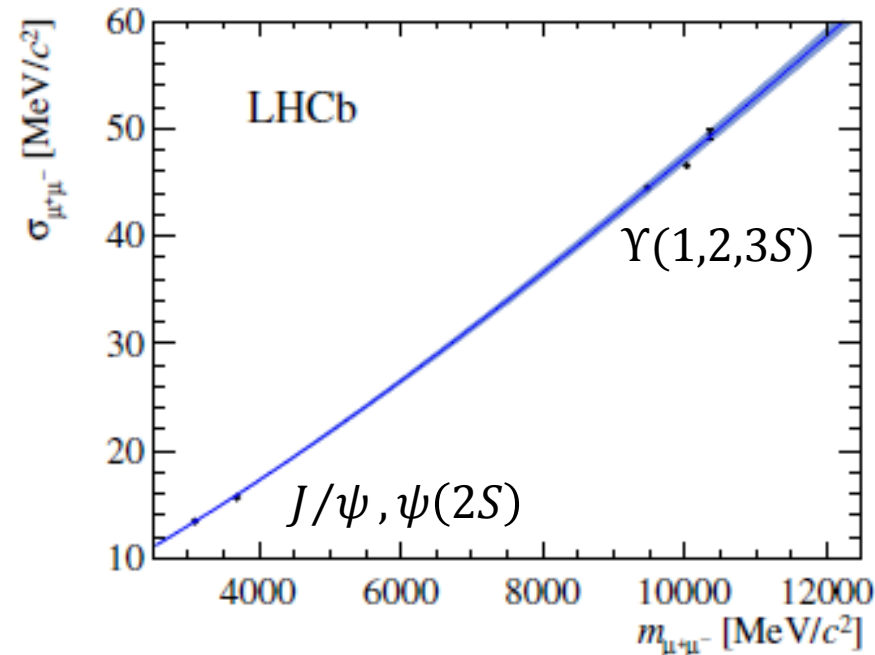
Expected background
yield in [4.9-6] GeV/c²

- $B^0 \rightarrow \pi, K^+ \mu^- \bar{\nu}_\mu$, $B^{0,+} \rightarrow \pi^{0,+} \mu^+ \mu^-$: included in fit
 - Mass PDF in each BDT bin determined from MC
 - normalization fixed to expected yield
- $\Lambda_b^0 \rightarrow p \mu^- \bar{\nu}_\mu$: treated as a systematic

Signal Expectations - PDF

BDT PDF:

- $B_{(s)}^0 \rightarrow h^+ h'^-$ same geometry as signal
- PDF by extracting yields with a $m_{\mu\mu}$ fit in each bin



Mass PDF, Crystal Ball

- **Mean** $B_{(s)}^0$ mass, from $B_{(s)}^0 \rightarrow h^+ h'^-$
- Mass **resolution**, from $J/\psi, \psi(2S), \Upsilon(1,2,3S)$ and $B_{(s)}^0 \rightarrow h^+ h'^-$
- Radiative tail from MC

$$\sigma_{B^0} = 22.8 \pm 0.4 \text{ MeV}$$

$$m_{B_s} - m_{B_d} \sim 3.5\sigma_{B^0}$$

Signal Expectations - Yields

- Number of signal events corresponding to a BF :

$$N_{B_{(s)}^0 \rightarrow \mu^+ \mu^-} \propto BF(B_{(s)}^0 \rightarrow \mu^+ \mu^-) \times N_{B_s}$$

- N_{B_s} obtained by normalising to channels of known BF :

$$B^+ \rightarrow J/\psi K^+ \text{ and } B^0 \rightarrow K\pi$$

- Correcting for efficiencies and hadronisation probability:

$$N_{B_{(s)}^0 \rightarrow \mu^+ \mu^-} = BF(B_{(s)}^0 \rightarrow \mu^+ \mu^-) \times \frac{N_{norm}}{BF_{norm}}$$

$$\times \frac{f_{B_{(s)}^0}}{f_{norm}}$$

$$\times \frac{\epsilon_{sig}}{\epsilon_{norm}}$$

Ratio of probability for a b quark to hadronise into a $B_{(s)}^0$ or into the normalisation initial state

Normalisation Ingredients

$$\begin{aligned}
 N_{B_{(s)}^0 \rightarrow \mu^+ \mu^-} &= BF(B_{(s)}^0 \rightarrow \mu^+ \mu^-) \\
 &\times \frac{N_{norm}}{BF_{norm}} \longleftarrow \text{Obtained by fitting control channels invariant mass} \\
 &\times \frac{f_{B_{(s)}^0}}{f_{norm}} \longleftarrow \text{Measured in LHCb*} \\
 &\times \frac{\epsilon_{sig}}{\epsilon_{norm}} \longleftarrow \text{Measured with simulations}
 \end{aligned}$$

Averaging the results from the two control channels:

SM expectations in signal mass windows:

$$40 \pm 4 \quad B_s^0 \rightarrow \mu^+ \mu^- \quad \text{and} \quad 4.5 \pm 0.4 \quad B^0 \rightarrow \mu^+ \mu^-$$

Time Acceptance Correction - 1

- Recall, **decay rate depends on $A_{\Delta\Gamma}$** :

$$\langle \Gamma(B_{(s)}^0(t) \rightarrow \ell^+ \ell^-) \rangle = R_H e^{-\Gamma_H^{(s)} t} + R_L e^{-\Gamma_L^{(s)} t} \quad \text{and} \quad A_{\Delta\Gamma} = \frac{R_H - R_L}{R_H + R_L}$$

- So $B_s^0 \rightarrow \mu^+ \mu^-$ signal **efficiency ϵ_{sig} depend on $A_{\Delta\Gamma}$** :

$$\epsilon_{sig}(A_{\Delta\Gamma}) = \frac{\int \Gamma(A_{\Delta\Gamma}, t) \times \epsilon(t) dt}{\int \Gamma(A_{\Delta\Gamma}, t) dt}$$

- Signal efficiency used in **normalisation**...

$$BF_{sig} = BF_{norm} \times \frac{N_{sig}}{N_{norm}} \times \frac{f_{sig}}{f_{norm}} \times \frac{\epsilon_{sig}(A_{\Delta\Gamma})}{\epsilon_{norm}}$$

...is obtained from MC and must be corrected to match latest y_s and $\tau_{B_s^0}$ values:

$$\epsilon_{B_s^0 \rightarrow \mu\mu}^{SM} / \epsilon^{MC} = 1.0457$$

$$\epsilon_{B^0 \rightarrow \mu\mu}^{SM} / \epsilon^{MC} = 1.015$$

Time Acceptance Correction - 2

- BDT uses **decay-time as input variable**
- BDT PDF obtained with mainly $B^0 \rightarrow h^+ h'^-$
- $B^0 \rightarrow h^+ h'^-$ and $B_s^0 \rightarrow \mu^+ \mu^-$ have **different lifetime distributions**
- Need corrections:

$$\frac{PDF_{corr}^i}{PDF_{raw}^i} = \delta_{PDF}^i$$

- Nota: all these corrections depend on the value assumed for $A_{\Delta\Gamma}$

Bin	PDF Correction $\delta_{PDF}^i - 1$ (%)
1	-3.1061 ± 0.0196
2	-1.3778 ± 0.0290
3	-0.3887 ± 0.0392
4	$+0.2701 \pm 0.0423$
5	$+0.7193 \pm 0.0447$
6	$+1.3650 \pm 0.0457$
7	$+2.5423 \pm 0.0463$
8	$+4.7365 \pm 0.0433$

Analysis Overview

- Answering the question:

Which BF is (in-)compatible with the observed data?

- Observed data = $N(B_{(s)}^0 \rightarrow \mu^+ \mu^- + \mathbf{Bkg})$

1. Increasing sensitivity:

- Events **Selection and Classification** in categories

2. Derive **Signal and Bkg expectations** from control channels

3. Compare expectations with observation and infer about BF

- **CLs method** and **Fitting** procedure if signal evidence

- **Data Set:**

2011	1.0 fb ⁻¹	7TeV	
2012	+1.1 fb ⁻¹	8TeV	PRL 110, 021801, 2013
2012	+0.9 fb ⁻¹	8TeV	PRL 111, 101805, 2013

Sensitivity Expectations (CLs method)

Invariant mass [MeV/c ²]		BDT							
		0.0 – 0.25	0.25 – 0.4	0.4 – 0.5	0.5 – 0.6	0.6 – 0.7	0.7 – 0.8	0.8 – 0.9	0.9 – 1.0
5311 – 5431	Exp. comb. bkg	6138 ⁺¹¹⁴ ₋₁₁₂	121.6 ^{+4.8} _{-4.7}	28.2 ^{+2.2} _{-2.1}	11.9 ^{+1.5} _{-1.4}	4.77 ^{+1.11} _{-0.95}	2.17 ^{+0.79} _{-0.65}	0.79 ^{+0.48} _{-0.34}	0.29 ^{+0.32} _{-0.18}
	Exp. peak. bkg	0.330 ^{+0.105} _{-0.089}	0.210 ^{+0.068} _{-0.058}	0.140 ^{+0.045} _{-0.038}	0.148 ^{+0.048} _{-0.040}	0.147 ^{+0.047} _{-0.040}	0.140 ^{+0.045} _{-0.038}	0.130 ^{+0.042} _{-0.035}	0.111 ^{+0.035} _{-0.030}
	Exp. signal	8.78 ^{+1.09} _{-0.99}	5.40 ^{+0.75} _{-0.67}	3.52 ^{+0.46} _{-0.41}	3.75 ^{+0.47} _{-0.43}	3.76 ^{+0.47} _{-0.43}	3.61 ^{+0.46} _{-0.42}	3.68 ^{+0.46} _{-0.42}	3.79 ^{+0.46} _{-0.42}

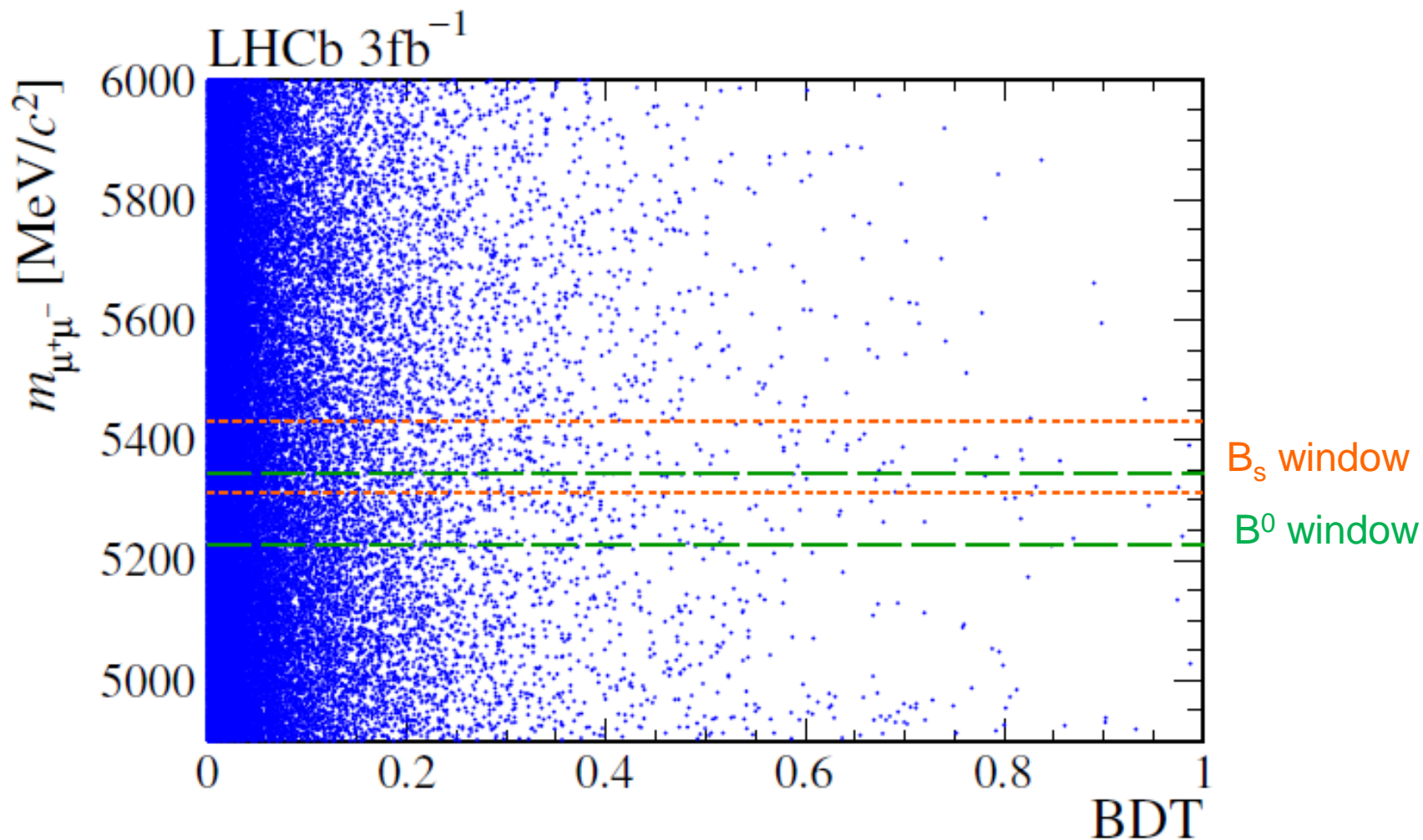
Expected **significance** for a $B_s^0 \rightarrow \mu^+ \mu^-$ SM signal : **5.0 σ**

