

# The physics of the spallation (target)

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*International Training Course (ITC-8)  
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Politecnico di Torino*

# Introduction: content and general ideas

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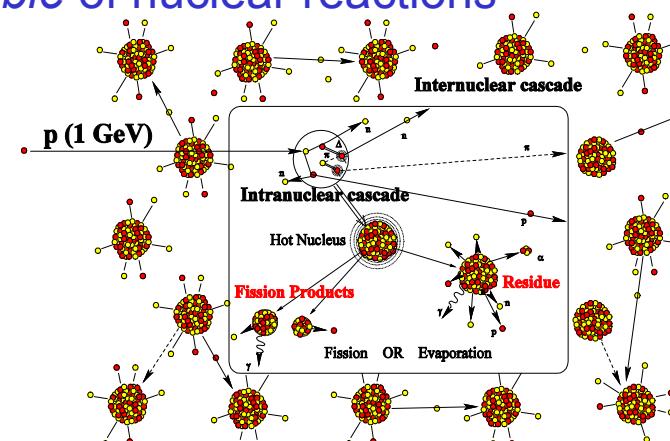
- Two lectures, one on **physics** and one on **applications** :
  - General description of spallation process
    - Models
    - Comparison with experimental data
  - Application to spallation targets
    - Few chosen examples
- Global bias from my past and current work
  - Models (INCL)
  - Targets (MEGAPIE)
- I will never use the word « subcritical » since I only concentrate on the target (the surrounding core does not exist... for me!!!)
- Acknowledgements: Alain Boudard (CEA), Sylvie Leray (CEA), Luca Zanini (PSI)

# Introduction: spallation physics

- General characteristics and observables
- Strategy:
  - observables for the range 20 MeV-200MeV
  - models beyond 200 MeV
- Modelling of the spallation physics
  - Two or three steps
  - Low energy models
- Experimental information:
  - Large list of observables
  - Comparison with model predictions
- What we have and what we still need...

# Spallation: definition and history

- Spallation definition (*G.T. Seaborg, PhD thesis, 1937*)
  - Process between a **light particle** (p,n) with an energy of at least 100 MeV with an “**heavy**” nucleus leading to **emission of light particles** and leaving an **heavy residue**
  - NOT a reaction!!! But an **ensemble of nuclear reactions**
    - Huge variety of final states
- History:
  - observation of particle cascades in cosmic rays interactions  
*G. Rossi, ZP82 (1933) 151*
  - first accelerators: many nucleons emitted by the target nucleus  
*Cunningham, PR72 (1947) 739*
  - two step mechanism  
*Serber, PR72 (1947) 1114*



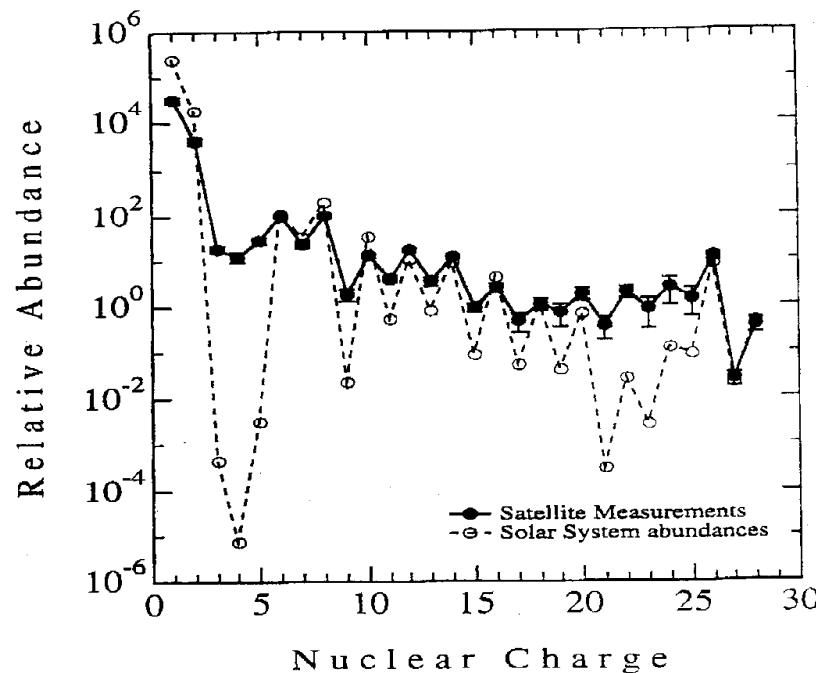
# Spallation: observables

- Observables needed for the design of a target:
  - Neutron production
    - Number → power of the system / needed accelerator intensity
    - Energy and spatial distribution → target
    - High energy neutrons → shielding
  - Charged particle production
    - Gas production ( $H_2$ , He) → embrittlement
    - Energy distributions → Energy deposition, dpa
  - Residual nuclei production
    - Element distribution → corrosion, change in metallurgical properties
    - Isotope distribution → activity (short lived isotopes), radiotoxicity (long lived isotopes), decay heat
    - Recoil energies → dpa in structures, energy deposition

# Spallation: applications in different fields

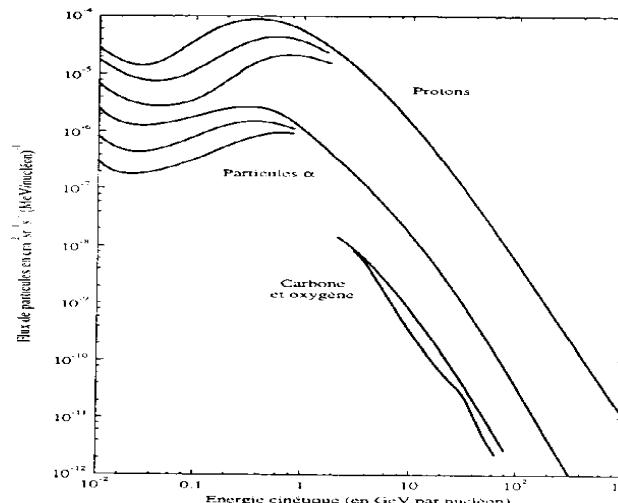
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- Astrophysics
  - Secondary reactions of cosmic rays in interstellar medium
    - explanation of abundance of isotopes
    - decide among models for galactic nucleosynthesis
    - origin of cosmic rays
  - Composition of meteorites



# Spallation: applications in different fields

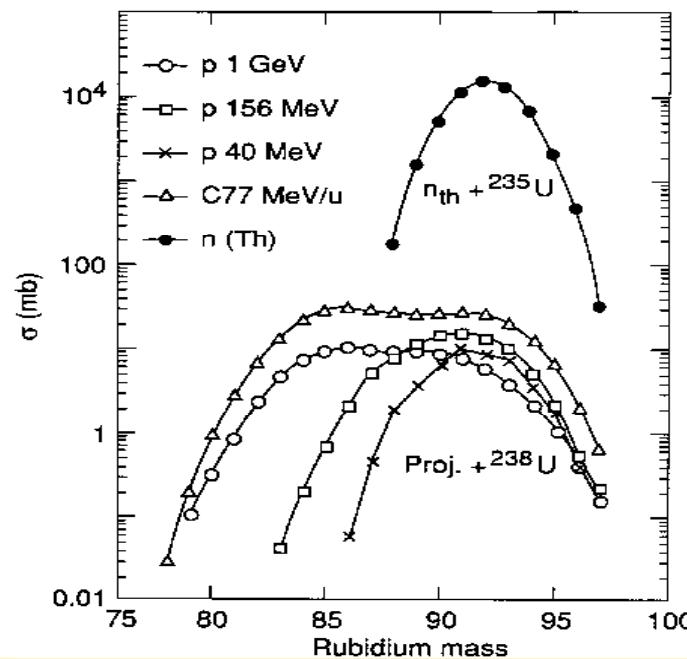
- Space instruments
  - Cosmic ray bombardment of the spacecraft and instruments
    - Radiation damage on electronics
    - Radioprotection of space crew
    - Noise due to secondary gammas, neutrons and spallation residues
  - Ex.: spectrometer of the INTEGRAL mission devoted to high resolution  $\gamma$ -ray astronomy



# Spallation: applications in different fields

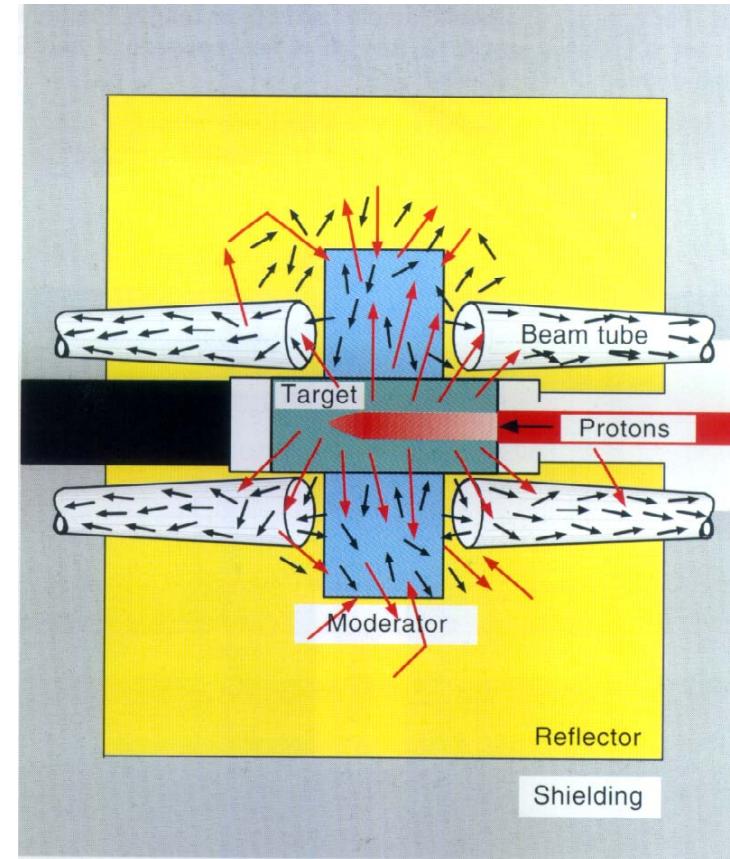
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- Rare isotope production and RIB
  - Direct methods
    - $p$  (1 GeV) + A → low energy RIB
    - fragmentation of GeV/A heavy ions → high energy RIB
  - Converter methods: use of produced neutrons to
    - induce fission → low energy RIB
    - produce tritium and radioisotopes for medicine



# Spallation: applications in different fields

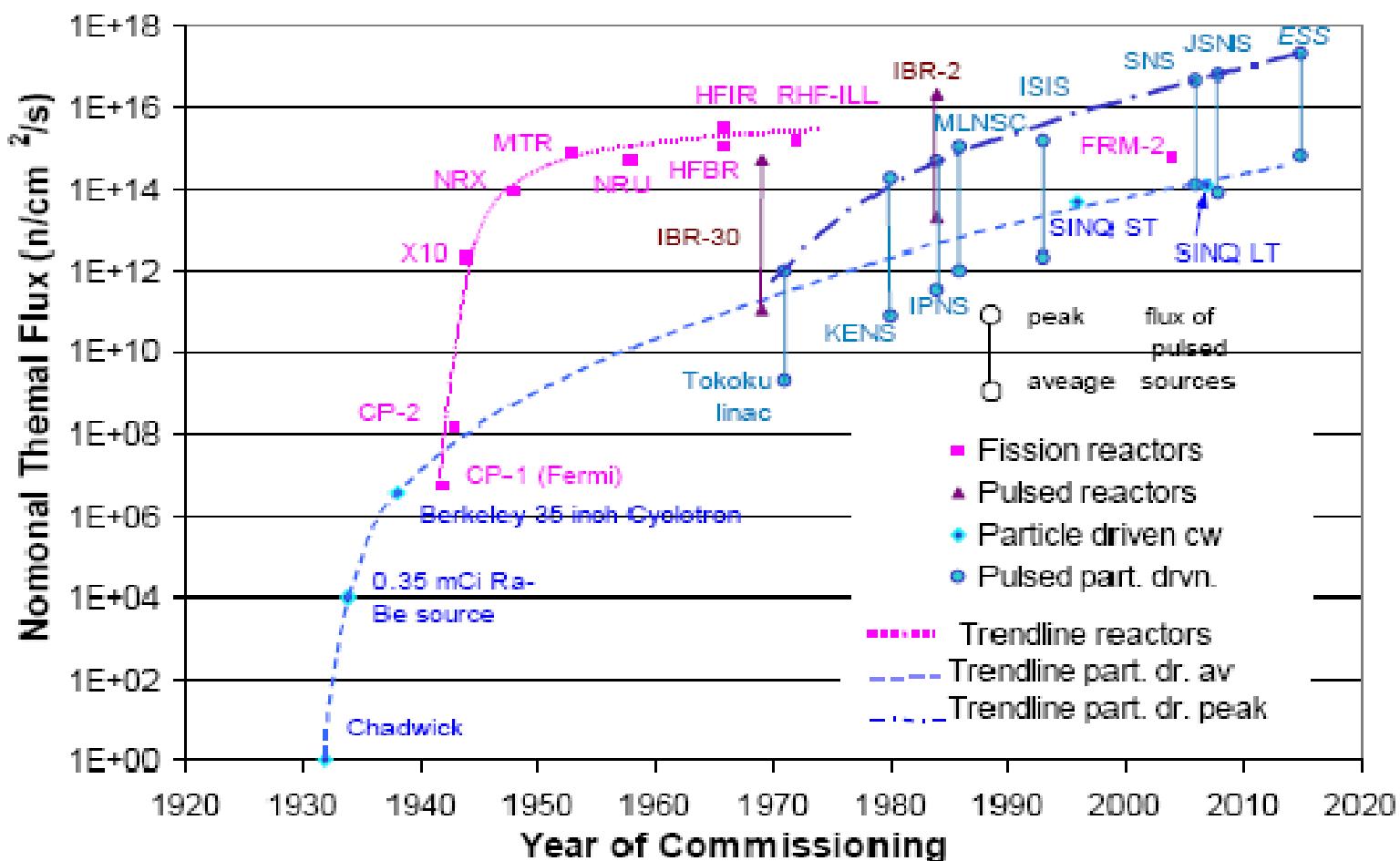
- Spallation neutron sources
  - Moderation of spallation neutrons in (heavy) water
  - Reflectors to direct escaping neutrons into beam tubes
    - **pulsed sources**: well-defined time structure, high peak flux  
→ TOF experiments
    - **continuous sources**: high neutron flux in a large volume  
→ irradiation experiments, imaging



