

Gluon saturation in high energy hadrons

SPhN, April 2010

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary

François Gelis
CEA, IPHT



① Deep Inelastic Scattering

② Gluon saturation at small x

③ DIS in the CGC framework

④ Connection to Nucleus-Nucleus collisions

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary

**DIS**

Inclusive DIS
Experimental results (I)
Experimental results (II)

Gluon saturation

Structure of a nucleon
Gluon evolution
Saturation domain
Multiple scatterings
Color Glass Condensate

DIS and CGC

Leading Order
NLO and Leading Logs
Inclusive DIS
Exclusive processes
EIC project

AA collisions

Stages of AA collisions
Energy-Momentum tensor
Correlations in rapidity

Summary**1 Deep Inelastic Scattering**

Inclusive DIS

Experimental results (I)

Experimental results (II)

2 Gluon saturation at small x

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate effective theory

3 DIS in the CGC framework

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

4 Connection to Nucleus-Nucleus collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity



DIS

Inclusive DIS

Experimental results (I)
Experimental results (II)

Gluon saturation

Structure of a nucleon
Gluon evolution
Saturation domain
Multiple scatterings
Color Glass Condensate

DIS and CGC

Leading Order
NLO and Leading Logs
Inclusive DIS
Exclusive processes
EIC project

AA collisions

Stages of AA collisions
Energy-Momentum tensor
Correlations in rapidity

Summary

1 Deep Inelastic Scattering

Inclusive DIS

Experimental results (I)
Experimental results (II)

2 Gluon saturation at small x

Structure of a nucleon
Gluon evolution
Saturation domain
Multiple scatterings
Color Glass Condensate effective theory

3 DIS in the CGC framework

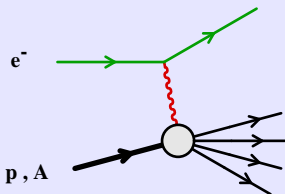
Leading Order
NLO and Leading Logs
Inclusive DIS
Exclusive processes
EIC project

4 Connection to Nucleus-Nucleus collisions

Stages of AA collisions
Energy-Momentum tensor
Correlations in rapidity

Basic idea : smash a well known probe on a nucleon or nucleus in order to try to figure out what is inside...

- Photons are very well suited for that purpose because their interactions are well understood
- **Deep Inelastic Scattering** : collision between an electron and a nucleon or nucleus, by exchange of a virtual photon



- Variant : collision with a neutrino, by exchange of Z^0 , W^\pm

DIS

Inclusive DIS

- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

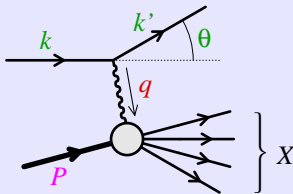
AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



Kinematical variables



- Note : the virtual photon is **space-like**: $q^2 \leq 0$

Other invariants of the reaction :

$$\nu \equiv P \cdot q$$

$$s \equiv (P + k)^2$$

$$M_x^2 \equiv (P + q)^2 = m_N^2 + 2\nu + q^2$$

- One uses commonly : $Q^2 \equiv -q^2$ and $x \equiv Q^2/2\nu$
- In general $M_x^2 \geq m_N^2$, and we have : $0 \leq x \leq 1$
($x = 1$ corresponds to the case of **elastic scattering**)

DIS

Inclusive DIS

- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



Inclusive cross-section :

$$E' \frac{d\sigma}{d^3\vec{k}'} = \frac{1}{32\pi^3(s - m_N^2)} \frac{e^2}{q^4} 4\pi L^{\mu\nu} W_{\mu\nu}$$

$$4\pi W_{\mu\nu} = \int d^4y e^{iq \cdot y} \left\langle \left\langle N \left| J_\nu^\dagger(y) J_\mu(0) \right| N \right\rangle \right\rangle_{\text{spin}}$$

- For DIS via photon exchange, the hadronic tensor reads

$$W_{\mu\nu} = -F_1 \left(g_{\mu\nu} - \frac{q_\mu q_\nu}{q^2} \right) + \frac{F_2}{\nu} \left(P_\mu - q_\mu \frac{P \cdot q}{q^2} \right) \left(P_\nu - q_\nu \frac{P \cdot q}{q^2} \right)$$

Inclusive DIS cross-section in the nucleon rest frame

$$\frac{d\sigma_{e-N}}{dE' d\Omega} = \frac{\alpha_{\text{em}}^2}{4m_N E^2 \sin^4(\theta/2)} \left[2 \sin^2(\theta/2) F_1 + \cos^2(\theta/2) \frac{m_N^2}{\nu} F_2 \right]$$

where Ω is the solid angle of the scattered electron

DIS

Inclusive DIS

- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary

**DIS**

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

Summary**1 Deep Inelastic Scattering**

Inclusive DIS

Experimental results (I)

Experimental results (II)

2 Gluon saturation at small x

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate effective theory

3 DIS in the CGC framework

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

4 Connection to Nucleus-Nucleus collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

- Bjorken scaling
- Asymptotic freedom
- Scaling violations



DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

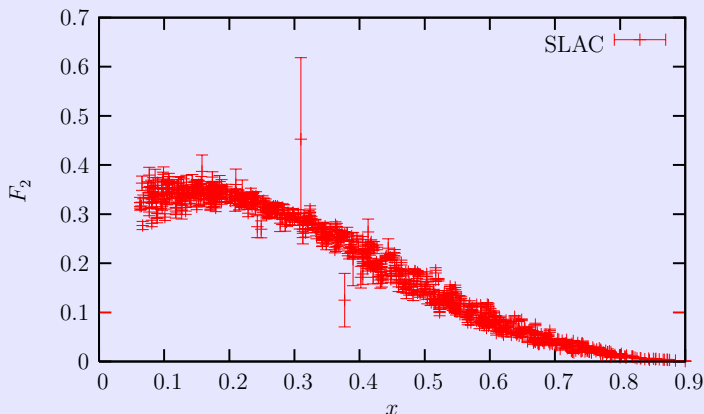
Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

