



GEORG-AUGUST-UNIVERSITÄT
GÖTTINGEN

GEFÖRDERT VOM



Bundesministerium
für Bildung
und Forschung

Observation of the single top production at the Tevatron



Elizaveta Shabalina
University of Goettingen, Germany

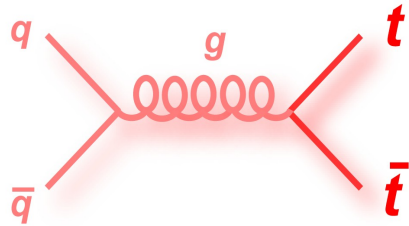


Outline

- Motivation
- Signal and background
- Event selection
 - Systematic uncertainties
- Statistical analysis
 - Cross section extraction
 - Significance calculation
- Multivariate Methods
- Combination
- $|V_{tb}|$ measurement
- Summary and outlook

The Top quark

Discovered in March 1995



$$\sigma_{\text{NLO}} = 6.8 \pm 0.6 \text{ pb @175 GeV}$$

N.Kidonakis et. al., M.Cacciari et. al.,
S.Moch, P.Uwer et.al.

- Main mechanism
- Distinct signature
- Thoroughly studied
- All knowledge comes from strong production

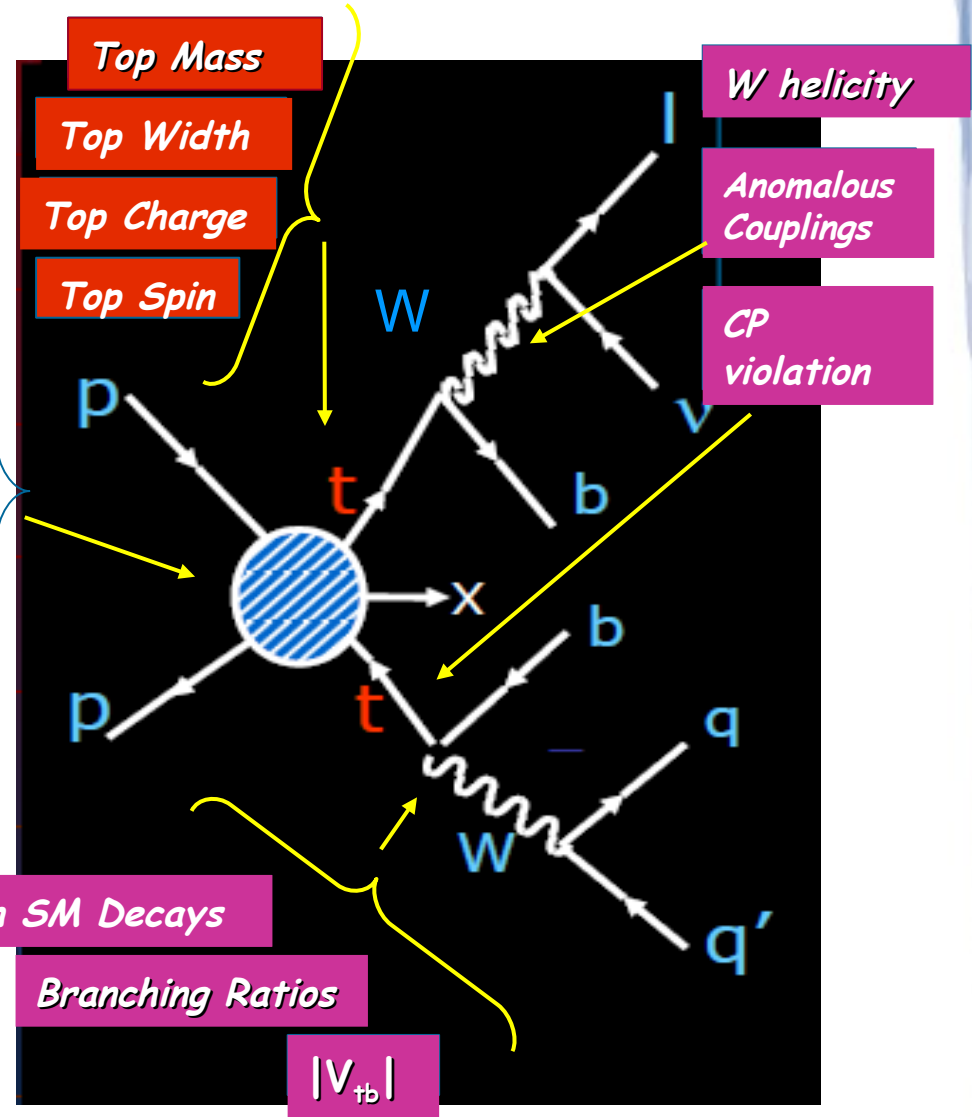
Production cross section

Production mechanism

Resonant production

Production kinematics

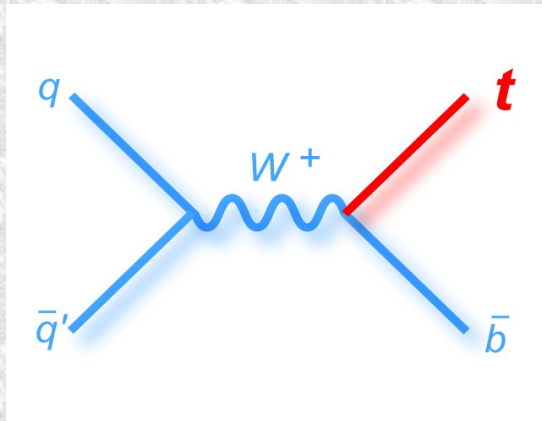
Top charge asymmetry



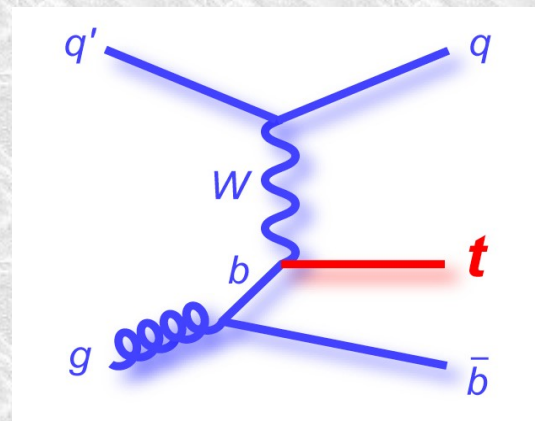
Electroweak production

- Predicted 10 years before top quark discovery
S.Willenbrock, D. Dicus, Phys. Rev. D34, 155 (1986); S Cortese and R Petronzio, PLB 253, 494 (1991)
- Observed 14 years after top quark discovery...

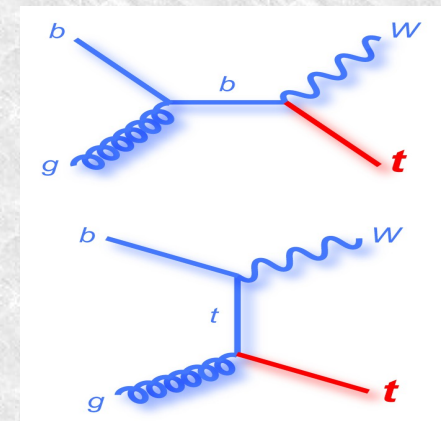
s-channel (tb)



t-channel (tqb)



Wt channel



m_t (GeV)

175	σ_{NLO}	0.88 ± 0.11 pb	1.98 ± 0.25 pb
170	$\sigma_{(\text{N})\text{NLO}}$	1.12 ± 0.05 pb	2.34 ± 0.13 pb

Z. Sullivan, Phys. Rev. D 70, 114012 (2004)

N. Kidonakis, Phys. Rev. D 74, 114012 (2006)

**Small at Tevatron
Important for LHC**

In observation analysis CDF (D0) assumes $m_t=175$ (170) GeV

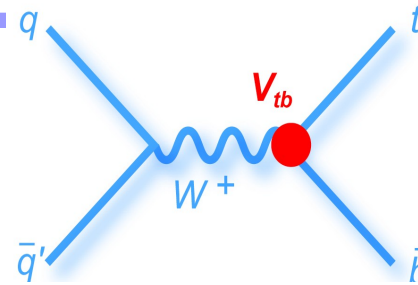
What will we learn?

Access to W-t-b vertex

- Probe V-A structure
- Top quark spin

Direct measurement of $|V_{tb}|^2$

- Test unitarity of CKM matrix
- Is it 3×3 matrix?
- Is 4th generation possible?



$$\sigma \propto |V_{tb}|^2$$

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} & V_{uX} ? \\ V_{cd} & V_{cs} & V_{cb} & V_{cX} ? \\ V_{td} & V_{ts} & V_{tb} & V_{tX} ? \\ V_{Yd} ? & V_{Ys} ? & V_{Yb} ? & V_{YX} ? \end{pmatrix}$$

Small mixing with 4th family is favored
Quite large mixing is still not excluded

Constraints:

tree-level 3×3 CKM elements

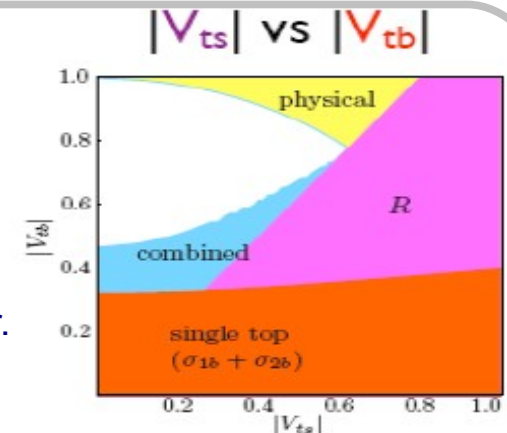
FCNC processes (K-, D-, B_d-, B_s-mixing, b → s)

Assumption: unitary 4×4 CKM matrix

A. Lenz et al. in arXiv 0902.4883 [hep-ph]

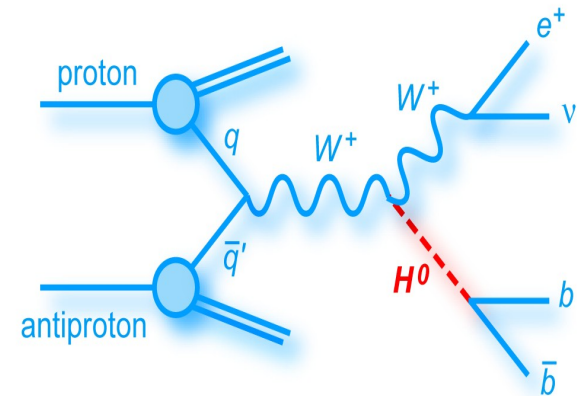
Combination of R_b and s- & t-channel cross sections

J. Alwall et. al., Eur. Phys. J. C49 791 (2007):



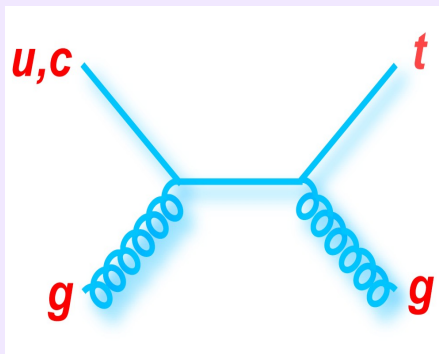
SM and beyond

- Milestone for Higgs search in WH channel
 - Same signature, 10 times smaller σ
 - Background to Higgs search
- s- and t-channels are sensitive to different processes **beyond the standard model**

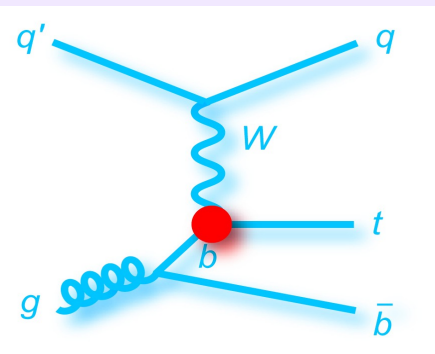


$$p\bar{p} \rightarrow WH$$

t-channel

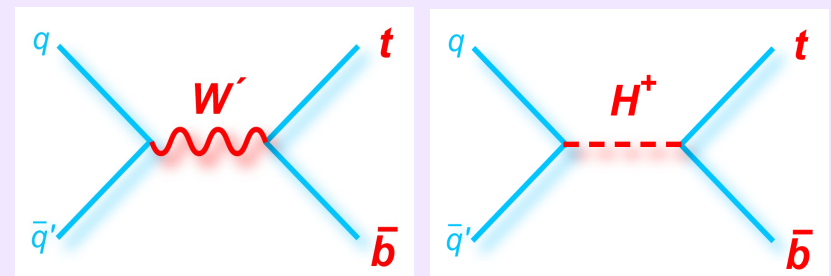


FCNC ($ug \rightarrow t$)



Anomalous couplings

s-channel



Resonances

Long way to discovery



- Search: PRD 63, 031101 (2000)
- Search: PLB 517, 282 (2001)

- Search: PLB 622, 265 (2005)
- W': PLB 641, 423 (2006)
- Search: PRD 75, 092007 (2007)
- Evidence: PRL 98, 181802 (2007)
- FCNC: PRL 99, 191802 (2007)
- W': PRL 100, 211802 (2007)
- Evidence: PRD 78, 012005 (2008)
- Wtb: PRL 101, 221801 (2008)
- Wtb: PRL 102, 092002 (2009)
- H[±]: (PRL) arXiv:0807.0859
- Observation: (PRL) arXiv:0903.0850

Run I

Run II



- Search: PRD 65, 091102 (2002)
- W': PRL 90, 081802 (2003)
- Search: PRD 69, 052003 (2004)

- Search: PRD 71, 012005 (2005)
- Evidence: PRL 101, 252001 (2008)
- FCNC: (PRL) arXiv:0812.3400
- W': (PRL) arXiv:0902.3276
- Observation: (PRL) arXiv:0903.0885

Single Top Cross Section	Signal Significance		CKM Matrix Element V_{tb}
	Expected	Observed	
December 2006 DØ (0.9 fb⁻¹)			PRL 98, 181802 (2007)
4.7 ± 1.3 pb	2.3σ	3.6σ	$ V_{tb}f_1^L = 1.31^{+0.25}_{-0.21}$ $ V_{tb} > 0.68$ at 95% CL
September 2008 CDF (2.2 fb⁻¹)			PRL 101, 252001 (2008)
2.2 ± 0.7 pb	4.9σ	3.7σ	$ V_{tb}f_1^L = 0.88^{+0.13}_{-0.12}$ $ V_{tb} > 0.66$ at 95% CL

The Tevatron

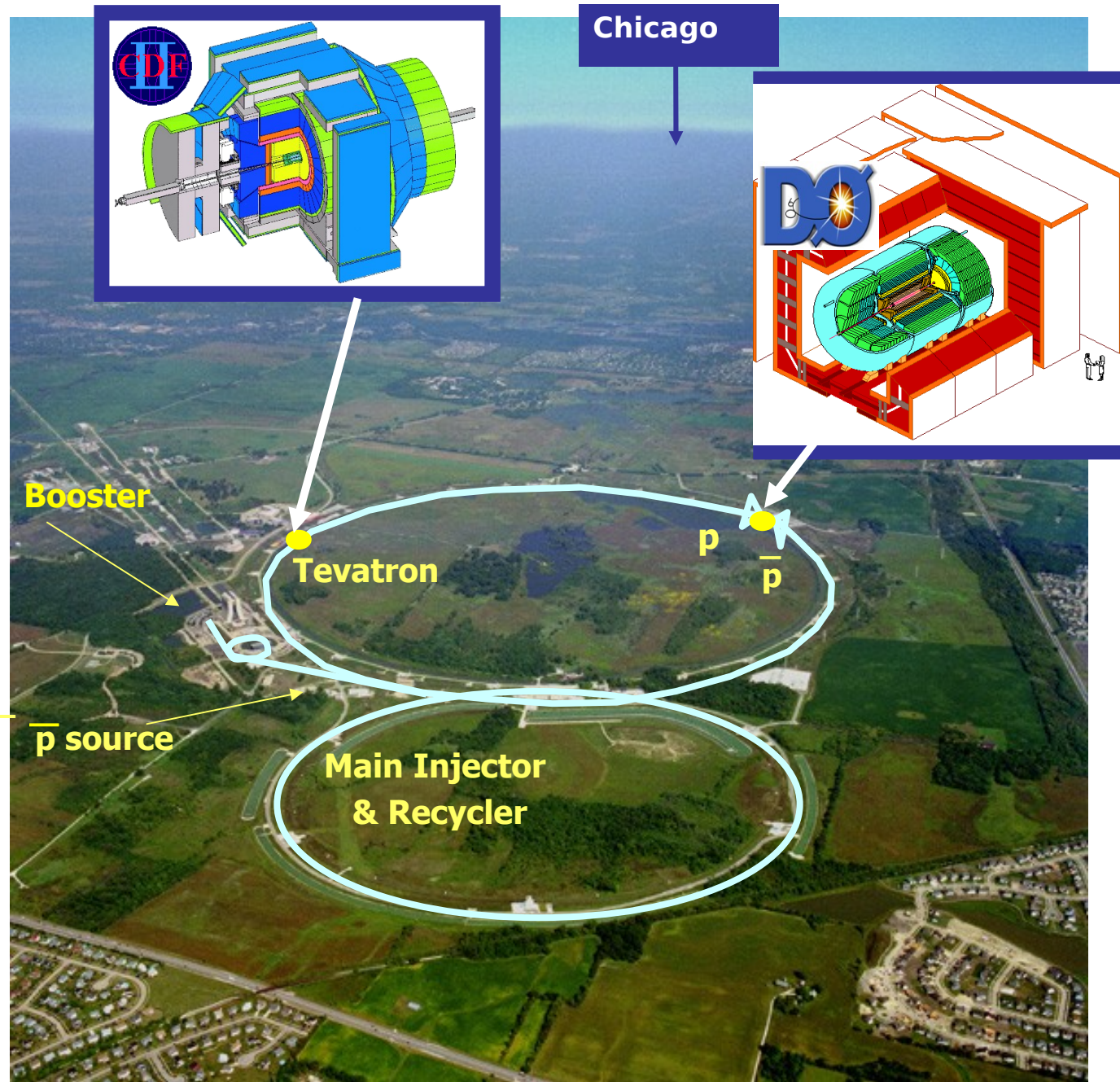
- The highest energy particle accelerator in the world
- Proton-antiproton collider with $\sqrt{s} = 1.96 \text{ TeV}$

Run I 1992-1995

Top quark discovered!