Invariant mass [MeV/c ²]		BDT							
		0.0 – 0.25	0.25 – 0.4	0.4 – 0.5	0.5 – 0.6	0.6 – 0.7	0.7 – 0.8	0.8 – 0.9	0.9 – 1.0
5224 – 5344	Exp. comb. bkg	6520 ⁺¹¹⁹ ₋₁₁₇	127.0 ^{+5.2} _{-5.0}	29.4 ^{+2.4} _{-2.3}	12.8 ^{+1.7} _{-1.5}	4.9 ^{+1.2} _{-1.1}	2.14 ^{+0.88} _{-0.70}	0.82 ^{+0.53} _{-0.37}	0.29 ^{+0.35} _{-0.19}
	Exp. peak. bkg	1.97 ^{+0.64} _{-0.47}	1.25 ^{+0.41} _{-0.31}	0.83 ^{+0.27} _{-0.20}	0.88 ^{+0.29} _{-0.21}	0.88 ^{+0.28} _{-0.21}	0.83 ^{+0.27} _{-0.20}	0.77 ^{+0.25} _{-0.18}	0.66 ^{+0.21} _{-0.16}
	Exp. Cross-feed	1.38 ^{+0.18} _{-0.16}	0.85 ^{+0.12} _{-0.11}	0.554 ^{+0.075} _{-0.067}	0.590 ^{+0.078} _{-0.070}	0.591 ^{+0.076} _{-0.070}	0.567 ^{+0.077} _{-0.069}	0.579 ^{+0.076} _{-0.069}	0.595 ^{+0.077} _{-0.069}
	Exp. signal	0.99 ^{+0.12} _{-0.11}	0.610 ^{+0.081} _{-0.075}	0.398 ^{+0.049} _{-0.046}	0.424 ^{+0.050} _{-0.047}	0.425 ^{+0.050} _{-0.047}	0.408 ^{+0.050} _{-0.047}	0.416 ^{+0.049} _{-0.046}	0.428 ^{+0.050} _{-0.046}

No significant $B^0 \rightarrow \mu^+ \mu^-$ SM signal expected:

$$B(B^0 \rightarrow \mu^+ \mu^-) < 5.4 \times 10^{-10} \text{ at 95\% CL}$$

Open the box



Fit Projection

$$B_s^0 \rightarrow \mu^+ \mu^-$$

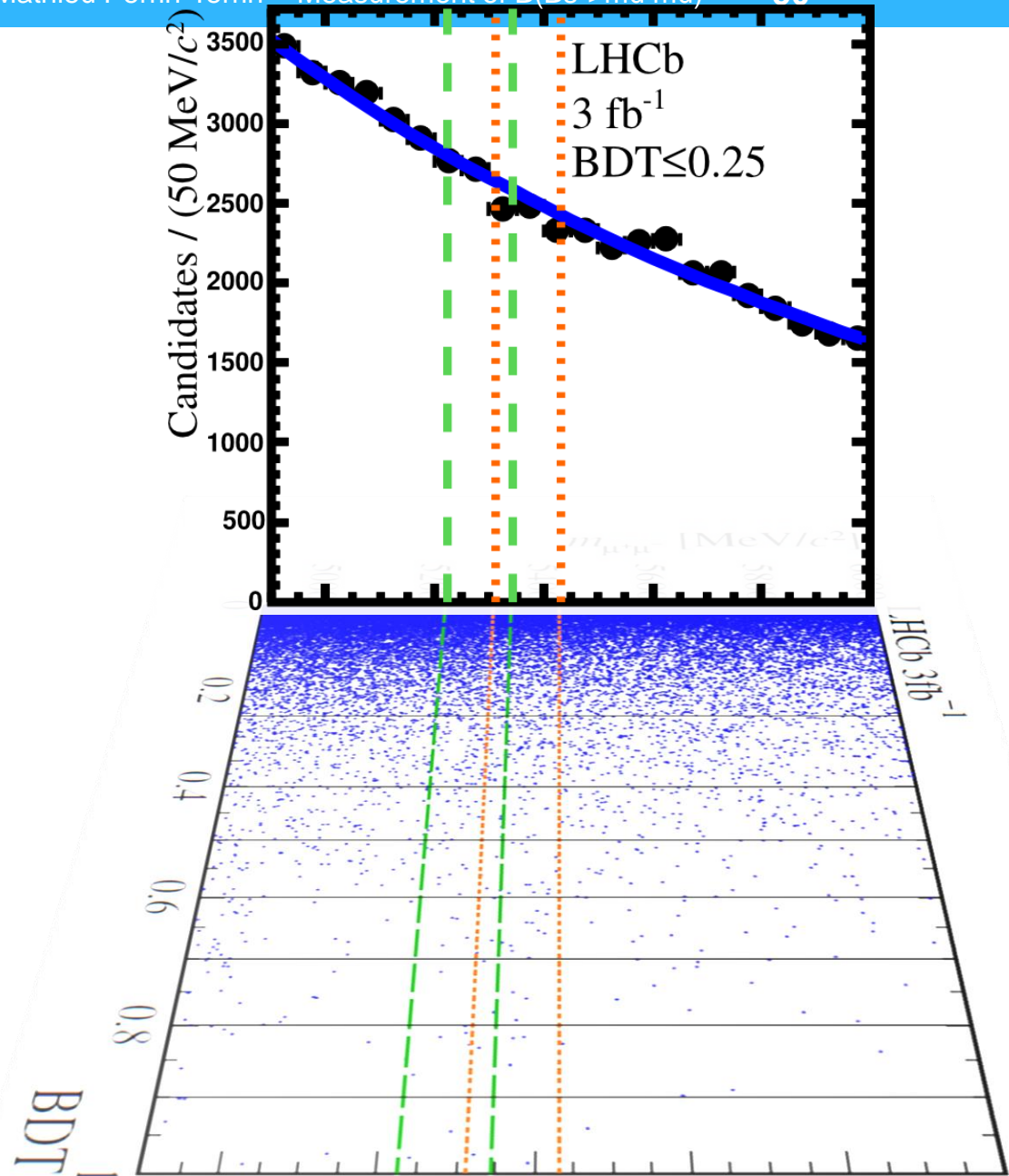
$$B^0 \rightarrow \mu^+ \mu^-$$

$$B^0 \rightarrow \pi, K^+ \mu^- \bar{\nu}_\mu$$

$$B^{0,+} \rightarrow \pi^{0,+} \mu^+ \mu^-$$

$$B_{(s)}^0 \rightarrow h^+ h'^-$$

Total



Fit Projection

$$B_s^0 \rightarrow \mu^+ \mu^-$$

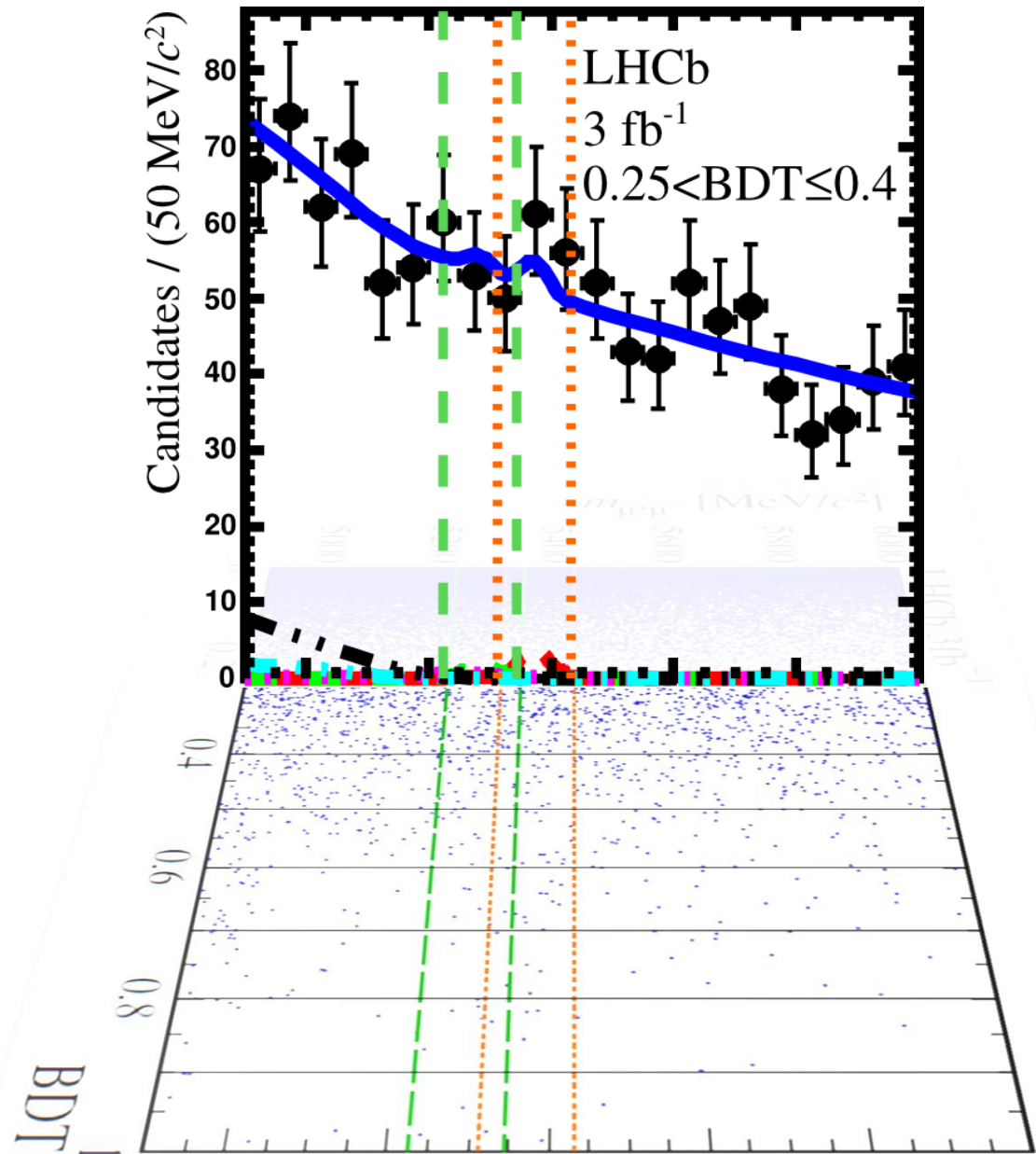
$$B^0 \rightarrow \mu^+ \mu^-$$

$$B^0 \rightarrow \pi, K^+ \mu^- \bar{\nu}_\mu$$

$$B^{0,+} \rightarrow \pi^{0,+} \mu^+ \mu^-$$

$$B_{(s)}^0 \rightarrow h^+ h'^-$$

Total



Fit Projection

$$B_s^0 \rightarrow \mu^+ \mu^-$$

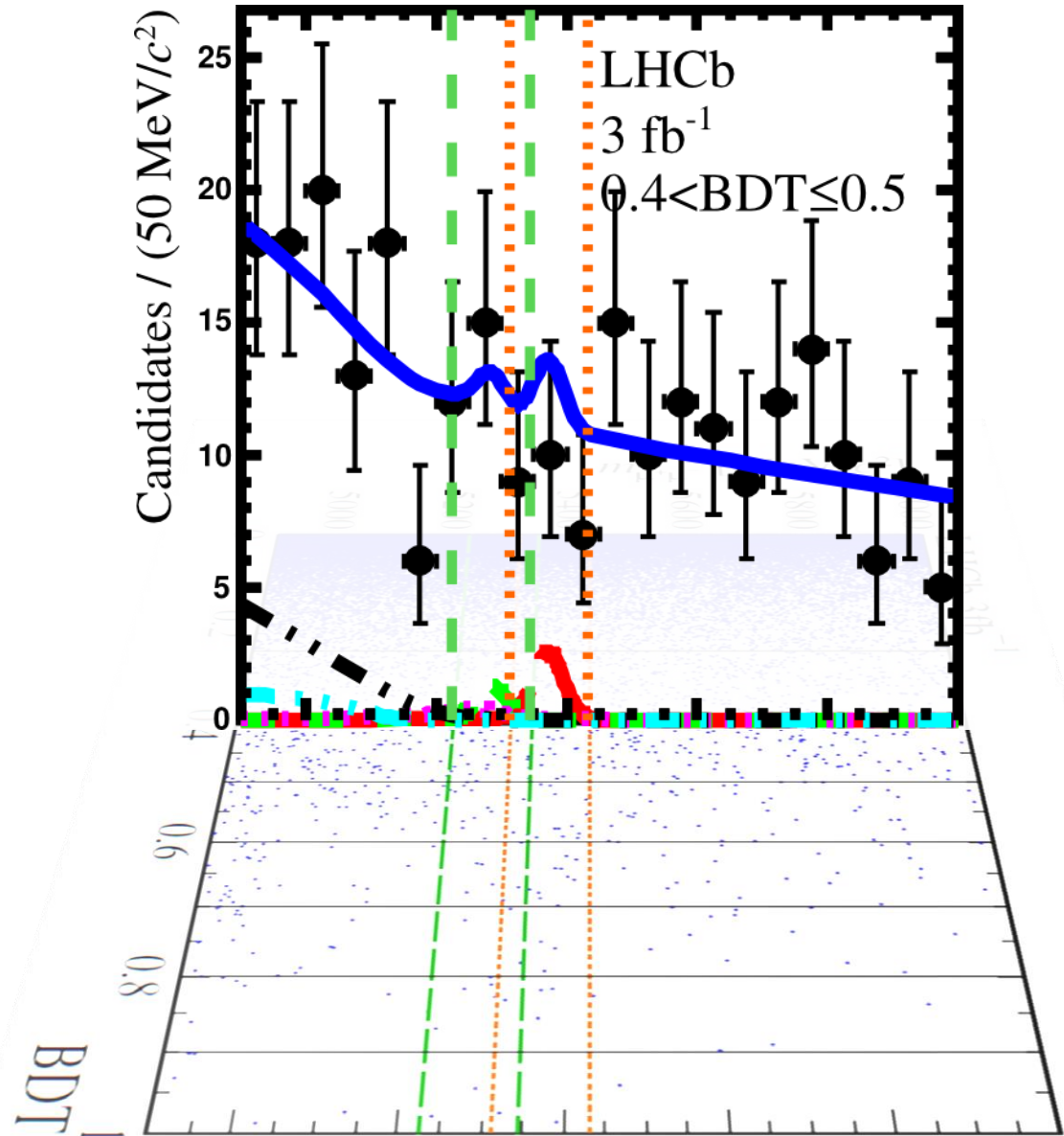
$$B^0 \rightarrow \mu^+ \mu^-$$

$$B^0 \rightarrow \pi, K^+ \mu^- \bar{\nu}_\mu$$

$$B^{0,+} \rightarrow \pi^{0,+} \mu^+ \mu^-$$

$$B_{(s)}^0 \rightarrow h^+ h'^-$$

Total



Fit Projection

$$B_s^0 \rightarrow \mu^+ \mu^-$$

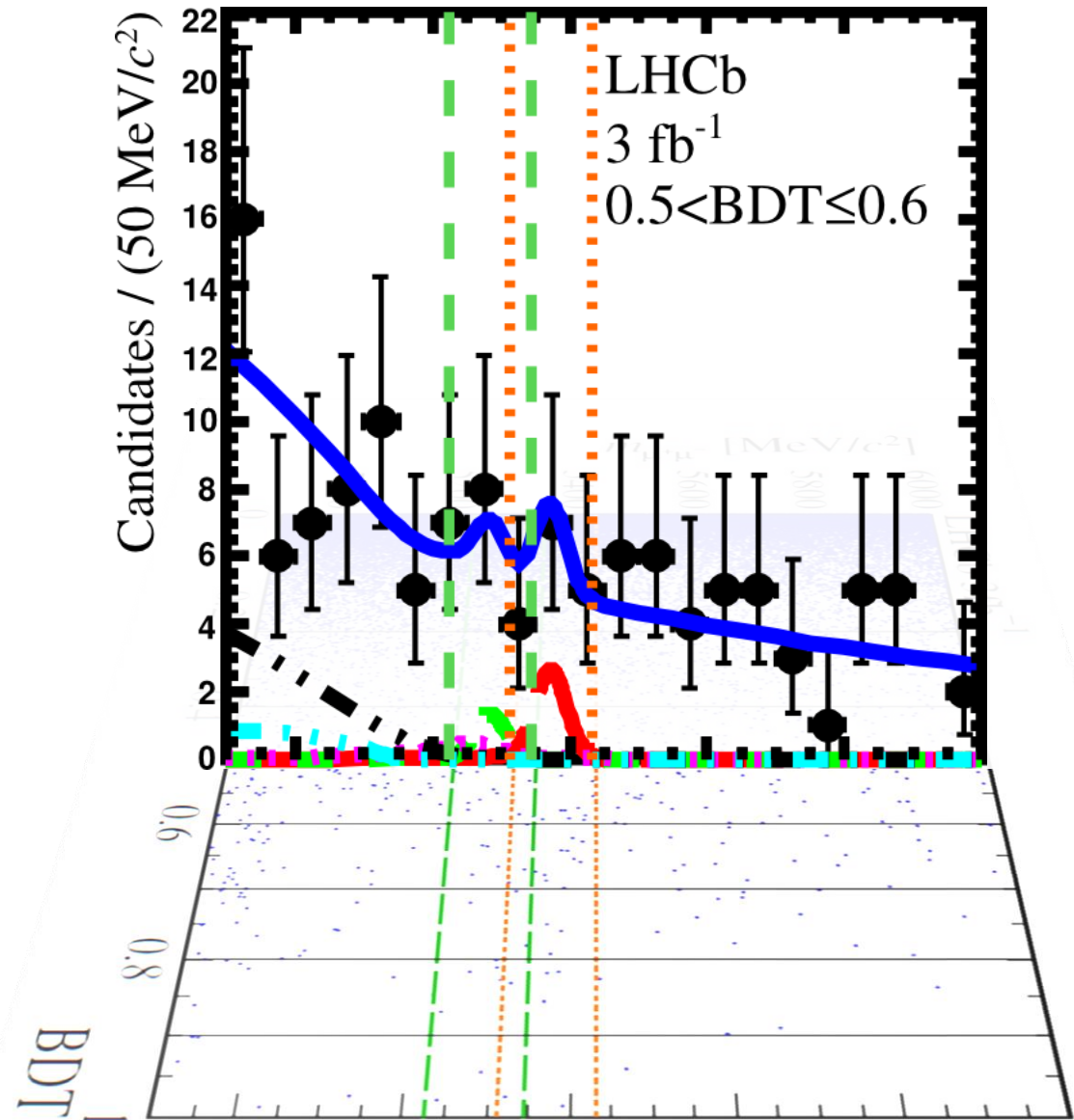
$$B^0 \rightarrow \mu^+ \mu^-$$

$$B^0 \rightarrow \pi, K^+ \mu^- \bar{\nu}_\mu$$

$$B^{0,+} \rightarrow \pi^{0,+} \mu^+ \mu^-$$

$$B_{(s)}^0 \rightarrow h^+ h'^-$$

Total



Fit Projection

$$B_s^0 \rightarrow \mu^+ \mu^-$$

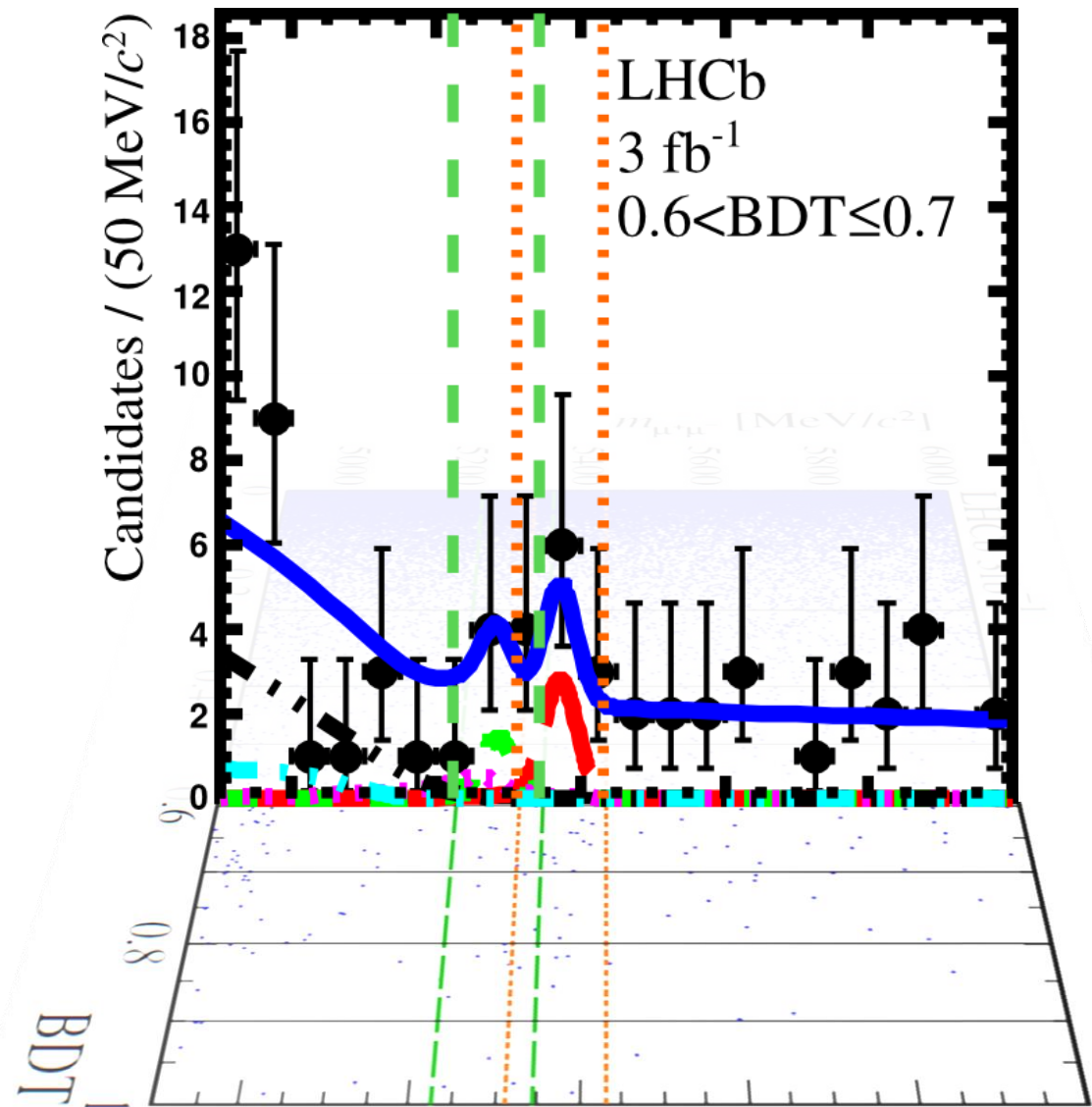
$$B^0 \rightarrow \mu^+ \mu^-$$

$$B^0 \rightarrow \pi, K^+ \mu^- \bar{\nu}_\mu$$

$$B^{0,+} \rightarrow \pi^{0,+} \mu^+ \mu^-$$

$$B_{(s)}^0 \rightarrow h^+ h'^-$$

Total



Fit Projection

$$B_s^0 \rightarrow \mu^+ \mu^-$$

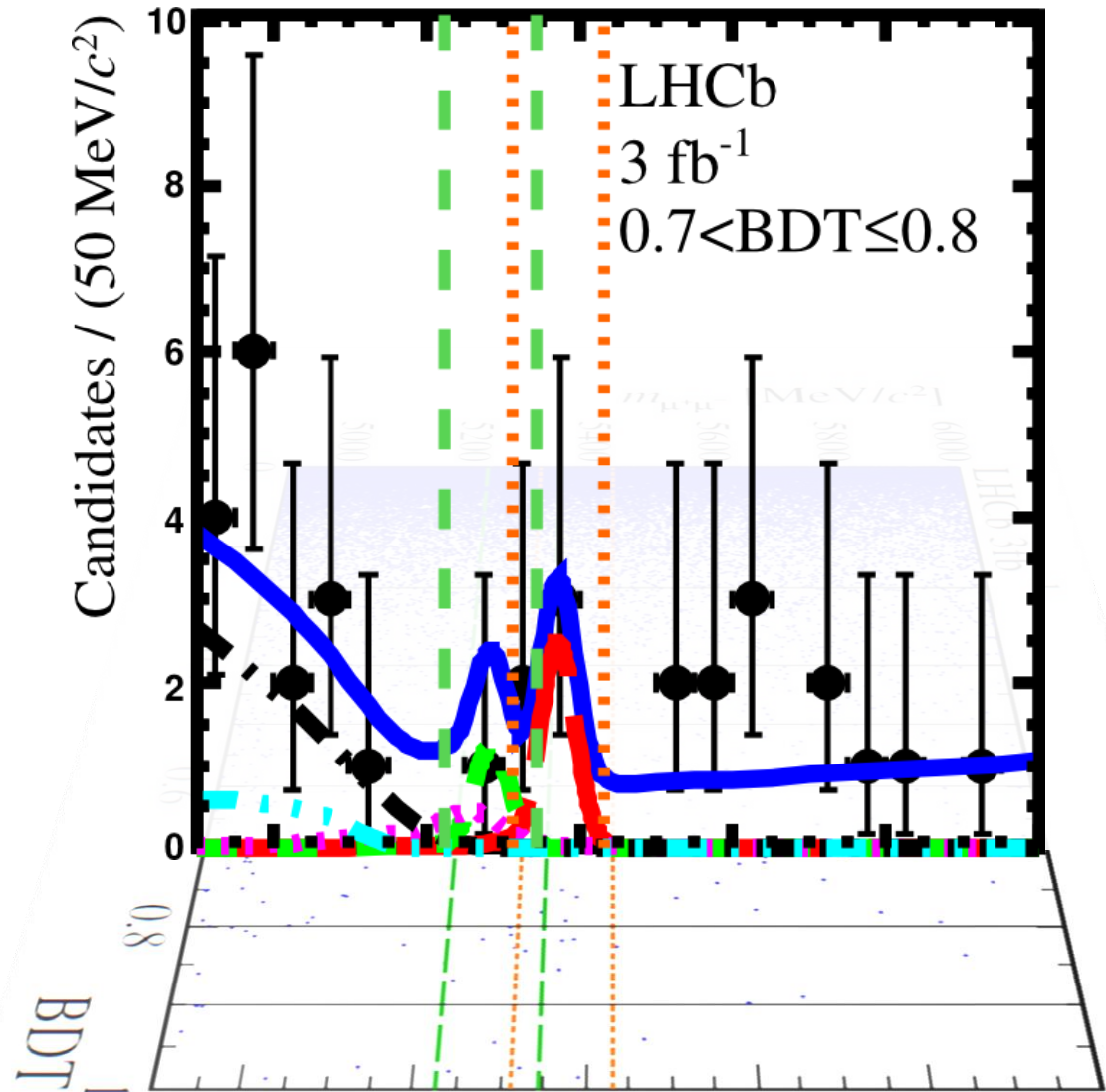