Summary

Bjorken scaling : F_2 depends very weakly on Q^2



- Bjorken scaling implies that the constituents are quasi-free

DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

Stages of AA collisions

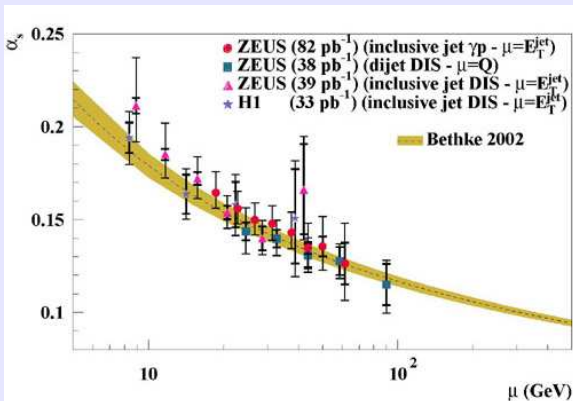
Energy-Momentum tensor

Correlations in rapidity

Summary



Asymptotic freedom



DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

Stages of AA collisions

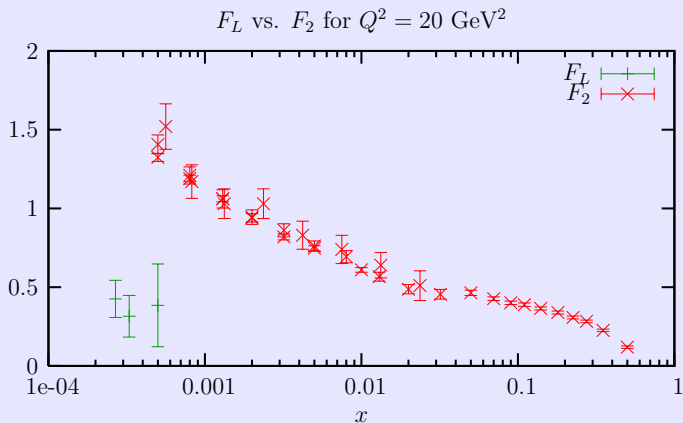
Energy-Momentum tensor

Correlations in rapidity

Summary

Longitudinal structure function

$F_L \equiv F_2 - 2xF_1$ is quite smaller than F_2



- The smallness of F_L implies that the struck partons are spin 1/2 point-like particles

DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

Summary



DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

Stages of AA collisions

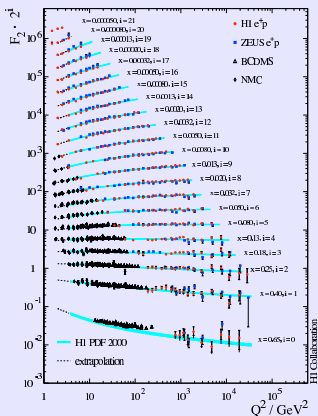
Energy-Momentum tensor

Correlations in rapidity

Summary

Scaling violations

Scaling violations



- Scaling violations probe the interactions among quark and gluons



1 Deep Inelastic Scattering

Inclusive DIS

Experimental results (I)

Experimental results (II)

2 Gluon saturation at small x

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate effective theory

3 DIS in the CGC framework

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

4 Connection to Nucleus-Nucleus collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

Summary

- Gluon growth at small x
- Geometric scaling
- F_L at small x and small Q^2



DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

Stages of AA collisions

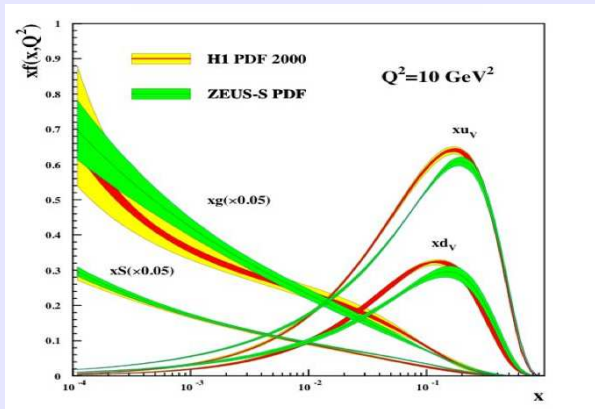
Energy-Momentum tensor

Correlations in rapidity

Summary

Growth of the gluon distribution at small x

Gluon distribution at small x



DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

Stages of AA collisions

Energy-Momentum tensor

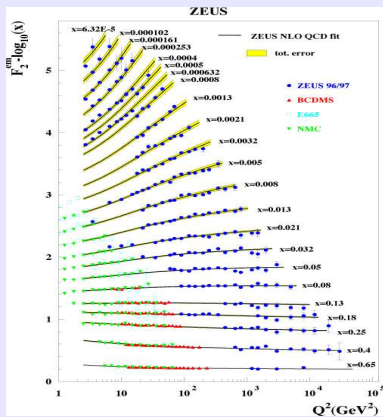
Correlations in rapidity

Summary



Geometrical scaling

Geometrical scaling : $\tau \sim Q^2 x^{0.3}$



DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

Stages of AA collisions

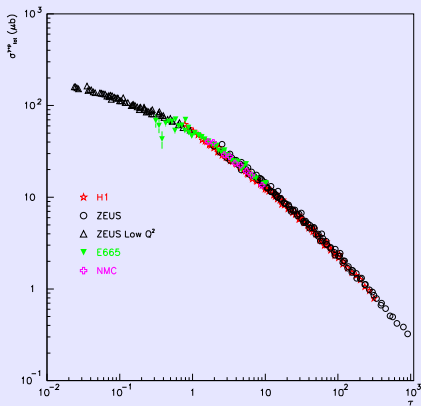
Energy-Momentum tensor

Correlations in rapidity

Summary



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DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

Stages of AA collisions

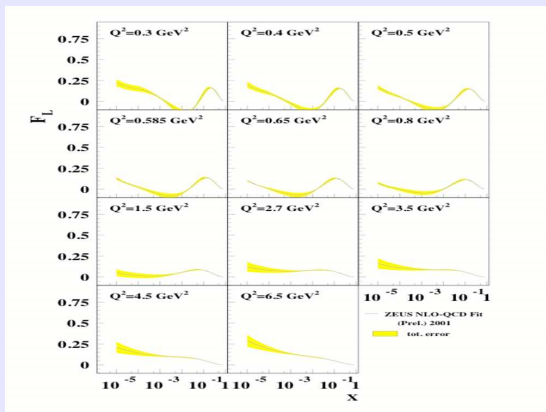
Energy-Momentum tensor

Correlations in rapidity

Summary

Some trouble with F_L at small Q^2

F_L from DIS fits



DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

Summary

**DIS**

Inclusive DIS
Experimental results (I)
Experimental results (II)

Gluon saturation

Structure of a nucleon
Gluon evolution
Saturation domain
Multiple scatterings
Color Glass Condensate

DIS and CGC

Leading Order
NLO and Leading Logs
Inclusive DIS
Exclusive processes
EIC project

AA collisions

Stages of AA collisions
Energy-Momentum tensor
Correlations in rapidity

Summary**1 Deep Inelastic Scattering**

Inclusive DIS
Experimental results (I)
Experimental results (II)

2 Gluon saturation at small x

Structure of a nucleon
Gluon evolution
Saturation domain
Multiple scatterings
Color Glass Condensate effective theory