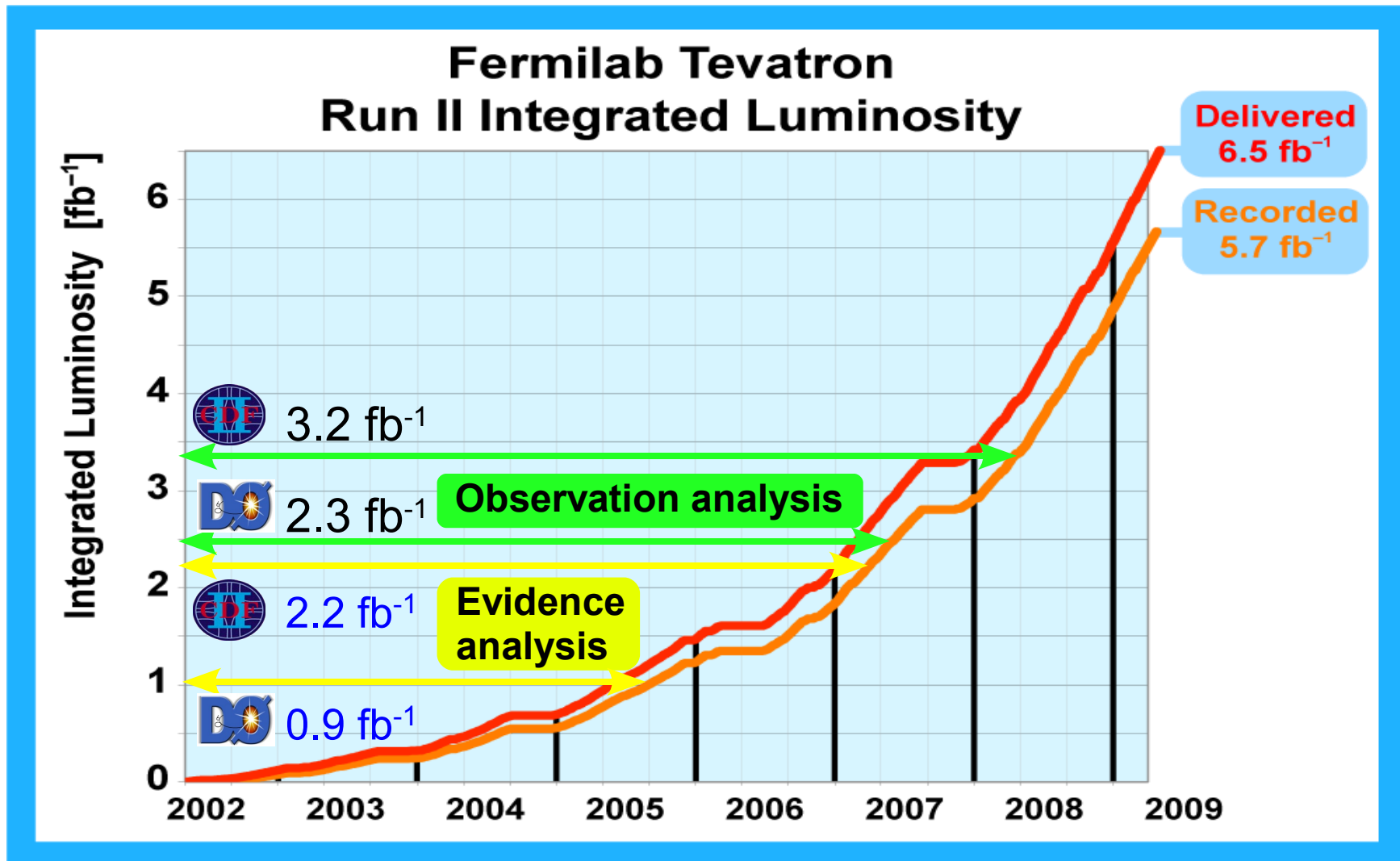
Run II 2001-11(?)

Single top quark discovered!



Climbing to the top...

Outstanding performance of the Tevatron!

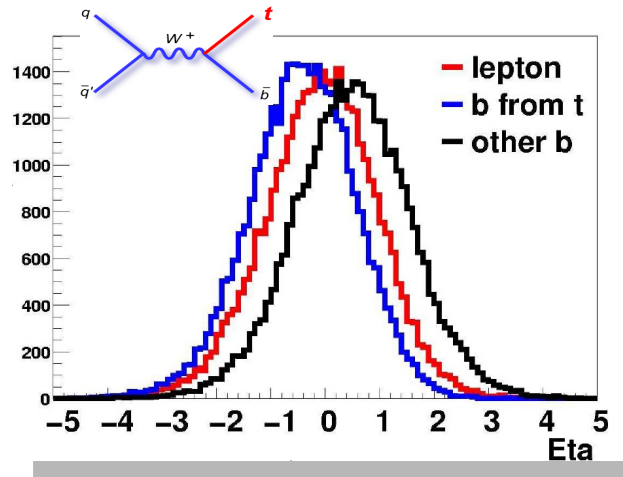


Signal

s-channel

2 b -jets

Top quark decay products and the b tend to be all central



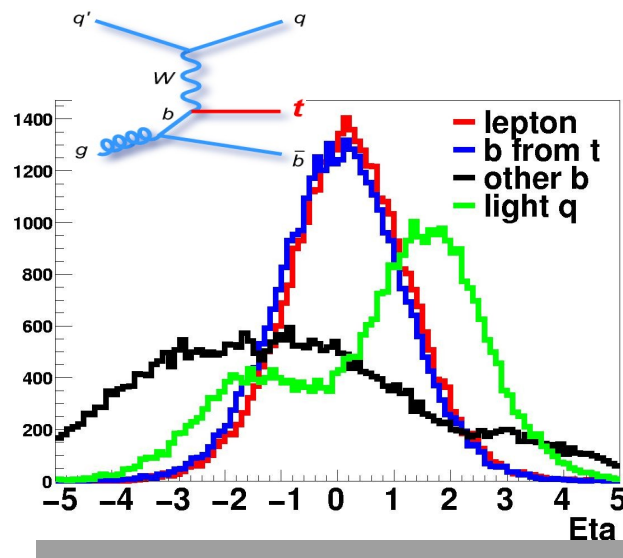
t-channel

2 b -jets and one light

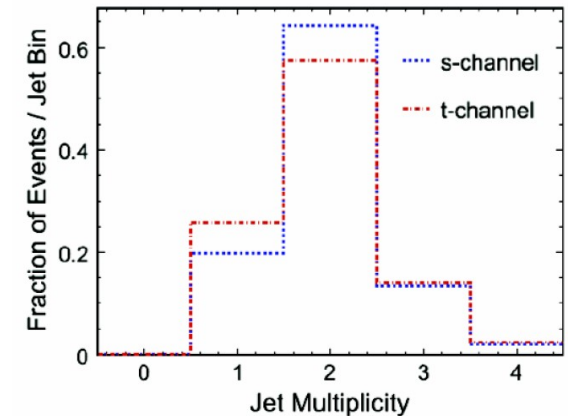
One of b 's tends to be very close to the beam pipe

No striking signatures as for $t\bar{t}$

Signal and background distributions look similar



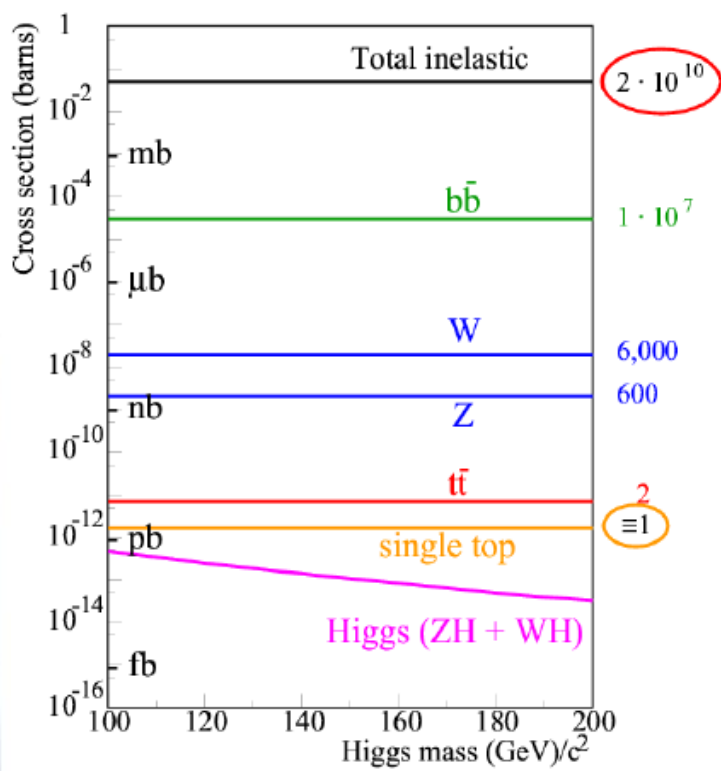
CDF Run II Preliminary



Simulated with

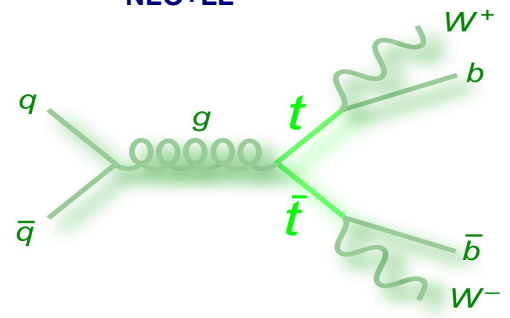
- CompHEP–SingleTop (D0)
- MadEvent (CDF)
- Matching of LO and NLO calculations

Backgrounds



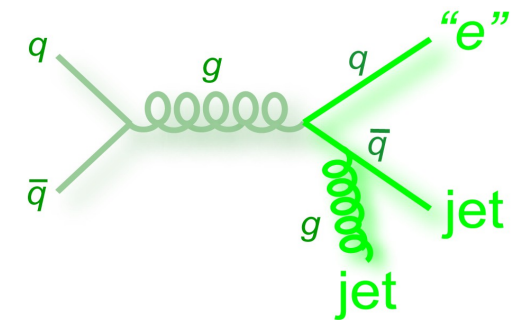
Top pairs

- Alpgen or Pythia
- $\sigma_{\text{NLO+LL}}$



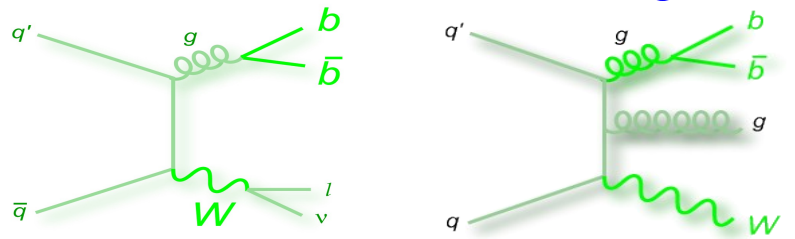
Multijet (instrumental)

- From data



Other small backgrounds: Z+jets, diboson – MC

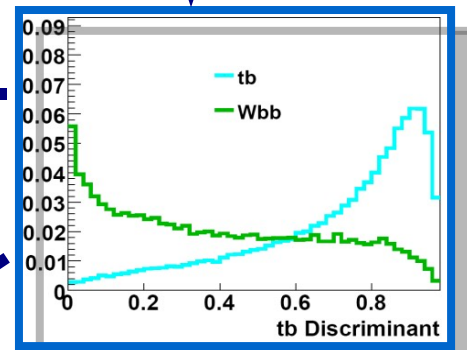
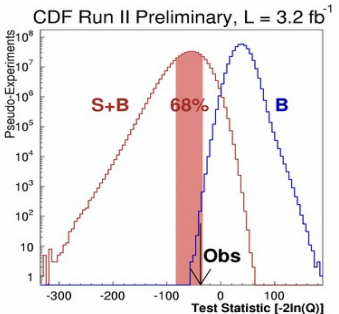
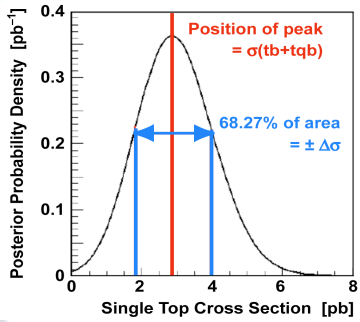
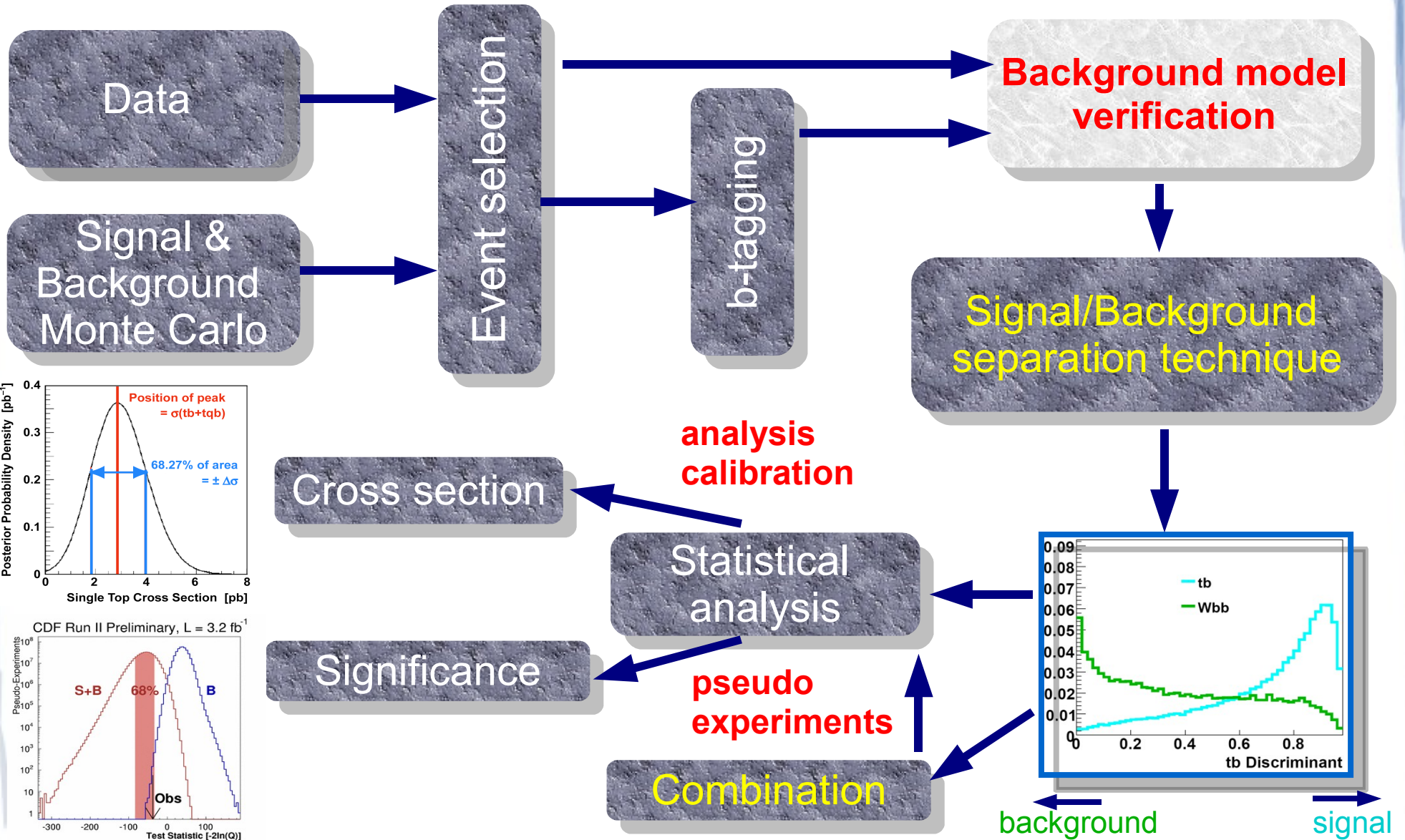
W+jets – dominant background



- Estimated from data and MC

Challenge:

- Backgrounds are large and similar in shape to signal
- Multivariate techniques are necessary to exploit all available information



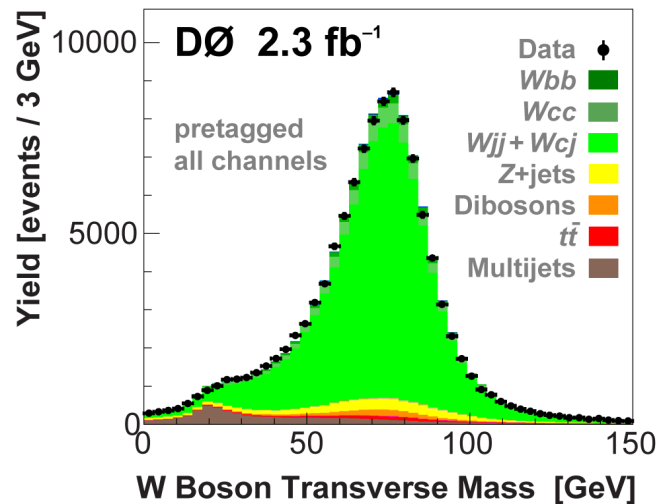
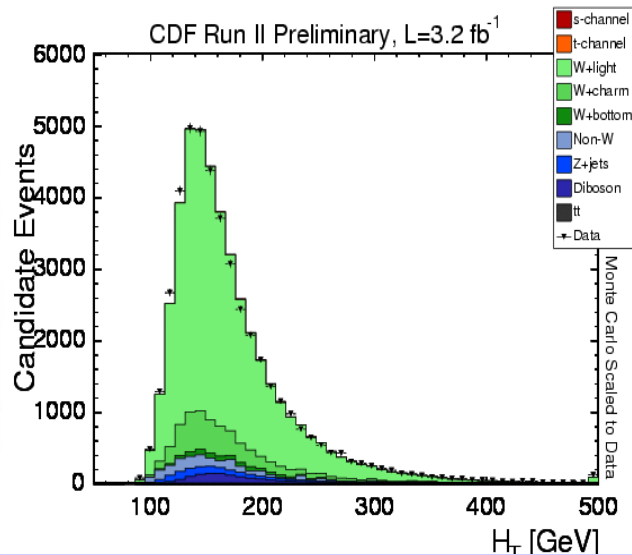
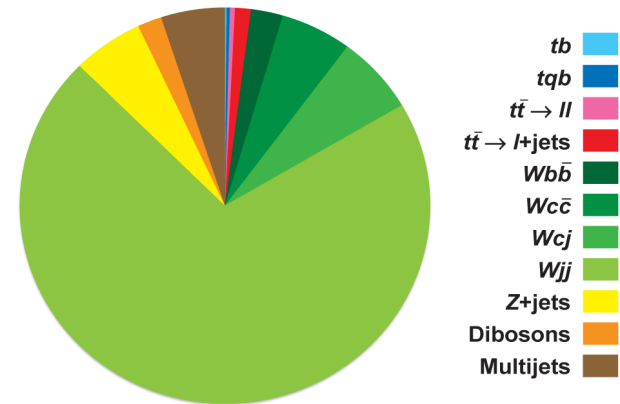
background signal

Selection I (l+jets)

Starting S:B = 1:10⁹

- Single lepton (e, μ) & MET+ jets triggers
- One high p_T lepton
- MET and 2-4 (D0), 2-3 (CDF) high p_T jets
- Cuts to suppress multijet background
- Veto to suppress Z+jets and $t\bar{t}$ dilepton
- S:B ~ 1: 260

DØ Single Top 2.3 fb⁻¹ Signals and Backgrounds
(All channels combined, before *b*-tagging)



- Verify background model before *b*-jet tagging
- Dominated by W+ light jets

Selection II: *b*-tagging (l+jets)



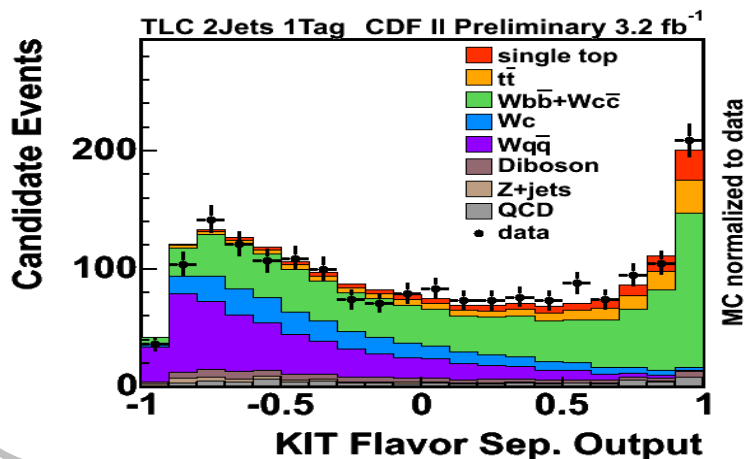
NN tagger

- 1 tight tag (40/9/0.4% *b/c/light*) or
- 2 loose (50/14/1.5% *b/c/light*)
- 1 SVX tag
- 50/9/0.5÷1.0% *b/c/light*