$$B^0 \rightarrow \mu^+ \mu^-$$

$$B^0 \rightarrow \pi, K^+ \mu^- \bar{\nu}_\mu$$

$$B^{0,+} \rightarrow \pi^{0,+} \mu^+ \mu^-$$

$$B_{(s)}^0 \rightarrow h^+ h'^-$$

Total



Fit Projection

$$B_s^0 \rightarrow \mu^+ \mu^-$$

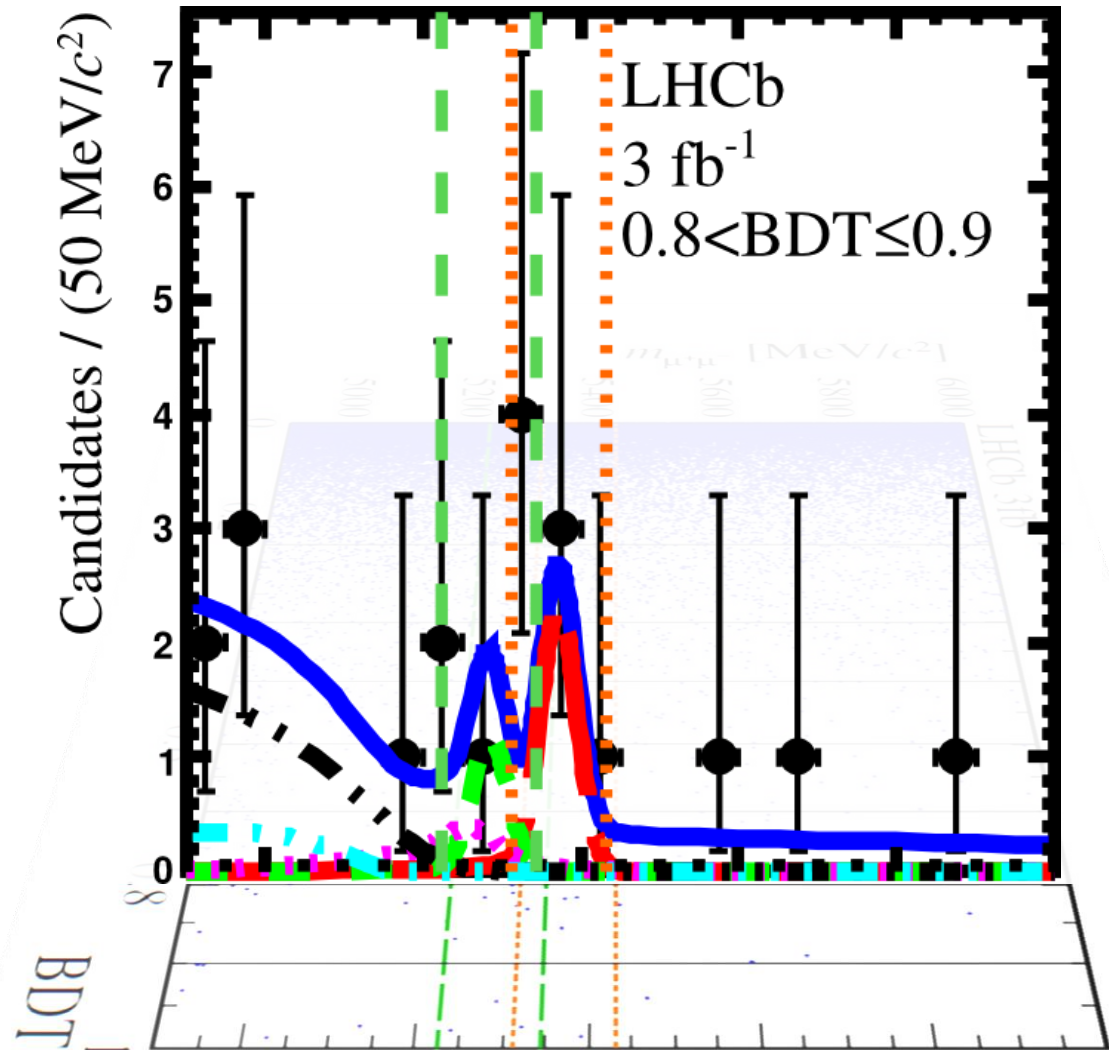
$$B^0 \rightarrow \mu^+ \mu^-$$

$$B^0 \rightarrow \pi, K^+ \mu^- \bar{\nu}_\mu$$

$$B^{0,+} \rightarrow \pi^{0,+} \mu^+ \mu^-$$

$$B_{(s)}^0 \rightarrow h^+ h'^-$$

Total



Fit Projection

$$B_s^0 \rightarrow \mu^+ \mu^-$$

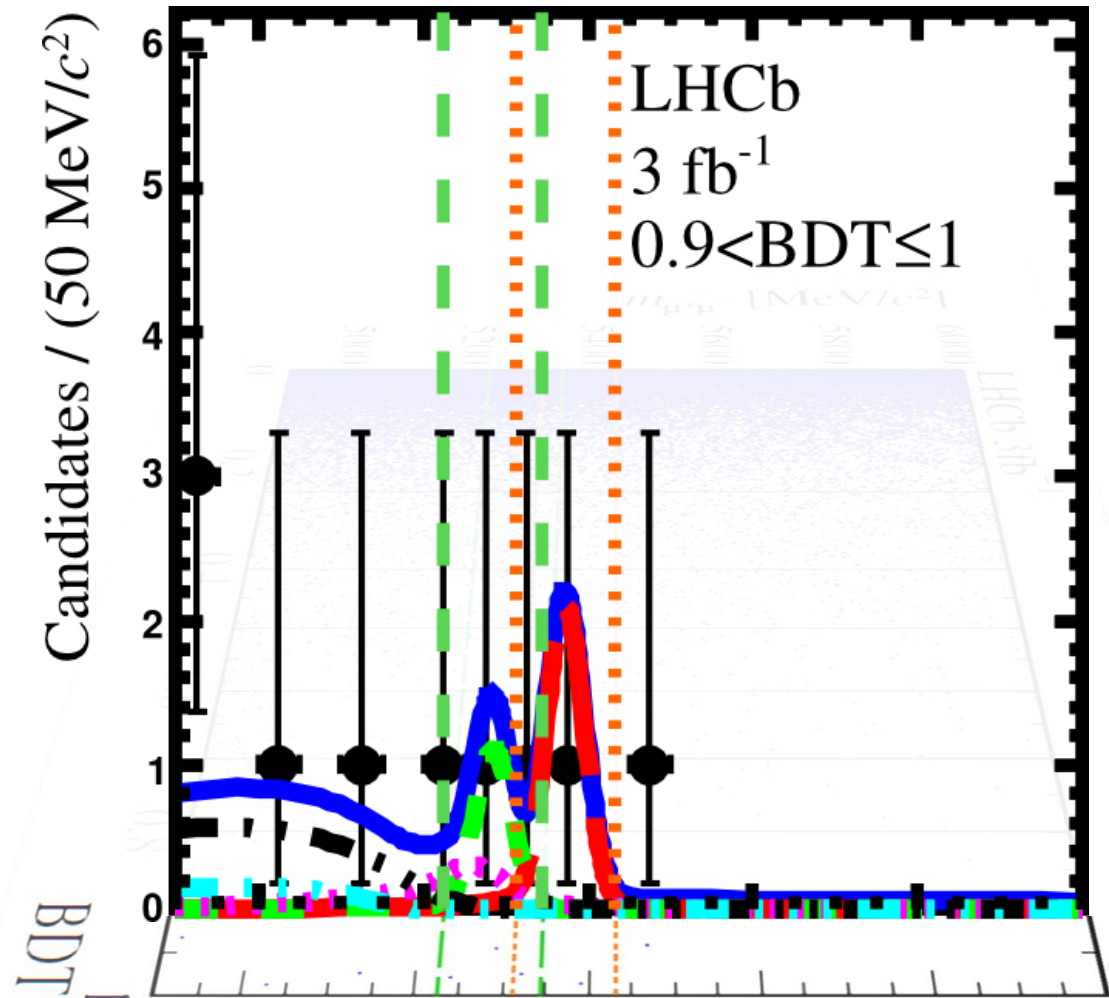
$$B^0 \rightarrow \mu^+ \mu^-$$

$$B^0 \rightarrow \pi, K^+ \mu^- \bar{\nu}_\mu$$

$$B^{0,+} \rightarrow \pi^{0,+} \mu^+ \mu^-$$

$$B_{(s)}^0 \rightarrow h^+ h'^-$$

Total



Fit Result

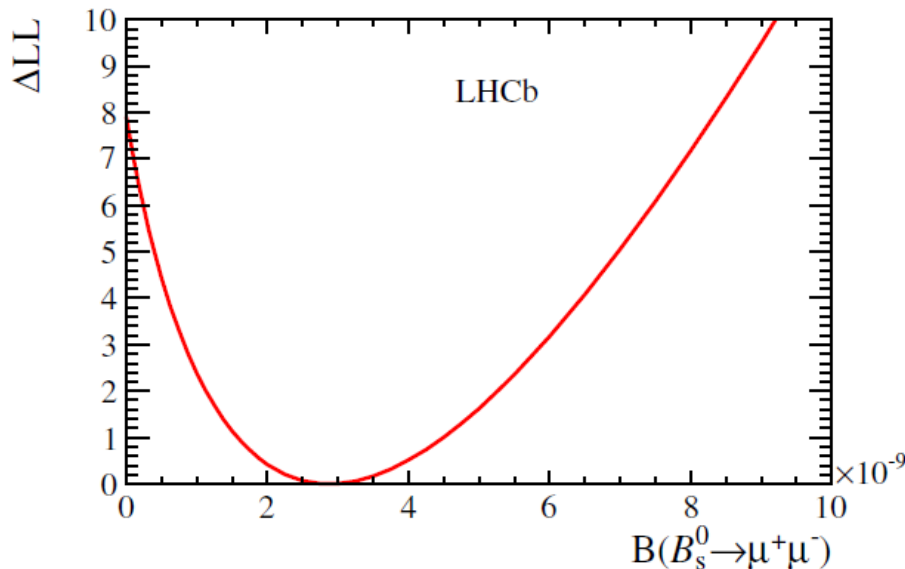
arXiv:1307.5024, Phys.Rev. Lett.111(2013) 101805

$$B(B_s^0 \rightarrow \mu^+ \mu^-) = (2.9_{-1.0}^{+1.1} (stat)_{-0.1}^{+0.3} (syst)) \times 10^{-9}$$

Significance: 4.0 σ
expected 5.0 σ (median)

$$B(B^0 \rightarrow \mu^+ \mu^-) = (3.7_{-2.1}^{+2.4} (stat)_{-0.4}^{+0.6} (syst)) \times 10^{-10}$$

Significance: 2.0 σ

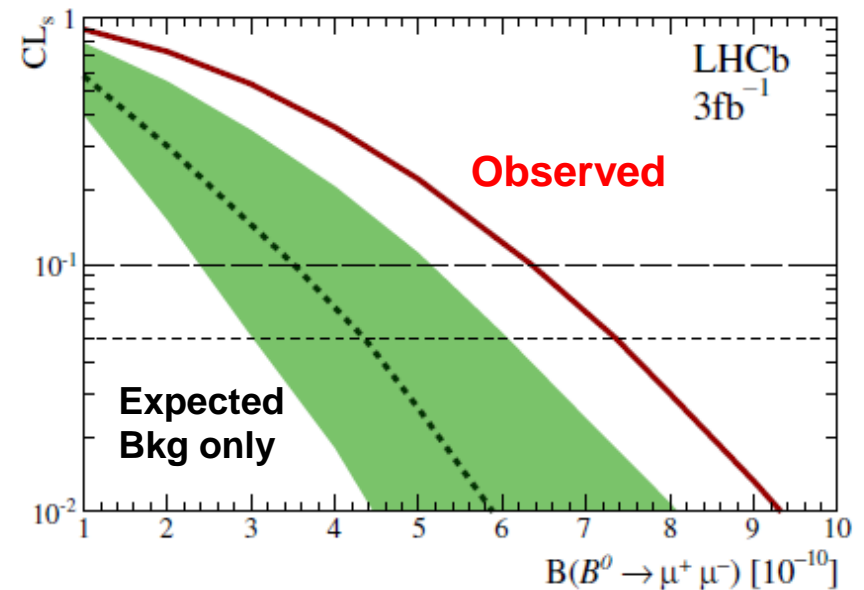
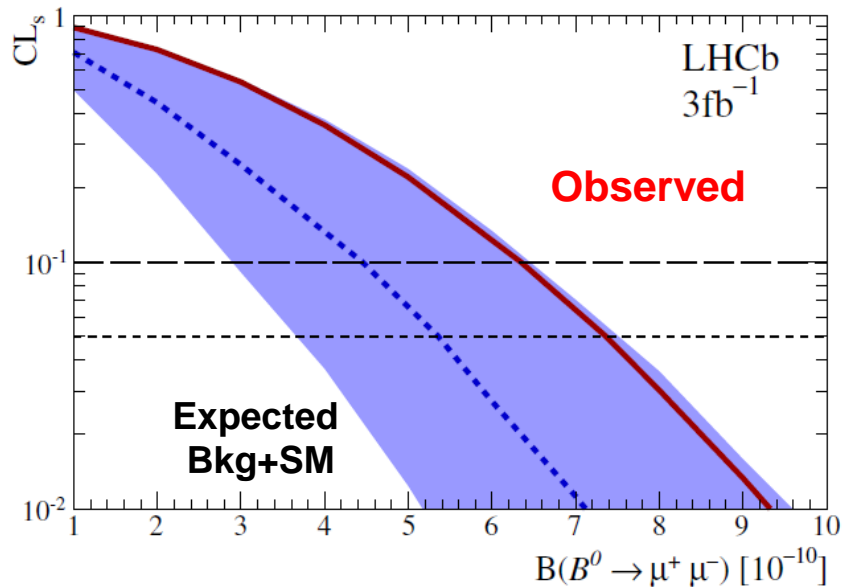


Correlation between $\text{BR}(B^0 \rightarrow \mu^+ \mu^-)$
and $\text{BR}(B_s \rightarrow \mu^+ \mu^-)$: 3.3%

Profile Likelihood:
All parameters except
 $B(B_s^0 \rightarrow \mu^+ \mu^-)$ are floated
within their errors.

$B^0 \rightarrow \mu^+ \mu^-$ upper limit

- Obtained with the CLs method



	Limit at 95%CL
Expected bkg only	4.4×10^{-10}