3 DIS in the CGC framework

Leading Order
NLO and Leading Logs
Inclusive DIS
Exclusive processes
EIC project

4 Connection to Nucleus-Nucleus collisions

Stages of AA collisions
Energy-Momentum tensor
Correlations in rapidity

**DIS**

Inclusive DIS
Experimental results (I)
Experimental results (II)

Gluon saturation

Structure of a nucleon
Gluon evolution
Saturation domain
Multiple scatterings
Color Glass Condensate

DIS and CGC

Leading Order
NLO and Leading Logs
Inclusive DIS
Exclusive processes
EIC project

AA collisions

Stages of AA collisions
Energy-Momentum tensor
Correlations in rapidity

Summary**1 Deep Inelastic Scattering**

Inclusive DIS
Experimental results (I)
Experimental results (II)

2 Gluon saturation at small x

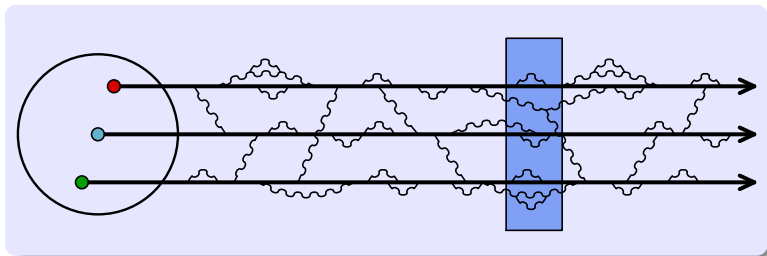
Structure of a nucleon
Gluon evolution
Saturation domain
Multiple scatterings
Color Glass Condensate effective theory

3 DIS in the CGC framework

Leading Order
NLO and Leading Logs
Inclusive DIS
Exclusive processes
EIC project

4 Connection to Nucleus-Nucleus collisions

Stages of AA collisions
Energy-Momentum tensor
Correlations in rapidity



At low energy:

- Fluctuations at all space-time scales smaller than its size
- Only the fluctuations that are longer lived than the external probe participate in the interaction process
- Interactions are very complicated if the constituents of the nucleon have a non trivial dynamics over time-scales comparable to those of the probe

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

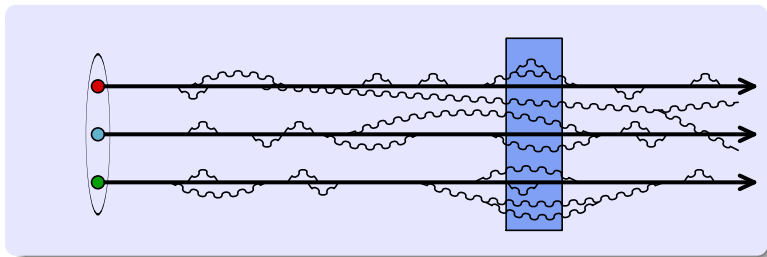
DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



At high energy:

- **Dilation** of all internal time-scales of the nucleon
- Interactions among constituents now take place over time-scales that are longer than the characteristic time-scale of the probe
 - ▷ **the constituents behave as if they were free**
- Many fluctuations live long enough to be seen by the probe
 - ▷ the nucleon appears **denser at small x**
- Pre-existing fluctuations are frozen over the time-scale of the probe, and act as static sources of new partons

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



1 Deep Inelastic Scattering

Inclusive DIS

Experimental results (I)

Experimental results (II)

2 Gluon saturation at small x

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate effective theory

3 DIS in the CGC framework

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

4 Connection to Nucleus-Nucleus collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

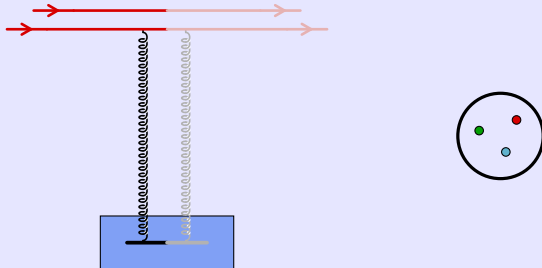
AA collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

Summary



- at low energy, the probe sees mostly the valence quarks

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

- Saturation domain
- Multiple scatterings
- Color Glass Condensate

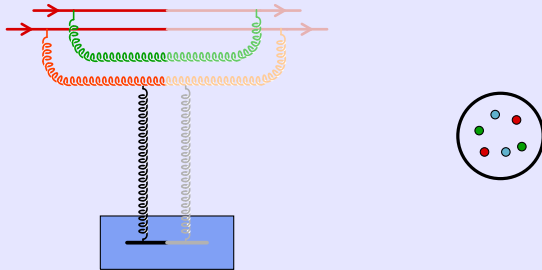
DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



- when energy increases, new partons are emitted
- the emission probability goes like $\alpha_s \int \frac{dx}{x} \sim \alpha_s \ln\left(\frac{1}{x}\right)$, with x the longitudinal momentum fraction of the gluon
- at small- x (i.e. high energy), these logs need to be resummed

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution**
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

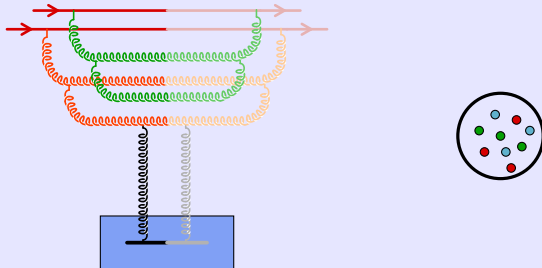
DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



- as long as the density of constituents remains small, the evolution is **linear**: the number of partons produced at a given step is proportional to the number of partons at the previous step (BFKL)

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution**
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

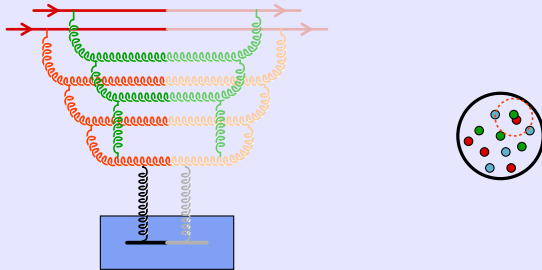
DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



- eventually, the partons start overlapping in phase-space
- **parton recombination** becomes favorable
- after this point, the evolution is **non-linear**:
the number of new partons depends non-linearly on the number of partons at the previous step

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution**
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



1 Deep Inelastic Scattering

Inclusive DIS

Experimental results (I)

Experimental results (II)

2 Gluon saturation at small x

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate effective theory

3 DIS in the CGC framework

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

4 Connection to Nucleus-Nucleus collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

Summary

Criterion for gluon recombination

Gribov, Levin, Ryskin (1983)