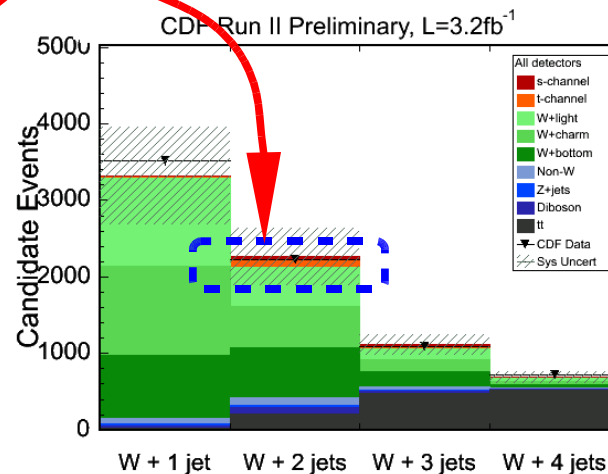
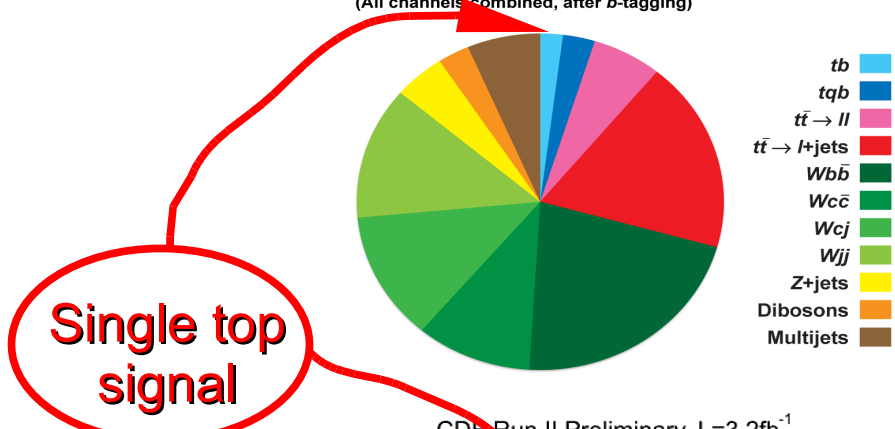


Additional flavor separation

- NN trained with 25 input variables
- Continuous variable
- Improves sensitivity by 10-15%



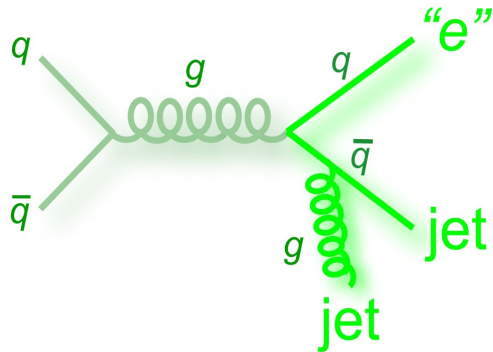
DØ Single Top 2.3 fb⁻¹ Signals and Backgrounds
(All channels combined, after *b*-tagging)



- Signal smaller than background error
- Cut-based analysis will not work
- Exploit kinematic differences between signal and background

Multijet background

- Jet misidentified as electron
- Muon in jet appeared isolated



Strategy:

- Reduce as much as possible using topological cuts (~5%)
- Determine before *b*-tagging

Modeling:

- Anti-Electrons (cuts reverted)
- Jet-Electrons (jets with high EM fraction)
- Anti-Muons (cuts reverted)



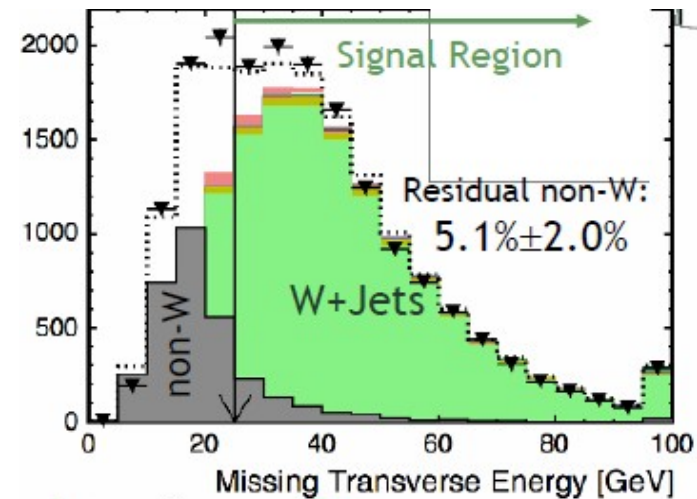
Method:

- Iterative template fits to data on three sensitive variables: $p_T(l)$, MET, $M_T(W)$

$$N_{\text{pretag}}^{\text{data}} - N_{\text{bkgd}}^{\text{MC}} = S_{W+\text{jets}} N_{W+\text{jets}}^{\text{MC}} + S_{\text{multijet}} N_{\text{multijet}}^{\text{data}}$$

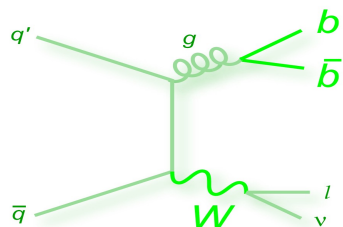


- Fit to MET distribution in data

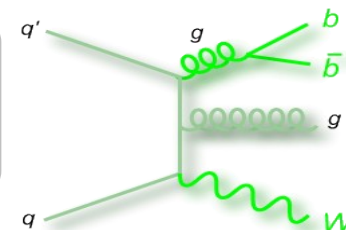


Large systematic uncertainties assigned (30÷50%)

W+jets background

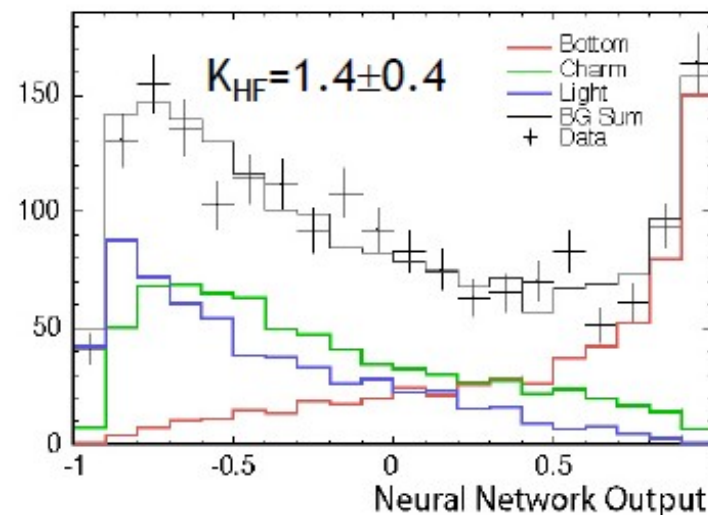


- Shapes simulated by Alpgen+Pythia MC
- Normalized to data before tagging



- W+HF normalized to theory (MCFM)
 - 1.47 (Wbb, Wcc), 1.38 (Wcj)
- Additional empirical correction
 - derived from two-jet data and simulation: includes 0-tag events
 - 0.95 ± 0.13 (Wbb, Wcc)
- Uncertainties considered
 - Data statistics $\pm 9\%$
 - $\pm 40\%$ single top cross section $\rightarrow \pm 7\%$ in SF
 - $\pm 10\%$ on Wcj theory SF $\rightarrow \pm 8\%$ in SF
 - $\pm 10\%$ Wbb/Wcc ratio $\rightarrow \pm 5\%$ in SF

- HF fractions (Wbb:Wcc:Wc) from Alpgen+Pythia MC
- HF contribution is boosted by factor from fit to flavor separator output in tagged W+1 jets events

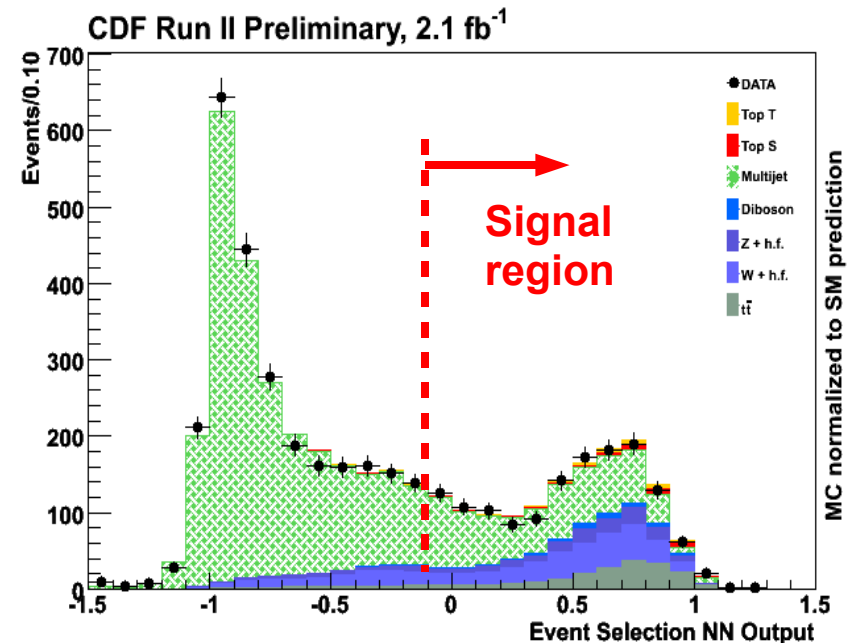




Selection II – MET+ jets

New channel

- Recover non-fiducial leptons and hadronic τ decay
 - Orthogonal to lepton+jets
- MET+ jets trigger
 - Huge instrumental background from QCD multijets
- MET > 50 GeV and veto leptons
- $E_T > 35$ (25) GeV 1st (2nd) jet
- At least 1 b -tag
- NN to suppress multijet bckg
 - Signal region: ANN > -0.1
 - Control region: ANN < -0.1



Quantity	Pre-selection	After QCDNN cut	Difference
Signal (S)	75	68	-9%
QCD Background	2960	675	-77%
Total Background (B)	3840	1350	-65%
$S/\sqrt{S+B}$	1.2	1.8	+50%
S/B	1/50	1/20	+150%



Improvements

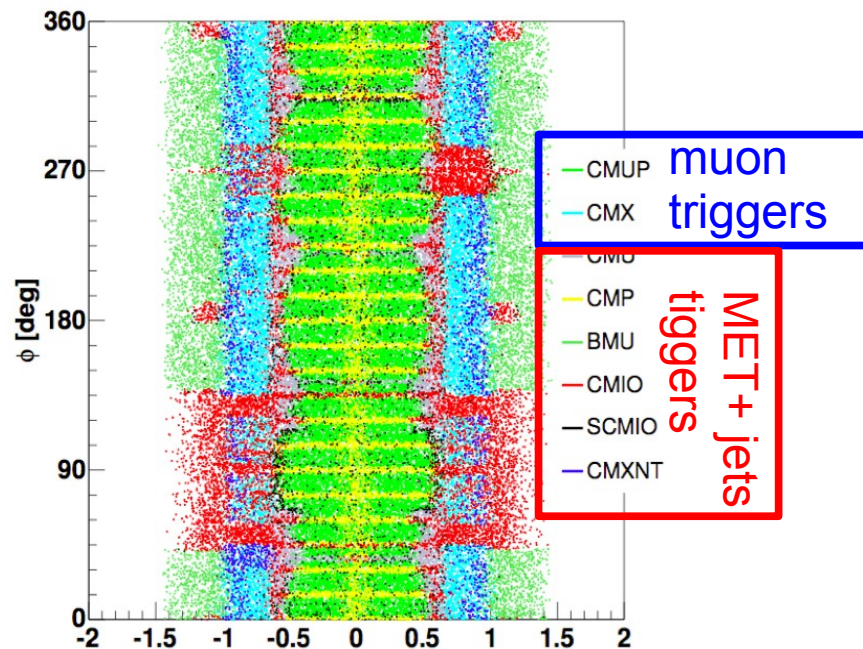


- 3.2 fb⁻¹ (2.2–2.7 fb⁻¹ in summer)

- Extended muon coverage

30% gain in muon acceptance

10-14% gain in sensitivity



- Additional channel MET+ jets
- 33% increase of acceptance**

- Separate s- and t-channel searches

- 2.6 times more data (2.3 fb⁻¹)

- 18% larger acceptance

- Logical OR of many triggers

- Looser cuts on 2nd jet and muon p_T

- Increased $|\eta|$ for 1st jet (2.5 → 3.4)

- Looser b-tagging requirements for 2 b-tag events

- Additional cuts to reduce background

- Improved (more detailed) background modeling

- Data-based corrections to Alpgen model of W+jets

- Improved treatment of multijet background



Yields



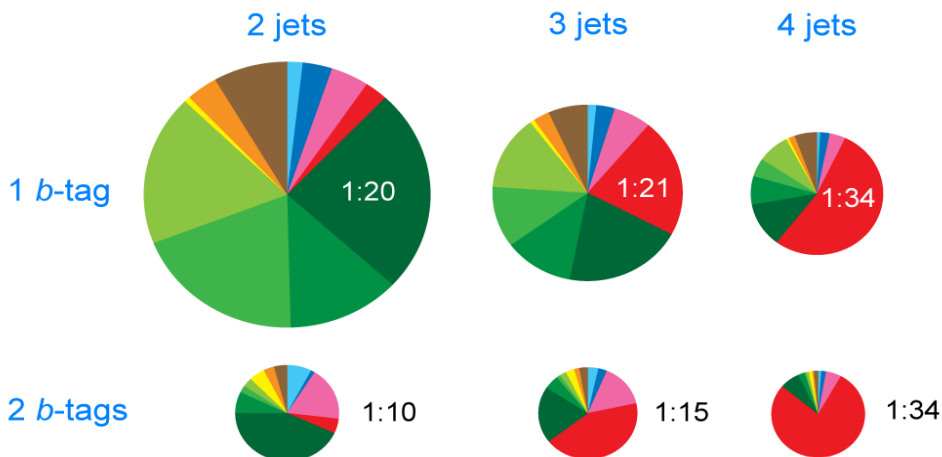
Event Yields in 2.3 fb⁻¹ of DØ Data

e,μ, 2,3,4-jets, 1,2-tags combined

<i>tb + tqb</i>	223 ± 30	for $m_t=170$
W+jets	2,647 ± 241	
Z+jets, dibosons	340 ± 61	
$t\bar{t}$ pairs	1,142 ± 168	
Multijets	300 ± 52	
Total prediction	4,652 ± 352	
Data	4,519	

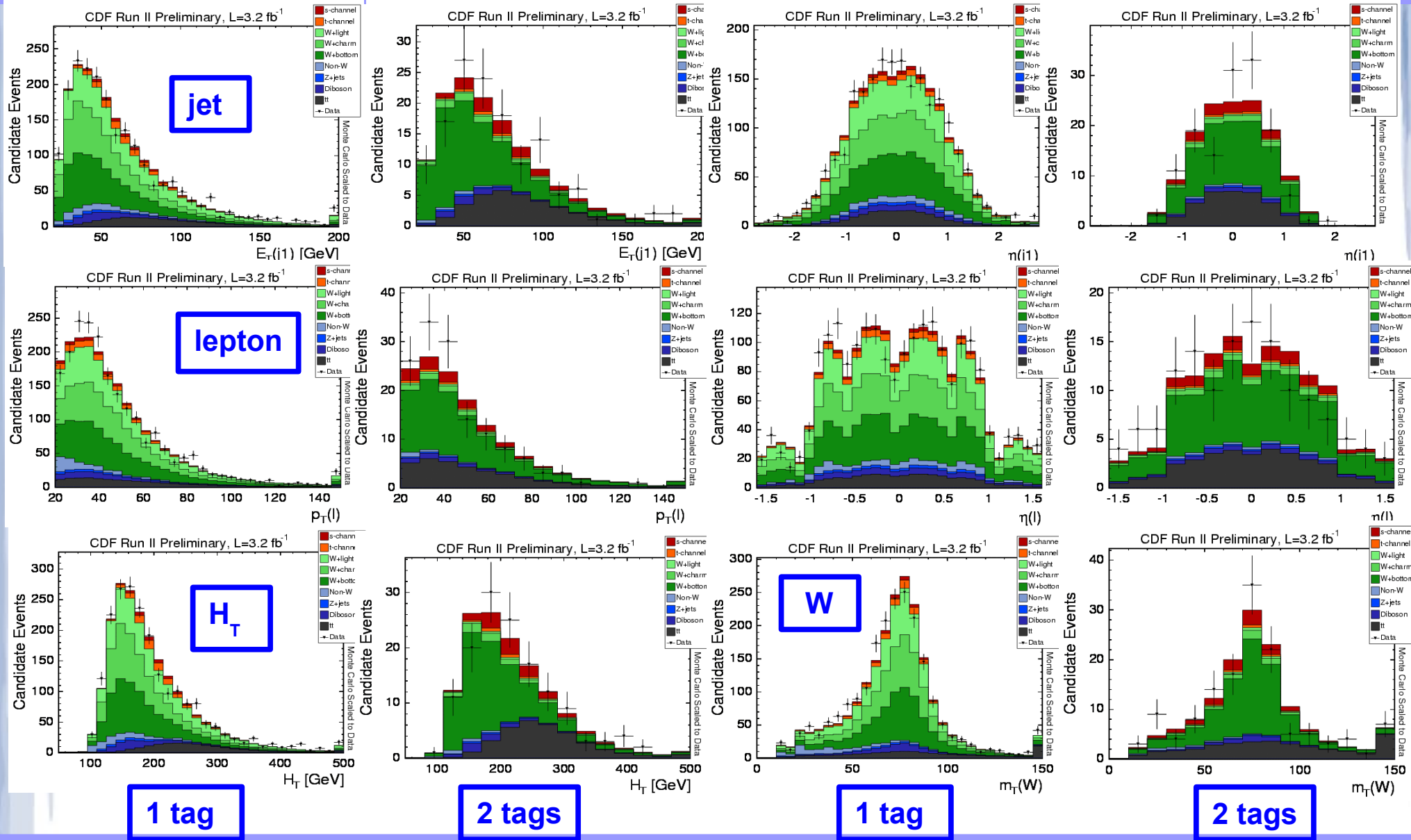
**255 events
for $m_t=175$**

Process	$\ell + \cancel{E}_T + \text{jets}$	$\cancel{E}_T + \text{jets}$
<i>s</i> -channel signal	77.3 ± 11.2	29.6 ± 3.7
<i>t</i> -channel signal	113.8 ± 16.9	34.5 ± 6.1
<i>W + HF</i>	1551.0 ± 472.3	304.4 ± 115.5
$t\bar{t}$	686.1 ± 99.4	184.5 ± 30.2
Z+jets	52.1 ± 8.0	128.6 ± 53.7
Diboson	118.4 ± 12.2	42.1 ± 6.7
QCD+mistags	777.9 ± 103.7	679.4 ± 27.9
Total prediction	3376.5 ± 504.9	1404 ± 172
Observed	3315	1411



- S:B – 1:10 to 1:34 depending on number of jets and tags
- Most powerful - 2 jets/1 tag
- Keep channels separately in the analysis to take advantage of different S:B and different background composition

