Mesures de précision et tests fondamentaux :

- La mesure de la constante de structure fine
- La détermination de la distribution de charge du proton

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Two effects of the quantum electrodynamics

Electron anomaly

Kusch and Foley *Phys. Rev.* **72**, 1256 (1947)



Lamb shift

Lamb and Retherford, *Phys. Rev.* **72**, 241 (1947)





Bloch oscillations

Determination of the fine structure constant

Measurement of the ratio h/M Determination of the fine structure constant

h/M is given by the recoil effect



Alpha is deduced from the ratio h/M

Rydberg constant in terms of energy :

$$hc R_{\infty} = \frac{1}{2}m_e c^2 \alpha^2$$

The measurement of *h/M* allows to determine α

$$\alpha^2 = \frac{2R_{\infty}}{c} \times \frac{h}{m_e}$$

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The measurement of h/M allows to determine α

$$\alpha^{2} = \frac{2R_{\infty}}{c} \times \frac{M}{m_{p}} \times \frac{m_{p}}{m_{e}} \times \frac{h}{M}$$

Relative uncertainty on each term : - Rydberg constant : 5×10^{-12} - mass ratio $M/m_{\rm p}$: 1,2×10⁻¹⁰

- mass ratio
$$\, m_{
m p}/m_{
m e}\,$$
 : 4,1×10⁻¹⁰

Experiments : Cs atoms (Stanford) Rb atoms (Paris)

Bloch oscillations

In a periodic potential, a particle oscillates

$$mv = h/\lambda_{DB}$$
$$mv = Ft$$
$$\tau_B = \frac{h}{Fd}$$



Atoms in a vertical standing wave



Coherent acceleration



M. Ben Dahan, E. Peik, J. Reichel, Y. Castin and C. Salomon , PRL. 76 (1996) 4508.

S.R. Wilkinson, C.F. Bharucha, K.W. Madison, Quian Niu and G.M. Raizen, PRL 76 (1996) 4512.

Band structure



Accélération ⇔ oscillations de Bloch dans la bande fondamentale



 $2\hbar k$ par oscillation Grande efficacité (99.95%)

















Principle of our experiment



$$\sigma_{v_r} = \sigma_v/2N$$



Combining Bloch oscillations with interferometry

Bloch oscillations are a coherent process Tranfer of recoils to any velocity distribution that fit into the first Brillouin zone



Measurement of the recoil velocity : determination of h/m (I)



Measurement of the recoil velocity : determination of h/m (II)



Observation of the interference fringes



Data acquisition time: 5 minutes

Relative uncertainty on h/m: 5.2×10⁻⁹ \rightarrow 2.6×10⁻⁹ on α

Results of one night acquisition



Relative uncertainty on h/m: 4.4×10⁻¹⁰ and 2.2×10⁻¹⁰ on α

Very good reliability of the experiment

Uncertainty budget

Source	Correction (α ⁻¹)(ppb)	Uncertainty (ppb)
Laser frequencies		0,13
Laser beams alignement	-0,33	0,33
Wave front curvature		
and Gouy phase	-2,51	0,3
Second order Zeeman effect	0,4	0,3
Light shift (1 photon)		0,01
Light shift(2 photon)		0,001
Light shift (Bloch)		0,05
Gravity gradient	-0,2	0,02
Refraction index of atom cloud		
and interactions		0,2
Total of the systematic effects	-2,64	0,59
Statistics		0,2
Rydberg constant and mass ratio		0,22
Final uncertainty		0,66

Electron anomaly and QED test

$$a_{e} = C_{1} \left(\frac{\alpha}{\pi}\right) + C_{2} \left(\frac{\alpha}{\pi}\right)^{2} + C_{3} \left(\frac{\alpha}{\pi}\right)^{3} + C_{4} \left(\frac{\alpha}{\pi}\right)^{4} + a \left(m_{e} / m_{\mu}, m_{e} / m_{\tau}, weak, hadron\right) + \dots$$

Expérience (Harvard University, 2008) : \longrightarrow $a_{e} = 0.001 \ 159 \ 652 \ 180 \ 73(28)$
LKB-10 (Paris) $1 / \alpha = 137.035 \ 999 \ 037(91) \longrightarrow$ $a_{e} = 0.001 \ 159 \ 652 \ 181 \ 88(78)$



Spectroscopy of atomic hydrogen

From the Rydberg constant to the size of the proton

A brief history

The simplest atom in nature : proton + electron involved in major advances of atomic physics and quantum mechanics