Number of gluons per unit area :

$$\rho \sim \frac{xG_A(x, Q^2)}{\pi R_A^2}$$

Recombination cross-section :

$$\sigma_{gg \rightarrow g} \sim \frac{\alpha_s}{Q^2}$$

Recombination happens if $\rho\sigma_{gg \rightarrow g} \gtrsim 1$, i.e. $Q^2 \lesssim Q_s^2$, with :

$$Q_s^2 \sim \frac{\alpha_s xG_A(x, Q_s^2)}{\pi R_A^2} \sim A^{1/3} \frac{1}{x^{0.3}}$$

Note: At a given energy, the saturation scale is larger for a nucleus (for $A = 200$, $A^{1/3} \approx 6$)

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution

Saturation domain

- Multiple scatterings
- Color Glass Condensate

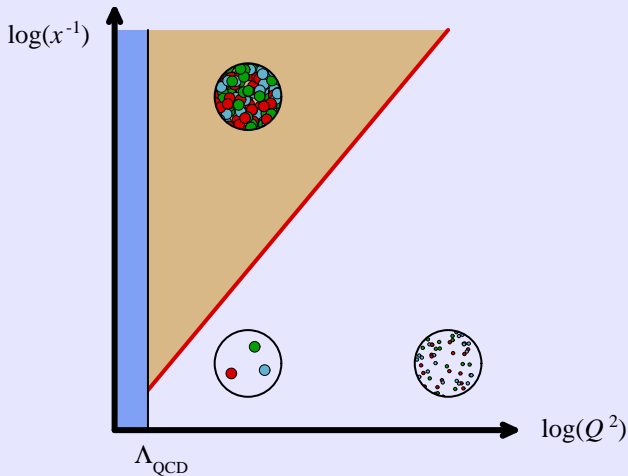
DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Glue saturation

- Structure of a nucleon
- Glue evolution

Saturation domain

- Multiple scatterings
- Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



1 Deep Inelastic Scattering

Inclusive DIS

Experimental results (I)

Experimental results (II)

2 Gluon saturation at small x

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate effective theory

3 DIS in the CGC framework

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

4 Connection to Nucleus-Nucleus collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

Summary



DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

Summary

- Power counting :

$$\frac{2 \text{ scatterings}}{1 \text{ scattering}} \sim \frac{Q_s^2}{P_\perp^2} \quad \text{with} \quad Q_s^2 \sim \alpha_s \frac{xG(x, Q_s^2)}{\pi R^2}$$

- When this ratio becomes ~ 1 , all the rescattering corrections become important

▷ one must resum all $[Q_s/P_\perp]^n$

- These effects are not accounted for in DGLAP or BFKL



1 Deep Inelastic Scattering

Inclusive DIS

Experimental results (I)

Experimental results (II)

2 Gluon saturation at small x

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate effective theory

3 DIS in the CGC framework

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

4 Connection to Nucleus-Nucleus collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

Summary

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings

Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



- Main difficulty: How to treat collisions involving a large number of partons?

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

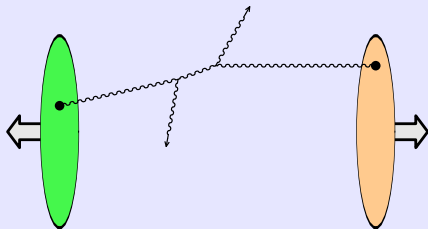
DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



- Main difficulty: How to treat collisions involving a large number of partons?
- Dilute regime : one parton in each projectile interact (what the standard perturbative techniques are made for)

Implications for a QCD approach

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings

Color Glass Condensate

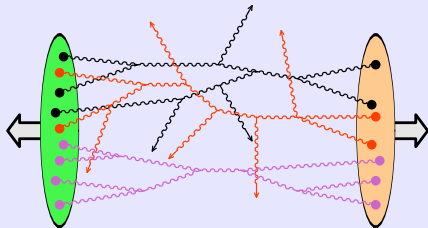
DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



- Main difficulty: How to treat collisions involving a large number of partons?
- **Dense regime** : **multiparton processes** become crucial
 - ▷ new techniques are required



Color Glass Condensate: Degrees of freedom

CGC = effective theory of small x gluons

- The fast partons ($k^+ > \Lambda^+$) are frozen by time dilation
 ▷ described as **static color sources** on the light-cone :

$$J^\mu = \delta^{\mu+} \rho(\mathbf{x}^-, \vec{\mathbf{x}}_\perp) \quad (0 < \mathbf{x}^- < 1/\Lambda^+)$$

- Slow partons ($k^+ < \Lambda^+$) cannot be considered static over the time-scales of the collision process
 ▷ they must be treated as standard gauge fields

Eikonal coupling to the current J^μ : $A_\mu J^\mu$

- The color sources ρ are **random**, and described by a **distribution functional** $W_{\Lambda^+}[\rho]$, with Λ^+ the longitudinal momentum that separates “soft” and “hard”

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings

Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



Evolution equation (JIMWLK) :

$$\frac{\partial W_{\Lambda^+}}{\partial \ln(\Lambda^+)} = \mathcal{H} W_{\Lambda^+}$$
$$\mathcal{H} = \frac{1}{2} \int_{\vec{x}_\perp, \vec{y}_\perp} \frac{\delta}{\delta \alpha(\vec{y}_\perp)} \eta(\vec{x}_\perp, \vec{y}_\perp) \frac{\delta}{\delta \alpha(\vec{x}_\perp)}$$

where $\alpha(\vec{x}_\perp) = \frac{1}{\nabla_\perp^2} \rho(1/\Lambda^+, \vec{x}_\perp)$

- $\eta(\vec{x}_\perp, \vec{y}_\perp)$ is a non-linear functional of ρ
- This evolution equation resums all the powers of $\alpha_s \ln(1/x)$ and of Q_s/p_\perp that arise in loop corrections
- This equation simplifies into the BFKL equation when the source ρ is small (one can expand η in powers of ρ)

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings

Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



1 Deep Inelastic Scattering

Inclusive DIS

Experimental results (I)

Experimental results (II)

2 Gluon saturation at small x

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate effective theory

3 DIS in the CGC framework

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

4 Connection to Nucleus-Nucleus collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

Summary



1 Deep Inelastic Scattering

Inclusive DIS

Experimental results (I)

Experimental results (II)

2 Gluon saturation at small x

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate effective theory

3 DIS in the CGC framework

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

4 Connection to Nucleus-Nucleus collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

Stages of AA collisions

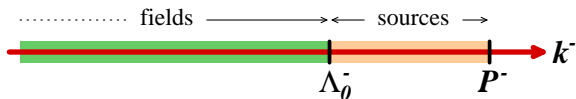
Energy-Momentum tensor

Correlations in rapidity

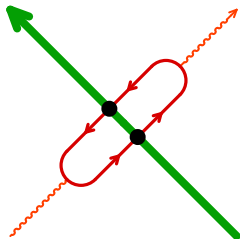
Summary

Inclusive DIS at Leading Order

- CGC effective theory with **cutoff at the scale Λ_0^-** :