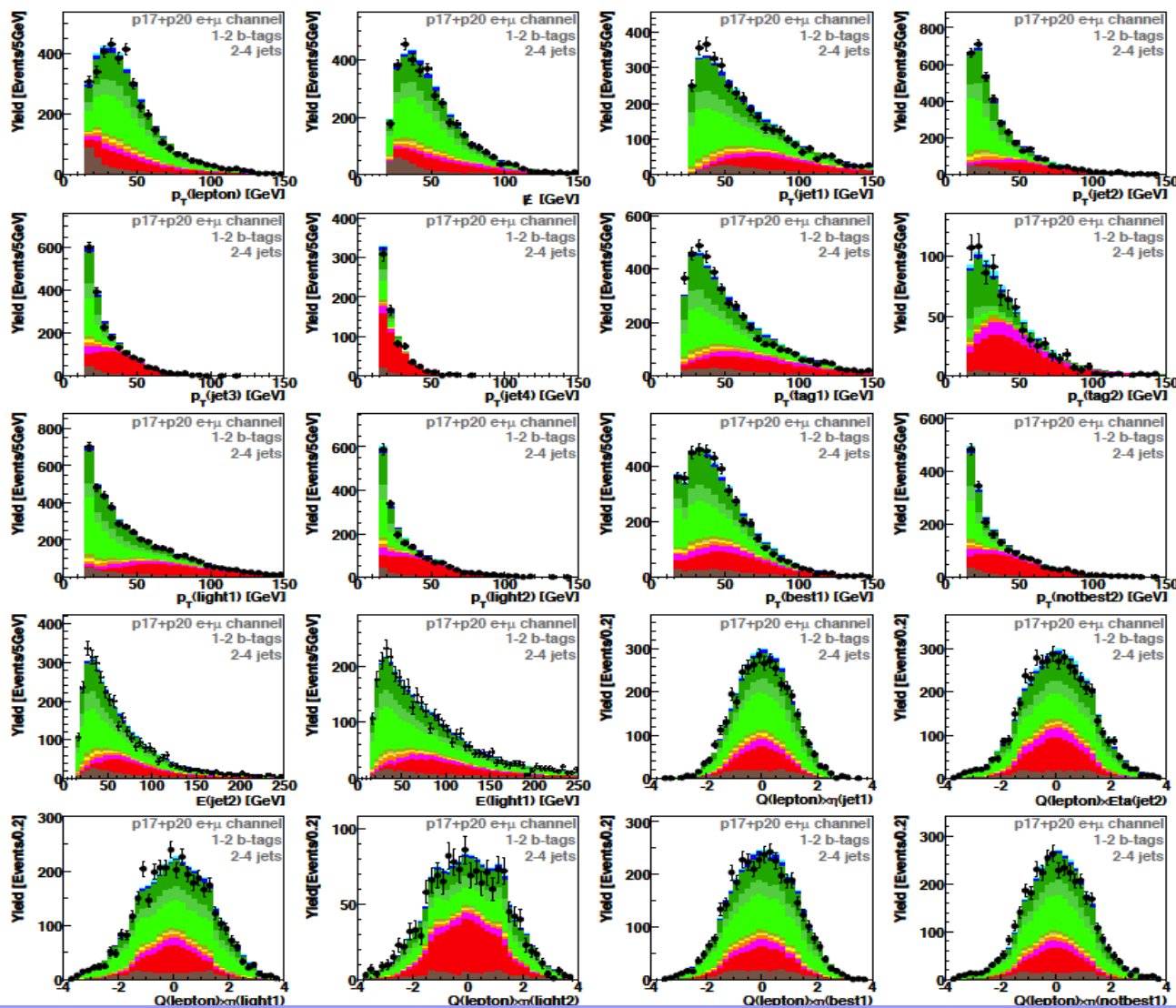
Background model validation



Background model validation



SINGLE OBJECT KINEMATICS



- Check thousands of distributions to verify background model before and after tagging
- Several classes of variables used in discriminants
 - Single object kinematics
 - Event kinematics
 - Jet reconstruction
 - Top quark reconstruction
 - Angular correlations



Systematics



- Statistically limited measurement
- But systematics is important
- Affects normalization and shapes
- Estimated for each background and signal source in each analysis channel
- Background uncertainty dominates

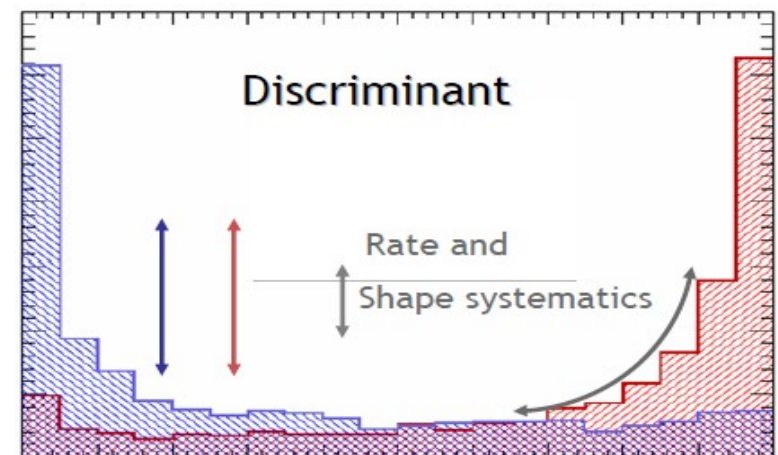
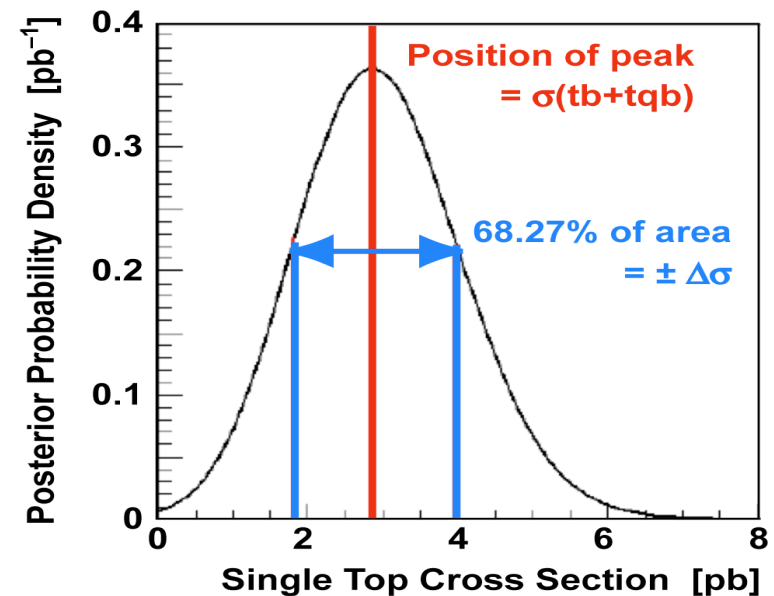
Systematic Uncertainties
Ranked from Largest to Smallest Effect
on Single Top Cross Section
DØ 2.3 fb⁻¹

Larger terms	
<i>b</i> -ID tag-rate functions (includes shape variations)	(2.1–7.0)% (1-tag) (9.0–11.4)% (2-tags)
Jet energy scale (includes shape variations)	(1.1–13.1)% (signal) (0.1–2.1)% (bkgd)
W+jets heavy-flavor correction	13.7%
Integrated luminosity	6.1%
Jet energy resolution	4.0%
Initial- and final-state radiation	(0.6–12.6)%
<i>b</i> -jet fragmentation	2.0%
<i>t</i> \bar{t} pairs theory cross section	12.7%
Lepton identification	2.5%
<i>Wbb/Wcc</i> correction ratio	5%
Primary vertex selection	1.4%

Systematic Uncertainty	Rate	Shape
Jet Energy Scale	0...10%	✓
Initial + Final State Radiation	0...15%	✓
Parton Distribution Functions	2...3%	✓
Monte Carlo Generator	1...5%	
Event Detection Efficiency	0...9%	
Luminosity	6%	
Neural Net B-tagger		✓
Mistag Model		✓
Q ² scale in ALPGEN MC		✓
Input variable mismodeling		✓
<i>Wbb+Wcc</i> normalization	30%	
<i>Wc</i> normalization	30%	
Mistag normalization	17...29%	
<i>t</i> \bar{t} normalization & m_{top}	23%	✓

Cross section

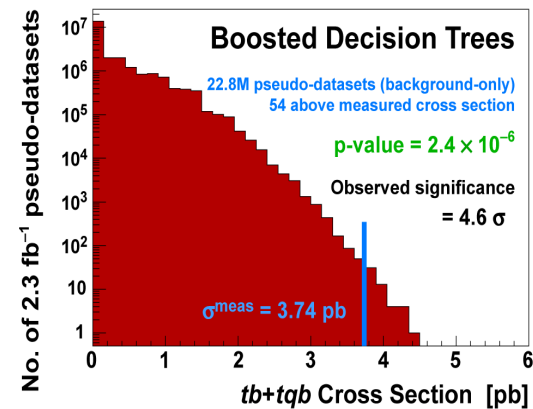
- Discriminant outputs (from each analysis channel separately) are used to measure cross section
- Build **Bayesian probability** density with flat nonnegative prior for the cross section
- Peak of posterior distribution gives the cross section, 68% interval gives the uncertainty
- Shape and normalization systematic uncertainties are treated through nuisance parameters with Gaussian distribution
 - Correlations are properly taken into account



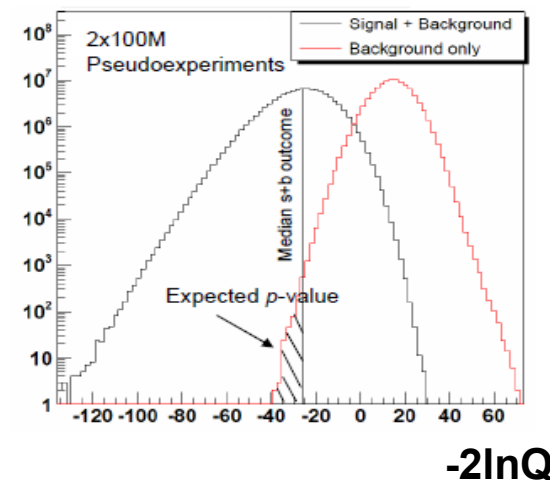
Statistical analysis

- Build ensembles of pseudo-data
 - Includes signal and background events or background only
 - Includes all systematic uncertainties
- Purpose before data
 - Test performance of different methods
 - Measure expected cross section uncertainty
 - **Expected significance**
- With data
 - Consistency of the measured cross section with the SM
 - **Observed significance**

Significance – probability of the upward background fluctuation that gives observed result in data



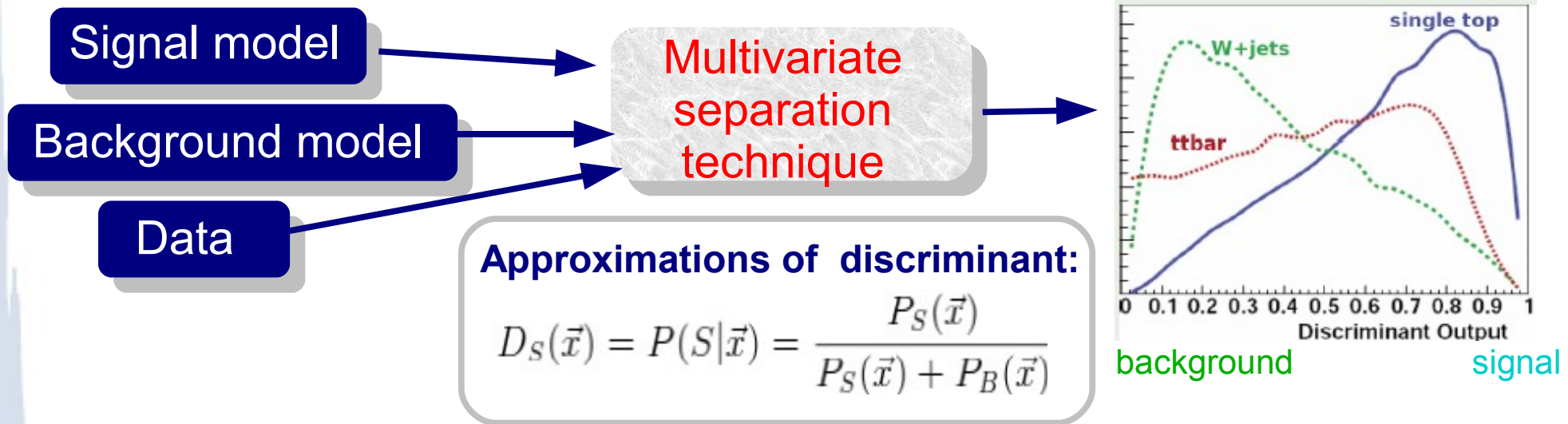
p-value:
 Fraction of zero-signal ensemble datasets that give $\sigma \geq \sigma_{\text{meas}}$



Likelihood ratio technique

$$Q = \frac{P(\text{data} | s + b, \hat{\theta})}{P(\text{data} | b, \hat{\theta})}$$

Signal from background separation

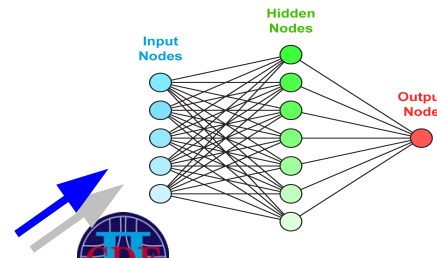
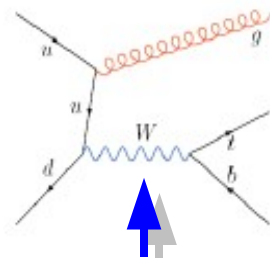
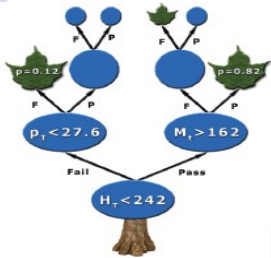


Boosted decision trees

Matrix elements

Neural Networks

Likelihood function



$$\mathcal{L}^{\text{signal}} = \frac{\prod_{i=1}^{n_{\text{val}}} P_i^{\text{signal}}}{\prod_{i=1}^{n_{\text{val}}} P_i^{\text{signal}} + \sum_{m=1}^{n_{\text{bkg}}} \prod_{i=1}^{n_{\text{val}}} P_i^m \times a^m}$$



Combined analysis





Separate search

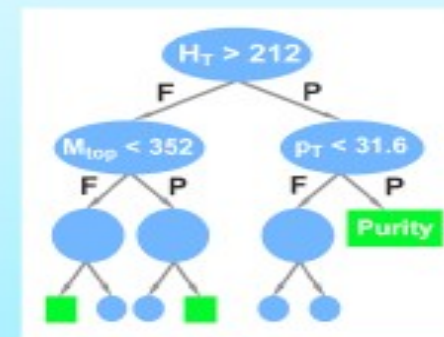


t-channel + s-channel = one single-top signal
cross section ratio is fixed to SM value.
important for „observation“ and $|V_{tb}|$ test

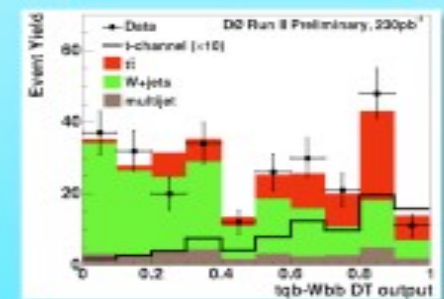
consider t-channel and s-channel as separate processes
important for new physics search

Boosted Decision Trees method

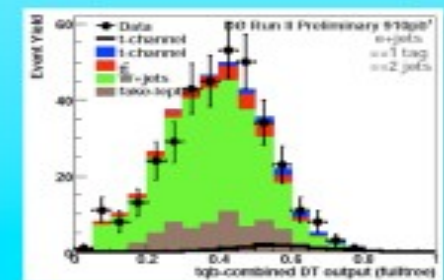
- Idea: recover events that fail criteria in cut-based analyses
- Start with all events (first node )
 - For each variable, find splitting value with best separation
 - Select variable and cut: produce Pass and Failed branches
- Repeat recursively on each node
- Stop when no improvement or too few (100) events left
- Terminal node: leaf  with purity = $N_S/(N_S+N_B)$
- Decision tree output for each event = leaf purity value (closer to 0 for background, closer to 1 for signal)
- Boosting – averaging over many trees – improves stability and performance by ~20% by diluting discrete output
- Adaptive boosting algorithm with 50 cycles
- Run independent MC and data through the tree to obtain the result



Before boosting



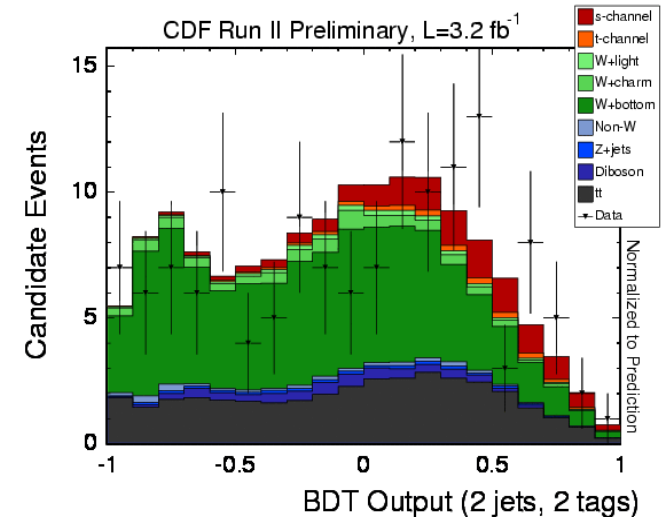
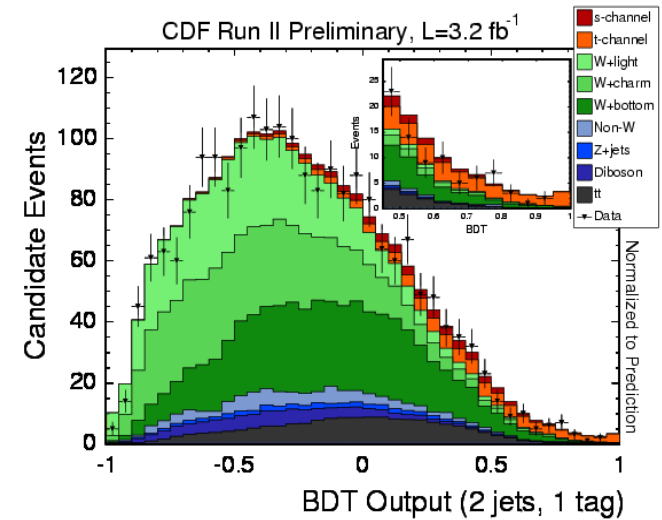
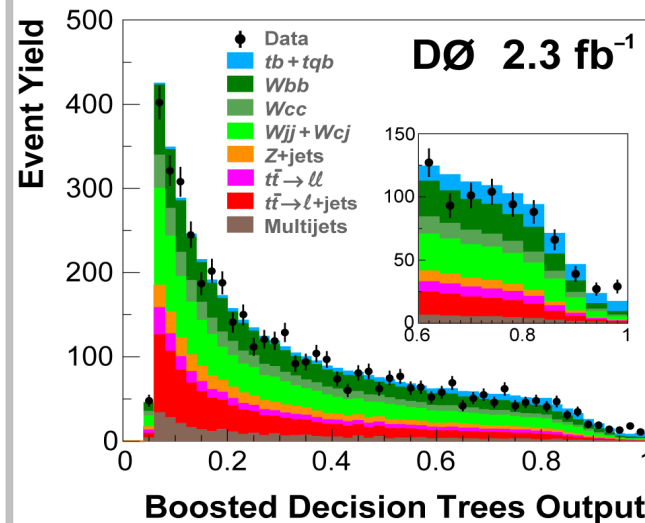
After boosting