# Neutron sources in the world

## Development of Neutron Sources ("Top of the Line")

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ADS@ICTP, Oct. 24

Target Design and Technology

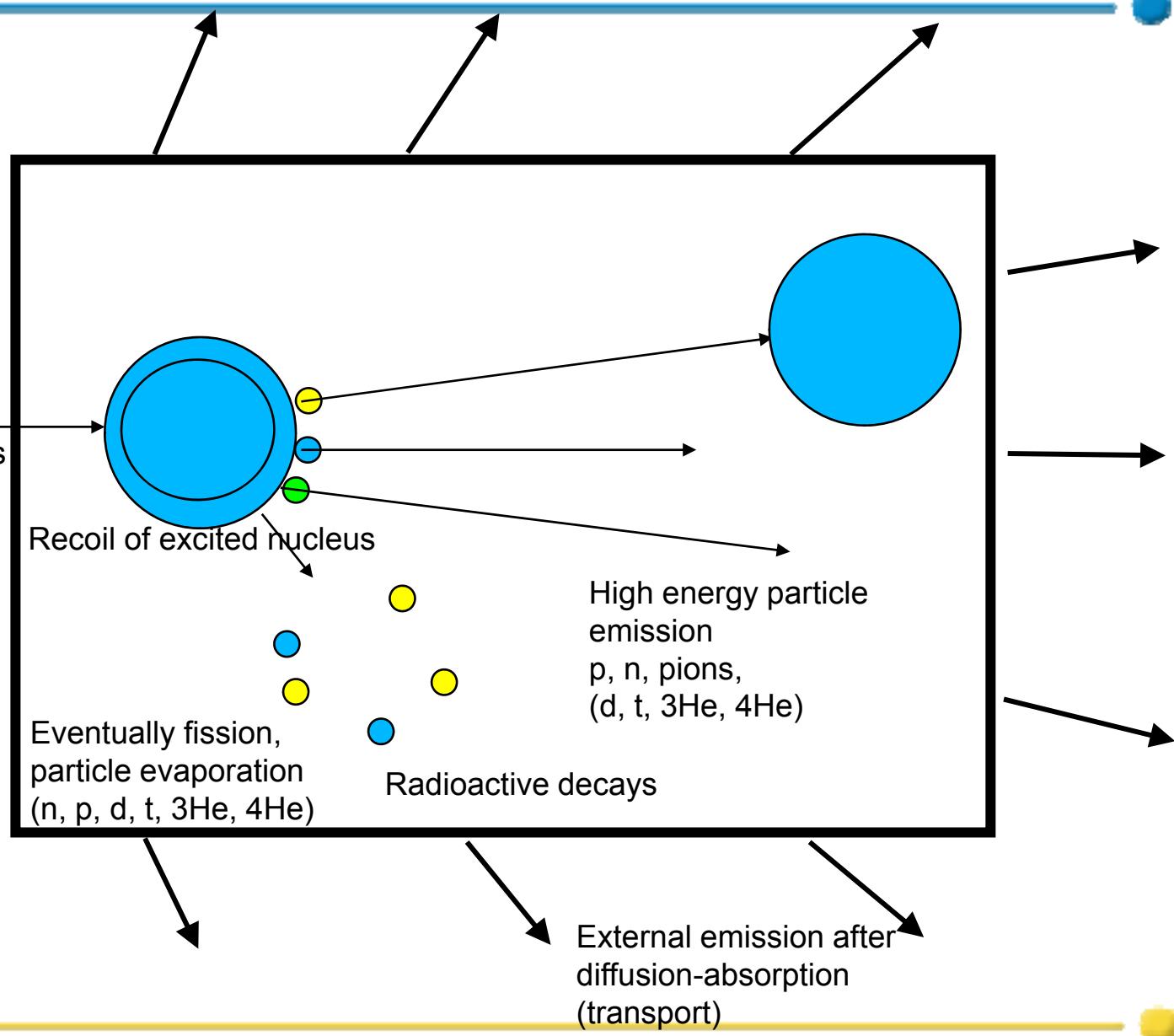
G. S. Bauer 4

# The spallation process as a cartoon....

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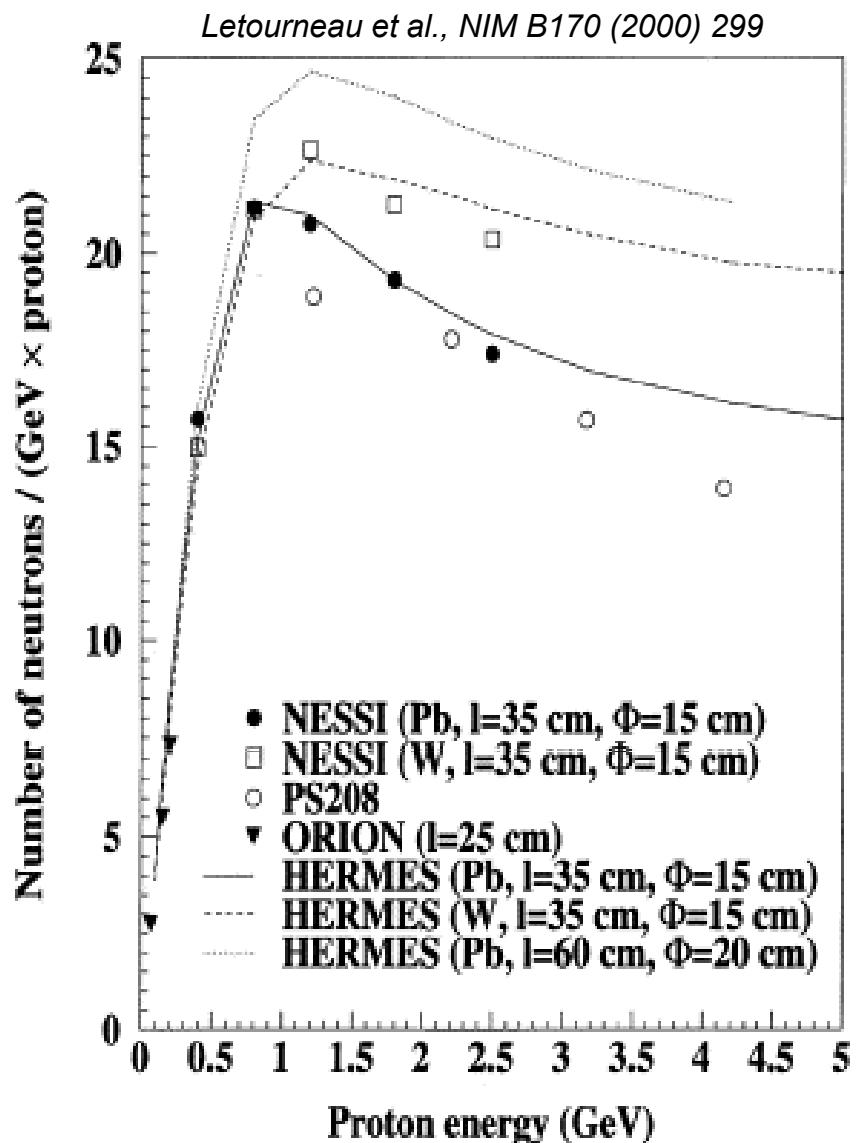
Interaction p-Nucleus

In thick target:  
again spallations  
(at lower energy but from  
p, n, pions)



# Spallation neutron production

- In heavy metal target (Pb, W, Ta) around **20 neutrons per incident proton and GeV**
- Maximal efficiency around 1GeV BUT...
  - Very dependent on geometry and optimization...



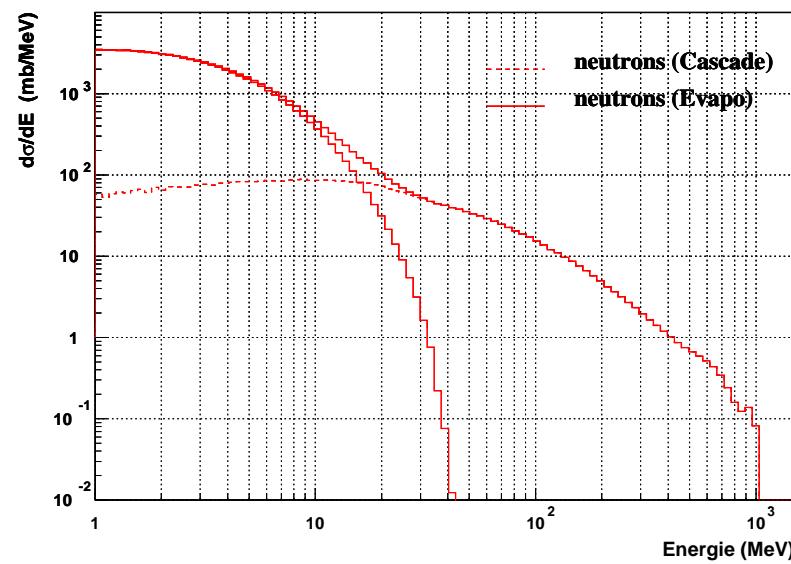
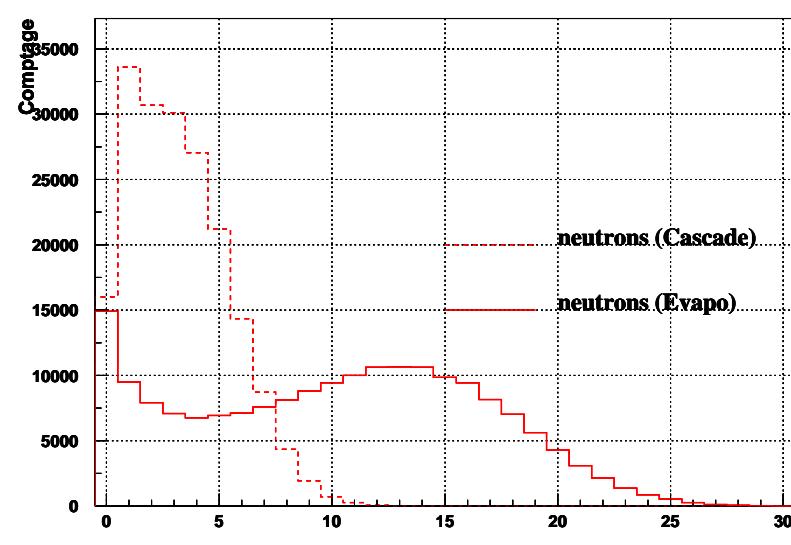
# Spallation characteristics: neutron spectrum

2006/08/30 18.41

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Neutrons come from:

- Cascade
  - High energy
  - Low multiplicity
- Evaporation
  - $E_n < 20$  MeV
    - High cross section
  - High multiplicity

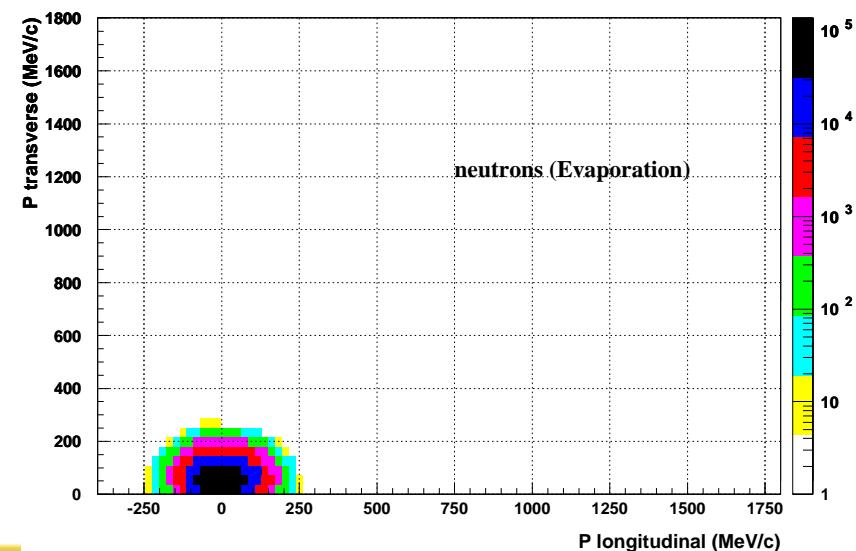
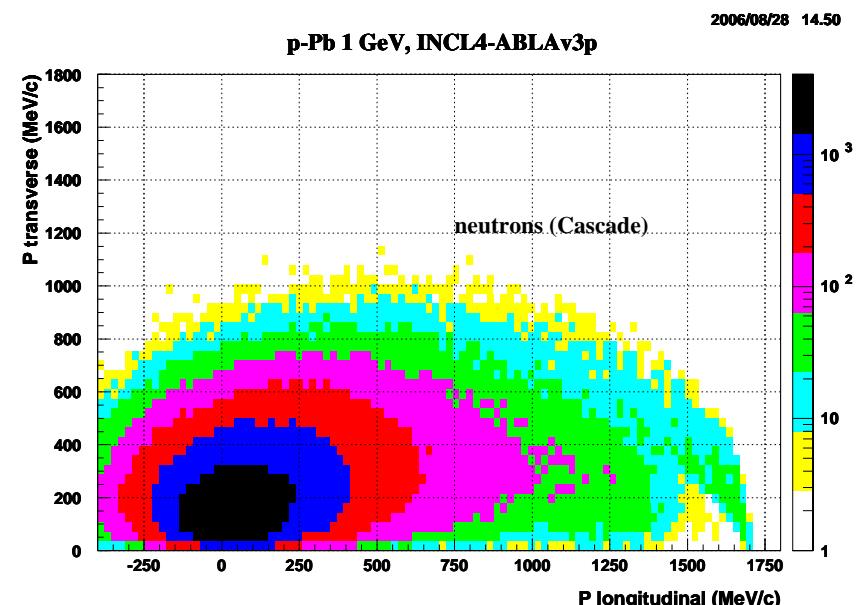


# Spallation characteristics: n angular distrib.

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Neutrons from:

- Cascade
  - Forward emission
- Evaporation
  - Isotropic emission

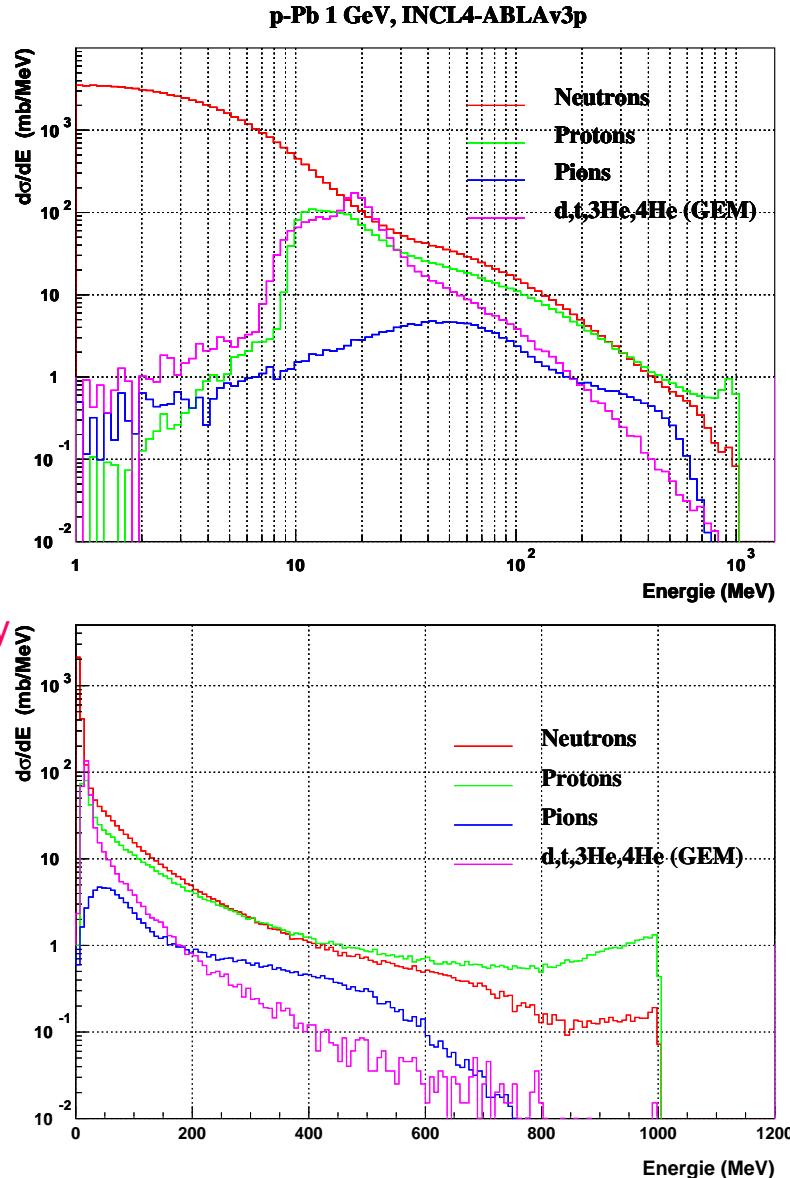


# Spallation characteristics: particle spectra

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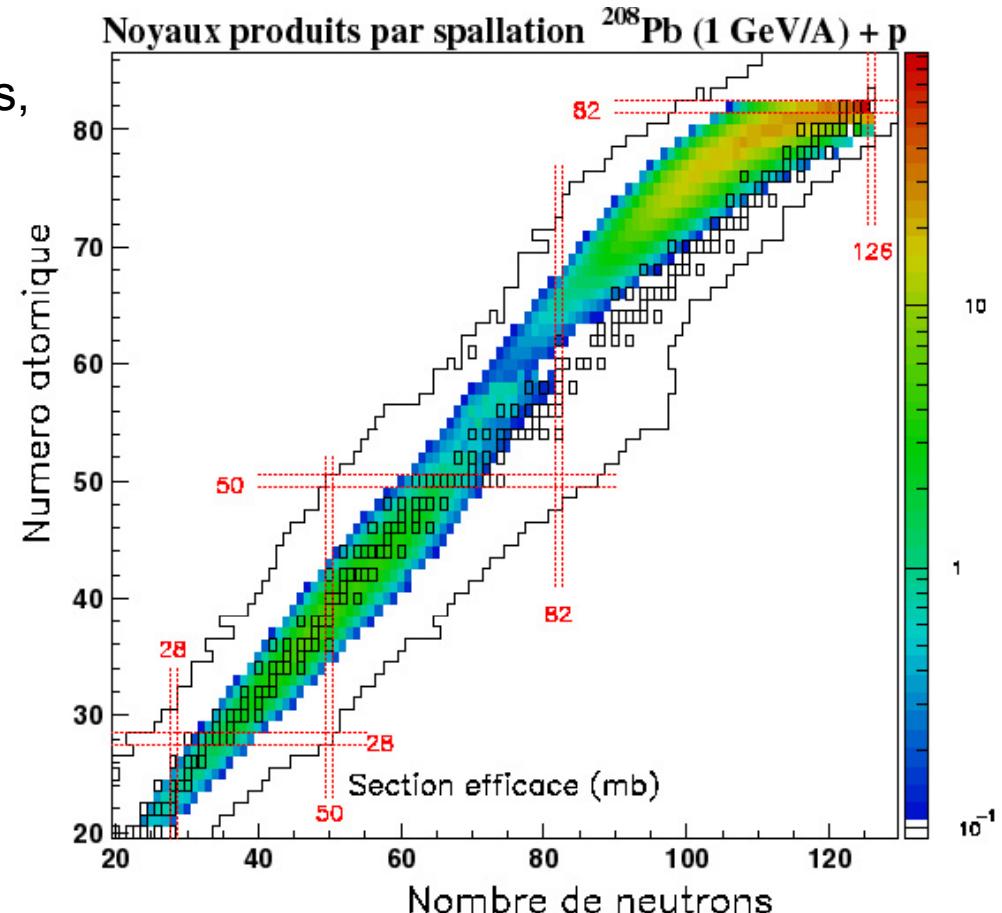
- Neutrons
  - Predominant at **low energy** (not sensitive to the Coulomb barrier)
- Protons
  - Predominant at **high energy**
- Light charged particles (LCP)
  - Important between **10 and 100 MeV**
- Pions
  - Non negligible between **100 MeV and 1 GeV**
- **Cascade particles have lower multiplicity BUT they mainly carry the beam energy**