- At **Leading Order**, DIS is an interaction between the target and a $q\bar{q}$ fluctuation of the virtual photon :



DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

Leading Order

- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



- Forward dipole amplitude at leading order:

$$\mathbf{T}_{\text{LO}}(\vec{\mathbf{x}}_{\perp}, \vec{\mathbf{y}}_{\perp}) = 1 - \frac{1}{N_c} \text{tr} \left(\underbrace{U(\vec{\mathbf{x}}_{\perp}) U^{\dagger}(\vec{\mathbf{y}}_{\perp})}_{\text{Wilson lines}} \right)$$

$$U(\vec{\mathbf{x}}_{\perp}) = \text{P exp } ig \int^{1/xP^-} dz^+ \mathcal{A}^-(z^+, \vec{\mathbf{x}}_{\perp})$$

$$[\mathcal{D}_{\mu}, \mathcal{F}^{\mu\nu}] = \delta^{\nu-} \rho(x^+, \vec{\mathbf{x}}_{\perp})$$

▷ at LO, the scattering amplitude on a saturated target is entirely given by classical fields

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

Leading Order

- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



1 Deep Inelastic Scattering

Inclusive DIS

Experimental results (I)

Experimental results (II)

2 Gluon saturation at small x

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate effective theory

3 DIS in the CGC framework

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

4 Connection to Nucleus-Nucleus collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

Stages of AA collisions

Energy-Momentum tensor

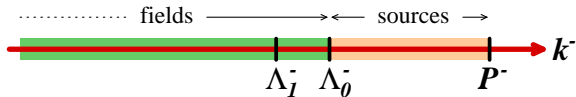
Correlations in rapidity

Summary

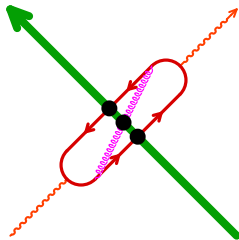


Inclusive DIS at NLO

- Consider now quantum corrections to the previous result, restricted to **field modes with $\Lambda_1^- < k^- < \Lambda_0^-$** (the upper bound prevents double-counting with the sources):



- At **NLO**, the $q\bar{q}$ dipole must be corrected by a gluon, e.g. :



DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

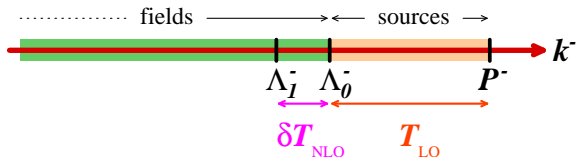
- Leading Order
- NLO and Leading Logs

- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



- At **leading log accuracy**, the contribution of the quantum modes in that strip is :

$$\delta T_{\text{NLO}}(\vec{x}_{\perp}, \vec{y}_{\perp}) = \ln \left(\frac{\Lambda_0^-}{\Lambda_1^-} \right) \mathcal{H} T_{\text{LO}}(\vec{x}_{\perp}, \vec{y}_{\perp})$$

\mathcal{H} = Hamiltonian of the JIMWLK evolution equation

- These NLO corrections can be absorbed in the LO result by a redefinition of the distribution of sources

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs

- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



- By iterating the previous process to integrate out all the slow field modes at leading log accuracy:

Inclusive DIS at Leading Log accuracy

$$\sigma_{\gamma^* T} = \int_0^1 dz \int d^2 \vec{r}_\perp |\psi(\mathbf{q}|z, \vec{r}_\perp)|^2 \sigma_{\text{dipole}}(\mathbf{x}, \vec{r}_\perp)$$
$$\sigma_{\text{dipole}}(\mathbf{x}, \vec{r}_\perp) \equiv 2 \int d^2 \vec{X}_\perp \int [D\rho] W_{xP-}[\rho] T_{\text{LO}}(\vec{x}_\perp, \vec{y}_\perp)$$

▷ the x dependence of the dipole cross-section can be predicted from the JIMWLK evolution equation

▷ one needs an initial condition at some x_0

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs

- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



1 Deep Inelastic Scattering

Inclusive DIS

Experimental results (I)

Experimental results (II)

2 Gluon saturation at small x

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate effective theory

3 DIS in the CGC framework

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

4 Connection to Nucleus-Nucleus collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

Summary



- In the saturated regime, the dipole cross-section depends on x and \vec{r}_\perp only through the combination

$$Q_s(x) |\vec{r}_\perp|$$

- If one neglects the light quark masses, the photon wavefunction depends only on

$$Q |\vec{r}_\perp|$$

▷ the $\gamma^* p$ cross-section depends only on

$$Q^2 / Q_s^2(x)$$

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs

Inclusive DIS

- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

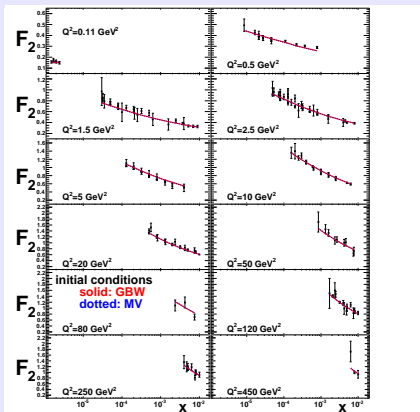
Summary



DIS fit at small x based on the CGC

Albacete, Armesto, Milhano, Salgado (2009)

Inclusive F_2



DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs

Inclusive DIS

- Exclusive processes
- EIC project

AA collisions

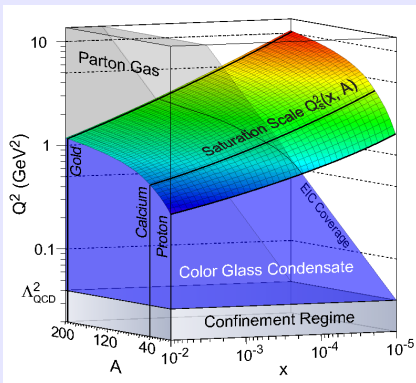
- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



Extraction of $Q_s(x)$

Kowalski, Lappi, Venugopalan (2007)



(figure from T. Ullrich)

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Glouon saturation

- Structure of a nucleon
- Glouon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs

Inclusive DIS

- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



1 Deep Inelastic Scattering

Inclusive DIS

Experimental results (I)

Experimental results (II)

2 Gluon saturation at small x

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate effective theory

3 DIS in the CGC framework

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

4 Connection to Nucleus-Nucleus collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

Summary



Kowalski, Motyka, Watt (2006)