Boosted Decision Trees results

Advantages:

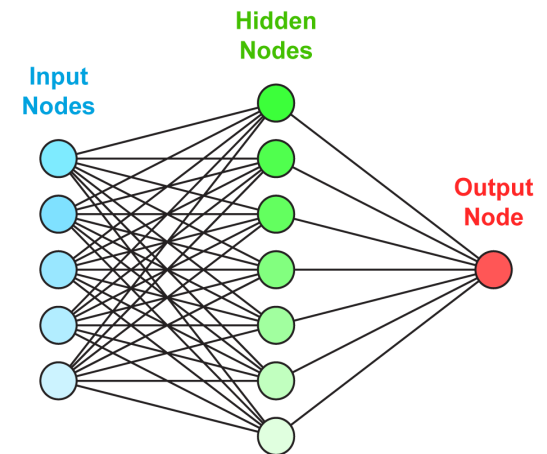
- Fast to train
- Not degraded by the addition of more input variables
- no need to optimize the choice
- use all sensitive variables with good agreement to data
- Input variables 64 (D0), 20 (CDF)



	\mathcal{L}	Significance		σ_{s+t}
	[fb ⁻¹]	Exp.	Obs.	[pb]
	2.3	4.3σ	4.6σ	3.7 ^{+1.0} _{-0.8}
	3.2	5.2σ	3.5σ	2.1 ^{+0.7} _{-0.6}

Neural Networks method

- A Neural Network (NN) is an Interconnected group of nodes. It can be used to model complex relationships between inputs and outputs, or to find patterns in data
- For this analysis:
 - Inputs: variables with high discriminating power
 - Output: probability for the event to be signal



NEUROBAYES

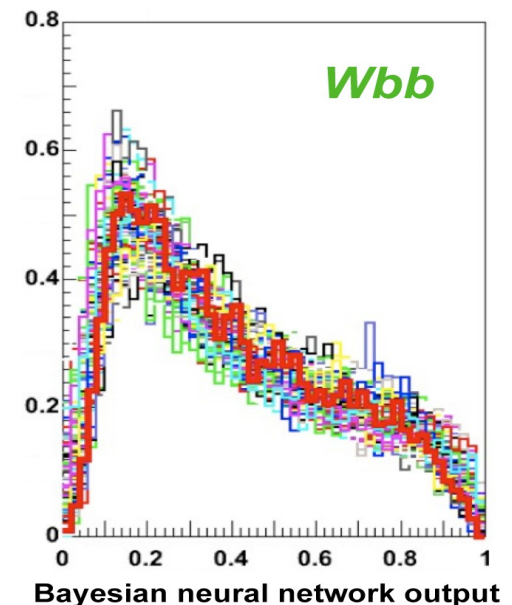


- 3 layer feed-forward network with complex and robust preprocessing of input variable
- Bayesian regularization to avoid over-training
- 4 networks, each divided into 2 channels based on trigger
- 14 variables

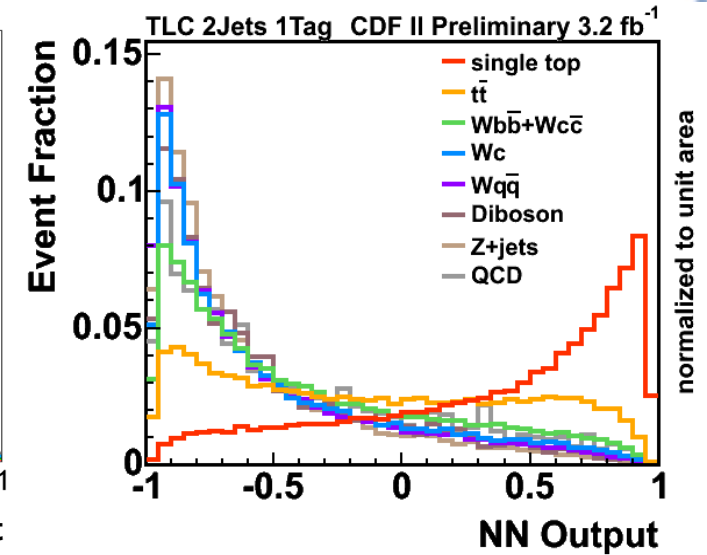
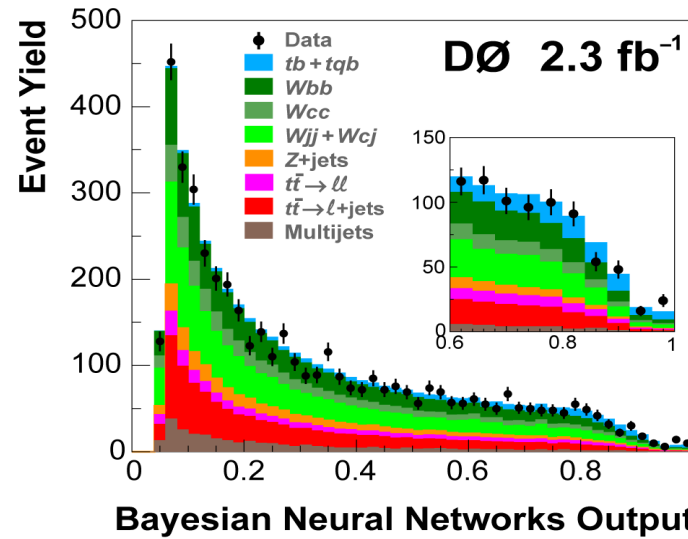
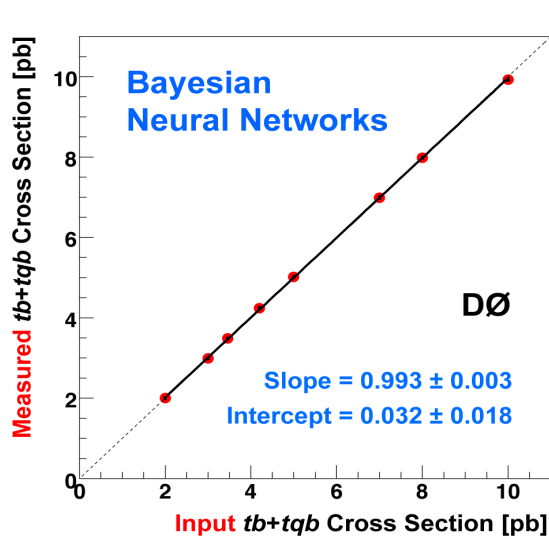
Bayesian NN





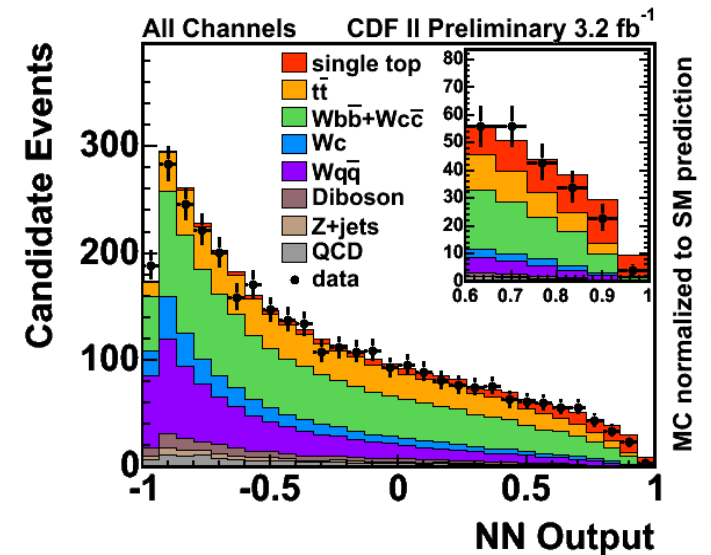
- Weighted average over hundreds of networks
- Better stability
- Immune to over-training
- 18-25 input variables



Neural Networks results



	\mathcal{L}	Significance		σ_{s+t}
	[fb ⁻¹]	Exp.	Obs.	[pb]
	2.3	4.1σ	5.2σ	$4.7^{+1.2}_{-0.9}$
	3.2	5.2σ	3.5σ	$1.8^{+0.6}_{-0.6}$



Matrix Elements method

- Given 4-vectors of reconstructed lepton and jets compute event probability density for signal and background hypothesis

$$P(\vec{x}) = \frac{1}{\sigma} \times \frac{\partial \sigma}{\partial \vec{x}}$$

$$d\sigma(\vec{x}) = \sum_{i,j} \int d\vec{y} \left[f_i(q_1, Q^2) dq_1 \times f_j(q_2, Q^2) dq_2 \times \frac{\partial \sigma_{hs,ij}(\vec{y})}{\partial \vec{y}} \times W(\vec{x}, \vec{y}) \times \Theta_{\text{Parton}}(\vec{y}) \right]$$

Parton distribution functions for initial parton i, j carrying momentum q

Differential cross section for the hard scatter. Uses leading-order matrix element

Transfer function which relates observed state in the detector (x) to original partons (y)

Matrix elements:



- 2 jets: $tb, tq, Wb\bar{b}, Wcg, Wgg, WW, WZ, ggg, t\bar{t}$

- 3 jets: $tbg, tqg, tqb, Wb\bar{b}g, t\bar{t}, Wugg$



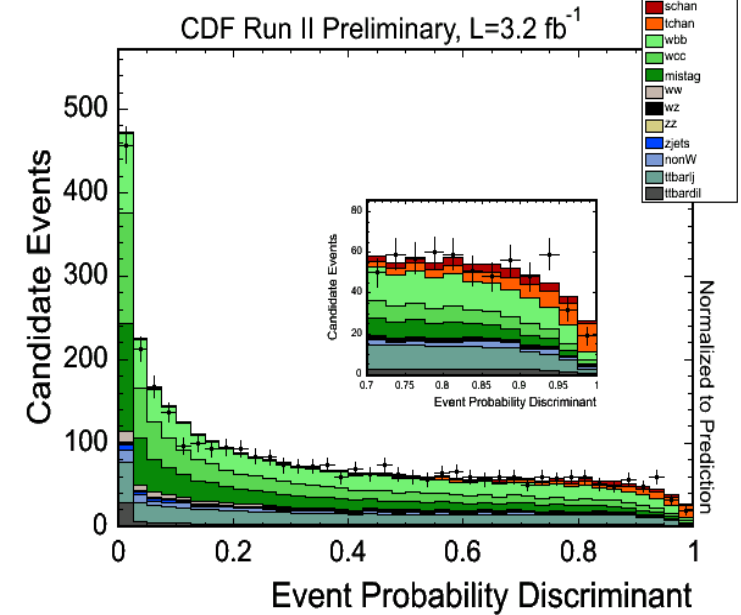
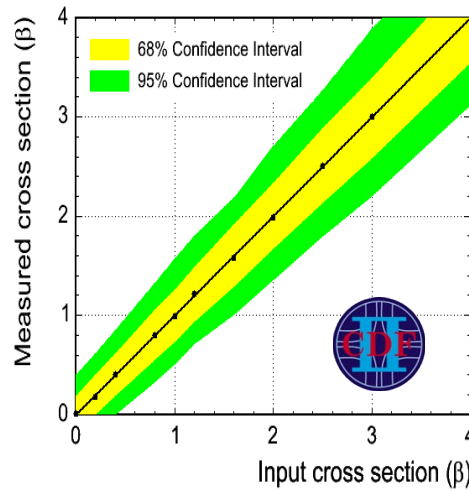
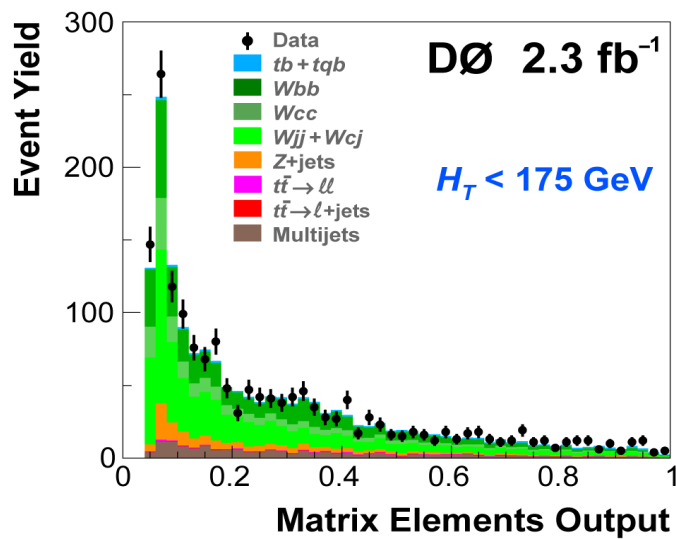
- $tb, tq, tbg, tqg, Wb\bar{b}, Wcg, Wgg, t\bar{t}, Wc\bar{c}$

Improve performance by

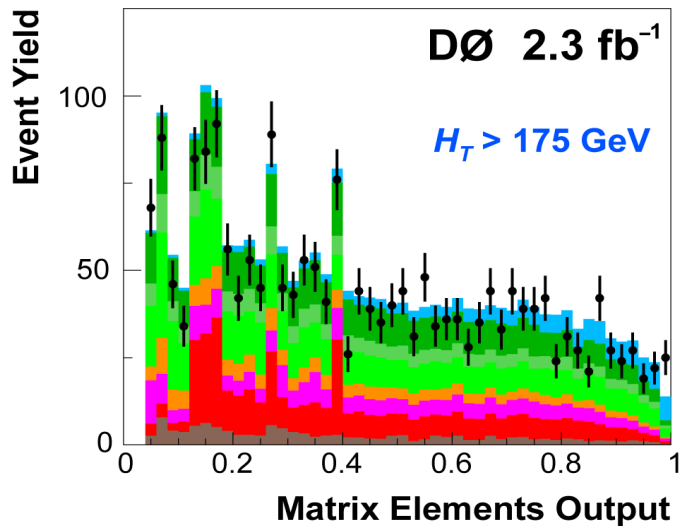
- D0: splitting samples by H_T into $t\bar{t}$ and W +jets dominated regions
- CDF&D0: weighting events by jet flavor probability



$$EPD = \frac{b \cdot P_{\text{sin gletop}}}{b \cdot P_{\text{sin gletop}} + b \cdot (P_{Wb\bar{b}} + P_{t\bar{t}}) + (1-b) \cdot (P_{Wc\bar{c}} + P_{Wcj} + P_{Wgg})}$$

Matrix Elements results



Linearity test



	\mathcal{L} [fb ⁻¹]	Significance Exp.	Obs.	σ_{s+t} [pb]
	2.3	4.1 σ	5.0 σ	4.3 ^{+1.0} _{-1.2}
	3.2	4.9 σ	4.3 σ	2.5 ^{+0.7} _{-0.6}

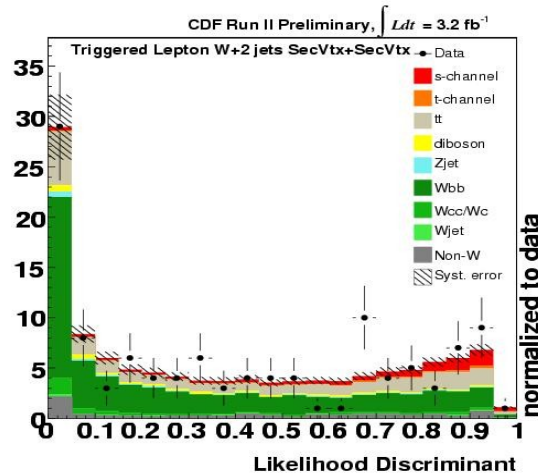


Multivariate Likelihood Function

Combine many variables into a likelihood function

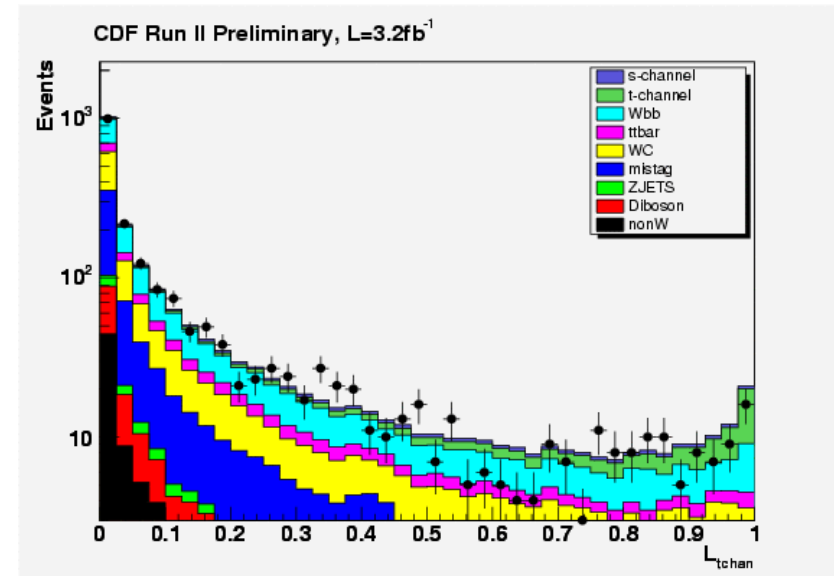
$$\mathcal{L}^{\text{signal}} = \frac{\prod_{i=1}^{N_{\text{val}}} P_i^{\text{signal}}}{\prod_{i=1}^{N_{\text{val}}} P_i^{\text{signal}} + \sum_{m=1}^{N_{\text{bkg}}} \prod_{i=1}^{N_{\text{val}}} P_i^m \times a^m}$$

s-channel



- Events with 2 *b*-tags
- 2 classes: $\bar{t}\bar{t}$ and $W+HF$
- 9-10 variables

t-channel likelihood



- Signal template built for t-channel
- 4 background classes: $Wb\bar{b}$, $Wc\bar{c}$, Wc , $\bar{t}\bar{t}$, mistags
- 7 (10) variables in 2 (3) jet bin to isolate t-channel contribution

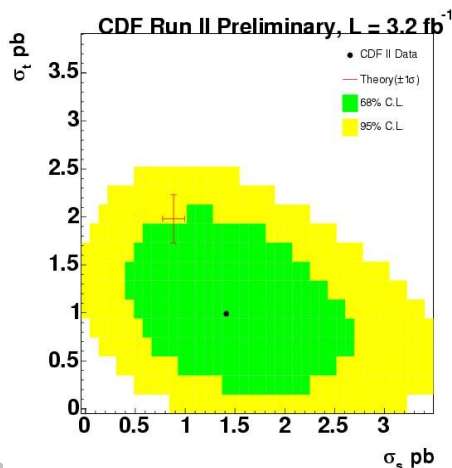
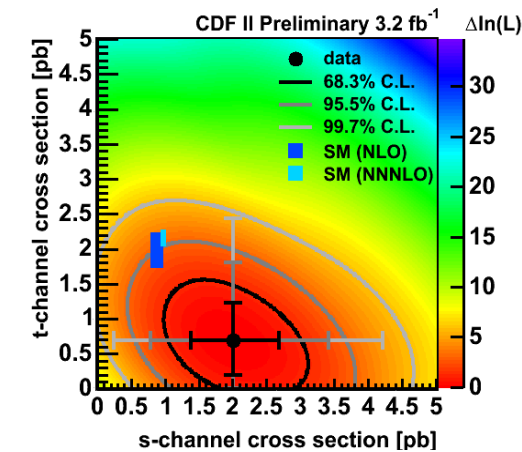
II	\mathcal{L} [fb ⁻¹]	Significance		σ_{s+t} [pb]
		Exp.	Obs.	
LF	3.2	4.0 σ	2.4 σ	1.6 ^{+1.0} _{-0.8}
s-channel	3.2	1.1 σ	2.0 σ	1.5 ^{+0.9} _{-0.8}



More results...