Type	Mean energy (MeV)	Fraction in cascade
n	355	85 %
p	364	98 %
$\pi$	58	100%
lcp	69	80%
Remnant ( $E^*$ )	137	



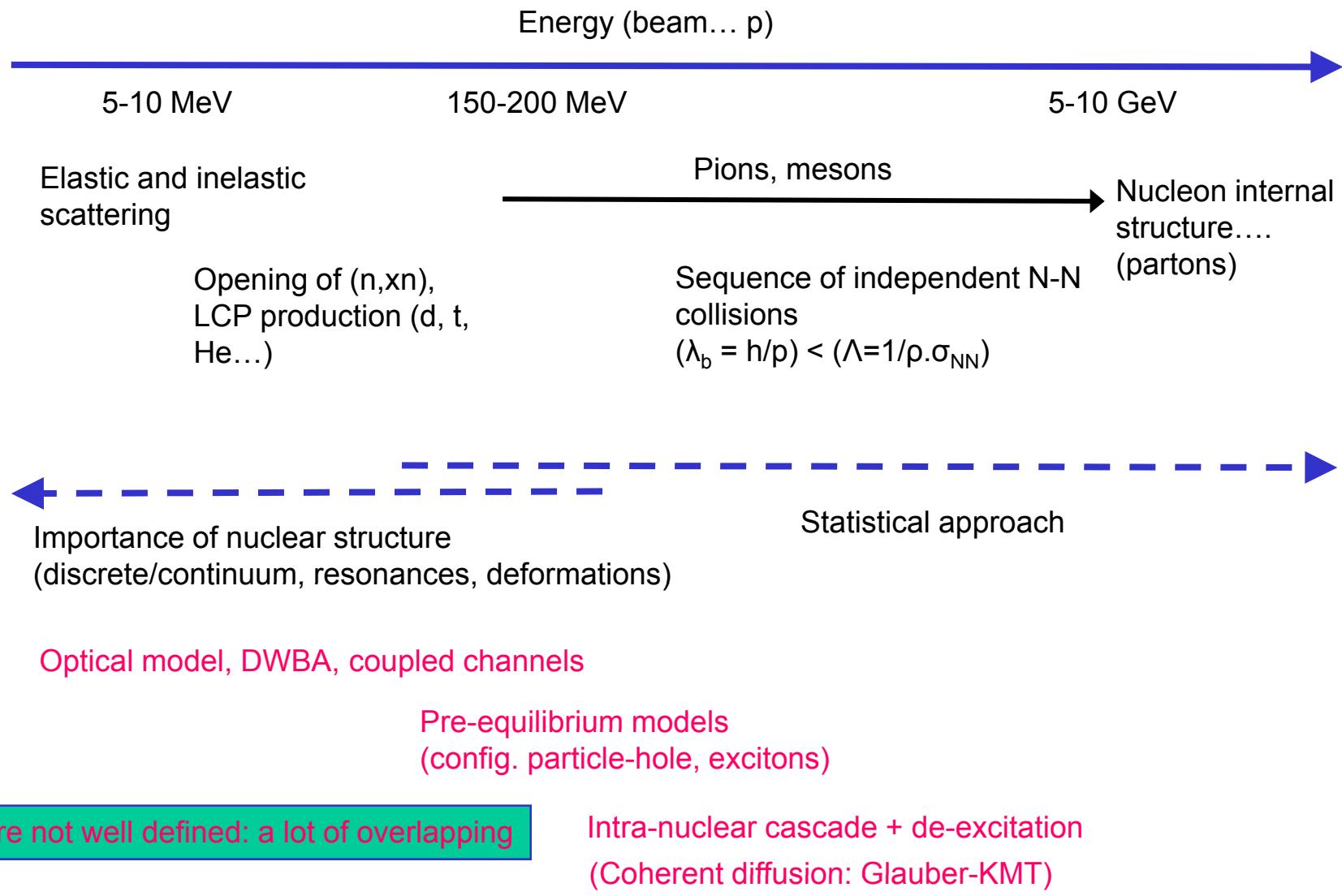
# Spallation characteristics: residues production

- Hundreds of different residues are produced by
  - **Evaporation** (high mass, near the target mass)
  - **Fission** (lighter mass)



# Modeling of spallation reactions

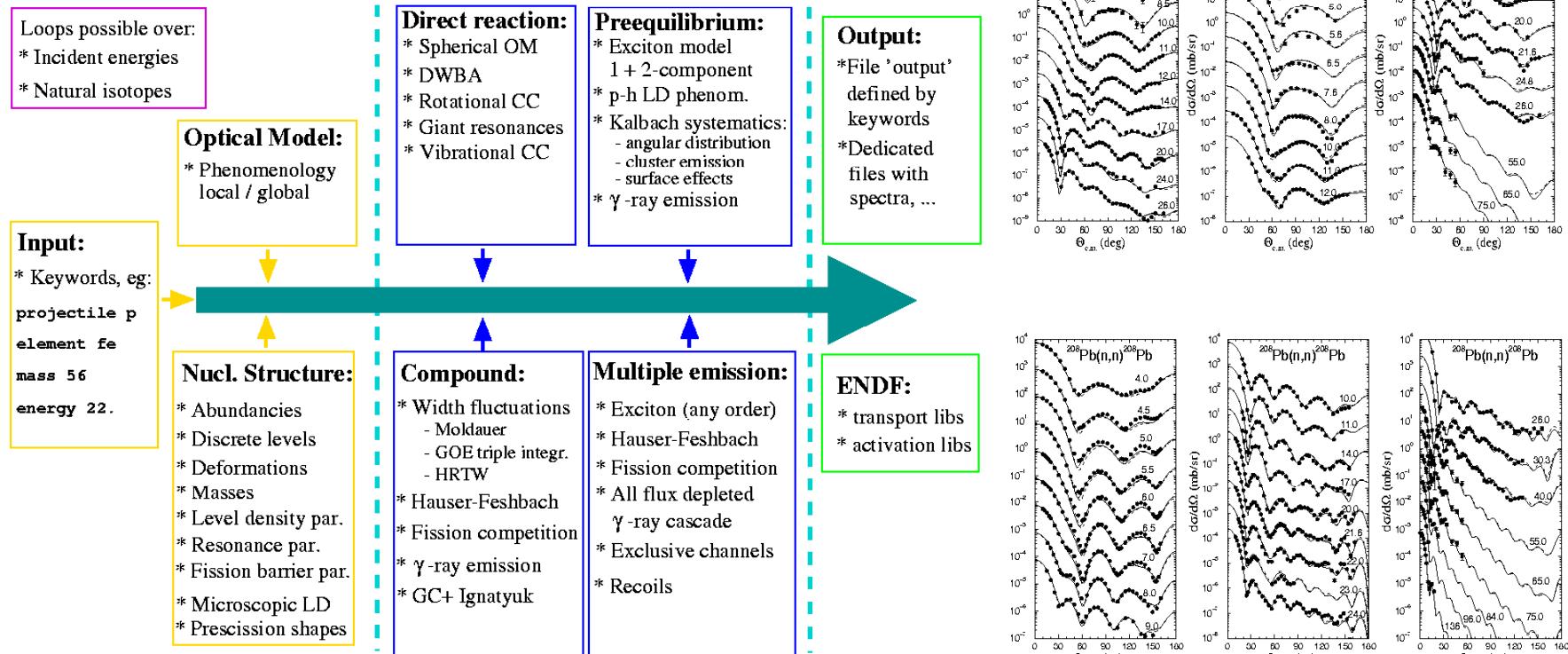
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# Modeling of spallation reactions

$E_p < 200$  MeV, code type: TALYS (A. Koning, JP Delaroche et al.)

## TALYS: CALCULATIONAL SCHEME



Lots of input, parameter fitting, phenomenological approach

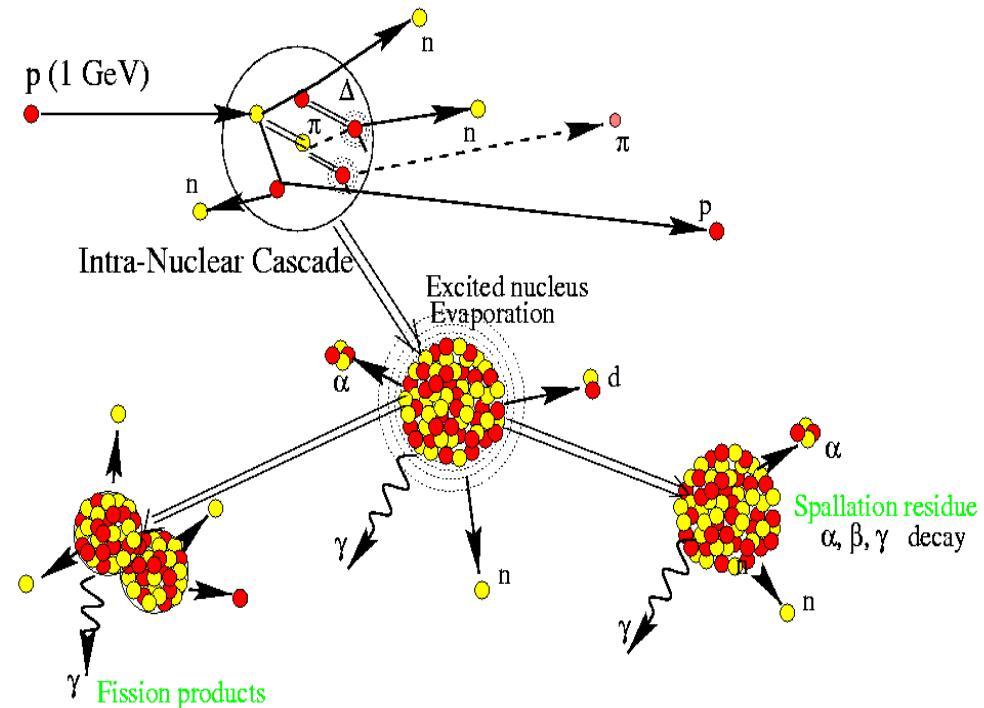
- Very good on elastic scattering, (also (n,xn) ou (n,xp), Koning, Duijvestijn)
- More difficult on compound production (LCP)

GNASH: older code but same type (P. Young et al. Los Alamos)

# Modeling of spallation reactions

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- Two step mechanism:
  - Intra-Nuclear Cascade
    - Sequence of independent N-N collisions
    - $\Lambda_b = hc/p \ll \lambda = 1/\rho\sigma_{NN}$  (mean free path)
    - Fast process ( $\approx 30$  fm/c)
  - De-excitation
    - Competition between evaporation and fission
    - Statistical models
    - Slow process (hundreds of fm/c)
- Three step mechanism
  - INC
  - Pre-equilibrium
  - Evaporation/fission



# Modeling of pre-equilibrium

Exciton = 1 particle - hole

« never come back »: towards more complexity

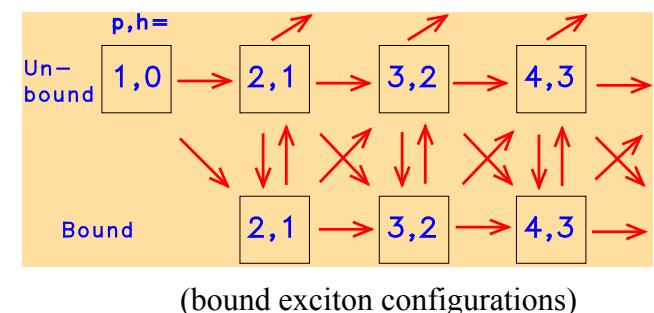
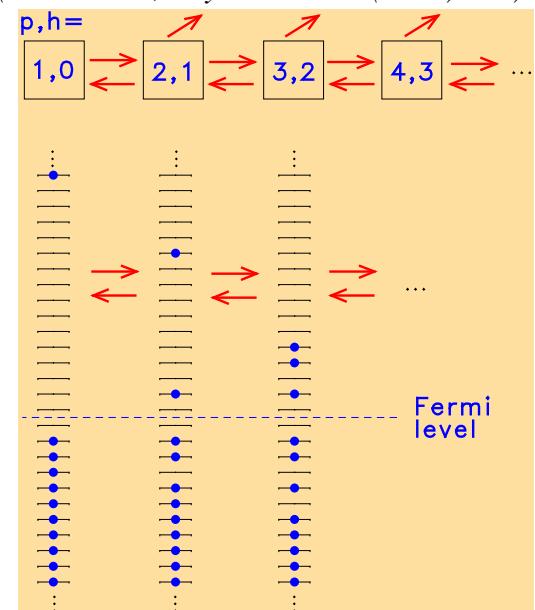
Ingredients:

- Transition between configurations
- Level density (statistical description, Gilbert-Cameron)
- Emission probability (Weisskopf-Ewing)
  - Direct emission (1 param.)
  - Compound emission (2 param.)