Expected bkg + SM	5.4×10^{-10}
observed	7.4×10^{-10}

Outlines

- Motivations to search for $B_{(s)}^0 \rightarrow \mu^+ \mu^-$
- Searching for $B_{(s)}^0 \rightarrow \mu^+ \mu^-$ at LHCb
- Combination with CMS
- Conclusions

CMS Analysis in Brief

- Dataset: 5 (7 TeV) + 20 (8 TeV) fb^{-1}
- Trigger requirement :
 - (sub-)leading muon $p_T > 3$ (4) GeV, dimuon $p_T > 4.9$ GeV for $|\eta_{\mu\mu}| < 1.8$
 - (sub-)leading muon $p_T > 4$ (4) GeV, dimuon $p_T > 7$ GeV for $|\eta_{\mu\mu}| > 1.8$
 - $4.8 < m_{\mu\mu} < 6$ GeV
 - Vertex fit $p(\chi^2) > 0.5\%$
- Discriminant variables: $m_{\mu\mu}$ and **BDT**
- Two categories and 2011 and 2012 data kept separated:
 - Both muons in barrel : $\sigma_{\mu\mu} \sim 40$ MeV
 - At least one muon in endcap: more events but $\sigma_{\mu\mu} \sim 60$ MeV

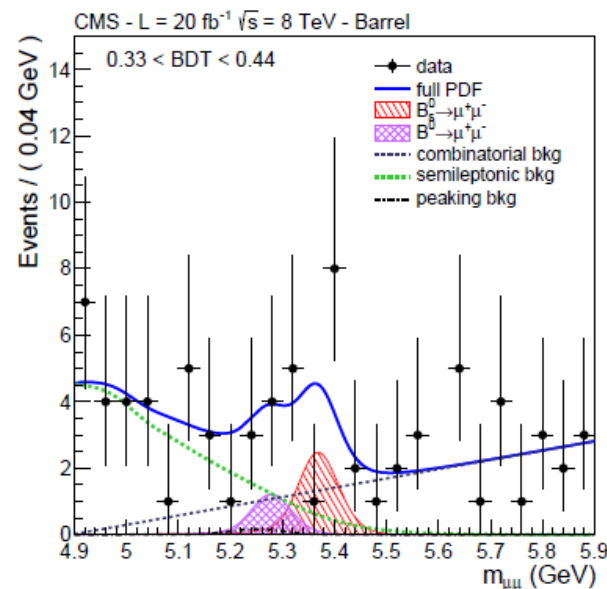
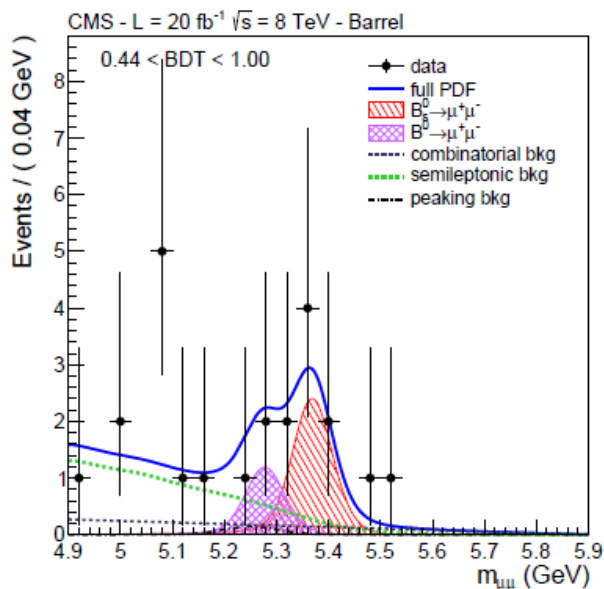
BDT

- Training on MC signal and data sidebands:
 - To avoid biases, use 3 separate samples:
train on 1st, test on 2nd and apply on 3rd \Rightarrow 3 BDT per categories
- 12 variables used, independent of pile-up conditions
- Signal BDT distribution taken from MC, systematics evaluated using control sample
- Then, 2 possible methods:
 - **Simple cut on BDT output**, optimised for each sample:
limit computation
 - **Analysis in 3 bins of BDT vs mass** (higher expected sensitivity):
simultaneous maximum likelihood fit

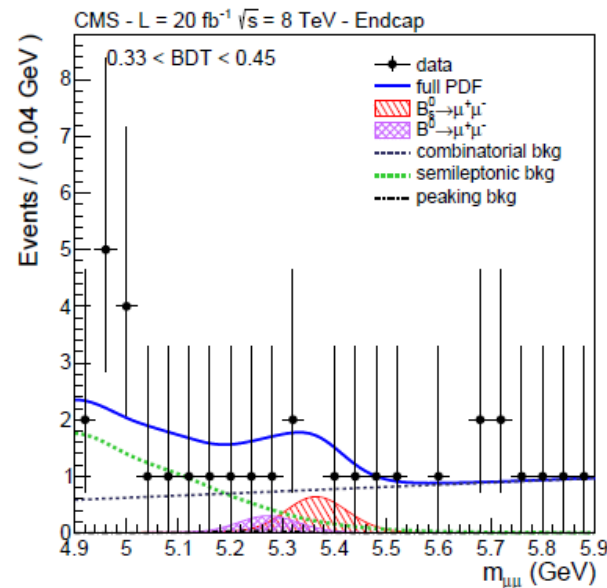
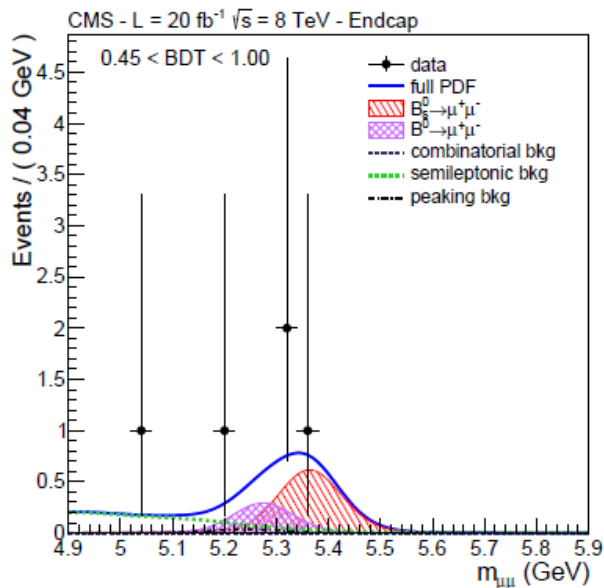
8 TeV data