Separate search using NN

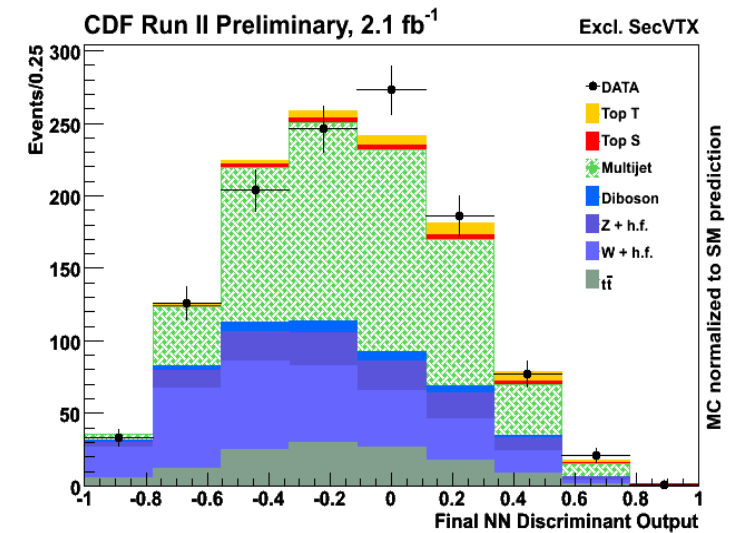
- 5 networks, 2 outputs combined into 2D discriminant in 2j1tag channel



	σ (pb)	
s-ch	$2.0^{+0.7}_{-0.6}$	1.4
t-ch	$0.7^{+0.5}_{-0.5}$	1.0

Simultaneous fit of σ_s and σ_t (LF)

MET+ jets combined search



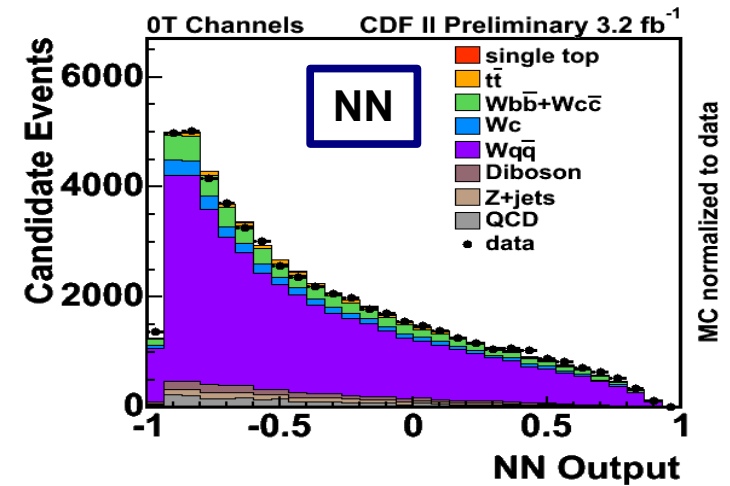
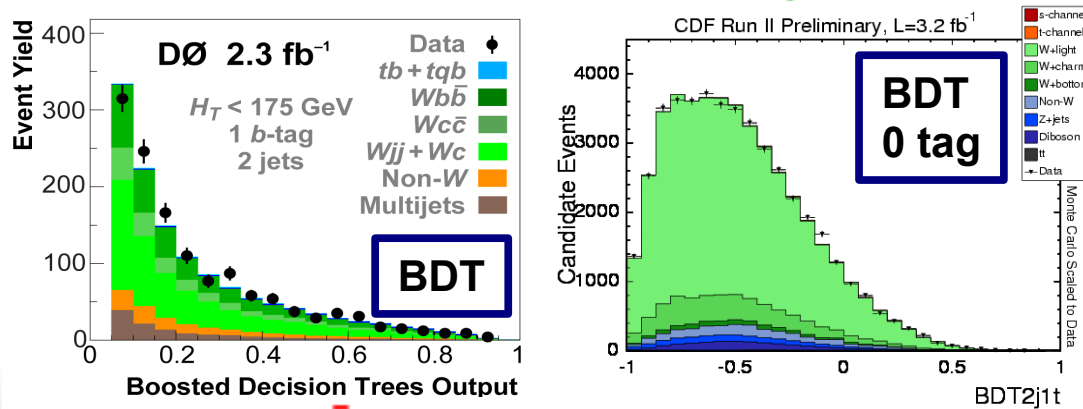
	\mathcal{L} [fb ⁻¹]	Significance		σ_{s+t} [pb]
		Exp.	Obs.	
\cancel{E}_T +jets	2.1	1.4 σ	2.1 σ	$4.9^{+2.5}_{-2.2}$

Cross check samples

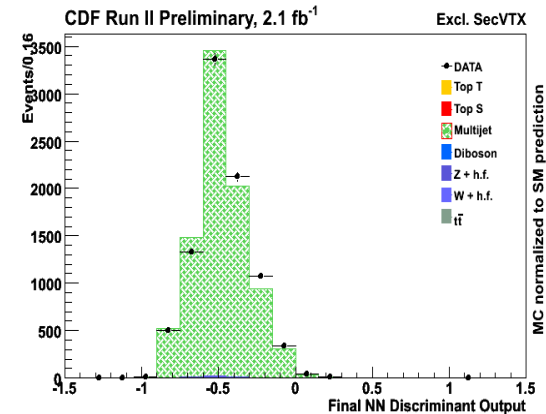
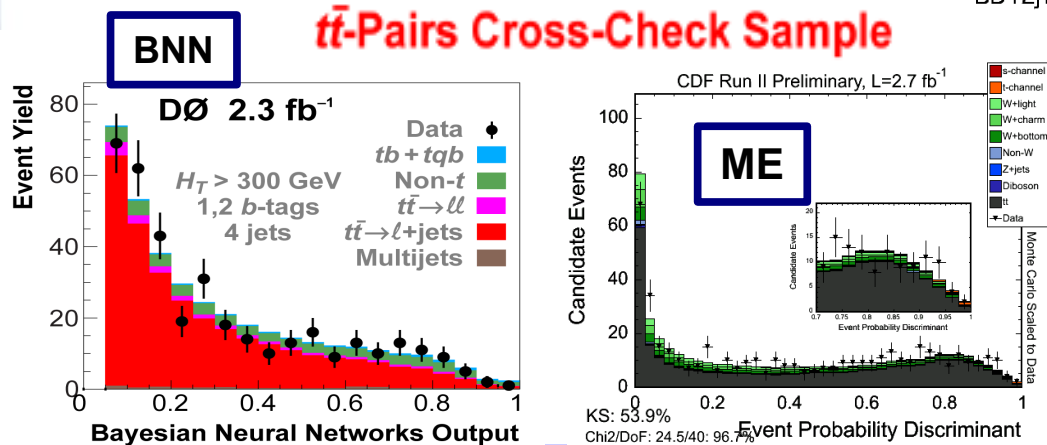
Cross checks of discriminant performance using samples depleted in signal

- Untagged (high statistics)
- W+jets ($n_j=2$, 1 b -tag, $H_T(l,\nu,jets) < 175$ GeV)
- $t\bar{t}$ dominated ($n_j=4$, ≥ 1 b -tag, $H_T > 300$ GeV)

W+Jets Cross-Check Sample



MET + jets
QCD enriched sample



Combination method

- Even though all (majority) D0 (CDF) MVA analyses use the same data they are not 100% correlated
- Choose a priori to quote combination result as main



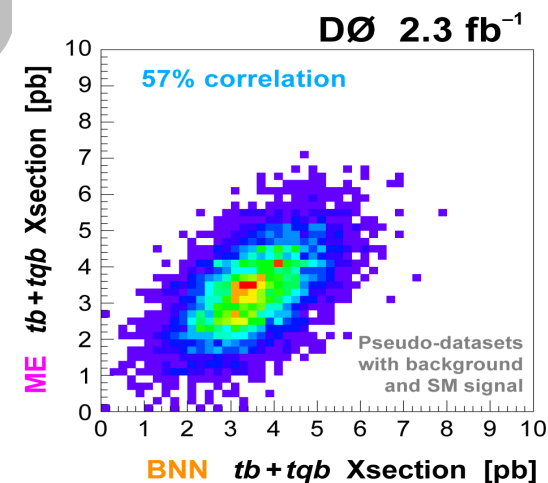
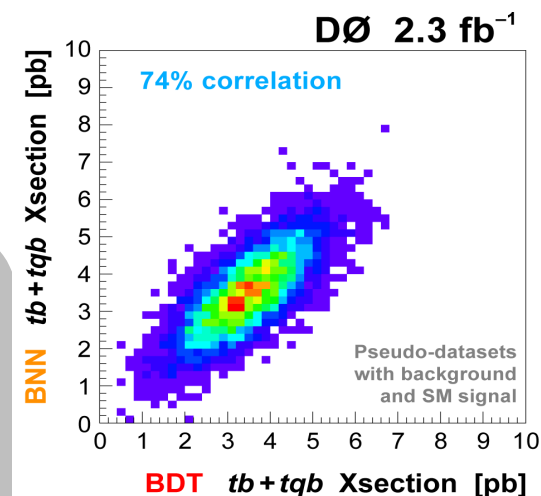
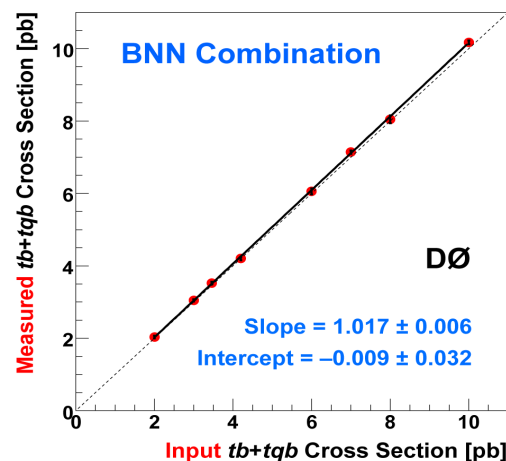
Technique: **NeuroEvolution of Augmenting Topologies**



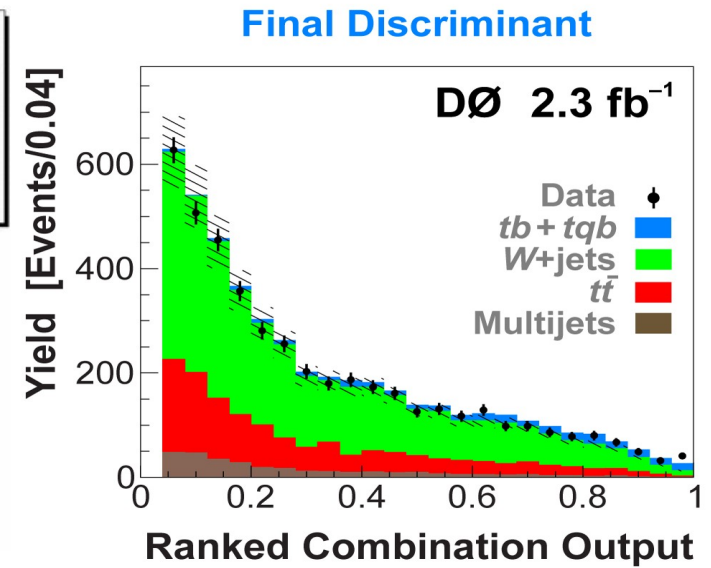
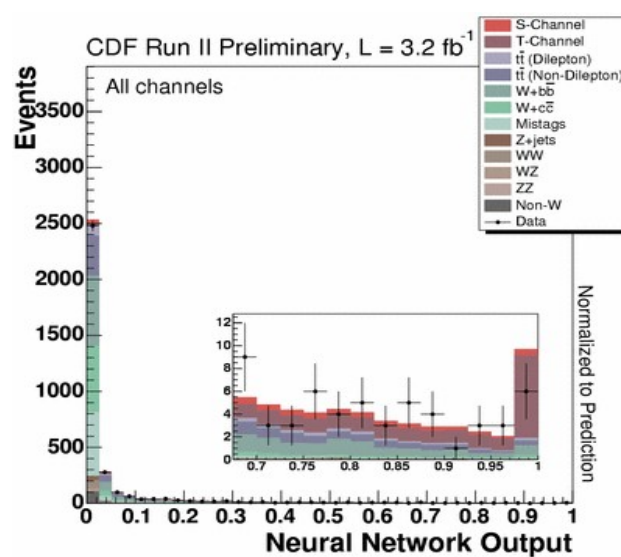
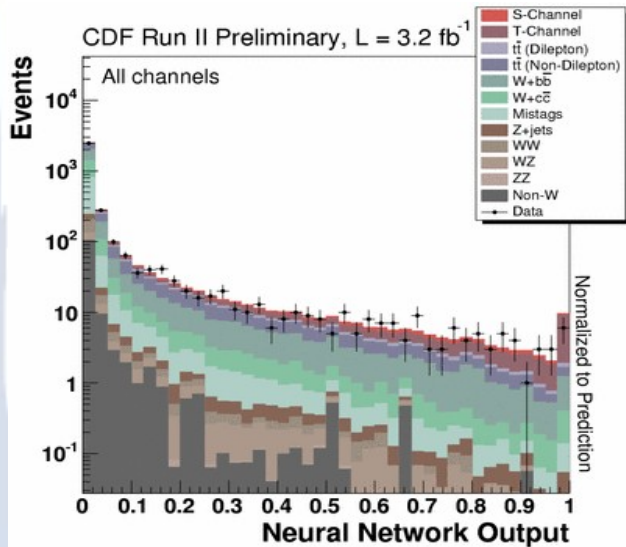
- Optimizes network topology, inter-node weights, output binning
- NN trained to give the best expected p -value
- Inputs: **5 l+jets discriminants (BDT, ME, NN, LF, SLF), and MET+ jets discriminant (8+3=11 channels)**
- Sensitivity: $5.2\sigma \rightarrow >5.9\sigma$

Technique: **Bayesian Neural Network**



- Inputs: **3 discriminant output distributions (BDT, ME, NN)**
- Sensitivity: $4.3\sigma \rightarrow 4.5\sigma$

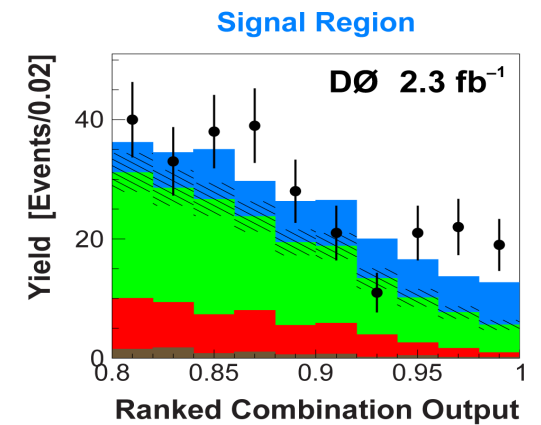
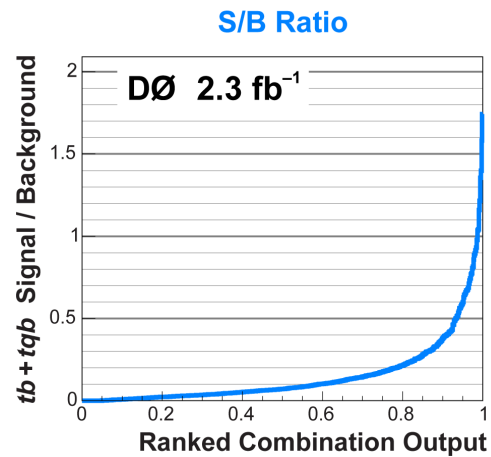


Combination results



Observation !!

	\mathcal{L} [fb ⁻¹]	Significance		σ_{s+t} [pb]
		Exp.	Obs.	
	2.3	4.5 σ	5.0 σ	3.9 ^{+0.9} _{-0.9}
	3.2	5.9 σ	5.0 σ	2.3 ^{+0.6} _{-0.5}



Signal normalized to measured cross section

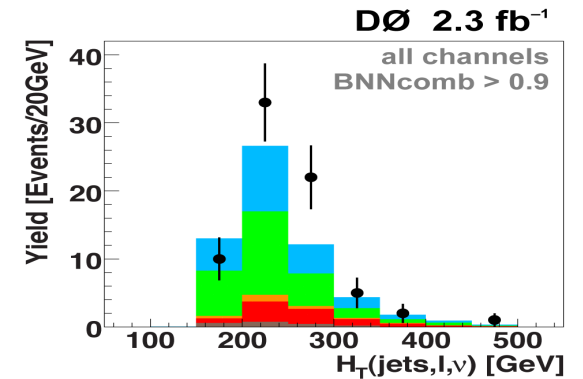
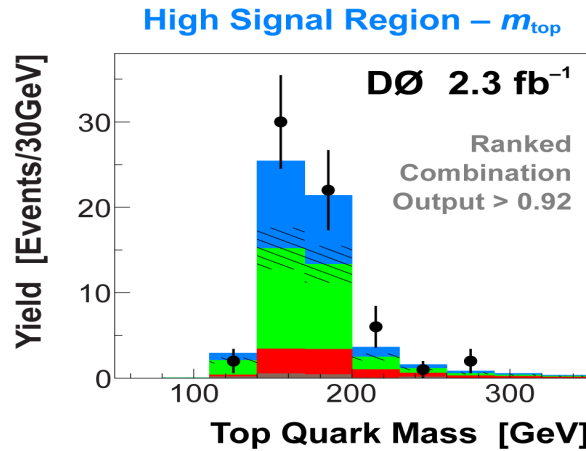
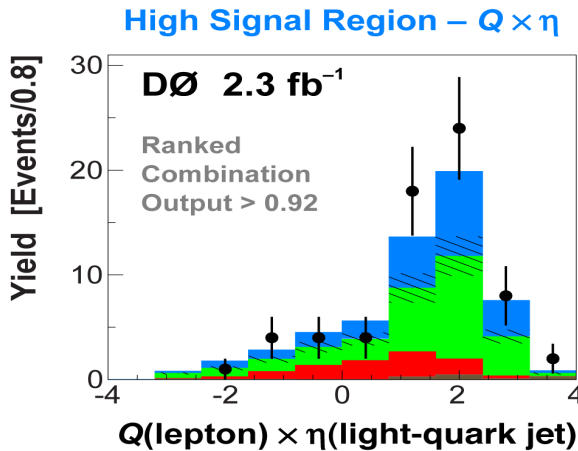
Can we see it?