Parameters are fitted on data  
(Kalbach systematic)

- Twofold differentiation: proton-neutron (shell and pairing effect taken into account)
- There are a lot of extensions
- This part is “naturally” taken into account in INC-EVAP models (but not energy levels)

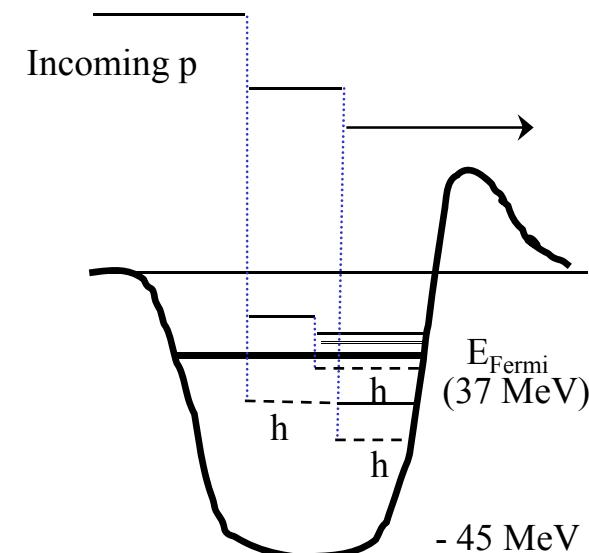
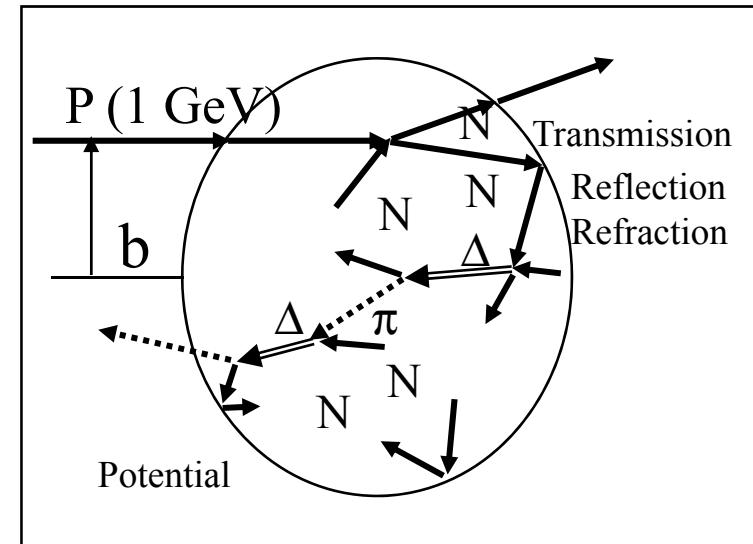
J. Griffin, Phys. Rev. Lett. 17 (1966) 478  
(C. Kalbach, Phys. Rev. C33 (1986) 818)



# Modeling of intra-nuclear cascade (INC)

## Ingredients:

- Realistic nuclear density ( $r, p$  space)
- Realistic NN interaction
  - $\sigma_{NN}(E), d\sigma/d\Omega(\theta)$
  - Elastic
  - Pion production
- Pauli blocking
- Particles are “followed” in space (and time)
- $N$  participants-spectators (participant beam +  $N$  interacting)
- Endpoint criteria (time or energy)
- The model leads to the production of particles and a residual nucleus ( $A', Z'$ ,  $E^*, J, P_{\text{recoil}}$ )



# Modeling of intra-nuclear cascade (INC)

(from J. Cugnon)

	BERTINI	ISABEL	INCL4	PEANUT
Scattering medium	continuous	continuous	collection of nucleons	collection of nucleons
Density profile	3 concentric spheres	15 concentric spheres + depletion	Saxon-Woods	16 concentric
Collision criterion	mfp <sup>a</sup>	mfp <sup>a</sup>	minimum distance of approach	proximity
Time structure	no	time steps	single time step between collisions	time steps
Pauli blocking	strict	strict (local)	statistical (local in phase space)	strict
$\pi$ production	through $\Delta$ forward only <sup>b</sup>	through $\Delta$	through $\Delta$	through $\Delta$ and other resonances
$\pi$ absorption behaviour at the surface	mfp <sup>c</sup> reflexion refraction	through $\Delta$ reflexion refraction	through $\Delta$ reflexion no refraction	through $\Delta$ ?
Stopping criterion	maximum energy <sup>d</sup>	maximum energy <sup>d</sup>	self-determined	maximum energy <sup>d</sup>
Residue	$E^*, J$	$E^*, J, E_{rec}$	$E^*, J, E_{rec}$	$E^*$

(in LAHET-MCNPX)

(in FLUKA-GEANT)

BERTINI: H.W. Bertini et al. Phys. Rev 131 (1963) 1801

ISABEL: Y. Yariv et Z. Fraenkel Phys. Rev. C 24 (1981) 488

INCL4: J. Cugnon et al. Nucl. Phys. A620 (1997) 475; A. Boudard et al. Phys. Rev. C66 (2002) 44615

PEANUT: A. Fasso, A. Ferrari et al Monte-Carlo Conf 2000 edited by A. Kling et al (Springer-Verlag, Berlin)

✓CEM2k (S. Maschnik et al. Los Alamos) : in LAHET, important pre-equilibrium + cascade

✓BRIC (H. Duarte CEA DIF) : derived from INCL, movement equations + refraction cross section in NN medium

# Modeling of de-excitation: evaporation

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Excited nucleus... a bit,... but not too much!

- > Nucleon emission threshold  
(high energy level density)
- <  $E^* \sim 3 \text{ MeV/u}$

**Statistical treatment:** emission independent from energy levels (only level density is important)

Explosion (multi-fragmentation) of the nucleus  
**Sequential emission is no longer valid!!!!**

**From QCD T-inversion invariance:**  
**(detailed balance principle)**

$$\rho_A P_{Aa} = \rho_{(A-a)} P_{(A-a)a}$$



$\rho$ : level density

$P_{Aa}$ : probability for  $A$  to emit  $a$

$P_{(A-a)a}$ : probability for  $A-a$  to absorb  $a$

- 1) Evaporation probability of particle  $a$ , energy  $\varepsilon$ , momentum  $p$  and spin  $s$  (*Weisskopf-Ewing*) :

$$P_a(\varepsilon) = \rho_f(Ef^*)/\rho_i(Ei^*) \ (2s+1) (4\pi p^2/h^3) \sigma_c(\varepsilon)$$

- 2) *Hauser-Feshbach* put explicitly the angular momentum  $l$  (of  $a$ ) and some transmission coefficients  $T_l(\varepsilon)$  calculated from the optical model

**Ingredients:**  $s_c(e)$  (capture cross section) and  $\rho(A,E)$  (level density)

# Modeling of de-excitation: evaporation

## Level density:

$$\rho(E^*, A) = \frac{\sqrt{\pi}}{12} \frac{e^{2\sqrt{aE^*}}}{a^{1/4}(E^*)^{5/4}}$$

$$E^* = a T^2$$

From static treatment of Fermi gas

T is the temperature,  
 $E^*$  is the excitation energy

a: Level density parameter.... A very long history... and literature!!!

$$a = f(A, E^*)$$

It should « partially » take into account nuclear effects (pairing, shells, magic numbers) and  $E^*$  evolution

The limit for high  $E^*$  is:  $a \sim A/8 \div A/13$

The most common parametrization is GCCI (Gilbert-Cameron-Cook-Ignatyuk)

## Inverse cross sections:

Geometrical model, fit on data or explicit calculation

Main difficulty: Fusion-Absorption for an excited nucleus!

# Modeling of de-excitation: fission

Atchison (RAL code, default in LAHET/MCNPX ~1980) (ORNL only for Z>90)

$Z > 70$  : competition limited to n evaporation (Weisskopf with simplified a)

$Z^2/A < 35$  : symmetric fission (fission fragments mass distribution)

$Z^2/A > 35$  : symmetric + asymmetric fission

*Mainly based on empirical data on actinides fission at low energy (thermal)*

K.H. Schmidt (J. Benlliure, B. Jurado @ GSI, ABLA code): time evolution of fission channel width

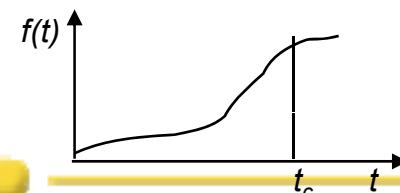
$$\Gamma_f^{BW} = \frac{1}{2\pi\rho_c(E)} T_{sad} \rho_{sad} (E - B_f)$$

Bohr-Wheeler: Temperature ( $T_{sad}$ ) and level density ( $\rho_{sad}$ ) at the saddle point calculated right above the fission barrier ( $B_f$ )

$$\Gamma_f^K = K(\beta) \Gamma_f^{BW}$$

Kramer- Grangé: Dissipative process giving a reduction parameter  $K(\beta)$ , where  $\beta$  is the viscosity, derived from Fokker-Planck equations

$$\Gamma_f^K = K(\beta) \Gamma_f^{BW} f(t)$$



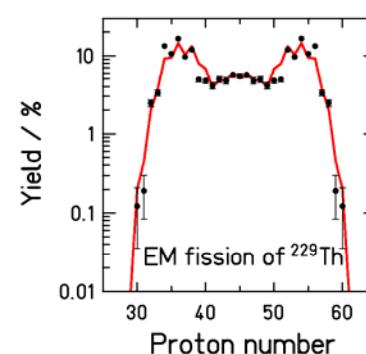
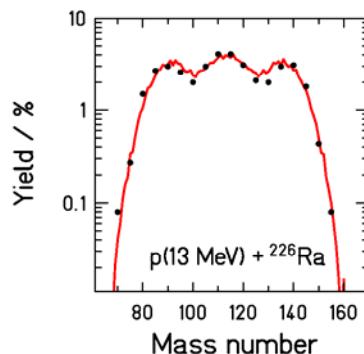
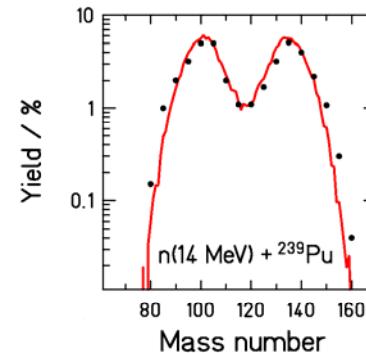
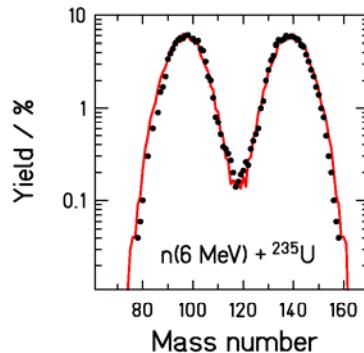
B. Jurado et al. (Phys. lett. B 533 (2003) 186): dynamical competition between fission and evaporation given by a transition function:  $t_c \sim 1.7 \cdot 10^{-21} \text{ s}$

# Modeling of de-excitation: fission fragments

Level density above the fission barrier (statistical approach)

Barrier defined by 3 terms giving 3 FF structures:

1. **Symmetric** (liquid drop model)
2. **Asymmetric N=82** (empirical)
3. **Asymmetric N=90** (empirical)



**ABLA**: the most detailed model for fission at spallation energies

Parameters based on experimental data → Still difficulties on Ta-W

# Modeling of de-excitation: extreme cases

- Light nuclei ( $A < 15-20$ ,  $E^* \approx 50$  MeV/u):
  - Small level density
  - $E^* \approx$  binding energy
  - Breaking in ONE STEP: Fermi breakup
  - All possible configurations are weighed by the phase space
    - The nucleus  $A$  is decomposed on  $n$  components,  $A_i$ , with weight  $W$

$$W = \frac{c}{A_1! \dots A_n!} \left( \frac{\text{Vol}}{h^3} \right)^{n-1} \int d\vec{p}_i \delta(\sum \vec{p}_i) \delta(E^* - S - \sum t_i)$$

$$A = \sum_1^n A_i$$

- High excitation energy ( $E^* > 3$  MeV/u):
  - Breaking in ONE step : Multifragmentation
  - Violent expansion up to a freeze-out volume (density  $\sim 1/3-1/6 \rho_0$ )
  - Weighting of possible configurations (high temperature: Boltzmann law)

$$W = \frac{c}{A_1! \dots A_n!} \prod_1^n e^{-\frac{E_i}{T}} g_i \frac{\text{Vol}(2\pi m_i T)^{3/2}}{h^3}$$

- Evaporation like a very asymmetric fission:
  - Transition state model
  - Alternative to classical evaporation, extended to light ion emission
  - Capture cross section is replaced by a barrier

# Modeling of de-excitation: the codes

- Dresner:
  - It is the oldest
  - Too high Coulomb barriers
  - Evaporation à la Weisskopf (up to  ${}^4\text{He}$ ) + Fission à la Atchison
- GEM
  - Revised (and modernized) version of Dresner-Atchison
  - Evaporation à la Weisskopf (up to  $A=24$ )
  - Revised masses, pairing, fission param., capture X sect., Coulomb barriers
- ABLA
  - Evaporation à la Weisskopf (only for p, n,  ${}^4\text{He}!!!!!!$ )
  - Fission VERY complex and detailed
  - Very active community on development (extended evapor., multifragm., dynamic fission)
- GEMINI
  - Evaporation à la Haussler-Feshbach (for  $Z < 2,4$ )
  - Transition state model (for  $Z > 2,4$ )
- SMM
  - Evaporation à la Weisskopf (up to  $A<18$ )
  - Multifragmentation

# Comparison between models and data

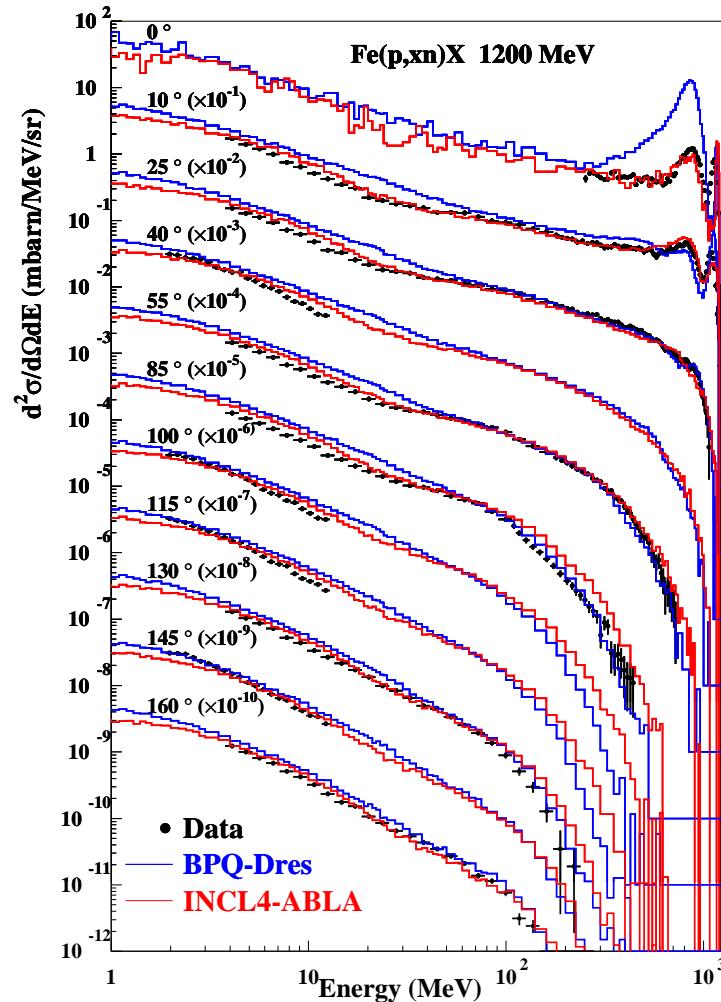
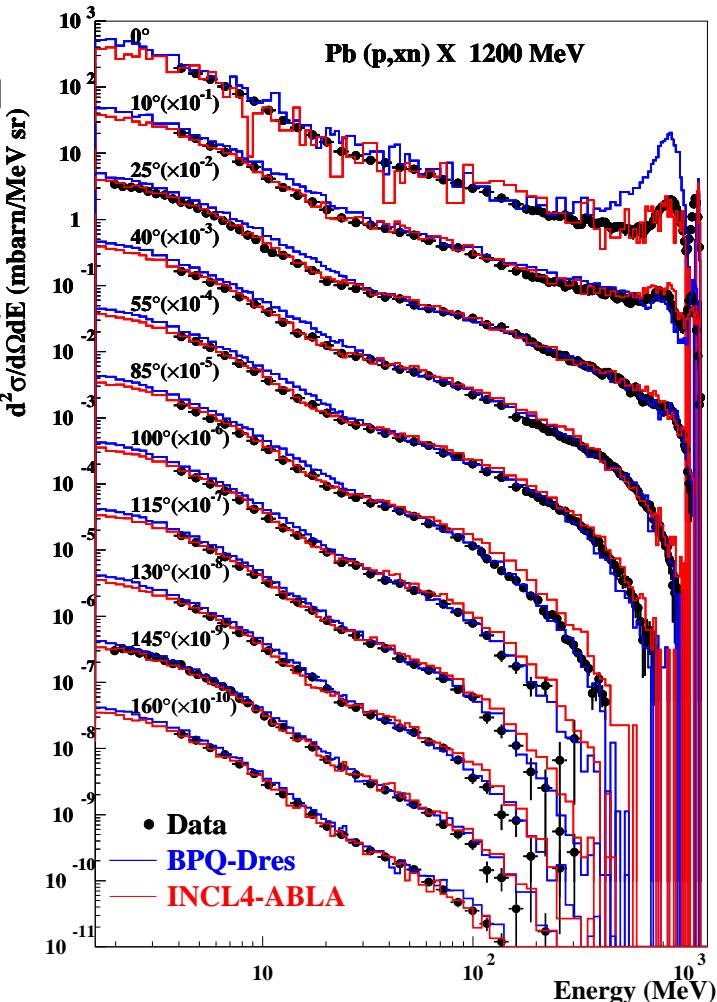
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- Large amount of high quality data has been collected
  - Neutron and LPC production
  - Isotopic residue distributions
  - Excitation functions
- Improvements on nuclear models
  - INCL4/ABLA tested against all the available data with the same set of parameters
  - Important improvements also in CEM and FLUKA
  - Implementation of INCL4/ABLA and CEM into MCNPX
  - Implementation of INCL4/ABLA in GEANT4