Most Sensitive Bin

2nd Most Sensitive Bin



Barrel



End Cap

Results

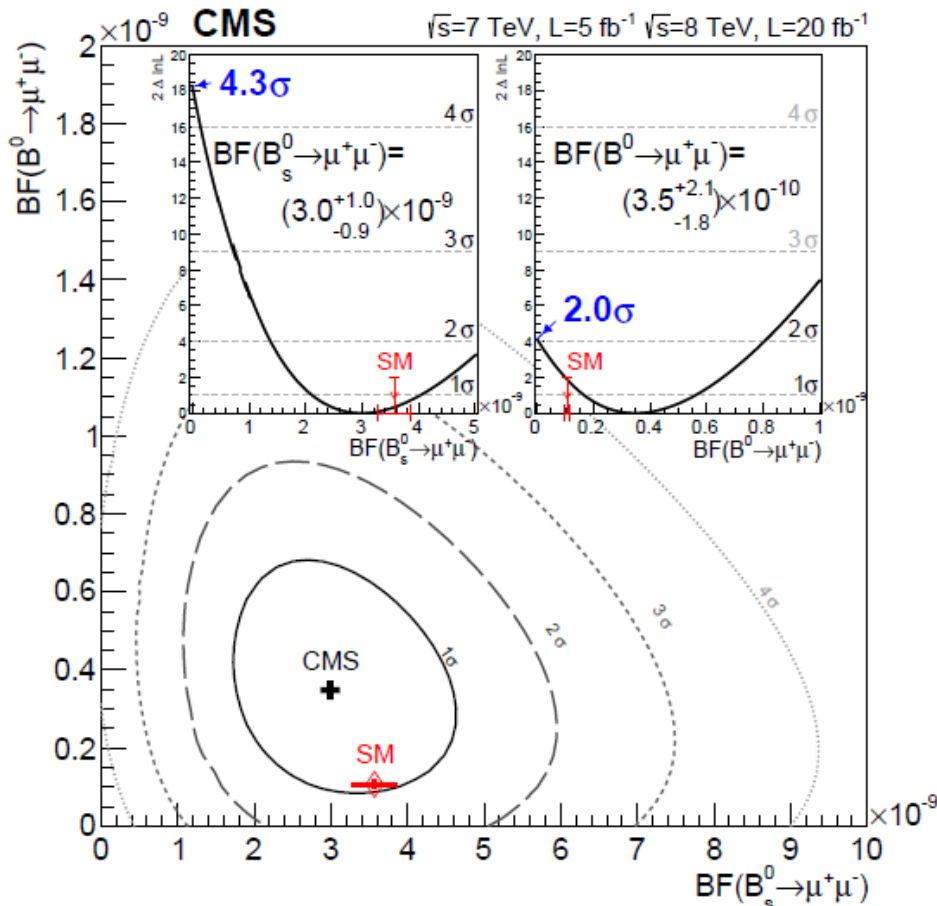
arXiv:1307.5025, Phys.Rev. Lett.111(2013) 101804

$$B(B_s^0 \rightarrow \mu^+ \mu^-) = (3.0^{+0.9}_{-0.8} (\text{stat})^{+0.6}_{-0.4} (\text{syst})) \times 10^{-9}$$

Significance: 4.3σ (exp. 4.8)

$$B(B^0 \rightarrow \mu^+ \mu^-) = (3.5^{+2.1}_{-1.8} (\text{stat} + \text{syst})) \times 10^{-10}$$

Significance: 2.0σ



CLs Method	Limit at 95%CL
Expected bkg + SM	6.3×10^{-10}
observed	11×10^{-10}

Combination CMS LHCb

- Simple average technique (arXiv:physics/0406120)
- Treat correlated systematic uncertainty: f_s/f_d
- Update CMS results with latest f_s/f_d *

$$B(B_s^0 \rightarrow \mu^+ \mu^-) = 2.96_{-0.85}^{+0.97} \pm 0.17_{f_s/f_d} \quad \text{CMS}$$

$$B(B_s^0 \rightarrow \mu^+ \mu^-) = 2.87_{-0.95}^{+1.09} \pm 0.17_{f_s/f_d} \quad \text{LHCb}$$

- Combined result:

$$B(B_s^0 \rightarrow \mu^+ \mu^-) = (2.9 \pm 0.7) \times 10^{-9} \quad \text{Significance} > 5\sigma$$

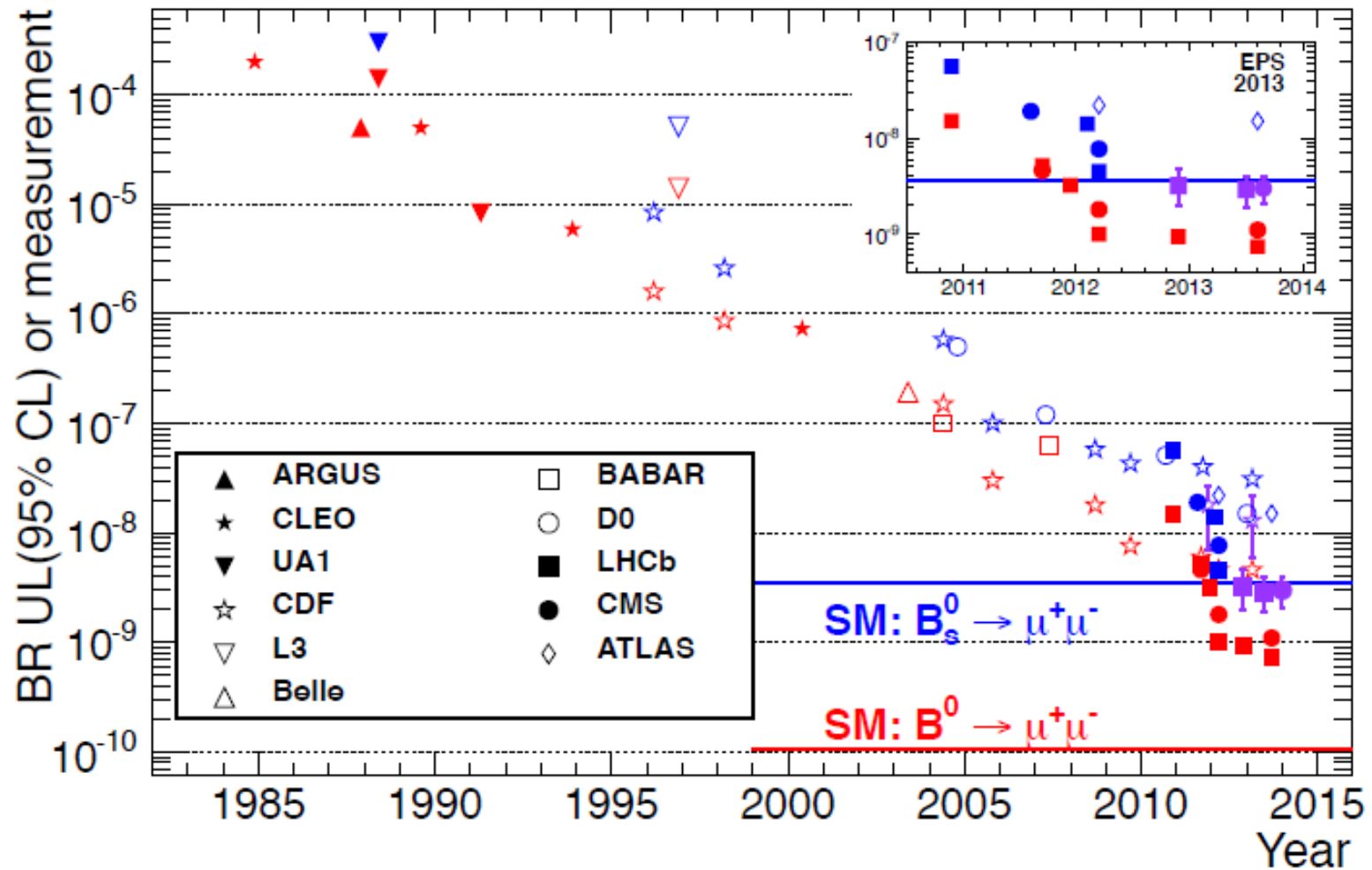
$$B(B^0 \rightarrow \mu^+ \mu^-) = (3.6_{-1.4}^{+1.6}) \times 10^{-10} \quad \text{Significance} < 3\sigma$$

*LHCb-CONF-2013-011

Outlines

- Motivations to search for $B_{(s)}^0 \rightarrow \mu^+ \mu^-$
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From 1984 to now...



Summary

CMS 25 fb⁻¹

$$B(B_s^0 \rightarrow \mu^+ \mu^-) = (3.0_{-0.9}^{+1.0}) \times 10^{-9} \quad 4.3 \sigma$$

$$B(B^0 \rightarrow \mu^+ \mu^-) = 3.5_{-1.8}^{+2.1} \times 10^{-10} \quad 2.0 \sigma$$

$$B(B^0 \rightarrow \mu^+ \mu^-) < 1.1 \times 10^{-9} \text{ @95\%CL}$$

LHCb 3 fb⁻¹

$$B(B_s^0 \rightarrow \mu^+ \mu^-) = (2.9_{-1.0}^{+1.1}) \times 10^{-9} \quad 4.0 \sigma$$

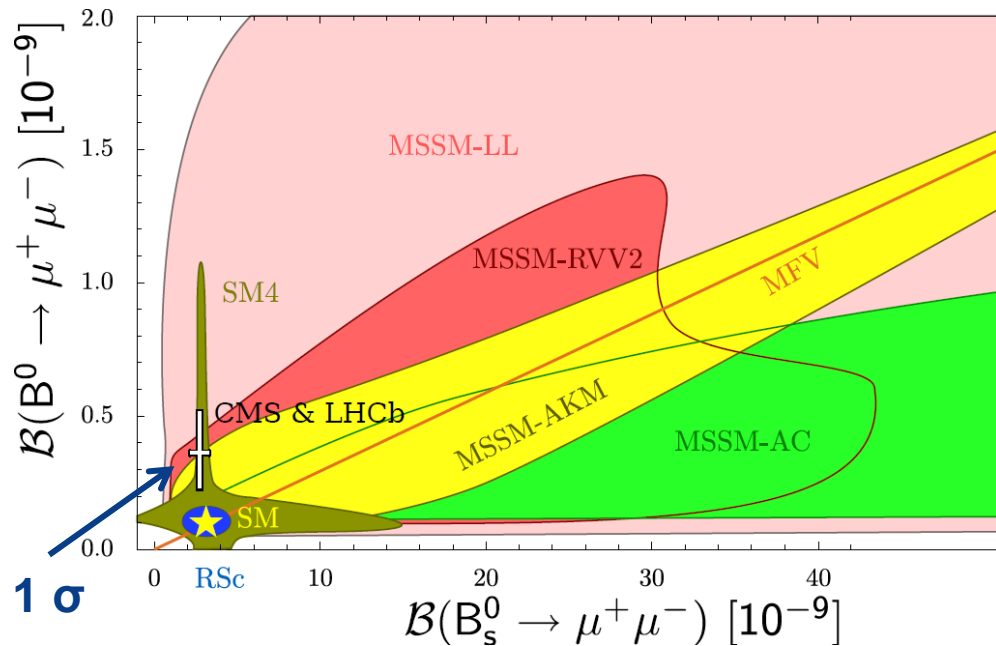
$$B(B^0 \rightarrow \mu^+ \mu^-) = 3.7_{-2.1}^{+2.4} \times 10^{-10} \quad 2.0 \sigma$$

$$B(B^0 \rightarrow \mu^+ \mu^-) < 7.4 \times 10^{-10} \text{ @95\%CL}$$

CMS + LHCb :