Balmer lines : n = 2

The energy levels of hydrogen atom



First explanation

Hydrogen is made with a nucleus and an electron (Rutherford 1911)

Bohr's model (1913): the frequency of the light is determined by the difference in energy between two states. The electron follows a circular orbit and the angular momentum is quantized: $n\hbar$

$$E = -\frac{R_H hc}{n^2}$$

$$R_H = R_\infty \left(1 + m_e / m_p\right)^{-1}$$

The Rydberg constant is linked to other fundamental constants

$$R_{\infty} = \frac{m_e e^4}{8\varepsilon_0^2 h^3 c}$$

Rydberg constant: relative uncertainty



The energy levels of hydrogen atom



Proton

Structure

2 quarks up (2/3 e) + 1 quark down (-1/3 e) + strong interaction (gluons)

Proton charge radius : r_{p}

$$r_{\rm p} = \sqrt{\langle r^2 \rangle} \qquad \langle r^2 \rangle = \frac{\int r^2 \rho(r) \, d^3 r}{\int \rho(r) \, d^3 r}$$

 $\rho(\textbf{r})$: proton charge distribution

QCD Calculations

• r_p (< 5%)

Electron-proton scattering



$$\frac{d\sigma}{d\Omega}(\mathsf{E}_{\mathsf{i}},\theta) \approx \left[\frac{d\sigma}{d\Omega}(\mathsf{E}_{\mathsf{i}},\theta)\right] \mathsf{G}(\mathsf{q}^{\mathsf{2}})$$

Rutherford

$$G(q^{2}) = \int d^{3}r \, e^{iqr} \frac{\rho(r)}{4\pi} \approx 1 - \frac{r_{p}^{2}}{6}q^{2}$$

Limiting factor

Calculation of the Lamb shift

The table below gives the various contributions to the Lamb shift

Term of the Lamb shift	Value for the 1S level	Uncertainties	_
Self-energy (one-loop)	$8383339.472\mathrm{kHz}$	$0.008 \mathrm{~kHz}$	-
Vacuum polarization (one-loop)	-214816.607 kHz	$0.001 \mathrm{~kHz}$	
Recoil corrections	$2401.701{\rm kHz}$	$0.780 \mathrm{\ kHz}$	
Proton size	1209.000 kHz	22 kHz	
Two-loop corrections	$727.700 \mathrm{kHz}$	2.000 kHz	
Radiative recoil corrections	-12.321 kHz	$0.740 \mathrm{\ kHz}$	
Vacuum polarization (muon)	-5.068 kHz	$< 0.001 \ \rm kHz$	
Vacuum polarization (hadron)	-3.401 kHz	$0.076 \mathrm{\ kHz}$	
Proton self-energy	$4.618 \mathrm{kHz}$	$0.160 \mathrm{kHz}$	
Three-loop corrections	$1.800 \mathrm{kHz}$	1.000 kHz	
Nuclear size corrections to SE and VP	-0.143 kHz	$0.011 \mathrm{\ kHz}$	
Proton polarization	-0.070 kHz	$0.013 \mathrm{~kHz}$	_
1S Lamb shift	8172847(23) kHz		_

The uncertainties of the one-loop corrections are mainly due to α

The theoretical uncertainty (QED) is ~ 2.5 kHz

Optical spectroscopy of hydrogen gives a test of QED until the two-loop corrections if the proton radius is known

Two-photon spectroscopy of the 1S-2S transition

This transition has been extensively studied by the T.W. Hänsch's group first in Stanford and then in Garching

natural width : 1.3 Hz !

First observation

with a cw laser: C.J. Foot, B. Couillaud, R.G. Beausoleil and T.W. Hänsch Phys. Rev. Lett. <u>54</u>, 1913 (1985)



Absolute frequency measurement of the 1S-2S hydrogen transition



Nobel Prize 2005 half awarded jointly to J. L. Hall and T.W. Hänsch

"for their contributions to the development of laser-based precision spectroscopy, including the optical frequency comb technique"

Frequency measurement:

2466 061 413 187 018 (11) Hz

accuracy of 4.5×10^{-15}

A. Matveev *et al.* Phys. Rev. Lett. <u>110</u>, 230801 (2013)

Test of the stability of fundamental constants : no drift observed at a level of 10⁻¹⁵ per year

Two-photon spectroscopy in hydrogen

The 1S-2S two-photon transition has been measured at a very high level of precision but the determination of the Rydberg constant and of the Lamb shifts needs the comparison of different optical frequencies