# Neutron production

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S.Leray et al., Phys. Rev. C 65 (2002) 044621

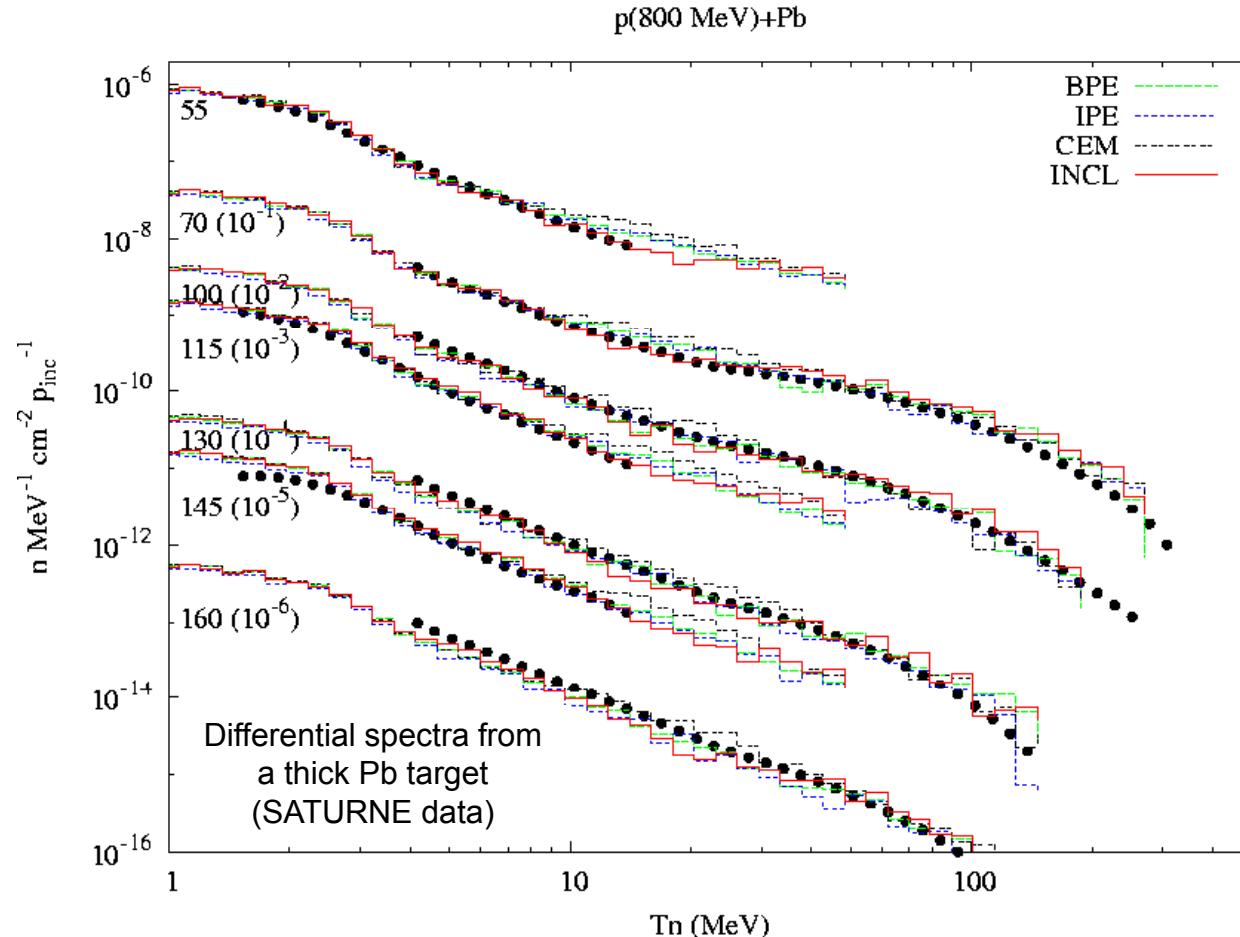


Neutron production can be predicted with a 10-20% precision by most of the models

# Neutron production

T. Aoust et al., ND2004, Santa Fe

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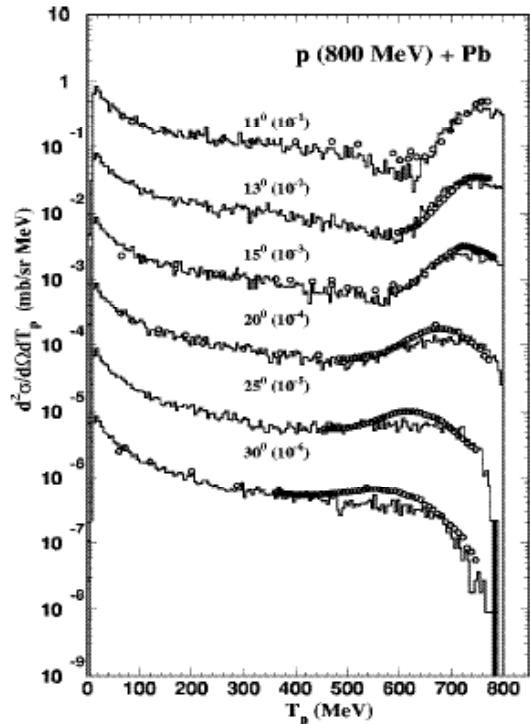


Energy and angular distribution are well reproduced

# Proton and pion production

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R. Chrien et al, Phys. Rev. C21 (1980) 1014

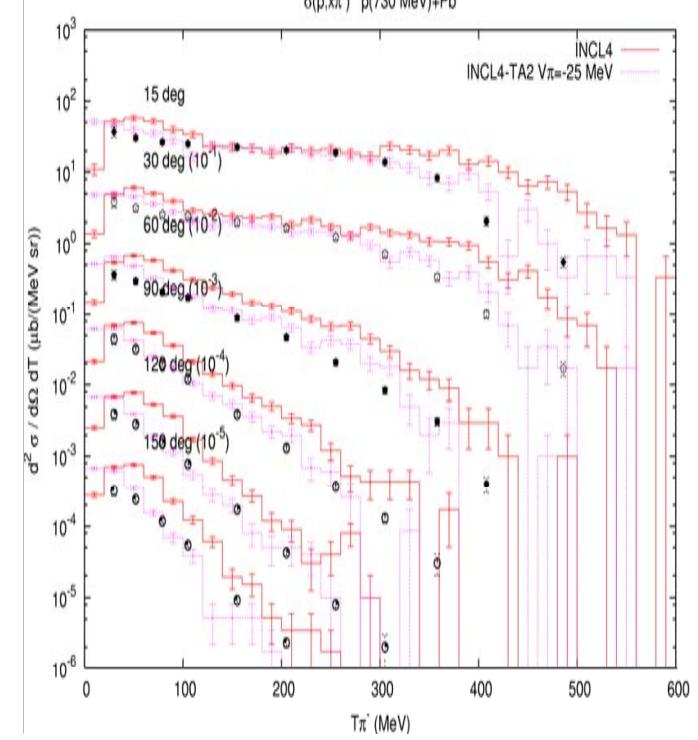


Protons

J. McGill et al Phys. Rev. C29 (1984) 204

D. Cochran et al, Phys. Rev. D6 (1972) 3085

$\sigma(p,\pi^+) p(730 \text{ MeV}) + \text{Pb}$



$\pi^+$

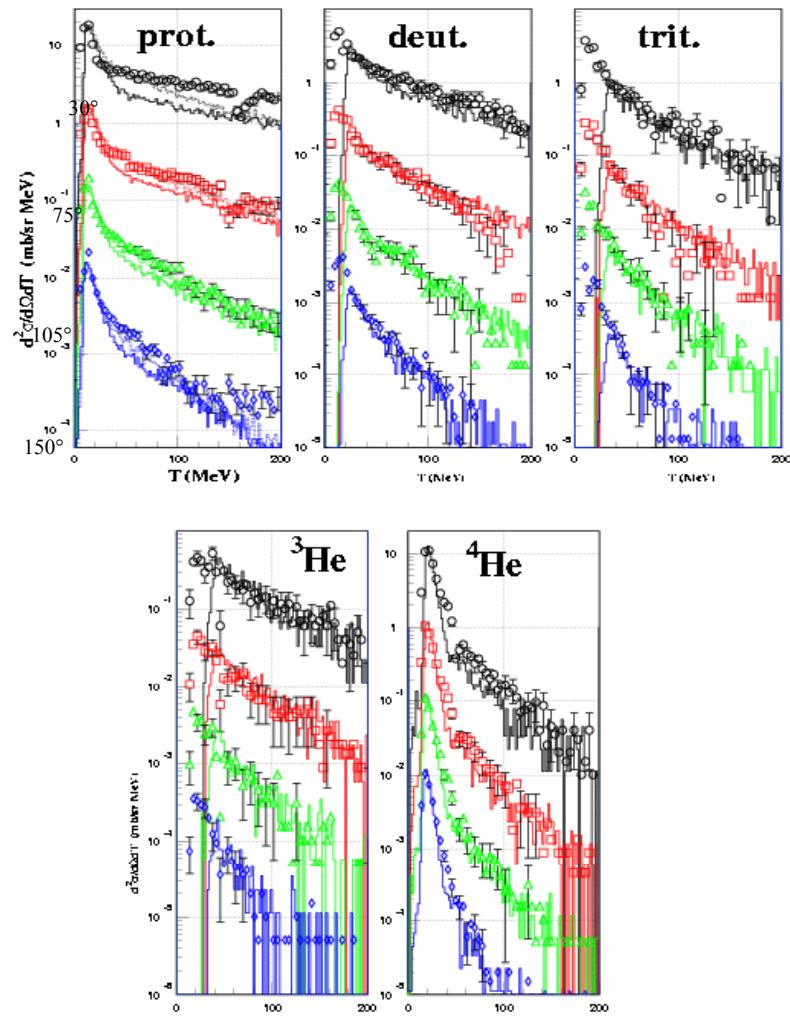
Quasi-elastic peak well reproduced but need to add of a pion potential

# LCP production

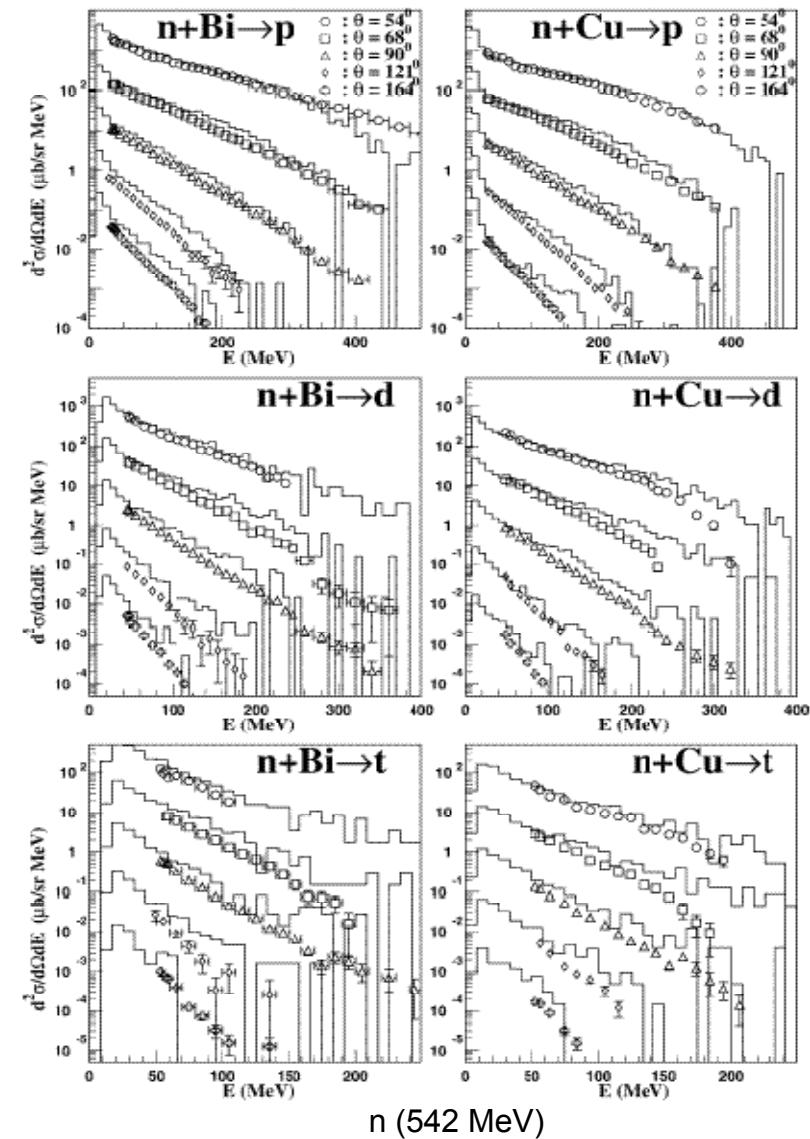
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A. Letourneau et al, Nucl. Phys. A712 (2002) 133

p + Au 2500 MeV, exp: NESSI



J. Franz et al, Nucl. Phys. A472 (1987) 733, Nucl. Phys. A510 (1990) 774



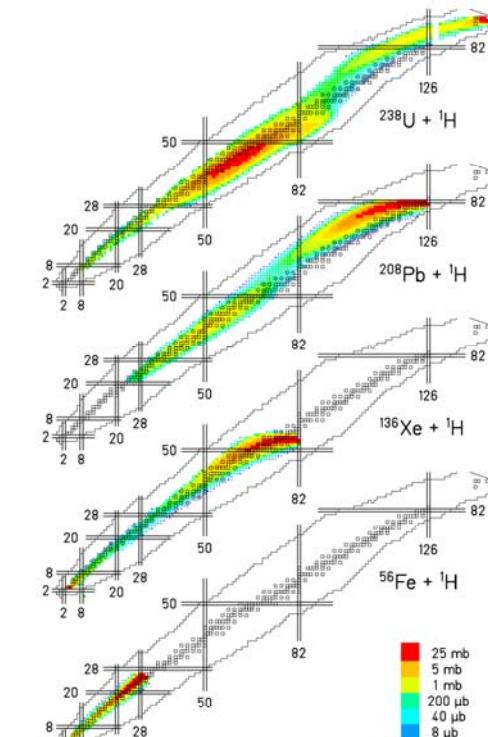
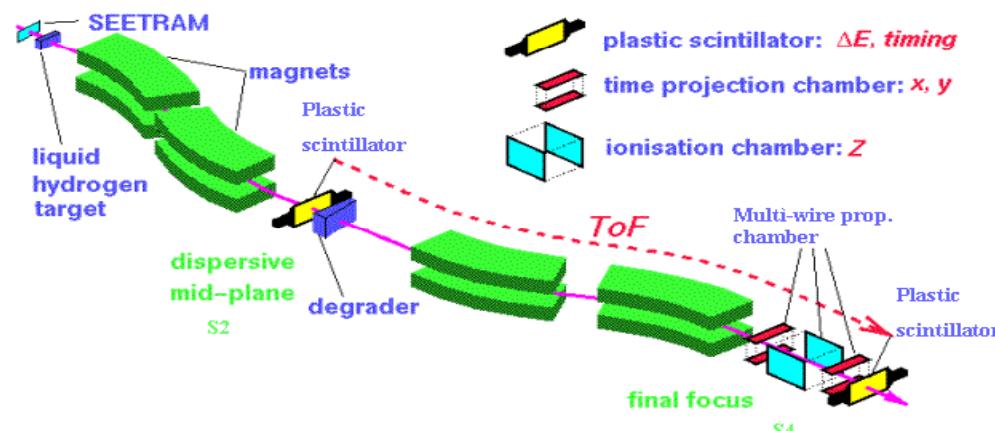
# A comment on LCP production

- **In the cascade:**
  - Extension out of standard description (N-N interactions)
  - In INCL4: hypothesis of cluster formation at the surface given by
    - Distance parameter (from R0):  $r = 1.75 \text{ fm}$
    - Phase space parameter  $\Delta r \Delta p < 387 \text{ fm}^* \text{MeV}/c$
- **In the evaporation:**
  - Can be treated on the same formalism as nucleons (state density, inverse cross section)