Look at high discriminant regions



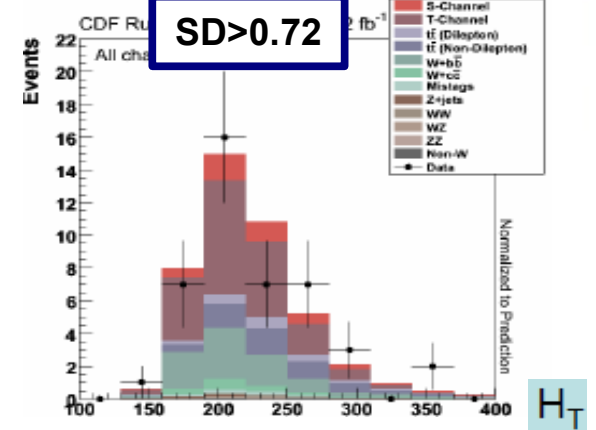
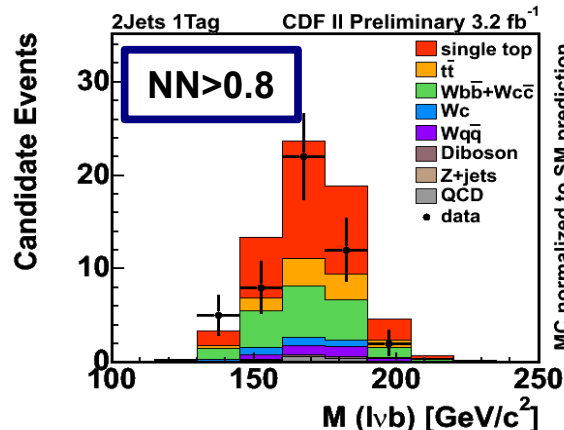
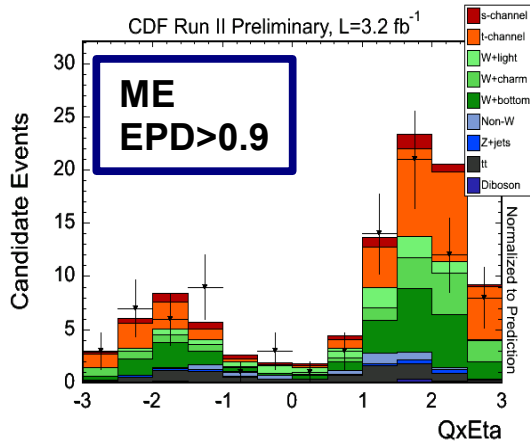
BNN combined D > 0.92, all channels

Signal normalized to measured σ



The most sensitive channel: 2 jets, 1 b-tag

Signal normalized to expected SM σ



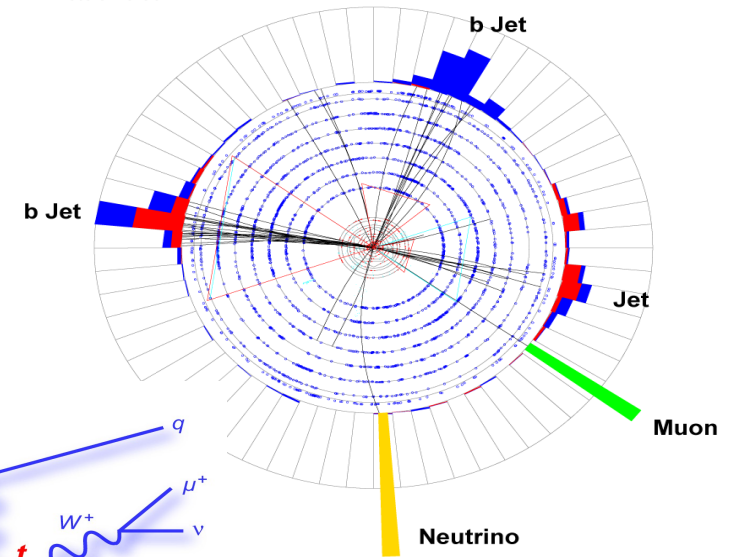
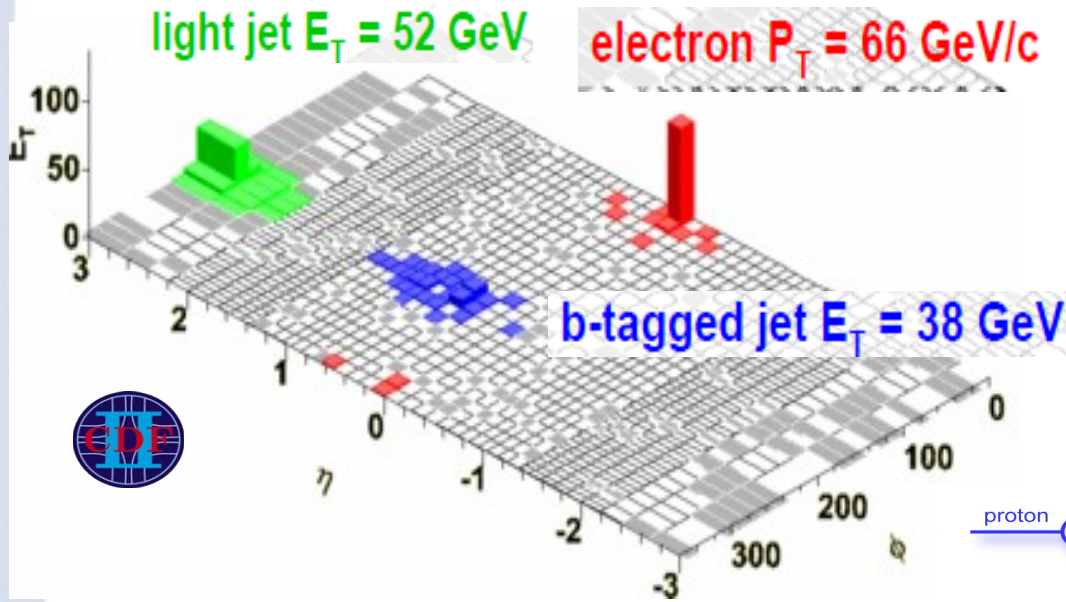
Events

DØ Experiment Event Display Single Top Quark Candidate Event, 2.3 fb^{-1} Analysis

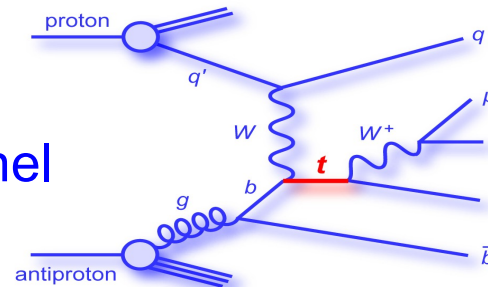


Run 223473 Evt 27278544 Sun Jul 23 19:21:41 2006

ET scale: 28 GeV

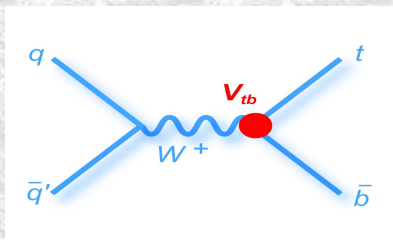


t-channel

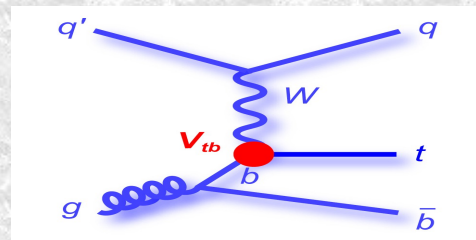


Run	Event	Lepton	KIT NN	BDT	LF	ME	NN	SD	H_T	$M_{l\nu b}$	$Q \times \eta$
148916	792764	CEM	0.94	0.76	0.94	0.97	0.94	0.99	219.0	189.7	-2.15
206282	3294678	CMUP	0.99	0.76	0.80	0.98	0.94	1.0	307.3	178.0	1.31
229936	4412760	CMX	1.00	0.95	1.00	0.99	0.97	1.0	221.0	171.1	2.03
242557	1564229	CEM	0.54	0.85	1.00	0.99	0.93	1.0	189.8	164.5	2.84
262776	4920497	CEM	0.86	0.95	1.00	1.00	0.92	1.0	191.8	160.8	2.67

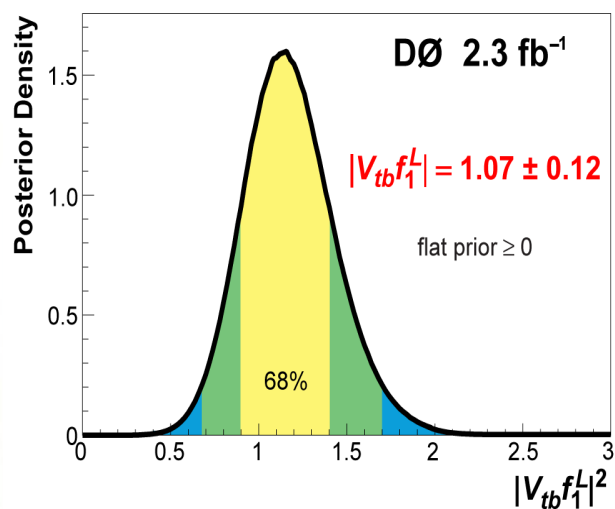
Measurement of $|V_{tb}|$



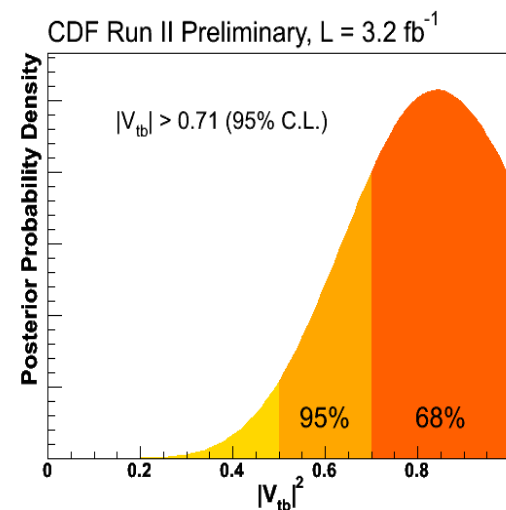
$$|V_{tb, meas}|^2 = \frac{\sigma_{meas}}{\sigma_{SM}} |V_{tb, SM}|^2$$



- Assume $|V_{td}|^2 + |V_{ts}|^2 \ll |V_{tb}|^2$, SM (V-A) and CP conserving Wtb vertex
- No assumption on the number of quark families or CKM unitarity



Additional Systematic Uncertainties for the $ V_{tb} $ Measurement	
DØ 2.3 fb ⁻¹	
For the $tb+qb$ theory cross section	
Top quark mass	4.2%
Parton distribution functions	3.0%
Factorization scale	2.4%
Strong coupling α_s	0.5%



$|V_{tbf_1^L}| = 1.07 \pm 0.12$ (sys+th)
 $|V_{tb}| > 0.78$ at 95% CL

$|V_{tb}| = 0.91 \pm 0.11$ (sys) ± 0.07 (th)
 $|V_{tb}| > 0.71$ at 95% CL



Summary

- Single top quark production has been observed at Tevatron by CDF and D0 with signal significance of 5σ
- Both cross section and $|V_{tb}|$ measurements agree with SM

Submitted to PRL

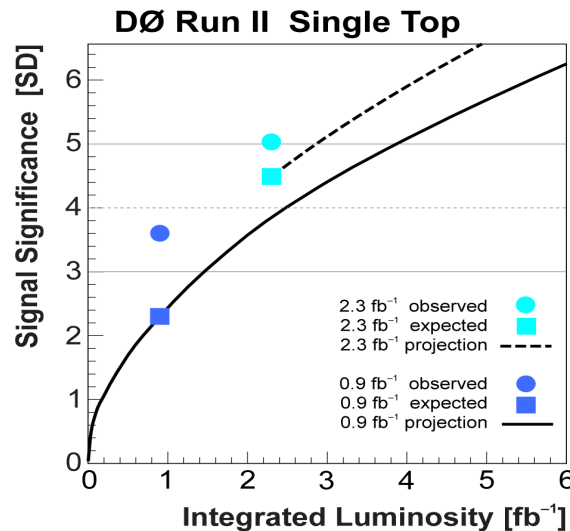
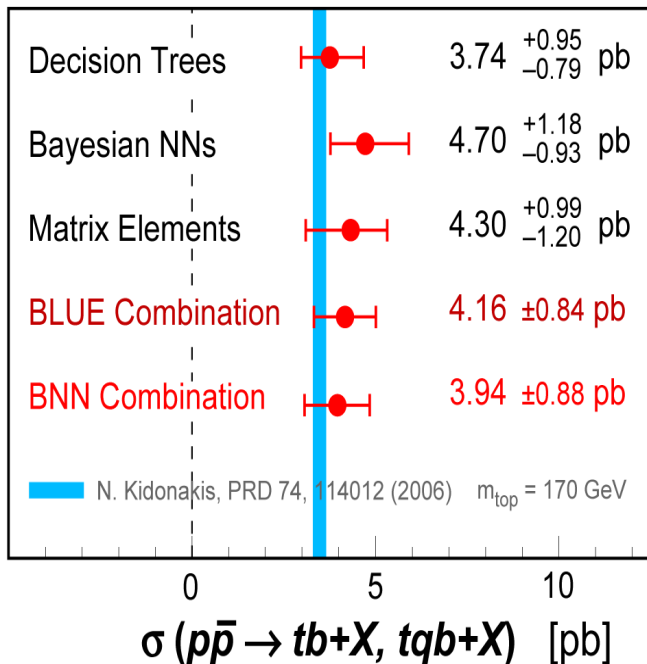


ArXiv:0903.0850

ArXiv:0903.0885

D0 2.3 fb⁻¹

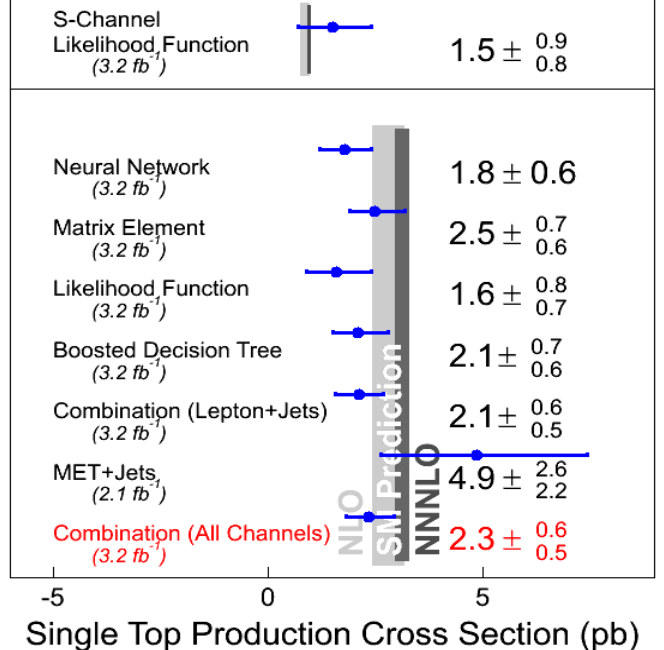
March 2009



D0 projection

CDF Preliminary Single Top Summary

For M_{top} = 175 GeV/c²

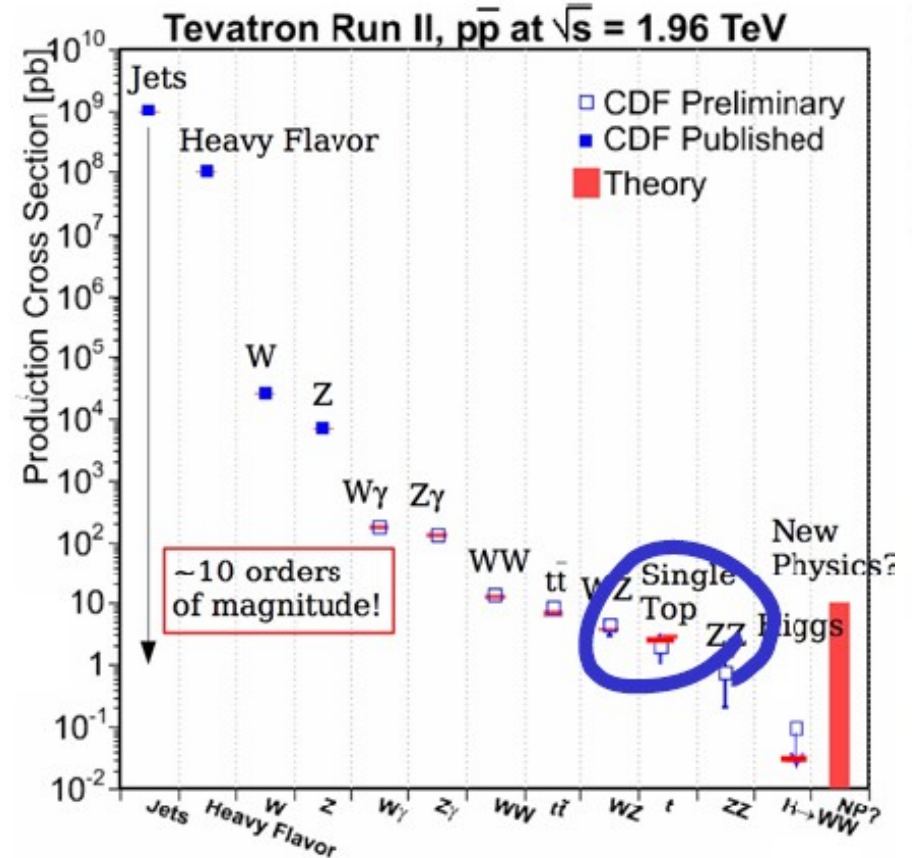


Outlook

This is just the beginning of the single top physics

- Precise measurements of σ_t and σ_s
- Top quark polarization
- Search for Anomalous Top quark couplings
- W' and H^+ searches
- Top production through FCNC

From R. Wallny's Wine and Cheese talk, 03/10/2009



Milestone in the race for Higgs Boson !