Our group in Paris has studied :

the 2S-nS et 2S-nD two-photon transitions from the metastable state towards the n = 8 and 12 levels

and the 1S-3S two-photon transition from the ground state

The 2S-nS and 2S-nD transitions





Measurement of the 2S-8S and 2S-8D frequencies (SYRTE-LKB)

First pure frequency measurement in 1993



B. de Beauvoir *et al.*, Phys. Rev. Lett. 78, 440 (1997) and Eur. Phys. J. D <u>12</u>, 61 (2000)

f (2S_{1/2}-8D_{5/2}) = 770 649 561 584.2 (6.4) kHz

relative uncertainty 8.3 x 10⁻¹²

How determine the Rydberg constant?

There are several way to deduce the Rydberg constant from the 1S-2S interval, the 2S-nD interval or from their combination

- B. de Beauvoir et al, Eur. Phys. J. D 12, 61 (2000)
- F. Biraben et al., in « The Hydrogen atom : precision physics of simple atomic systems » Springer (2001)
 F. Biraben, Eur. Phys. J. Special topics <u>172</u>, 109 (2009)
- From the 1S-2S frequency, using Lamb shifts deduced from QED calculations \rightarrow uncertainty ~9 x 10⁻¹² mainly limited by the proton size
- From the 2S-nD frequencies, using the 2S Lamb shift from QED calculations \rightarrow uncertainty ~7 x 10⁻¹² mainly limited by the frequency measurement and the proton size
- From the 2S-nD frequency, using the measured 2S Lamb shift
 → uncertainty ~10.6 x 10⁻¹² mainly limited by 2S Lamb shift mesurement
 independent from the proton size

Determination of the Rydberg constant

• From the 1S-2S and 2S-nD intervals, using the scaling law of the Lamb shift The Lamb shifts vary aproximatively as $1/n^3$; the deviation from this law is given by Δ_2 $\Delta_2 = L_{1S_{1/2}} - 8L_{2S_{1/2}}$

This quantity has been calculated very precisely and is independent from the proton size

S.G. Karshenboim, J. Phys. B<u>29</u>, L29 (1996); Z. Phys. D <u>39</u>, 103 (1997)

A. Czarnecki, U.D. Jentschura and K. Pachucki, Phys. Rev. Lett. <u>95</u>, 180404 (2005)

It is then possible to form a linear combination to eliminate these Lamb shifts

$$7f(2S_{1/2} - 8D_{5/2}) - f(1S_{1/2} - 2S_{1/2}) \approx \left(\frac{57}{64}\right)cR_{\infty} + 7L_{8D_{5/2}} + \Delta_2$$

This method gives together the Rydberg constant and the 1S and 2S Lamb shifts and is applicable to hydrogen and deuterium

The results in hydrogen are : $R_{\infty} = 10\ 973\ 731.568\ 505(97)\ {\rm cm^{-1}}\ [\ 8.8 \times 10^{-12}\]$ $L_{18} = 8172.834\ (25)\ {\rm MHz}$ $r_{\rm p} = 0.8742\ (94)\ {\rm fm}$

Determination of the Rydberg constant

- From a least square adjustment
 - it can be done using only the hydrogen data

the values of α and $m_{\rm e}/m_{\rm p}$ being given a priori

- or including data concerning all the fundamental constants

Since 1998, the CODATA (Committee on Data for Science and Technology) uses this method to determine the Rydberg constant

P.J. Mohr and B.N. Taylor, Rev. Mod. Phys. <u>72</u>, 351 (2000) Rev. Mod. Phys. <u>77</u>, 1 (2005)
P.J. Mohr, B.N. Taylor and D.B. Newell, Rev. Mod. Phys. <u>80</u>, 633 (2008)

The results obtained in the 2010 CODATA adjustment are :

 $R_{\infty} = 10\,973\,731.568\,539\,(55)\,\mathrm{cm}^{-1}$

with a relative uncertainty of 5.0×10^{-12}

 $r_{\rm p} = 0.8775 \ (51) \ {\rm fm}$

P.J. Mohr, B.N. Taylor and D.B. Newell, Rev. Mod. Phys. <u>84</u>,1527 (2012)