# Residues production

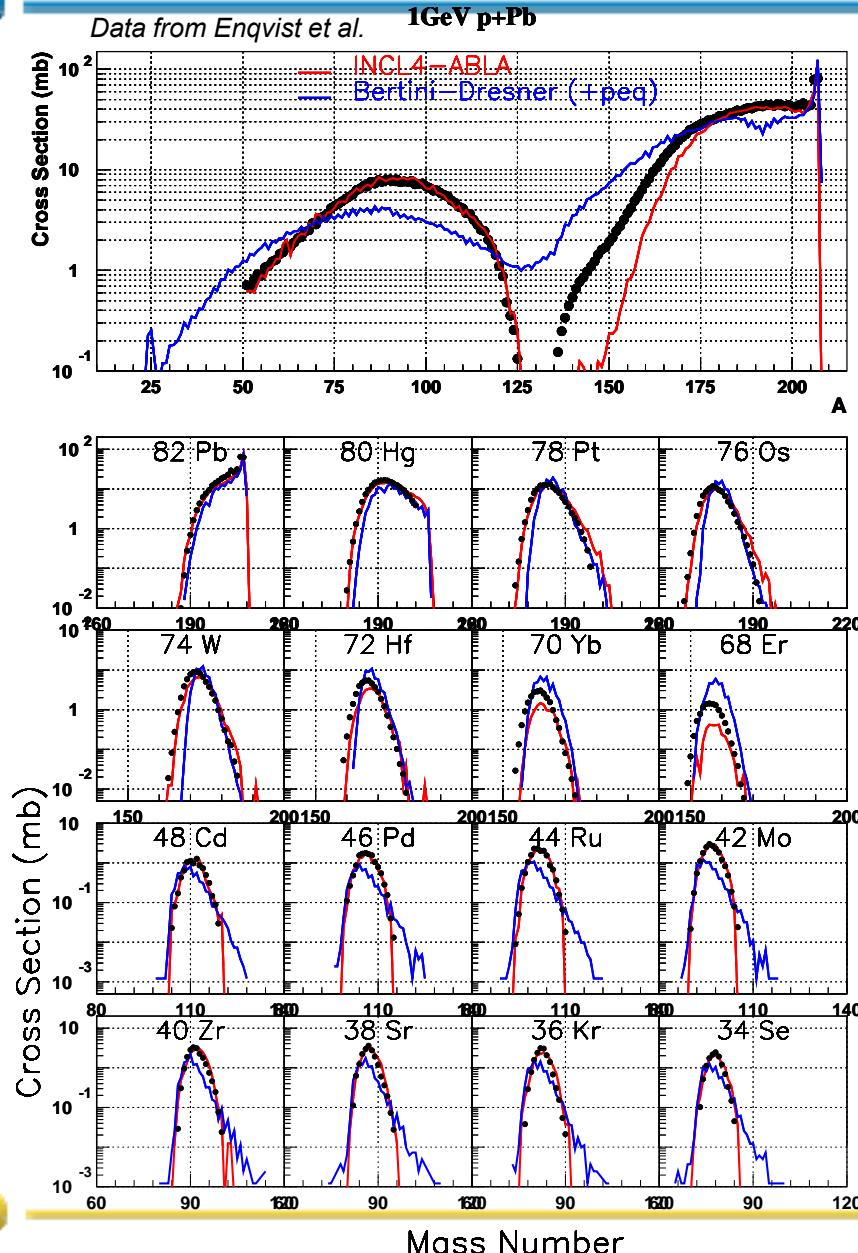
- New data obtained with reverse kinematics methods led to a considerable progress in reaction modeling
- Models:
  - Heavy evaporation residues: generally good very close to the target nucleus
  - Fission fragments: quite good, enough for activity calculations
  - Light evaporation residues: most models generally bad
  - Intermediate mass fragments: all models are wrong by orders of magnitude

**FRS experiments at GSI**  
 (coll. GSI, Santiago Univ., CEA/DSM, IN2P3)

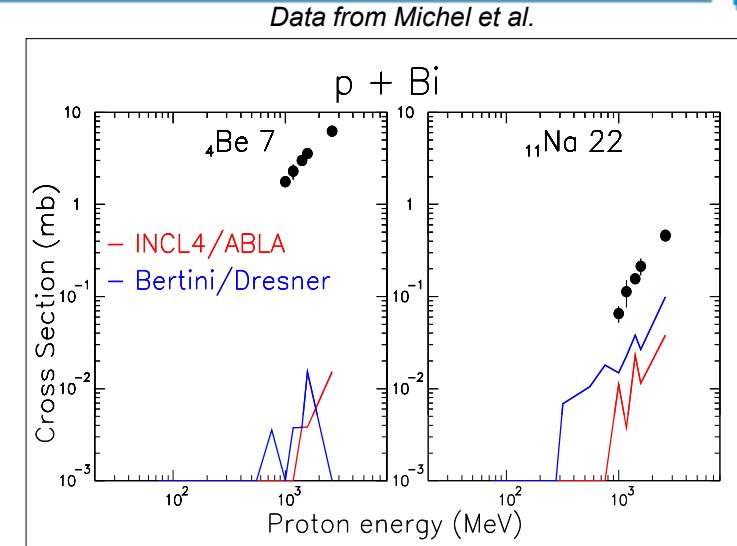


# Residues production: heavy systems

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Stefano PANEBIANCO – CEA Saclay, Irfu/Service de Physique Nucléaire

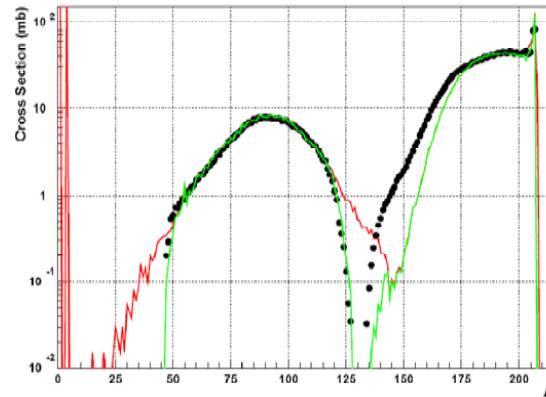


- INCL4/ABLA agrees much better with GSI data than Bertini/Dresner for fission fragments, very heavy residues and isotopic distribution shape
- Both fail for light evaporation residues and intermediate mass fragments

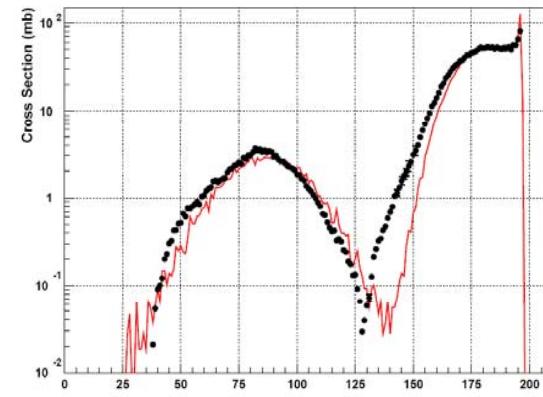
# Residues production: heavy systems

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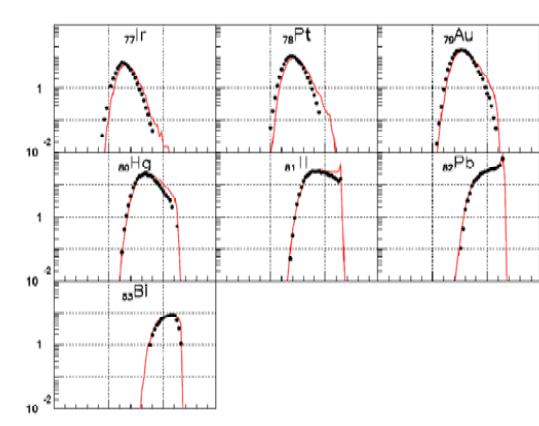
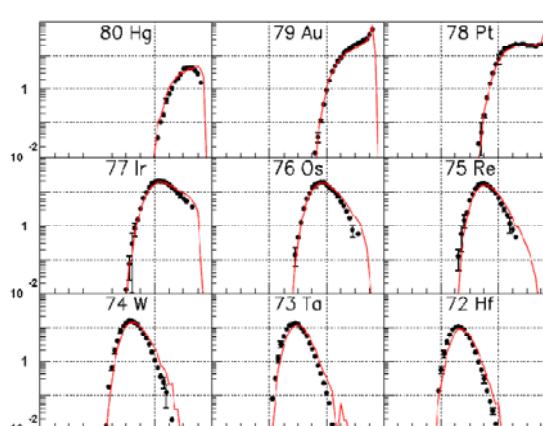
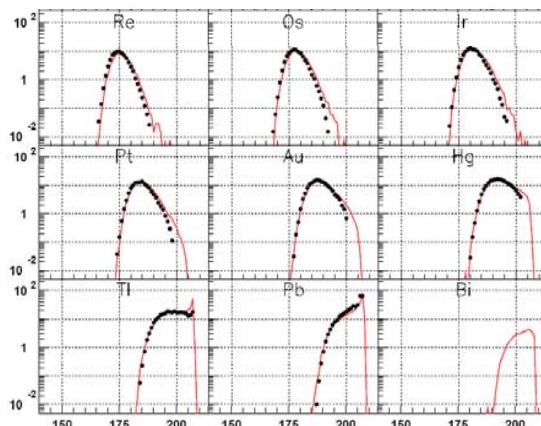
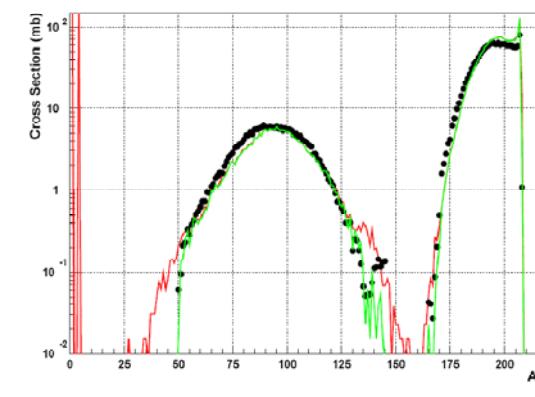
Pb (1 GeV/A) + p



Au (800 MeV/A) + p

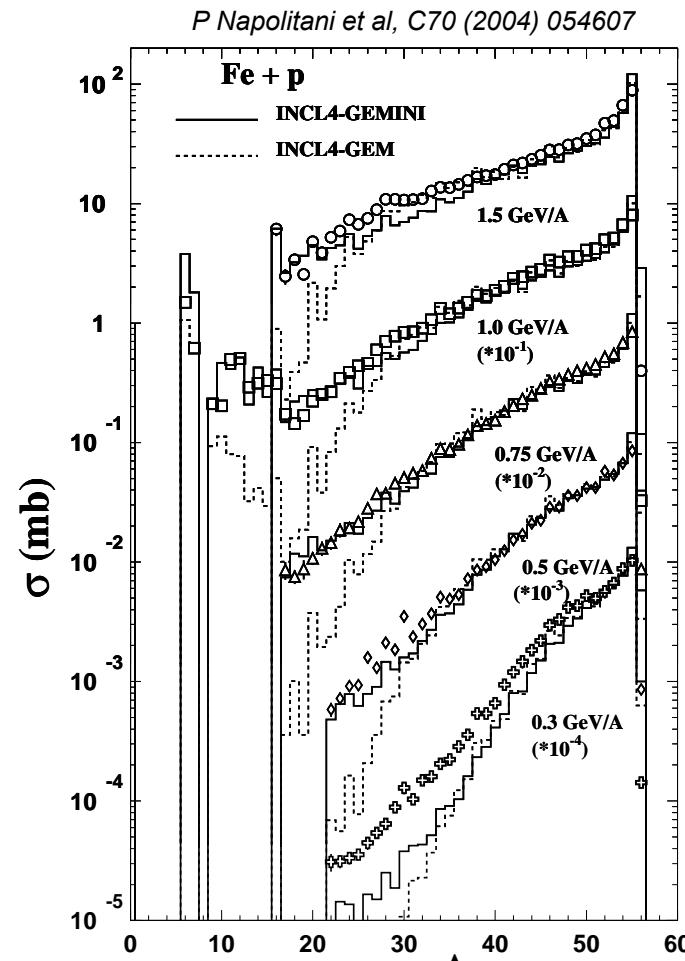


Pb (500 MeV/A) + p



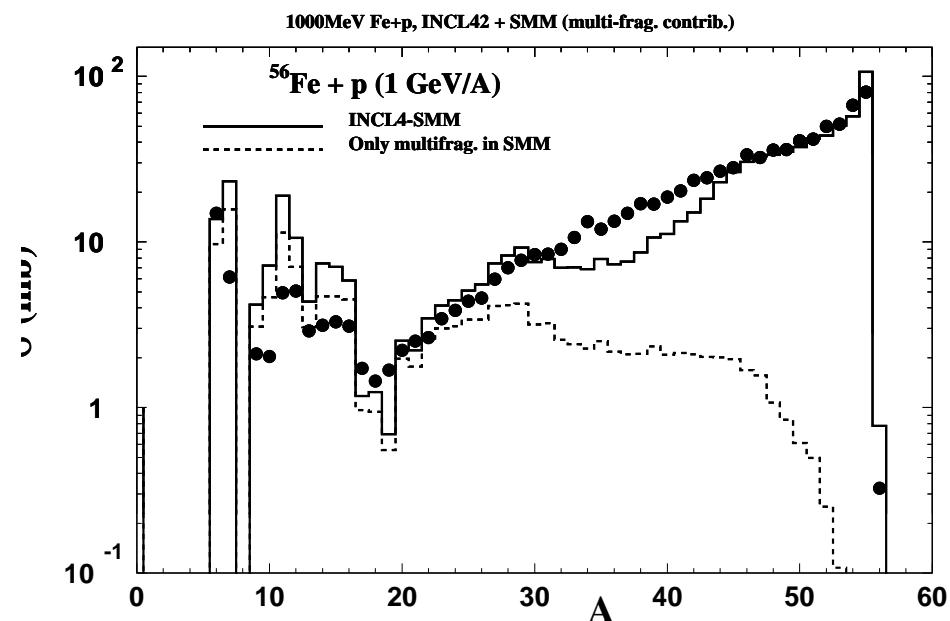
The only evaporation is not enough to explain the distributions at high excitation energy

# Residues production: light systems



Transition state model  
 (Gemini)