Public web sites

More details can be found on the public pages of the experiments:



http://www-cdf.fnal.gov/physics/new/top/public_singletop.html



http://www-d0.fnal.gov/Run2Physics/top/singletop_observation

Backup

V_{tb} measurement

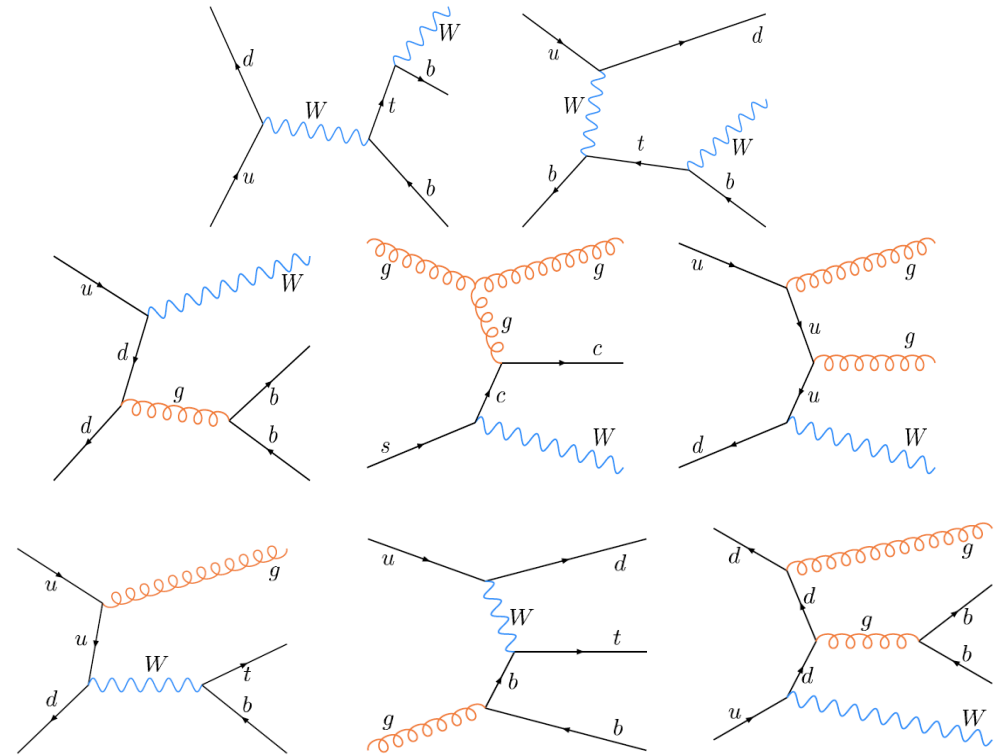
$$\Gamma_{Wtb}^\mu = -\frac{g}{\sqrt{2}} V_{tb} \left\{ \gamma^\mu [f_1^L P_L + f_1^R P_R] - \frac{i\sigma^{\mu\nu}}{M_W} (p_t - p_b)_\nu [f_2^L P_L + f_2^R P_R] \right\}$$

= 0



Summary of MEs

Matrix Elements used to Separate Single Top Signal from Background DØ 2.3 fb ⁻¹			
2 Jets		3 Jets	
$t\bar{b}$	$u\bar{d} \rightarrow t\bar{b}$	$t\bar{b}g$	$u\bar{d} \rightarrow t\bar{b}g$
tq	$ub \rightarrow td$ $d\bar{b} \rightarrow t\bar{u}$	tqg	$ub \rightarrow tdg$ $d\bar{b} \rightarrow t\bar{u}g$
		$tq\bar{b}$	$ug \rightarrow t\bar{d}\bar{b}$ $\bar{d}g \rightarrow t\bar{u}\bar{b}$
$Wb\bar{b}$	$u\bar{d} \rightarrow Wb\bar{b}$	$Wb\bar{b}g$	$u\bar{d} \rightarrow Wb\bar{b}g$
$Wc\bar{g}$	$\bar{s}g \rightarrow Wc\bar{g}$		
Wgg	$u\bar{d} \rightarrow Wgg$	$W\bar{u}gg$	$\bar{u}g \rightarrow W\bar{u}gg$
WW	$q\bar{q} \rightarrow WW$		
WZ	$q\bar{q} \rightarrow WZ$		
ggg	$gg \rightarrow ggg$		
$t\bar{t}$	$q\bar{q} \rightarrow t\bar{t} \rightarrow \ell^+ \nu b \ell^- \nu \bar{b}$		
$t\bar{t}$	$q\bar{q} \rightarrow t\bar{t} \rightarrow \ell^+ \nu b \bar{u} d \bar{b}$	$t\bar{t}$	$q\bar{q} \rightarrow t\bar{t} \rightarrow \ell^+ \nu b \bar{u} d \bar{b}$

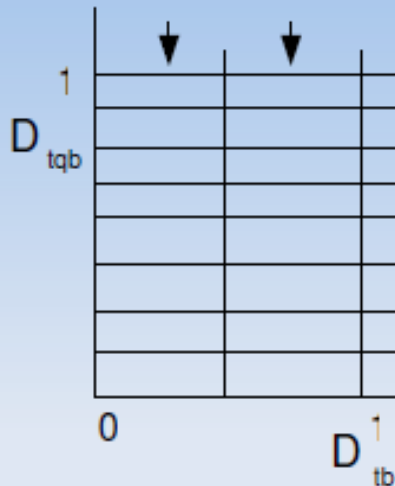


$$P_B(\vec{x}) = C_{Wb\bar{b}g} P_{Wb\bar{b}g}(\vec{x}) + C_{Wugg} P_{Wugg}(\vec{x}) + C_{t\bar{t}} P_{t\bar{t}}(\vec{x})$$

$$d\sigma_{Wcg}(\ell, j_1, j_2) = \varepsilon_c(j_1)(1 - \varepsilon_l(j_2))d\sigma_{Wcg}(\ell, j_1 \rightarrow c, j_2 \rightarrow g) + \varepsilon_l(j_2)(1 - \varepsilon_c(j_1))d\sigma_{Wcg}(\ell, j_2 \rightarrow c, j_1 \rightarrow g).$$

← Wcg example with one tagged and one not tagged jet

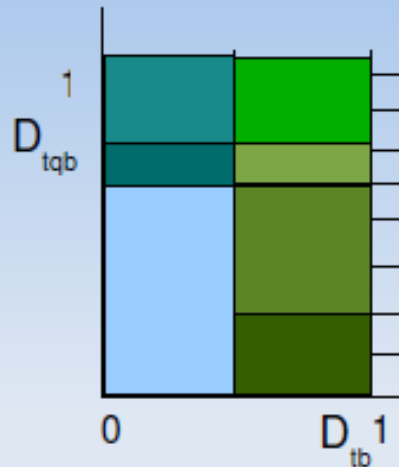
Presentation of discriminant



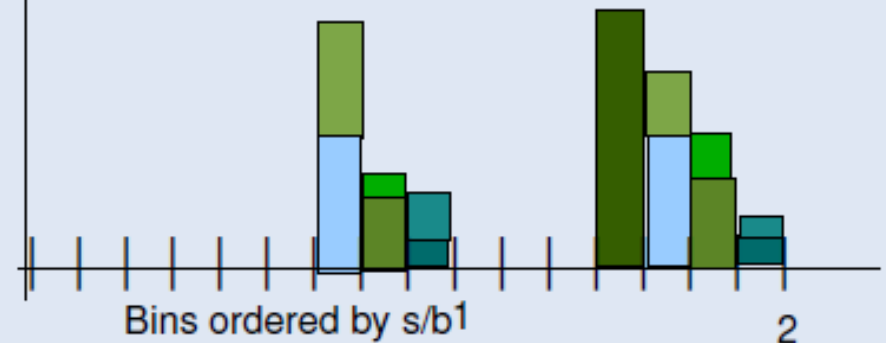
Step 1: t_b and t_{qb} 2-D discriminant divided into 16 bins total



Step 4: Merged bins ordered by s/b in 16 bins from 0 to 1. Red line signifies H_T cut where below the red line is yield < 175 GeV and above is yield > 175 GeV



Step 2: Merge bins so that have sufficient background \rightarrow 7 bins total



Step 5: Histogram divided into low H_T region $[0,1]$ and high H_T region $[1,2]$. Also these regions are rebinned to 16 bins from $[0,2]$

- $s/b = 0.90$
- $s/b = 0.85$
- $s/b = .80$
- $s/b = .60$
- $s/b = .34$
- $s/b = .16$
- $s/b = .15$



Variables in BDT and BNN

Object Kinematics

$p_T(\text{lepton})$
 \cancel{E}_T
 $p_T(\text{jet1})$
 $p_T(\text{jet2})$
 $p_T(\text{jet3})$
 $p_T(\text{jet4})$
 $p_T(\text{tag1})$
 $p_T(\text{tag2})$
 $p_T(\text{light1})$
 $p_T(\text{light2})$
 $p_T(\text{best1})$
 $p_T(\text{notbest2})$
 $E(\text{jet2})$
 $E(\text{light1})$
 $Q(\text{lepton}) \times \eta(\text{jet1})$
 $Q(\text{lepton}) \times \eta(\text{jet2})$
 $Q(\text{lepton}) \times \eta(\text{light1})$
 $Q(\text{lepton}) \times \eta(\text{light2})$
 $Q(\text{lepton}) \times \eta(\text{best1})$
 $Q(\text{lepton}) \times \eta(\text{notbest1})$

Event Kinematics Jet Reconstruction

$A_{\text{planarity}}(W, \text{alljets})$
 $C_{\text{entrality}}(\text{alljets})$
 $S_{\text{phericity}}(W, \text{alljets})$
 $H(\text{alljets} - \text{tag1})$
 $H_T(\text{alljets})$
 $H_T(\text{alljets} - \text{tag1})$
 $H_T(\text{alljets} - \text{best1})$
 $H_T(\text{jet1}, \text{jet2})$
 $H_T(\text{lepton}, \cancel{E}_T)$
 $H_T(\text{lepton}, \cancel{E}_T, \text{alljets})$
 $H_T(\text{lepton}, \cancel{E}_T, \text{jet1}, \text{jet2})$
 $M(\text{alljets})$
 $M(\text{alljets} - \text{tag1})$
 $M(\text{jet1}, \text{jet2})$
 $M(\text{jet3}, \text{jet4})$
 $M(\text{light1}, \text{light2})$
 $M(W, \text{jet1}, \text{jet2})$
 $M_T(\text{jet1}, \text{jet2})$
 $p_T(\text{jet1}, \text{jet2})$
 $\sqrt{\hat{s}}$
 $M_T(W)$

$\text{Width}_\eta(\text{jet1})$
 $\text{Width}_\eta(\text{jet2})$
 $\text{Width}_\eta(\text{jet4})$
 $\text{Width}_\eta(\text{tag1})$
 $\text{Width}_\eta(\text{tag2})$
 $\text{Width}_\eta(\text{best1})$
 $\text{Width}_\eta(\text{light2})$
 $\text{Width}_\eta(\text{notbest2})$
 $\text{Width}_\phi(\text{jet1})$
 $\text{Width}_\phi(\text{jet2})$
 $\text{Width}_\phi(\text{jet4})$
 $\text{Width}_\phi(\text{tag2})$
 $\text{Width}_\phi(\text{light1})$
 $\text{Width}_\phi(\text{light2})$
 $\text{Width}_\phi(\text{notbest1})$
 $p_T^{\text{rel}}(\text{jet1}, \mu)$
 $M(\text{jet1})$
 $M(\text{tag1})$
 $M(\text{best1})$

Top Quark Reconstruction

$M(W, \text{jet1})$ (leading jet top mass)
 $M(W, \text{jet1}, S2)$ (with second neutrino solution)
 $M(W, \text{jet2})$
 $M(W, \text{jet2}, S2)$
 $M(W, \text{jet3}, S2)$
 $M(W, \text{tag1})$ (“b-tagged” top mass)
 $M(W, \text{tag1}, S2)$
 $M(W, \text{tag2})$
 $M(W, \text{light1}, S2)$
 $M(W, \text{best1})$ (“best” top mass)
 $M(W, \text{best1}, S2)$
 $M(W, \text{notbest1}, S2)$
 $M(W, \text{notbest2})$
 $M(W, \text{notbest2}, S2)$
 $M_{\text{top}}^{\Delta M^{\text{min}}}$
 $M_{\text{top}}^{\text{sig}}$
 $\Delta M_{\text{top}}^{\text{min}}$
 $\text{Significance}_{\text{min}}(M_{\text{top}})$
 $p_z(\nu, S2)$

Angular Correlations

$\Delta R(\text{jet1}, \text{jet2})$
 $\Delta R(\text{lepton}, \text{jet1})$
 $\Delta R(\text{lepton}, \text{tag1})$
 $\Delta R(\text{lepton}, \text{best1})$
 $\Delta R(\text{lepton}, \text{light1})$
 $\Delta R^{\text{min}}(\text{alljets})$
 $\Delta R^{\text{min}}(\text{lepton}, \text{alljets})$
 $\Delta\phi(\text{lepton}, \cancel{E}_T)$
 $\Delta\phi(\text{lepton}, \text{tag1})$
 $\cos(\text{lepton}, \text{jet1})_{\text{btaggedtop}}$
 $\cos(\text{lepton}, \text{tag1})_{\text{btaggedtop}}$
 $\cos(\text{lepton}_{\text{btaggedtop}}, \text{btaggedtop}_{\text{CMframe}})$
 $\cos(\text{lepton}, \text{light1})_{\text{btaggedtop}}$
 $\cos(\text{lepton}, \text{best1})_{\text{besttop}}$
 $\cos(\text{best1}, \text{notbest1})_{\text{besttop}}$
 $\cos(\text{lepton}_{\text{besttop}}, \text{besttop}_{\text{CMframe}})$
 $\cos(\text{lepton}, Q(\text{lepton}) \times z)_{\text{besttop}}$



Choice of variables – BDT

- Start with 600 variables expected to differ between signal and at least one of the background components
- Remove variables from list with low KS-test value between data and background model
- Remove variables with not much discrimination power to reduce computation time later (rank them after decision tree training)

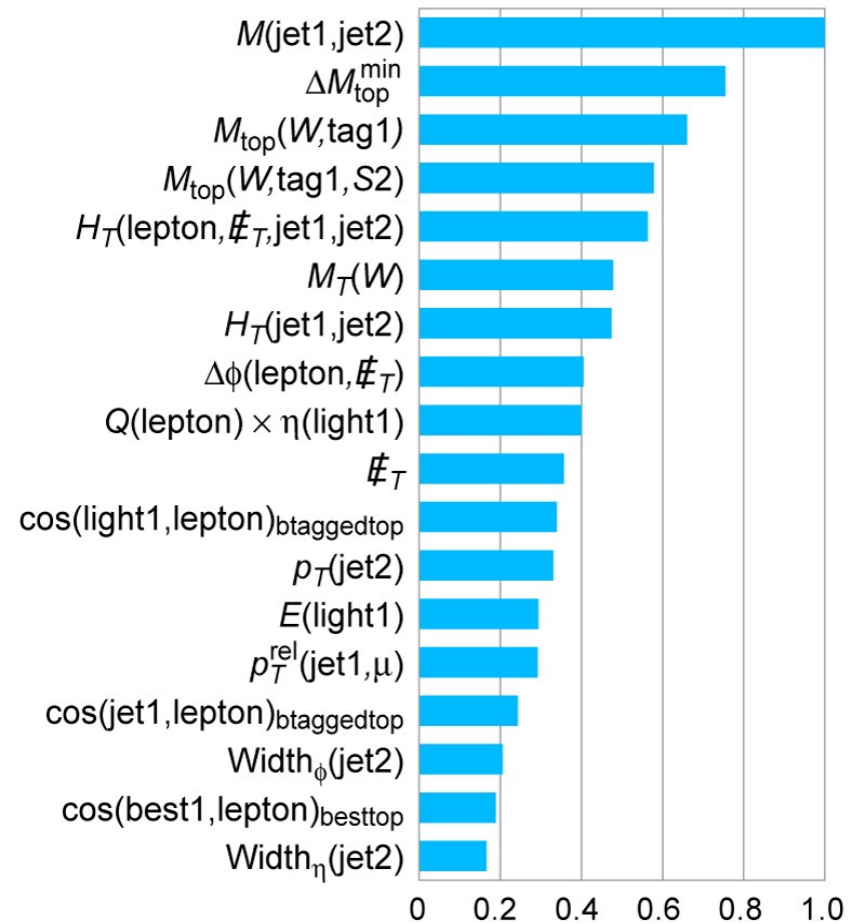
Best Variables to Separate Single Top from W+Jets	
DØ 2.3 fb ⁻¹ Analysis	
Object kinematics	\cancel{E}_T
	$p_T(\text{jet2})$
	$p_T^{\text{rel}}(\text{jet1}, \text{tag-}\mu)$
	$E(\text{light1})$
Event kinematics	$M(\text{jet1}, \text{jet2})$
	$M_T(W)$
	$H_T(\text{lepton}, \cancel{E}_T, \text{jet1}, \text{jet2})$
	$H_T(\text{jet1}, \text{jet2})$
	$H_T(\text{lepton}, \cancel{E}_T)$
Jet reconstruction	$\text{Width}_\phi(\text{jet2})$
	$\text{Width}_\eta(\text{jet2})$
Top quark reconstruction	$M_{\text{top}}(W, \text{tag1})$
	$\Delta M_{\text{top}}^{\text{min}}$
	$M_{\text{top}}(W, \text{tag1}, S2)$
Angular correlations	$\cos(\text{light1}, \text{lepton})_{\text{btaggedtop}}$
	$\Delta\phi(\text{lepton}, \cancel{E}_T)$
	$Q(\text{lepton}) \times \eta(\text{light1})$

Best Variables to Separate Single Top from Top Pairs	
DØ 2.3 fb ⁻¹ Analysis	
Object kinematics	$p_T(\text{notbest2})$
	$p_T(\text{jet4})$
	$p_T(\text{light2})$
Event kinematics	$M(\text{alljets} - \text{tag1})$
	Centrality(alljets)
	$M(\text{alljets} - \text{best1})$
	$H_T(\text{alljets} - \text{tag1})$
	$H_T(\text{lepton}, \cancel{E}_T, \text{alljets})$
	$M(\text{alljets})$
Jet reconstruction	$\text{Width}_\eta(\text{jet4})$
	$\text{Width}_\phi(\text{jet4})$
	$\text{Width}_\phi(\text{jet2})$
Angular correlations	$\cos(\text{lepton}_{\text{btaggedtop}}, \text{btaggedtop}_{\text{CMframe}})$
	$Q(\text{lepton}) \times \eta(\text{light1})$
	$\Delta R(\text{jet1}, \text{jet2})$

Choice of variables – BNN

- Start from a set of ~ 150 well modeled variables
- Use the highest ranked variables for each channel
- Ranking determined by Rulefit* -a MVA based on Decision Trees (DT)
- Uses 1/3 of the available MC samples. These samples are later not used for the measurement
- Importance of each variable given by how often it appears in the set of rules that define the DT
- Keep variables with Importance > 10
- Corresponds to 18-28 variables, depending on the channel

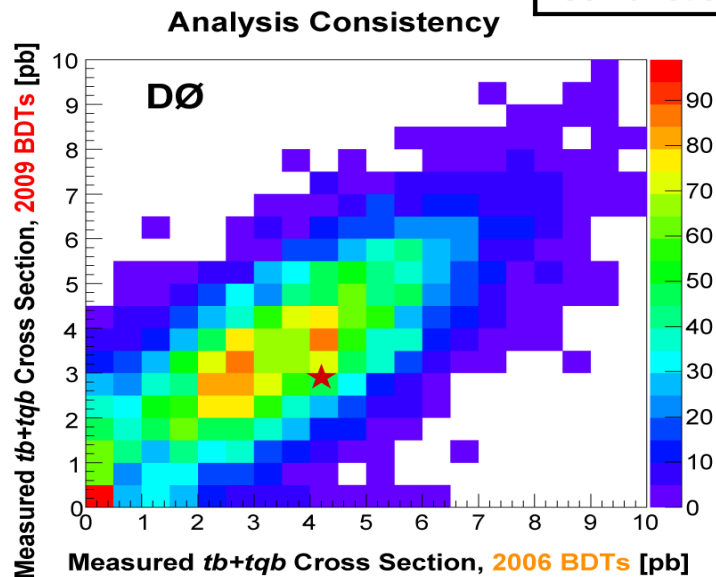
DØ 2.3 fb⁻¹ Single Top BNN Analysis
RuleFit Ranking for e+2jets/1tag Channel





Consistency test

Measured $tb+qb$ Cross Section [pb]					
DØ 2.3 fb ⁻¹ Analysis					
Method	All Channels	Electron Only	Muon Only	Run IIa Only	Run IIb Only
BDT	3.74 +0.95 -0.79	4.4 +1.5 -1.2	3.3 +1.2 -1.0	2.5 +1.3 -1.2	4.9 +1.4 -1.2
BNN	4.70 +1.18 -0.93	5.3 +1.5 -1.4	4.0 +1.3 -1.2	3.4 +1.4 -1.3	5.7 +1.5 -1.3
ME	4.30 +0.98 -1.20	3.2 +1.9 -1.6	3.9 +1.2 -1.2	2.6 +1.3 -1.2	5.4 +1.7 -1.4
Combination	3.94 +0.88 -0.88	4.5 +1.3 -1.2	3.5 +1.1 -1.0	2.6 +1.2 -1.1	5.0 +1.2 -1.2



Measured single top cross sections using the 2009 and the 2006 decision trees on 5,000 pseudo-datasets generated from the 2009 Run IIa e+jets samples.

The red star shows the measurements in real data: 4.2 pb from the 2006 analysis and 2.9 pb from the 2009 analysis. This 1.3 pb shift is not uncommon, as seen from the width of the distribution from the pseudo-datasets.

Systematics on combination