First observation of $BR(B_s \rightarrow \mu^+ \mu^-)$!!

$$B(B_s^0 \rightarrow \mu^+ \mu^-) = (2.9 \pm 0.7) \times 10^{-9}$$



Spares

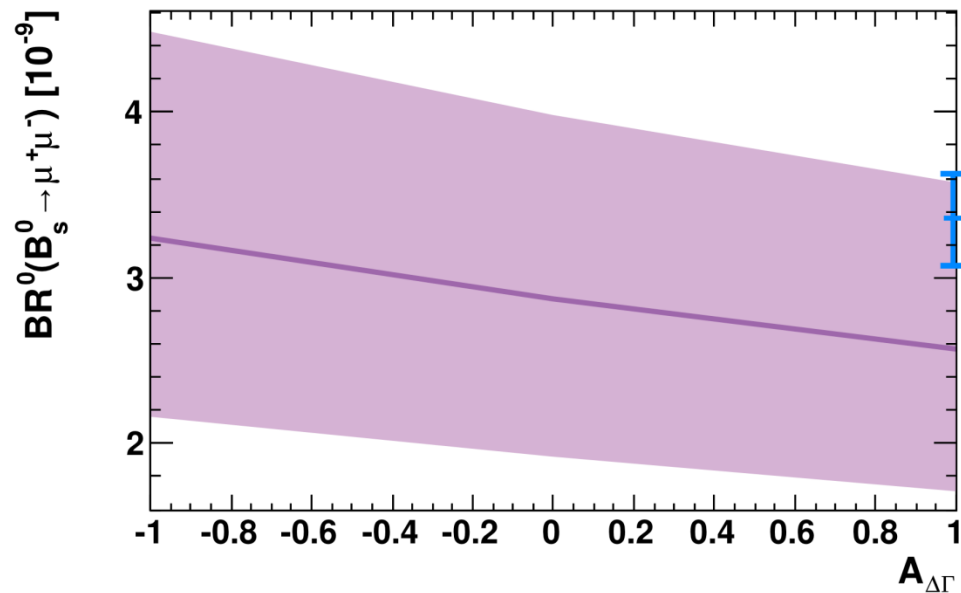
Some projections

- From LHCb-TDR-012:

Obs.	End 2018	LHCb upgrade $50fb^{-1}$
$B(B_s^0 \rightarrow \mu^+ \mu^-)$	0.5×10^{-9}	0.15×10^{-9}
$\frac{B(B_s^0 \rightarrow \mu^+ \mu^-)}{B(B^0 \rightarrow \mu^+ \mu^-)}$	100%	35%

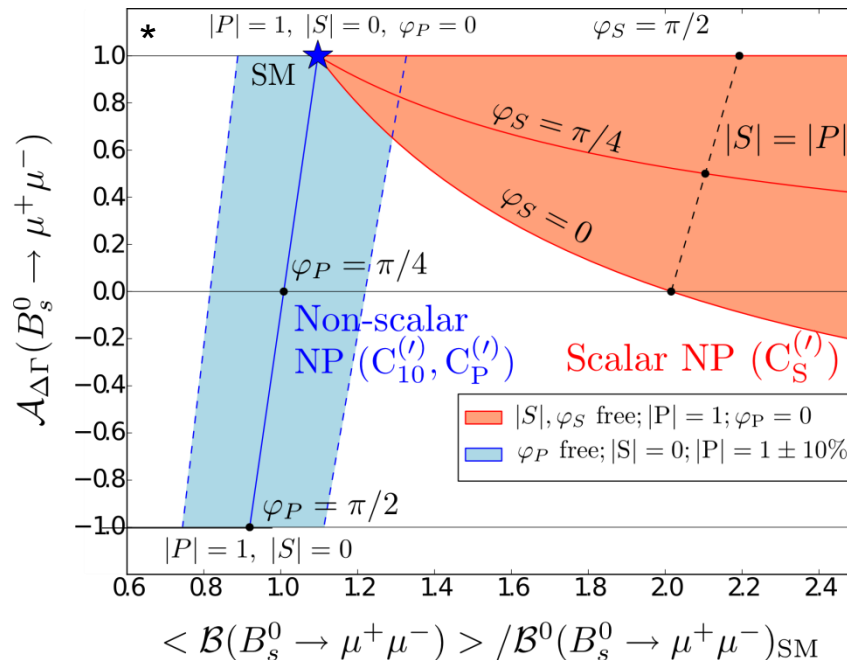
$A_{\Delta\Gamma}$ Dependency

- BR results valid only if $A_{\Delta\Gamma} = 1$
- In NP $A_{\Delta\Gamma}$ can take any value between -1 and +1
- Results depend on $A_{\Delta\Gamma}$:



Exploiting $A_{\Delta\Gamma}$ Dependency

- New Physics can enter **both** $BF_{t=0}$ and $A_{\Delta\Gamma}$
- The experi. BF dependency on $A_{\Delta\Gamma}$ must be accounted for
- The constraints are more accurate and more stringent

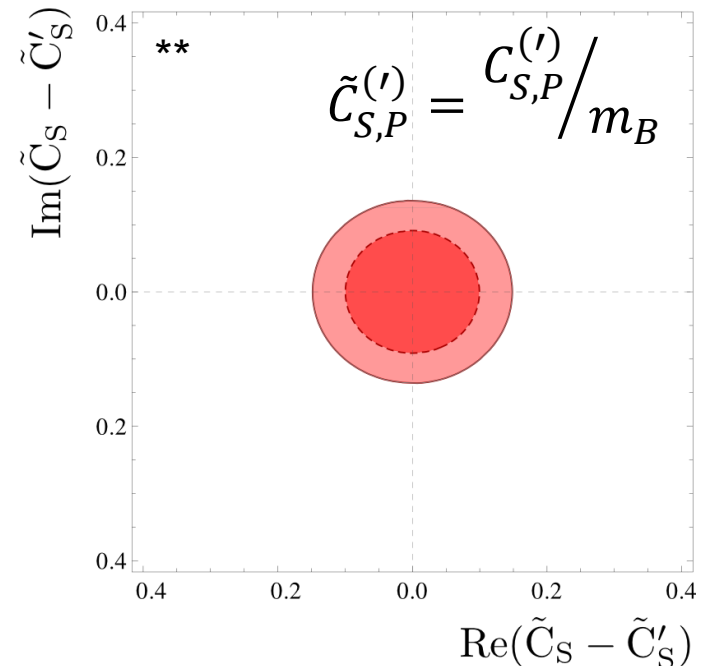
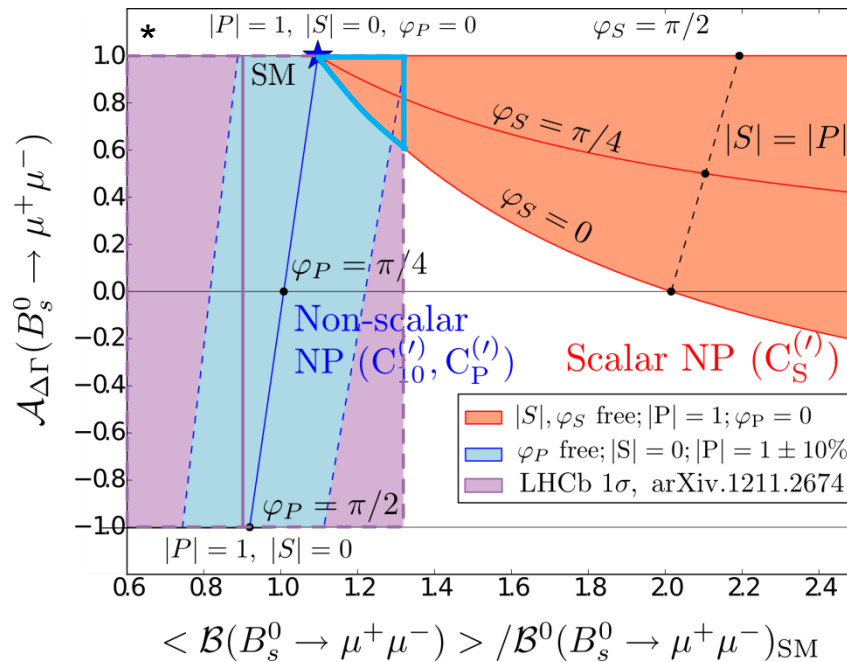


Different NP scenarios feature different **non-trivial** $A_{\Delta\Gamma} - BF$ correlations

* Modified from De Bruyn et al. PRL 109, 041801, 2012

Exploiting $A_{\Delta\Gamma}$ Dependency

- New Physics can enter both $BF_{t=0}$ and $A_{\Delta\Gamma}$
- The experi. BF dependency on $A_{\Delta\Gamma}$ must be accounted for
- The constraints are more accurate and more stringent

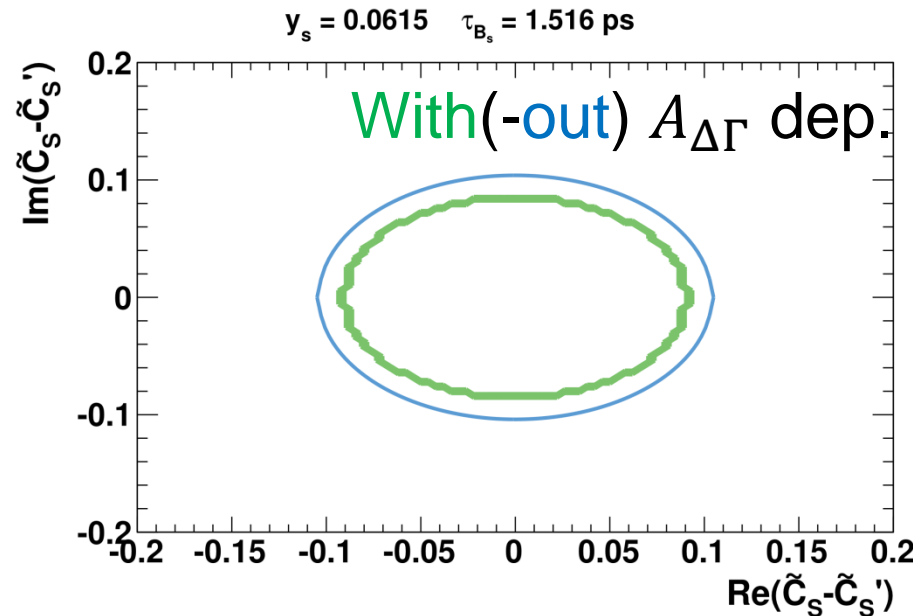
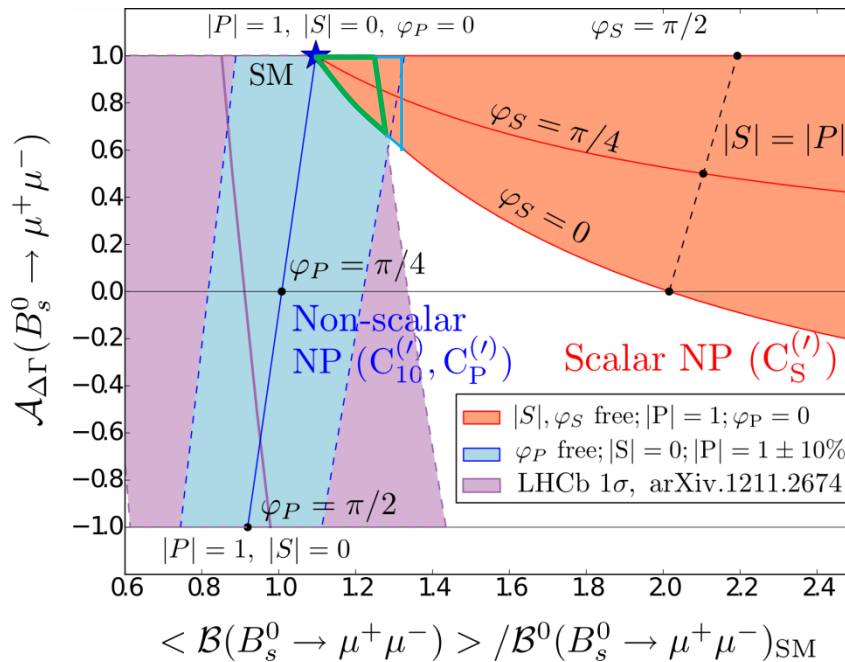