- So far, we have only considered the total DIS cross-section, obtained from the forward dipole amplitude via the optical theorem
- In order to study more exclusive processes, one needs non-forward amplitudes. They read :

$$\langle \Omega | \gamma^* \rangle = \int d^2 \vec{r}_\perp \int_0^1 dz \Psi_\Omega^* \psi \underbrace{\int d^2 \vec{b} e^{i \vec{q}_\perp \cdot \vec{b}} \left\langle T \left(\vec{b} - \frac{\vec{r}_\perp}{2}, \vec{b} + \frac{\vec{r}_\perp}{2} \right) \right\rangle}_{\text{non-forward dipole cross-section}}$$

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS

Exclusive processes

- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary

- By squaring this amplitude, one gets the diffractive cross-section for the production of the state Ω with momentum transfer \mathbf{q}_\perp

$$\frac{d\sigma_{\gamma^* p \rightarrow \Omega p}^{\text{diff}}}{d^2\vec{q}_\perp} = |\langle \Omega | \gamma^* \rangle|^2$$

- The relationship to the inclusive DIS cross-section is

$$\sigma_{\gamma^* p}^{\text{tot}}(Y, Q^2) = 2 \text{Im} \langle \gamma^* | \gamma^* \rangle_{\vec{q}_\perp=0}$$

Note : inclusive DIS only constrains the dipole amplitude averaged over impact parameter. However, if one measures the \mathbf{q}_\perp dependence in exclusive reactions, one obtains informations about the \mathbf{b} dependence of the dipole amplitude

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS

Exclusive processes

- EIC project

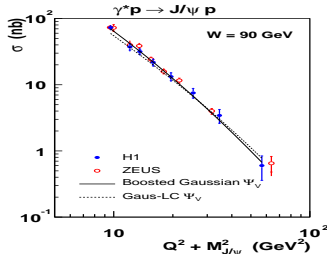
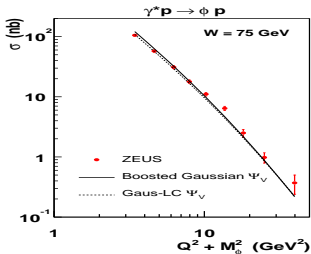
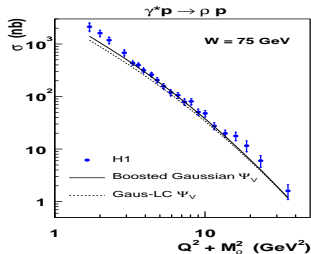
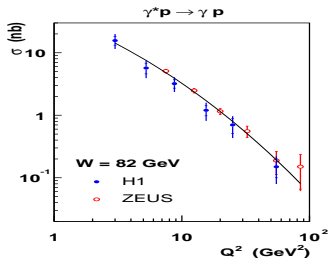
AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary

Exclusive reactions

- Exclusive photon and vector meson production :



DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS

Exclusive processes

- EIC project

AA collisions

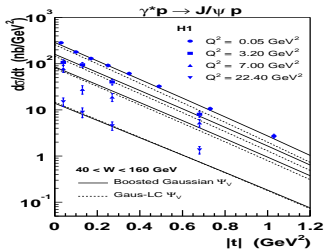
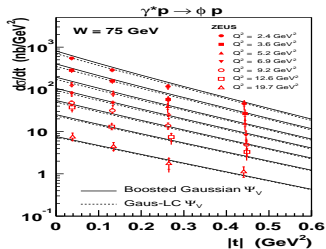
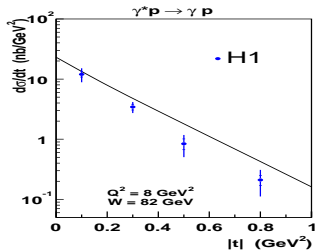
- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



Exclusive reactions

- Exclusive photon and vector meson production :



DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS

Exclusive processes

- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



1 Deep Inelastic Scattering

Inclusive DIS

Experimental results (I)

Experimental results (II)

2 Gluon saturation at small x

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate effective theory

3 DIS in the CGC framework

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

4 Connection to Nucleus-Nucleus collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

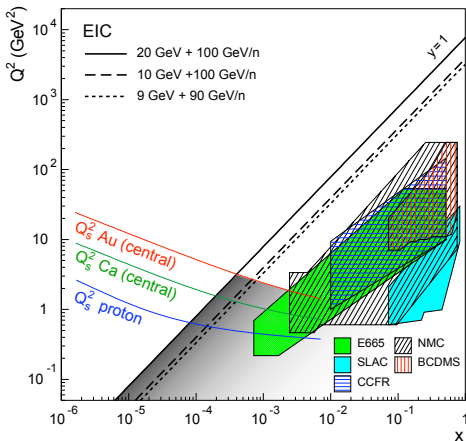
Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

Summary

Kinematical coverage



DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

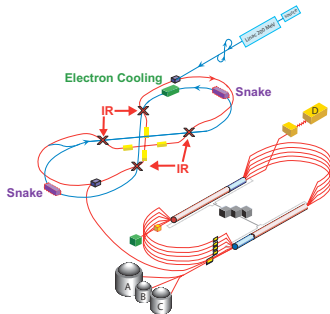
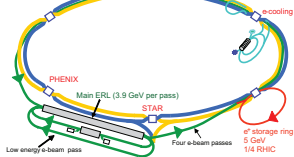
- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes

EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



Note: An EIC project is also being discussed at CERN (LHeC)

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes

EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



1 Deep Inelastic Scattering

Inclusive DIS

Experimental results (I)

Experimental results (II)

2 Gluon saturation at small x

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate effective theory

3 DIS in the CGC framework

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

4 Connection to Nucleus-Nucleus collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

Summary



1 Deep Inelastic Scattering

Inclusive DIS

Experimental results (I)

Experimental results (II)

2 Gluon saturation at small x

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate effective theory

3 DIS in the CGC framework

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

4 Connection to Nucleus-Nucleus collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

Stages of AA collisions

Energy-Momentum tensor

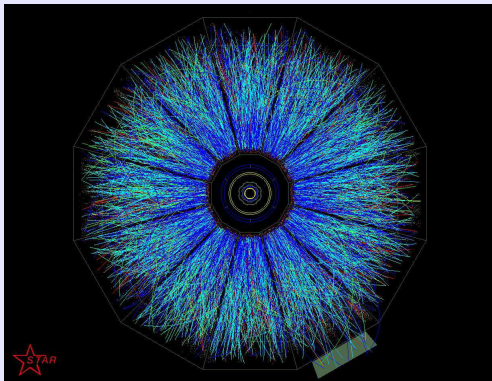
Correlations in rapidity

Summary



Longitudinal momentum fraction in AA collisions

Nucleus-Nucleus collision



- 99% of the multiplicity below $p_{\perp} \sim 2 \text{ GeV}$
 - $x \sim 10^{-2}$ at RHIC ($\sqrt{s} = 200 \text{ GeV}$)
 - $x \sim 4 \cdot 10^{-4}$ at the LHC ($\sqrt{s} = 5.5 \text{ TeV}$)
- ▷ partons at small x are the most important