Spectroscopy of muonic hydrogen determining the proton charge radius

F.D Amaro, A. Antognini, F.Biraben, J.M.R. Cardoso, D.S. Covita, A. Dax, S. Dhawan, L.M.P. Fernandes, A. Giesen, T. Graf, T.W. Hänsch, P. Indelicato, L.Julien, C.-Y. Kao, P.E. Knowles, F. Kottmann, J.A.M. Lopes, E. Le Bigot, Y.-W. Liu, L. Ludhova, C.M.B. Monteiro, F. Mulhauser, T. Nebel, F. Nez, R. Pohl, P. Rabinowitz, J.M.F. dos Santos, L.A. Schaller, K. Schuhmann, C. Schwob, D. Taqqu, J.F.C.A. Veloso

CREMA (Charge Radius Experiment with Muonic Atoms) collaboration



http://muhy.web.psi.ch

http://www.lkb.ens.fr/-Metrologie-Quantique-

Principle of the experiment :

measurement of the 2S-2P Lamb shift in muonic hydrogen µ-p

$$\frac{m_{\mu}}{m_{e}} \approx 207$$
 Bohr radius : $a_0/20^{\circ}$



Lamb shift = self-energy + vacuum polarization + proton radius

2S-2P	self-energy	vacuum pol.	r _p	total
e p	1085.8 MHz	-26.9 MHz	0.146 MHz	1057.8 MHz
μp	0.16 THz	-49.94 THz	0.93 THz	-49.05 THz



Production of muonic hydrogen in the 2S metastable state ...

- the muon is captured in a highly excited state which decays at 99 % to the ground state emitting a « prompt » X ray (K α , K β ,...)

- X rays are detected with LAAPDs (large area avalanche photodiodes) placed above and below the muon stop volume
- 1% of the stopped muons decay to the long-lived 2S state





... and excitation of the transition

A short laser pulse at 6 μm drives the 2S-2P transition

- the transition is detected through the 1.9 keV K α decay of the 2P state (« delayed » X ray)

The signature of the signal is the detection of K α , in time coincidence with the laser excitation, and of the electron originating from the muon decay (muon lifetime is 2.2 μ s)



2S_{1/2}(F=1) - 2P_{3/2}(F=2) transition observed in muonic hydrogen in 2009



Result and comparison with other best determinations



Determination of the proton radius from hydrogen frequencies



Ongoing experiments

2S-2P transition York university (E. Hessels) : "Ramsey method"

Measured @ 9kHz Lundeen and Pipkin PRL 72, 1172 (1994) $\Gamma(2S-2P)=100MHz$ proton radius : 11 kHz i.e. 10⁻⁴ of the linewidth

Advantages : 2S-2P mainly QED weak dependence on the Rydberg constant RF source well known

Difficulty : large line width 100MHz, lineshape controlled at 10⁻⁴ !

²⁰Ne⁹⁺ Rydberg states NIST : U. D. Jentschura et al, PRL 100, 160404 (2008)

Advantages : Rydberg states : high energy levels

- \succ no contribution of the nucleus structure, QED well known (1/n³)
- Direct measurement of the Rydberg constant

Difficulty : production of the ion ²⁰Ne⁹⁺

2S-4P transition MPQ Garching : Ann. Phys. (Berlin) 525 n°8-9 671-679 (2013)

Aim few kHz $\Gamma(2S-4P)=13$ MHz i.e. 10^{-3} of the linewidth

Advantages : cold hydrogen source

one ph transition weak laser power needed

Difficulty : transverse excitation but seems to be controlled controlled of the linewidth @ 10⁻³

Study of the 1S - 3S transition



Advantages

More atoms in 1S beam compared to 2S H-beam

Difficulties

- Laser @ 205nm
- No "easy" optical transition for Doppler spectroscopy
- Aim for 1S-3S frequency 1kHz i.e. 10-3 linewidth

CW laser source @ 205 nm 15mW



Compensation of 2nd order Doppler effect



Study of the 1S - 3S transition



Prospects

-Study of the velocity distribution versus pressure (current)



Proton radius puzzle

Assume the experiments are ok

C.E. Carlson, Progress in Particle and Nuclear Physics 82 (2015) 59-77

Introduction... "The reasons for this (i.e. proton radius puzzle) are not yet clear"

•Unexpected QCD corrections : "haywire" hadronic behaviour ...one is still left with an implausible 600MeV electromagnetic contributions to individual nucleon masses...

- Exotic explanations : new particles as $(g-2)_{\mu}$ (theo) \neq $(g-2)_{\mu}$ (exp) ...constrains from K decay (K[±] $\rightarrow \mu^{\pm}v$), from hfs in muonium,...
- Pb with the full collection of elec measurements (i.e. H spectroscopy, e-p scatt.) ...e-p scattering uncertainty larger than quoted...

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