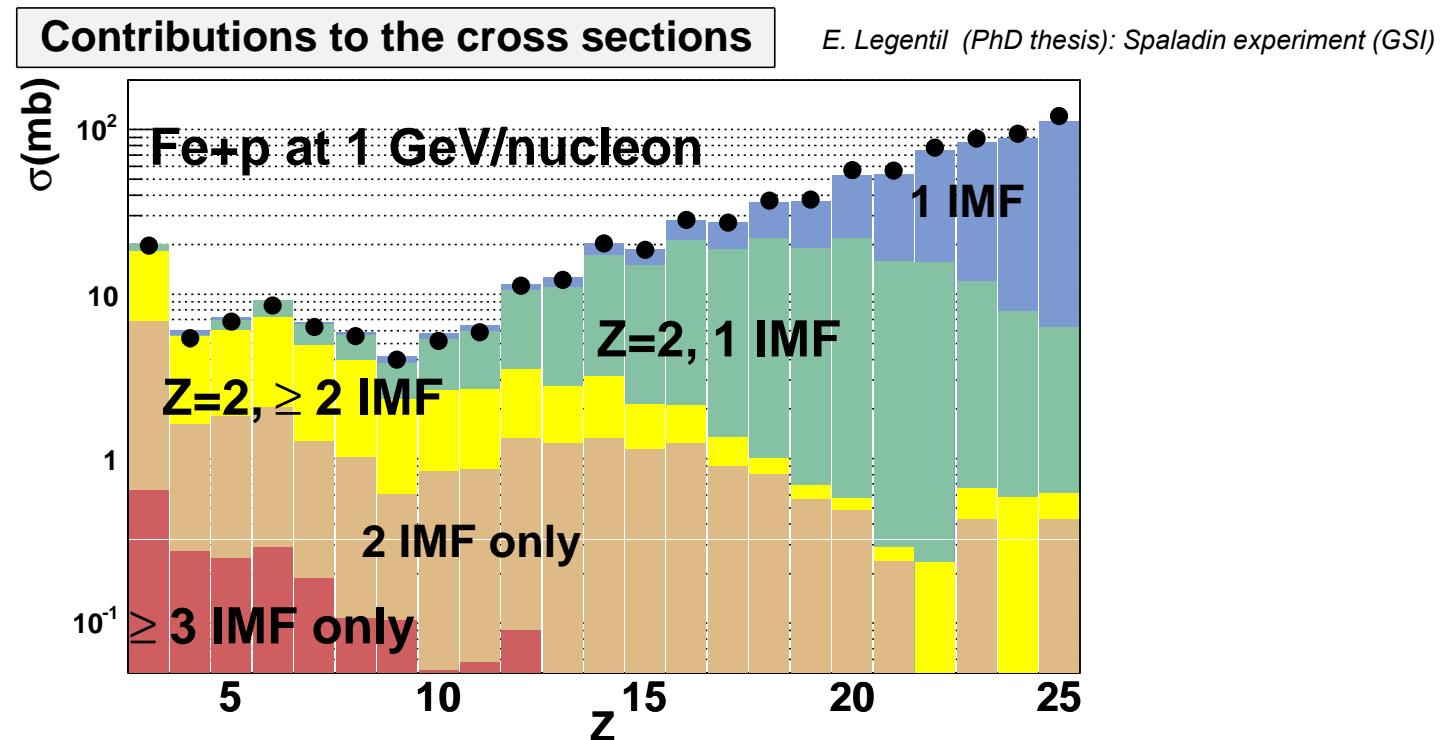
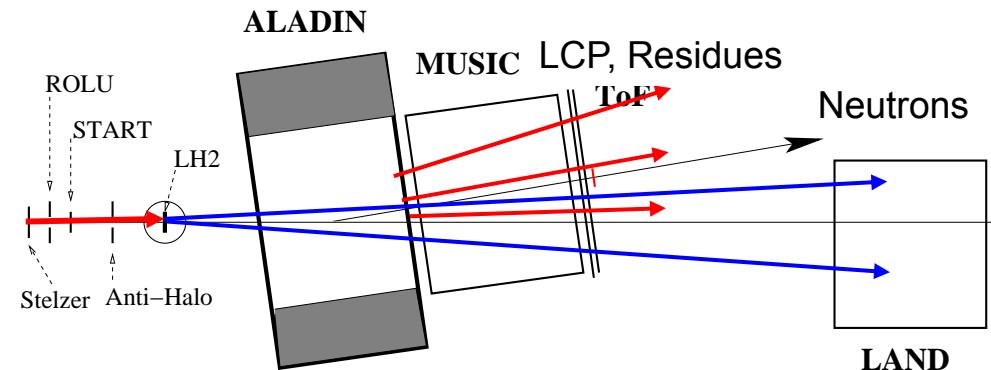
**NOTE:** same beam energy, therefore higher excitation energy  
 (per nucleon) on a lighter nucleus (nucleus diameter/volume)



...or multifragmentation ?  
 (SMM)

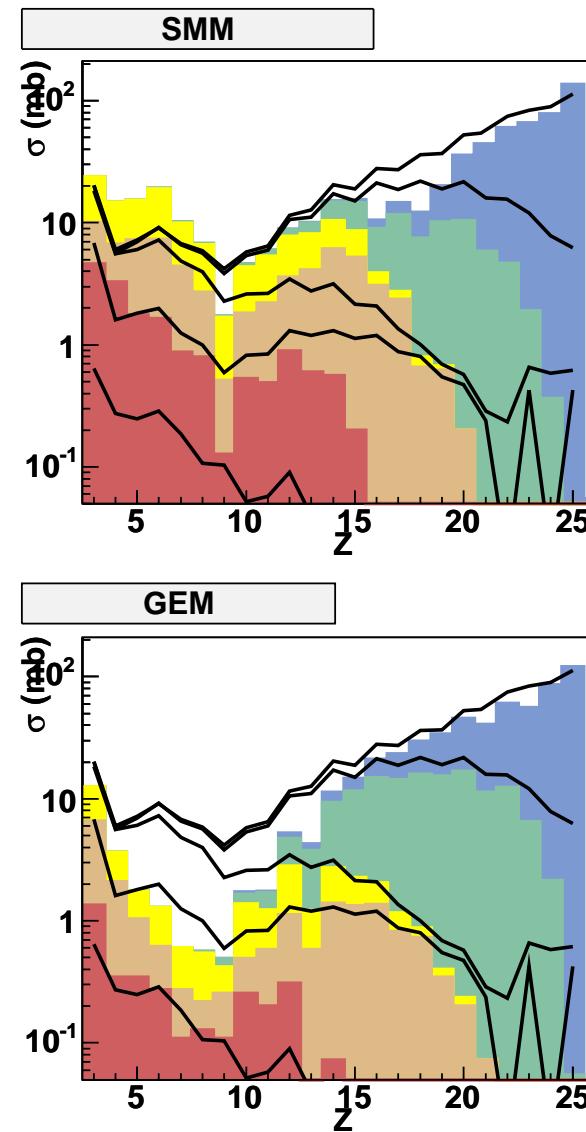
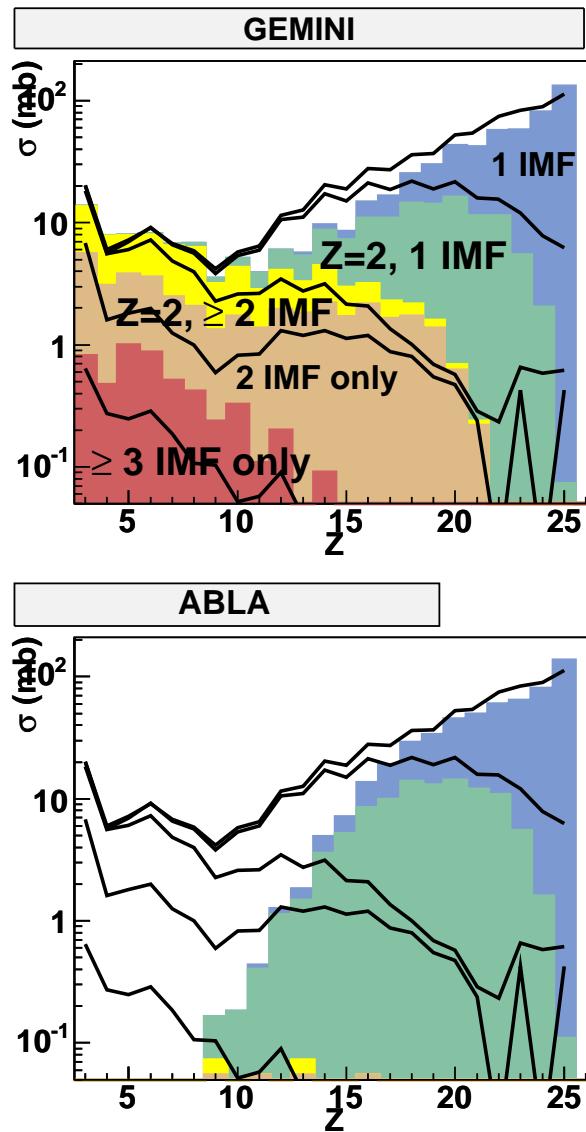
# Study of the mechanism: coincidence technique

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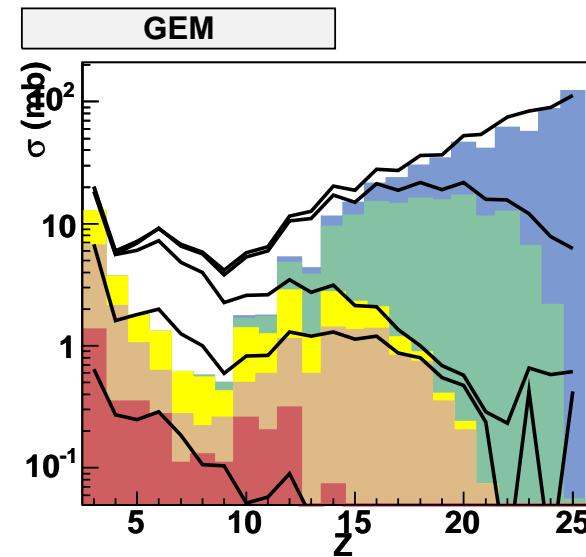
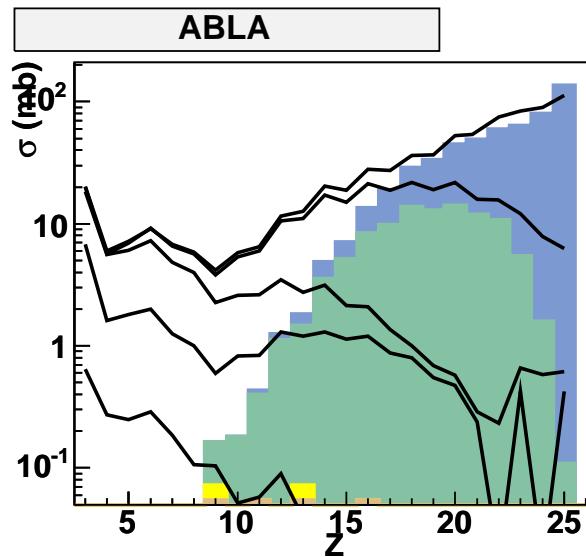


# Study of the mechanism: models/data

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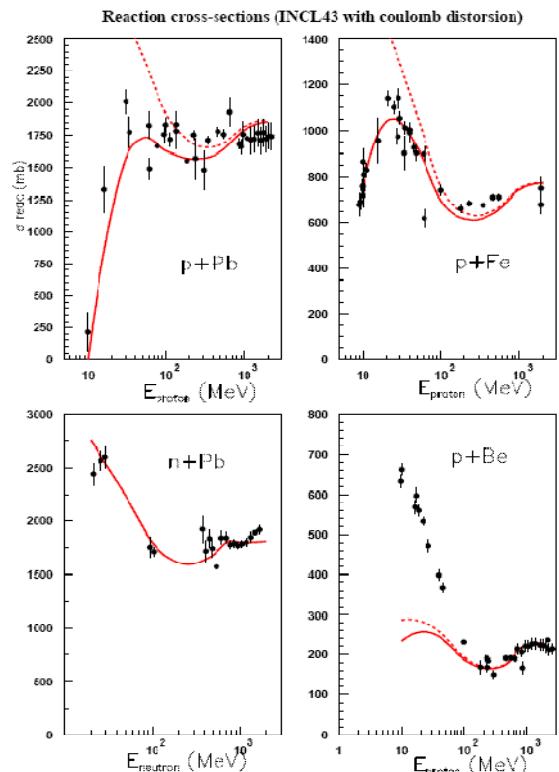


Black: data  
Histos: model

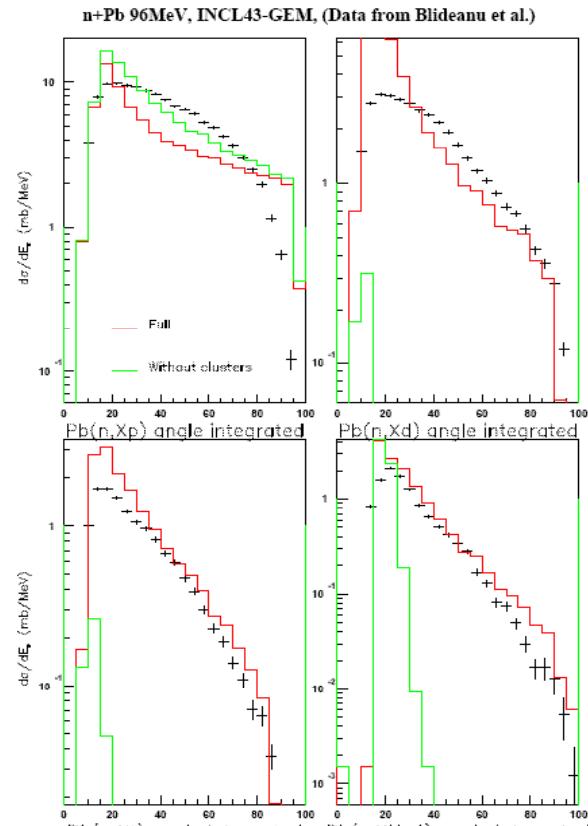


Best agreement: Gemini  
Haussner-Feshbach  $Z < 5$ ,  
Transition State Model  
above.

# Validity at lower energy



Reaction  $\sigma$  is correct:  
Absolute normalization  
in the calculation



$p$  (62.9 MeV) +  $^{208}Pb$

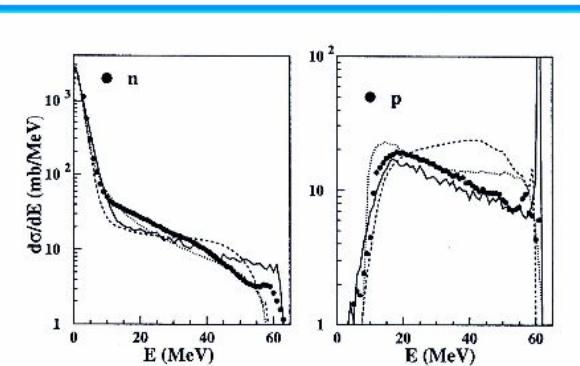


Fig. 20. Neutron and proton energy differential cross-sections. Data are presented as full circles. Theoretical results for MCNPX(INCL4), TALYS and FLUKA are displayed using, respectively, full, dashed and dotted lines.

A. Guertin et al, EPJ A23(2005)49

Solid: INCL4+ABLA  
Dashed: TALYS  
Dotted: FLUKA

INCL at low energy under development  
Good hope of model continuity...