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary

Stages of a nucleus-nucleus collision

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

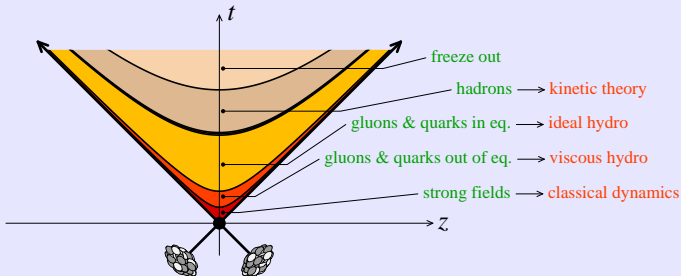
DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



- The Color Glass Condensate provides a framework to describe nucleus-nucleus collisions up to a time $\tau \sim Q_s^{-1}$
- Subsequent stages are usually described as fluid dynamics



1 Deep Inelastic Scattering

Inclusive DIS

Experimental results (I)

Experimental results (II)

2 Gluon saturation at small x

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate effective theory

3 DIS in the CGC framework

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

4 Connection to Nucleus-Nucleus collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

Summary



Equations of hydrodynamics = energy-momentum conservation:

$$\partial_\mu T^{\mu\nu} = 0$$

Inputs from the underlying microscopic theory :

EoS : $p = f(\epsilon)$, Transport coefficients : η, ζ, \dots

- Required initial conditions : $T^{\mu\nu}(\tau = \tau_0, \eta, \vec{\mathbf{x}}_\perp)$

DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

Stages of AA collisions

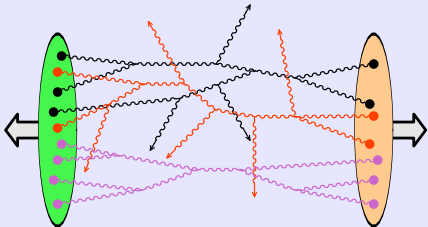
Energy-Momentum tensor

Correlations in rapidity

Summary



$$J^\mu \equiv \delta^{\mu+} \rho_1(x^-, \vec{x}_\perp) + \delta^{\mu-} \rho_2(x^+, \vec{x}_\perp)$$
$$\mathcal{S} = \underbrace{-\frac{1}{2} \int d^4x \operatorname{tr} F_{\mu\nu} F^{\mu\nu}}_{\text{gluon interactions}} + \int d^4x J^\mu A_\mu$$



Note: the dots denote insertions of the color current J^μ

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions

Energy-Momentum tensor

- Correlations in rapidity

Summary



DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions

Energy-Momentum tensor

- Correlations in rapidity

Summary

- Small coupling expansion for $T^{\mu\nu}$:

$$T^{\mu\nu} = \frac{Q_s^4}{g^2} \left[c_0 + c_1 g^2 + c_2 g^4 + \dots \right]$$

- The Leading Order contribution is given by **classical fields** :

$$T_{\text{LO}}^{\mu\nu} \equiv c_0 \frac{Q_s^4}{g^2} = \frac{1}{4} g^{\mu\nu} \mathcal{F}^{\lambda\sigma} \mathcal{F}_{\lambda\sigma} - \mathcal{F}^{\mu\lambda} \mathcal{F}^{\nu}_{\lambda}$$

with $\underbrace{[\mathcal{D}_\mu, \mathcal{F}^{\mu\nu}]}_{\text{Yang-Mills equation}} = \mathcal{J}^\nu$, $\lim_{t \rightarrow -\infty} \mathcal{A}^\mu(t, \vec{x}) = 0$



Initial conditions from CGC: Leading Log resummation

- The previous power counting implicitly assumes that the coefficients c_n are numbers of order one. However, large logarithms of the CGC cutoffs appear at NLO
- Like in DIS, the coefficients of the logs are given by the action of the JIMWLK Hamiltonian on the LO observable:

$$\delta T_{\text{NLO}}^{\mu\nu} = \left[\ln \left(\frac{\Lambda_0^-}{\Lambda_1^-} \right) \mathcal{H}_1 + \ln \left(\frac{\Lambda_0^+}{\Lambda_1^+} \right) \mathcal{H}_2 \right] T_{\text{LO}}^{\mu\nu}$$

- By resumming the leading logs, one obtains:

$$\langle T^{\mu\nu}(\tau, \eta, \vec{x}_\perp) \rangle_{\text{LLog}} = \int [D\rho_1 D\rho_2] W_1[\rho_1] W_2[\rho_2] \underbrace{T_{\text{LO}}^{\mu\nu}(\tau, \vec{x}_\perp)}_{\text{for fixed } \rho_{1,2}}$$

(FG, Lappi, Venugopalan (2008))

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions

Energy-Momentum tensor

- Correlations in rapidity

Summary

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

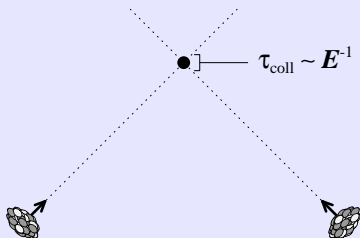
AA collisions

- Stages of AA collisions

Energy-Momentum tensor

- Correlations in rapidity

Summary



- The duration of the collision is very short: $\tau_{\text{coll}} \sim E^{-1}$

DIS

Inclusive DIS
Experimental results (I)
Experimental results (II)

Gluon saturation

Structure of a nucleon
Gluon evolution
Saturation domain
Multiple scatterings
Color Glass Condensate

DIS and CGC

Leading Order
NLO and Leading Logs
Inclusive DIS
Exclusive processes
EIC project

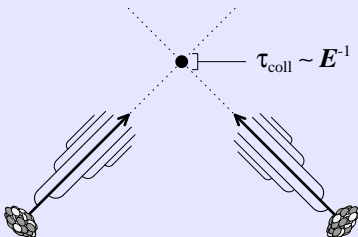
AA collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

Summary



- The duration of the collision is very short: $\tau_{\text{coll}} \sim E^{-1}$
- The logarithms we need to resum arise from the radiation of soft gluons, which takes a long time
 - ▷ it must happen (long) before the collision

DIS

Inclusive DIS
Experimental results (I)
Experimental results (II)

Gluon saturation

Structure of a nucleon
Gluon evolution
Saturation domain
Multiple scatterings
Color Glass Condensate