* Modified from De Bruyn et al. PRL 109, 041801, 2012

** Altmannshofer, arXiv:1306.0022

Exploiting $A_{\Delta\Gamma}$ Dependency

- New Physics can enter both $BF_{t=0}$ and $A_{\Delta\Gamma}$
- The expe. BF dependency on $A_{\Delta\Gamma}$ must be accounted for
- The constraints are **more accurate** and **more stringent**



- Constraints on scalar are **30% more stringent**

Sensitivity Projection on $A_{\Delta\Gamma}$

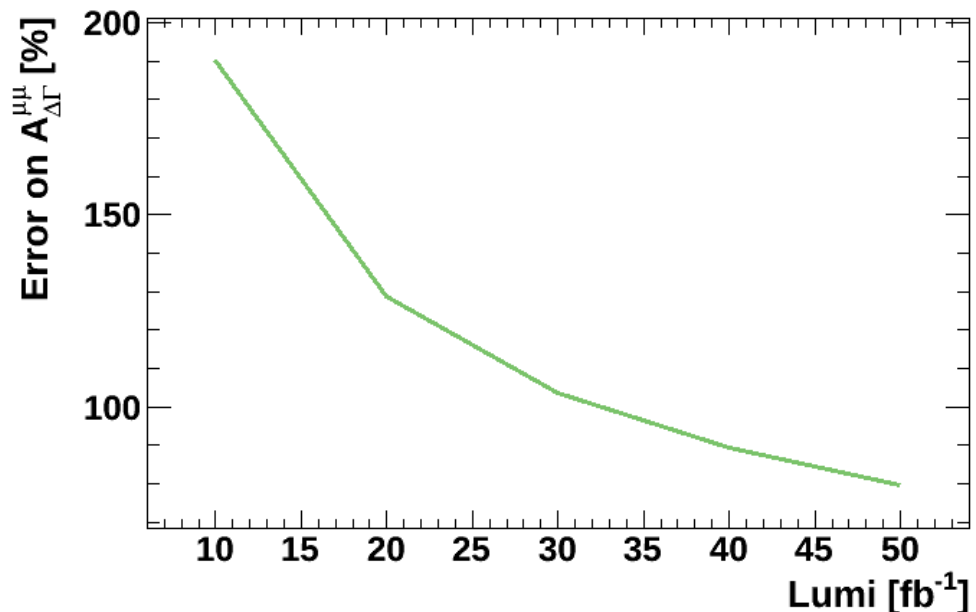
- $A_{\Delta\Gamma}$ can be obtained from effective lifetime,

$$\tau_{eff} = \frac{\int \langle \Gamma(B_s^0(t) \rightarrow \mu^+ \mu^-) \rangle \times t dt}{\int \langle \Gamma(B_s^0(t) \rightarrow \mu^+ \mu^-) \rangle dt} = \frac{\tau_{B_s}}{1 - y_s^2} \times \frac{1 + 2A_{\Delta\Gamma} y_s + y_s^2}{1 + A_{\Delta\Gamma} y_s}$$

- LHCb measured $\tau_{eff}(B_s^0 \rightarrow K^+ K^-)$ at 7% precision with 552 signal events which give an uncertainty on $A_{\Delta\Gamma}$ of 100%

- Assuming the same sensitivity (S/B = 10) for $B_s^0 \rightarrow \mu^+ \mu^-$, with 50 fb^{-1} :

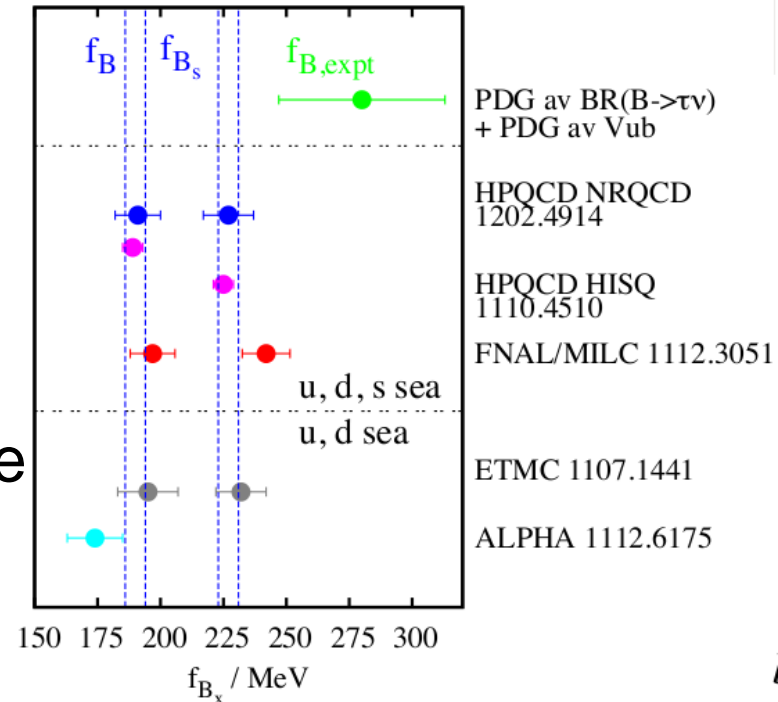
$$A_{\Delta\Gamma}^{\mu\mu} / \delta A_{\Delta\Gamma}^{\mu\mu} = 75\%$$



Uncertainty with new lattice F_B

- Recent works in Lattice QCD claims **uncertainties at 1.3%**
- Results still **discussed**
- 'Conservative' approach:

Central value from weighted average
+ uncertainty of 8 MeV



- If results confirmed:

$$BF(B_s^0 \rightarrow \mu^+ \mu^-) = 3.57 \pm 0.18 \times 10^{-9}$$

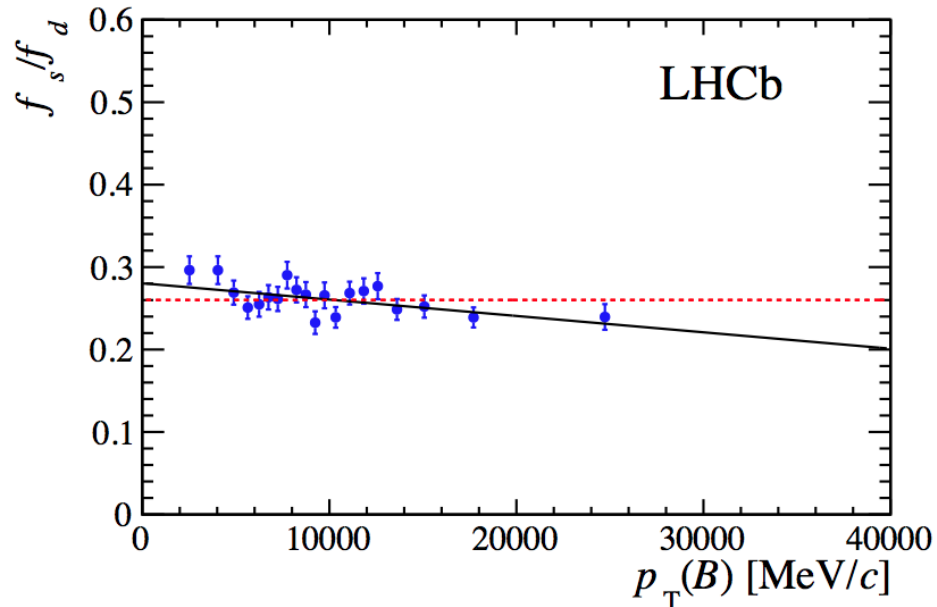
- Dominant uncertainty $|V_{tb}^* V_{ts}|$

Uncertainty Budget		
F_{B_s}	72.5%	27.0%
$ V_{tb}^* V_{ts} $	22.8%	60.0%
m_t	3.7%	9.8%
τ_{B_s} and y_s	1.1%	2.8%

Hadronisation Probability f_s/f_d

- f_s/f_d is measured at LHCb by comparing abundances of:
 - $B_s^0 \rightarrow D_s^- \pi^+$, $B^0 \rightarrow D^- K^+$ and $B^0 \rightarrow D^- \pi^+$ arXiv:111.2357 aka PRD85 032008 (2012)
 - $B_s^0 \rightarrow D_s^- \mu^+ X$ and $B^0 \rightarrow D^- \mu^+ X$ LHCb-paper-2012-037 in preparation
- Use $B(D_s^- \rightarrow K^+ K^- \pi^-)$ and τ_B
- at 7 TeV: $f_s/f_d = 0.259 \pm 0.015$

- p_T dependency small enough to be negligible
- \sqrt{s} dependency checked with $B^+ \rightarrow J/\psi K^+$ and $B_s^0 \rightarrow J/\psi \phi$: stable within 1σ



Exclusive Backgrounds :

$$B_s^0 \rightarrow K^+ \mu^- \bar{\nu}_\mu \text{ and } B^0 \rightarrow \pi^+ \mu^- \bar{\nu}_\mu$$

- Lower contribution from $B_s^0 \rightarrow K^+ \mu^- \bar{\nu}_\mu$ explained by:
 - $f_s/f_d = 0.26$
 - $B(B_s^0 \rightarrow K^+ \mu^- \bar{\nu}_\mu)/B(B^0 \rightarrow \pi^+ \mu^- \bar{\nu}_\mu) = 0.88$
 - $\epsilon_{K \rightarrow \mu}/\epsilon_{\pi \rightarrow \mu} = 0.28$ (RICH efficiency and $B(K^- \rightarrow \mu^- \bar{\nu}_\mu)/B(\pi^- \rightarrow \mu^- \bar{\nu}_\mu)$)

BDT Variables

Muon isolation: number of other tracks with which the muon can make a good vertex

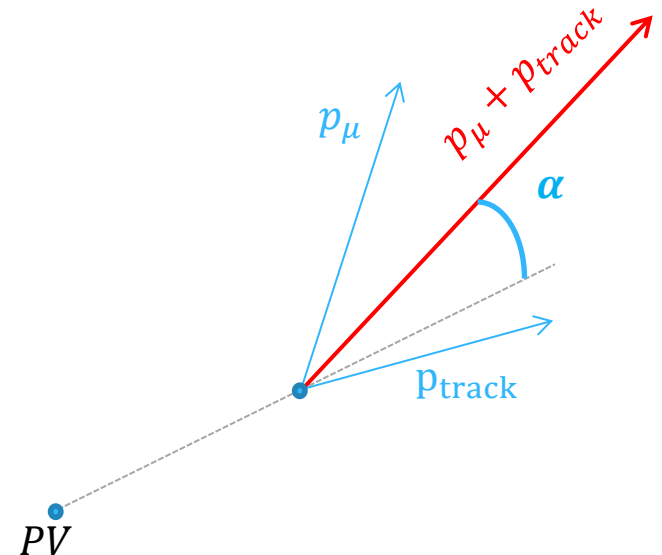
Other tracks requirement:

- Long track
- Impact Param Significance with PV > 3

Vertex requirement:

- Angle track-muon $< 0.27 \text{ rad}$
- Distance of Closest Approach $< 130 \mu\text{m}$
- Distance to PV: $0.5 \text{ cm} < d < 4 \text{ cm}$
- Distance to SV: $-0.15 \text{ cm} < d < 30 \text{ cm}$

$$\frac{|\vec{p}_\mu + \vec{p}_{track}| \sin \alpha}{|\vec{p}_\mu + \vec{p}_{track}| \sin \alpha + p_{T,\mu} + p_{T,track}} < 0.6$$



BDT Variables

Polarisation Angle:

angle between the muon momentum in the B rest frame and the vector perpendicular to the B momentum and the beam axis

B Isolation:

$$I = \frac{p_{T,B}}{p_{T,B} + \sum_{tracks} p_{T,track}}$$

sum running on the tracks such that $\delta\eta^2 + \delta\phi^2 < 1.0$

MVA Selection Variables

- B Candidate
 - impact parameter*
 - impact parameter χ^2
 - χ^2 of the vertex
 - pointing angle
 - distance of closest approach*
- Muons
 - min IP

*common with BDT