# Pay attention to Bertini-Dresner-Atchison!

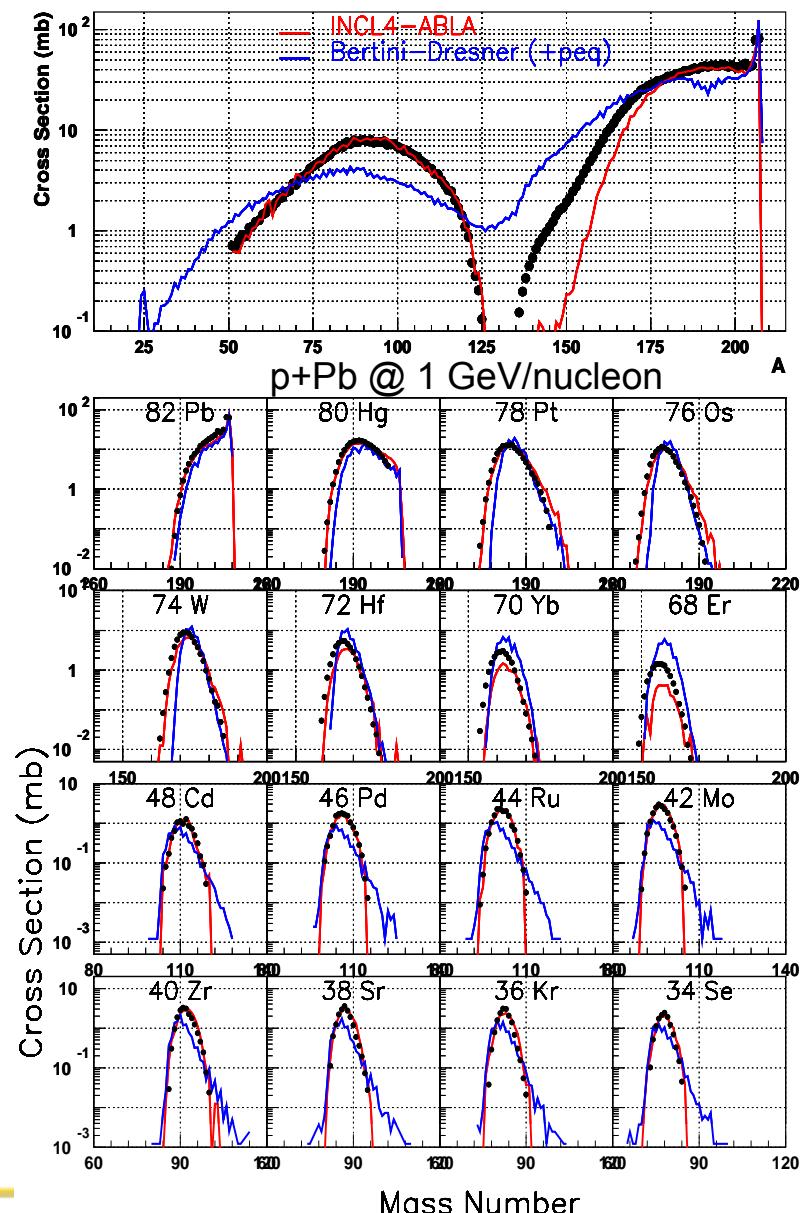
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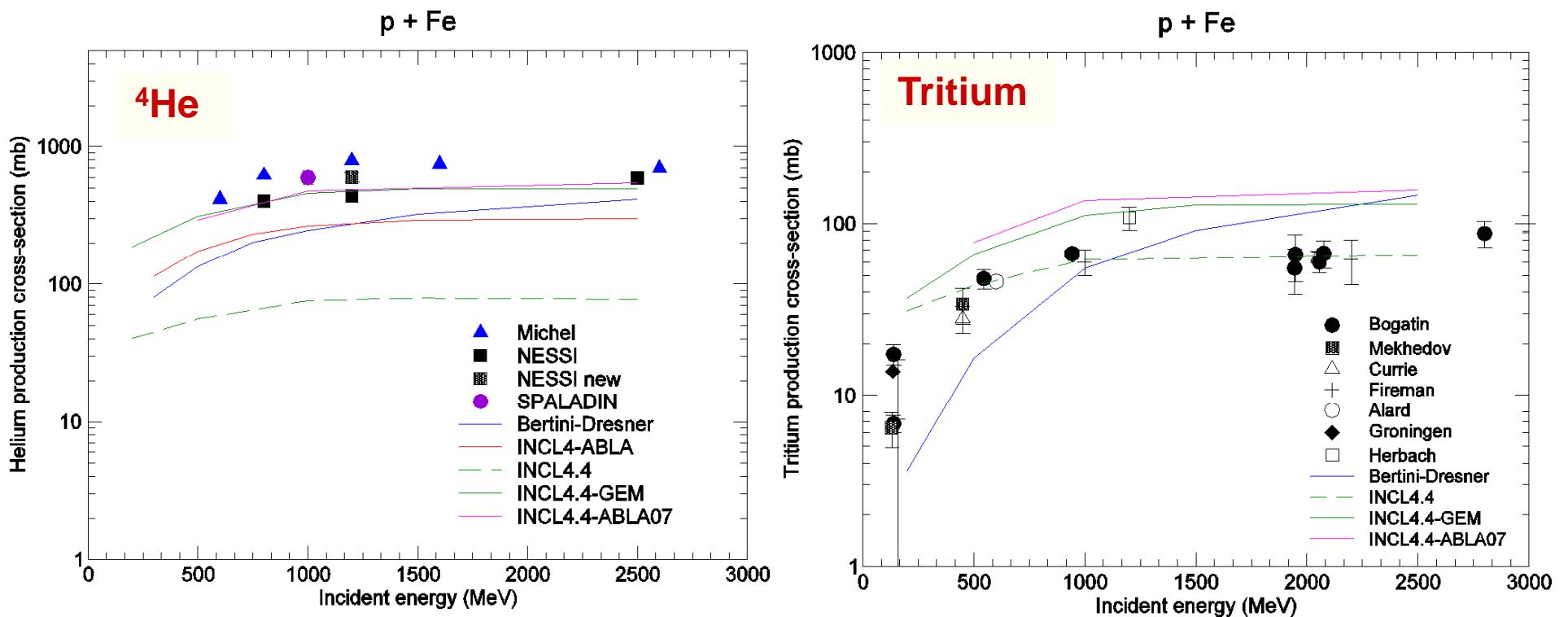
- Default option in LAHET
- Calculation is fast
- Global order of magnitude is correct  
(i.e. on neutron production)

BUT

- $E^*$  too much high
- Fission/evaporation badly balanced
- Isotopic yields doubtful

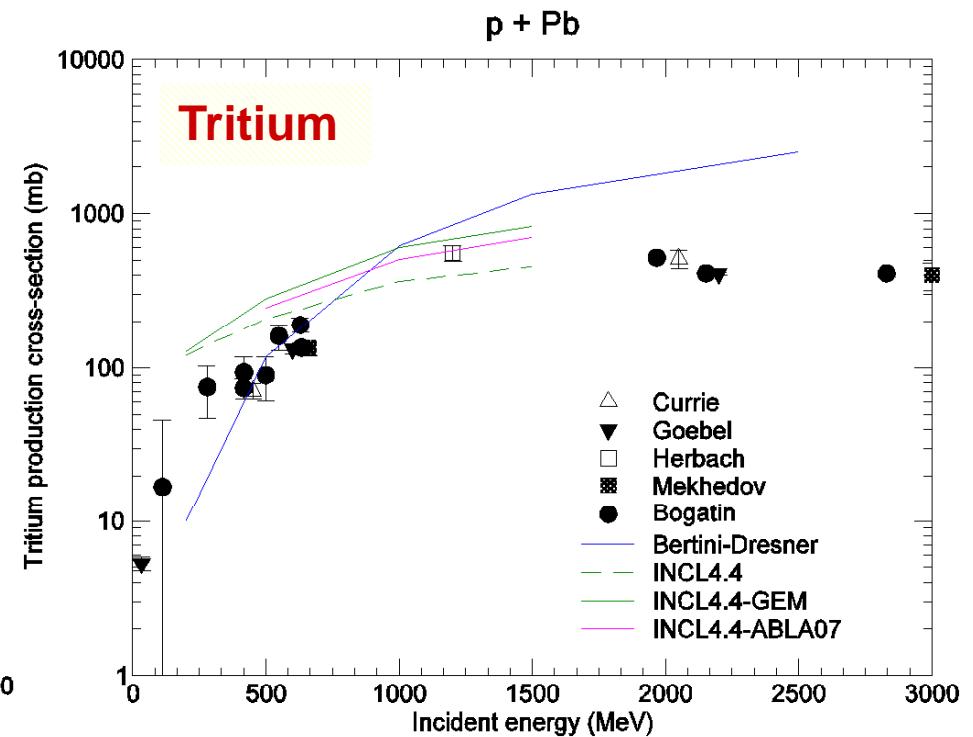
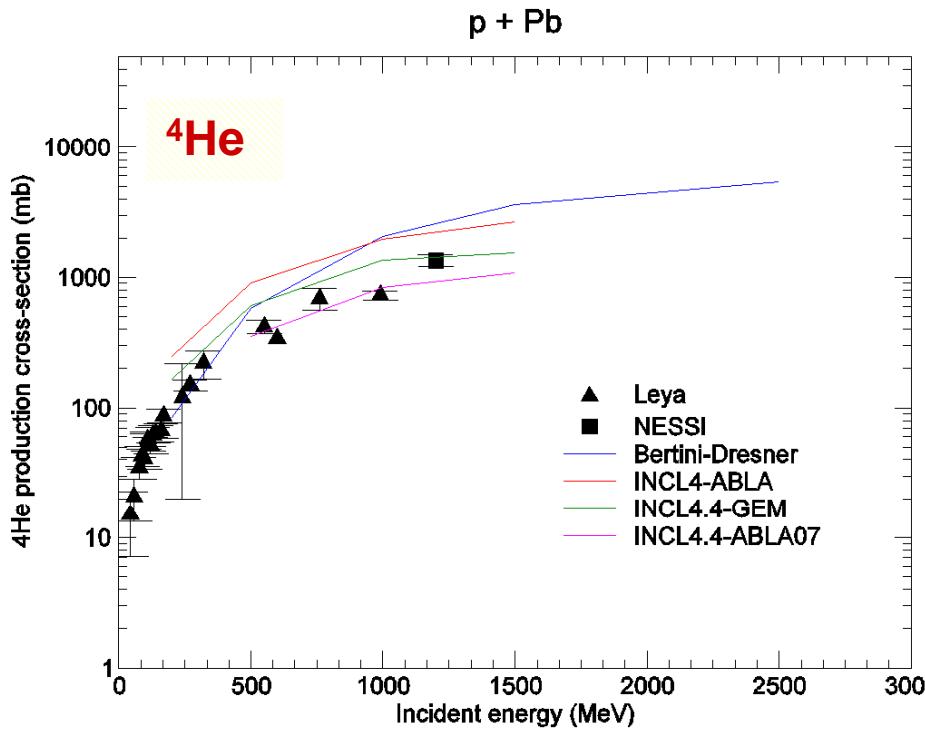


# Gas production in Fe



- INCL4.4-ABLA07 now produces tritium
- Situation improved compared to models presently in MCNPX

# Gas production in Pb



- INCL4.4-ABLA07 now produces tritium
- Situation improved compared to models presently in MCNPX

# Xe production on thick target

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Influence from the:  
cascade (production level)  
evaporation (isotopic yield)

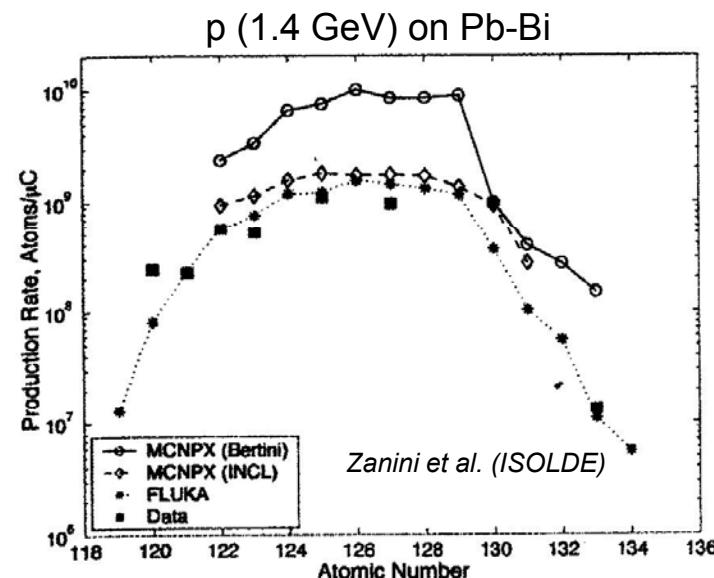
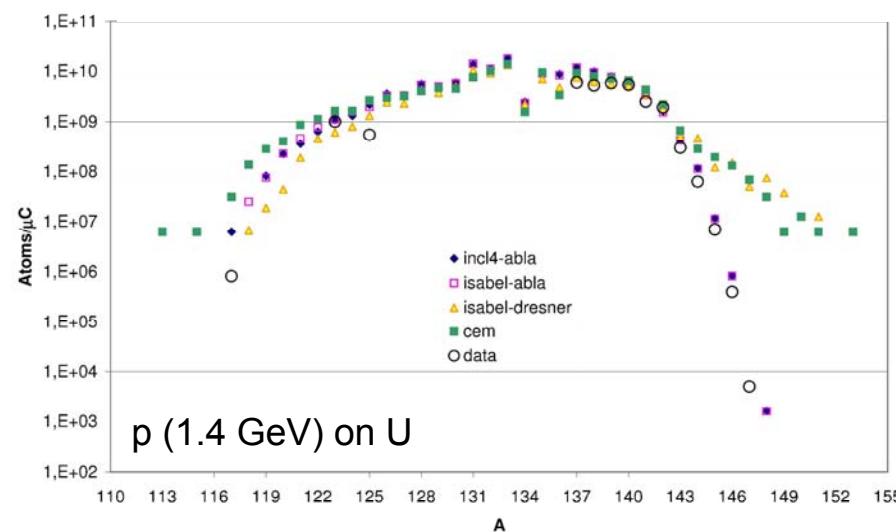
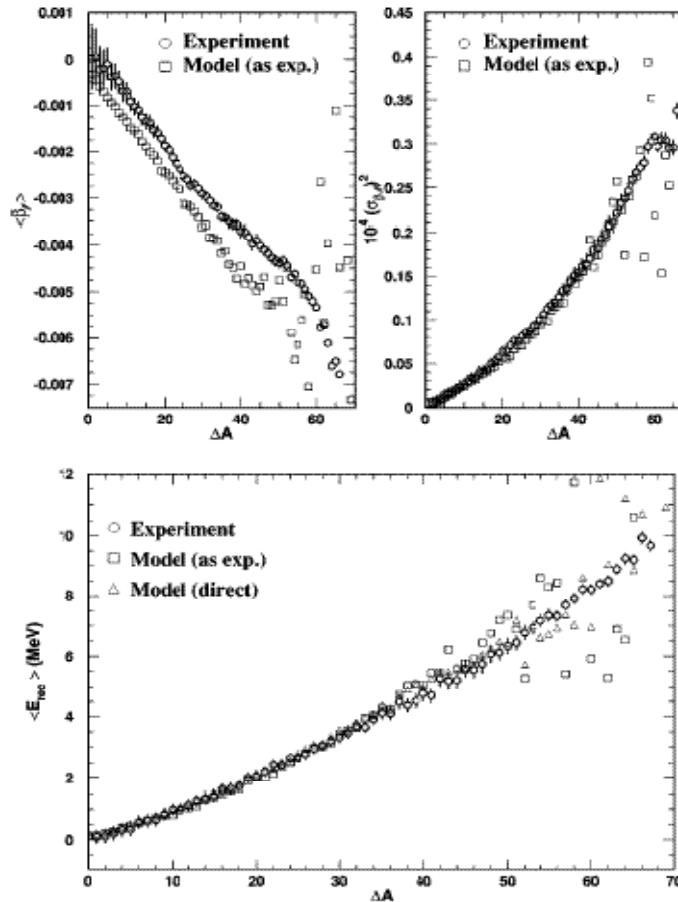


FIGURE 3. Same as Fig. 2 but for Xe isotopes.



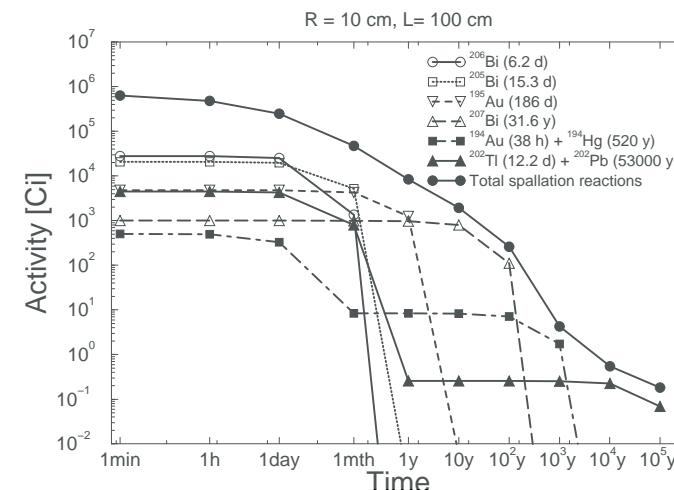
# Velocity and recoil energy

Pb (1 GeV/A) + p (GSI)

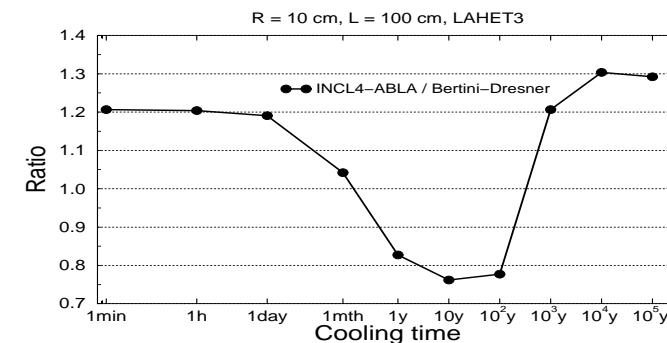


GSI: Measurement of recoil velocity distributions  
 And mean energy  
 INCL4+ABLA seems correct  
**DPA calculations are meaningful**

p (1 GeV, 1 mA) + PbBi



p (1 GeV, 1 mA) + PbBi



## Activity calculations:

Multiple contributions (mostly heavy nuclei)  
 INCL4-ABLA and Bertini-Dresner equivalent

# Conclusions

- Large set of available **high-energy data** allowing the **testing of nuclear models**
- **INC models**
  - The widely used Bertini model ruled out (lead to too high excitation energies)
  - Isabel and INCL models seem to agree quite well with the data
  - Encouraging behaviour of the INCL4 version
- **De-excitation models**
  - Dresner-Atchison unable to reproduce isotopic distributions, fission, LCP emission
  - GSI model better for residues but deficiencies for LCP emission
- **Perspectives**
  - Improvements still needed to have a model reproducing all the bulk of data
  - Coincidence experiments will allow a deeper insight into the reactions mechanisms