DIS and CGC

Leading Order
NLO and Leading Logs
Inclusive DIS
Exclusive processes
EIC project

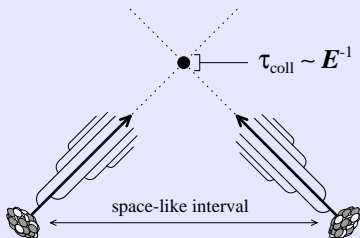
AA collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

Summary



- The duration of the collision is very short: $\tau_{\text{coll}} \sim E^{-1}$
- The logarithms we need to resum arise from the radiation of soft gluons, which takes a long time
 - ▷ it must happen (long) before the collision
- The projectiles are not in causal contact before the impact
 - ▷ the logarithms are intrinsic properties of the projectiles, independent of the measured observable



1 Deep Inelastic Scattering

Inclusive DIS

Experimental results (I)

Experimental results (II)

2 Gluon saturation at small x

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate effective theory

3 DIS in the CGC framework

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

4 Connection to Nucleus-Nucleus collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

Summary



- The factorization valid for $\langle T^{\mu\nu} \rangle$ can be extended to multi-point correlations :

$$\begin{aligned} \langle T^{\mu_1\nu_1}(\tau, \eta_1, \vec{x}_{1\perp}) \cdots T^{\mu_n\nu_n}(\tau, \eta_n, \vec{x}_{n\perp}) \rangle_{\text{LLog}} &= \\ &= \int [D\rho_1 D\rho_2] W_1[\rho_1] W_2[\rho_2] \\ &\quad \times T_{\text{LO}}^{\mu_1\nu_1}(\tau, \vec{x}_{1\perp}) \cdots T_{\text{LO}}^{\mu_n\nu_n}(\tau, \vec{x}_{n\perp}) \end{aligned}$$

▷ at leading log accuracy, all the correlations come from the distributions $W_{1,2}[\rho_{1,2}]$ (i.e. they pre-exist in the wavefunctions of the incoming projectiles)

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

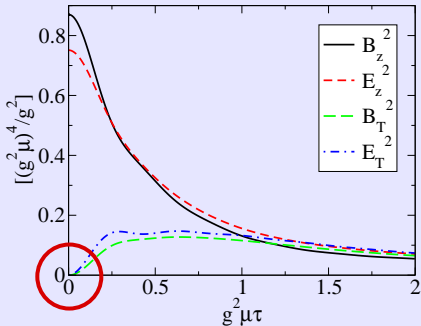
- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary

Initial classical fields

Lappi, McLerran (2006)

- Immediately after the collision, the chromo- \vec{E} and \vec{B} fields are purely longitudinal and boost invariant :



DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

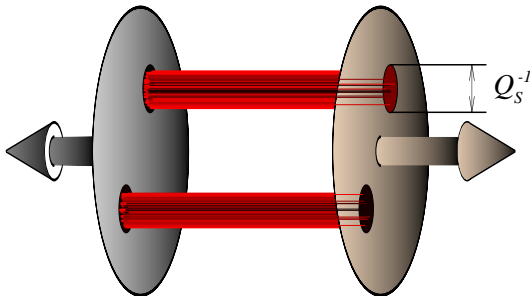
- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary

- The initial chromo- \vec{E} and \vec{B} fields form longitudinal “flux tubes” extending between the projectiles:



- The color correlation length in the transverse plane is Q_s^{-1}
 - ▷ flux tubes of diameter Q_s^{-1} , filling up the transverse area
- The correlation length in the η direction is $\Delta\eta \sim \alpha_s^{-1}$
 - ▷ long range rapidity correlations expected in the data

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary

Importance of initial rapidity correlations

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

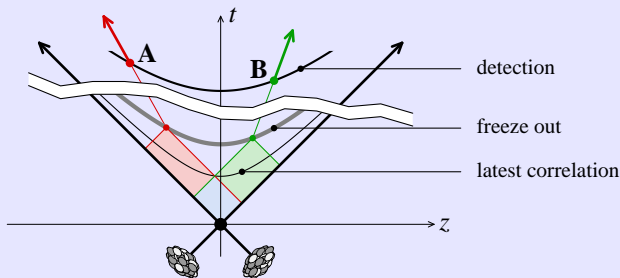
DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

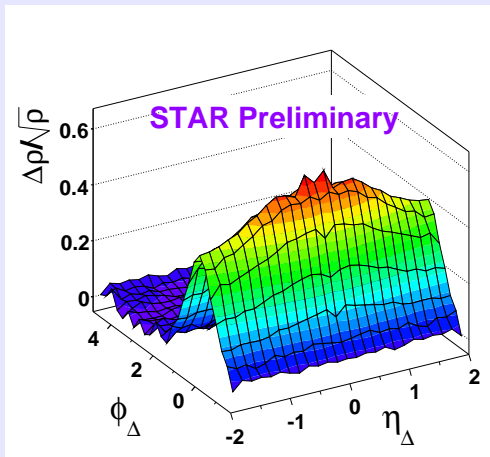
Summary



Long range rapidity correlations must be created early

$$t_{\text{correlation}} \leq t_{\text{freeze out}} e^{-\frac{1}{2}|\eta_A - \eta_B|}$$

▷ the near η -independence of the initial color fields should induce a long range correlation in rapidity among the produced particles



- Long range correlation in $\Delta\eta$ (rapidity)
- Narrow correlation in $\Delta\varphi$ (azimuthal angle)

DIS

- Inclusive DIS
- Experimental results (I)
- Experimental results (II)

Gluon saturation

- Structure of a nucleon
- Gluon evolution
- Saturation domain
- Multiple scatterings
- Color Glass Condensate

DIS and CGC

- Leading Order
- NLO and Leading Logs
- Inclusive DIS
- Exclusive processes
- EIC project

AA collisions

- Stages of AA collisions
- Energy-Momentum tensor
- Correlations in rapidity

Summary



- The dynamics of gluons at small x is altered by high density effects \triangleright saturation
- At a given energy, gluon saturation is more important for nuclei
- Saturation plays an important role in DIS at small x and in the description of nucleus-nucleus collisions
- A factorization theorem relates DIS and AA collisions in the saturated regime
- Design goals of an eA collider for saturation studies :
 - Energy comparable to that of HERA
 - Much higher luminosity than HERA
 - Variable \sqrt{s} for direct measurement of F_L
 - Detector with good η coverage

DIS

Inclusive DIS

Experimental results (I)

Experimental results (II)

Gluon saturation

Structure of a nucleon

Gluon evolution

Saturation domain

Multiple scatterings

Color Glass Condensate

DIS and CGC

Leading Order

NLO and Leading Logs

Inclusive DIS

Exclusive processes

EIC project

AA collisions

Stages of AA collisions

Energy-Momentum tensor

Correlations in rapidity

Summary