

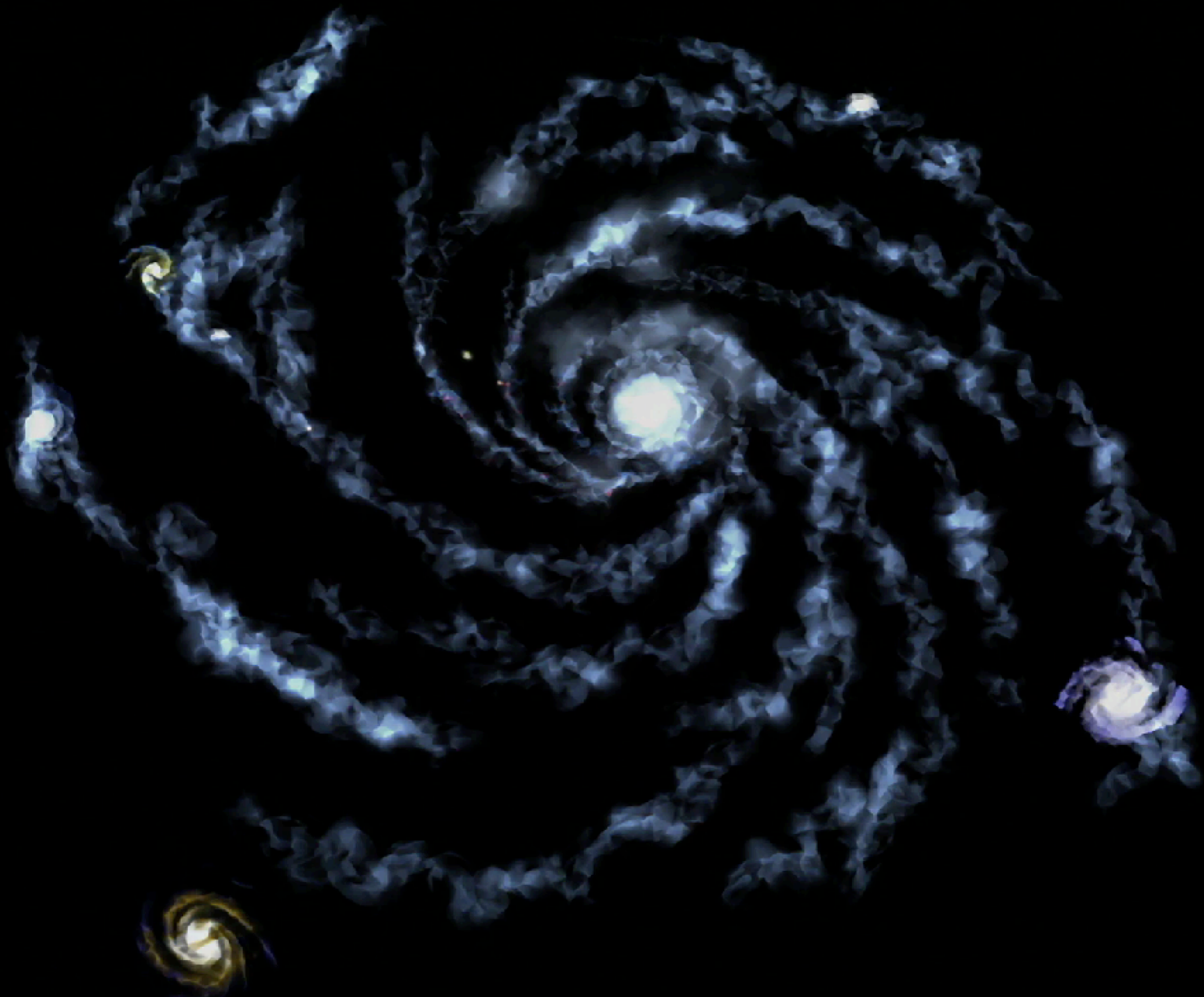
Finding Cosmic Inflation

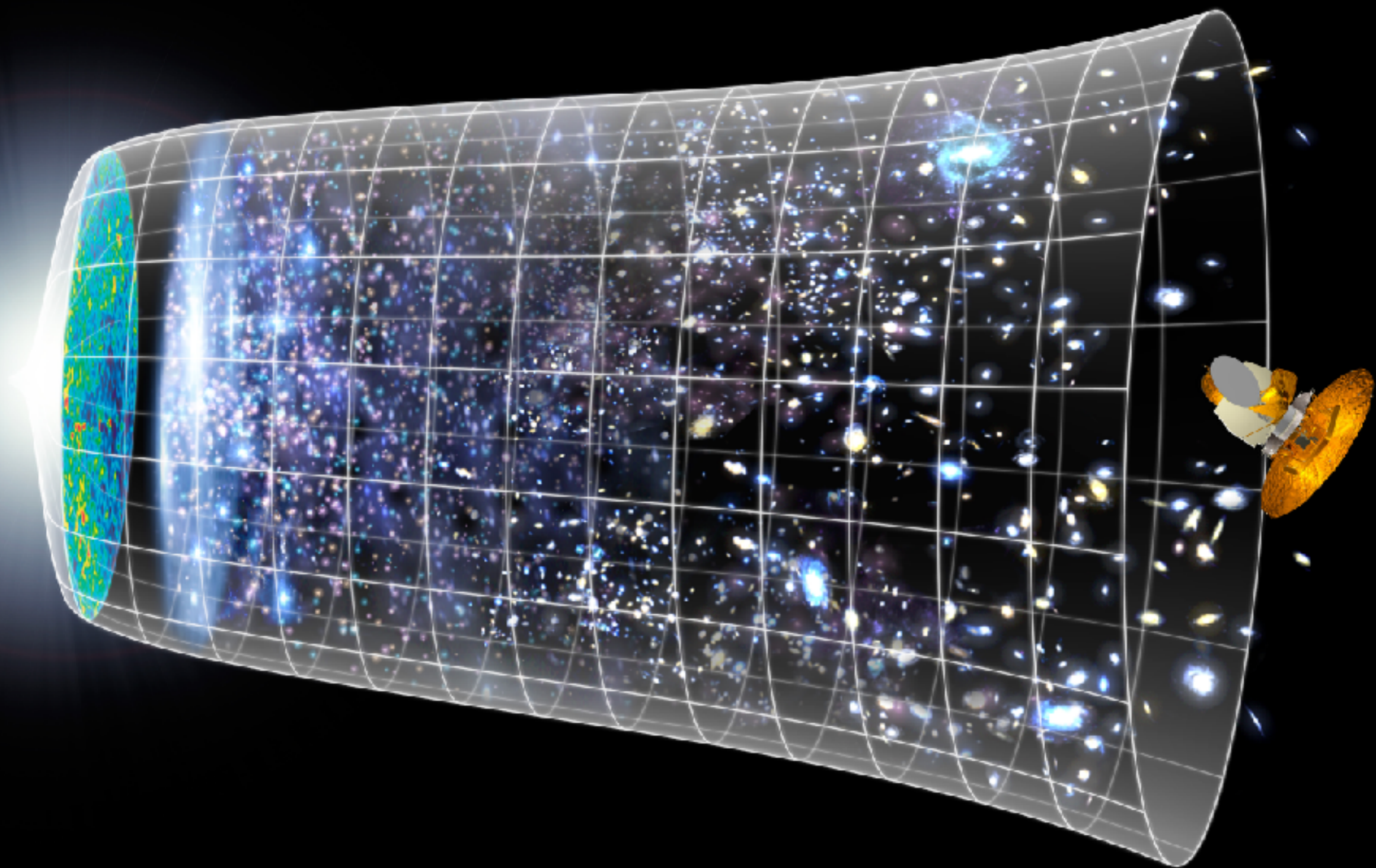
Eiichiro Komatsu

[Max Planck Institute for Astrophysics]

Séminaire du DAp, CEA Paris-Saclay

September 24, 2019





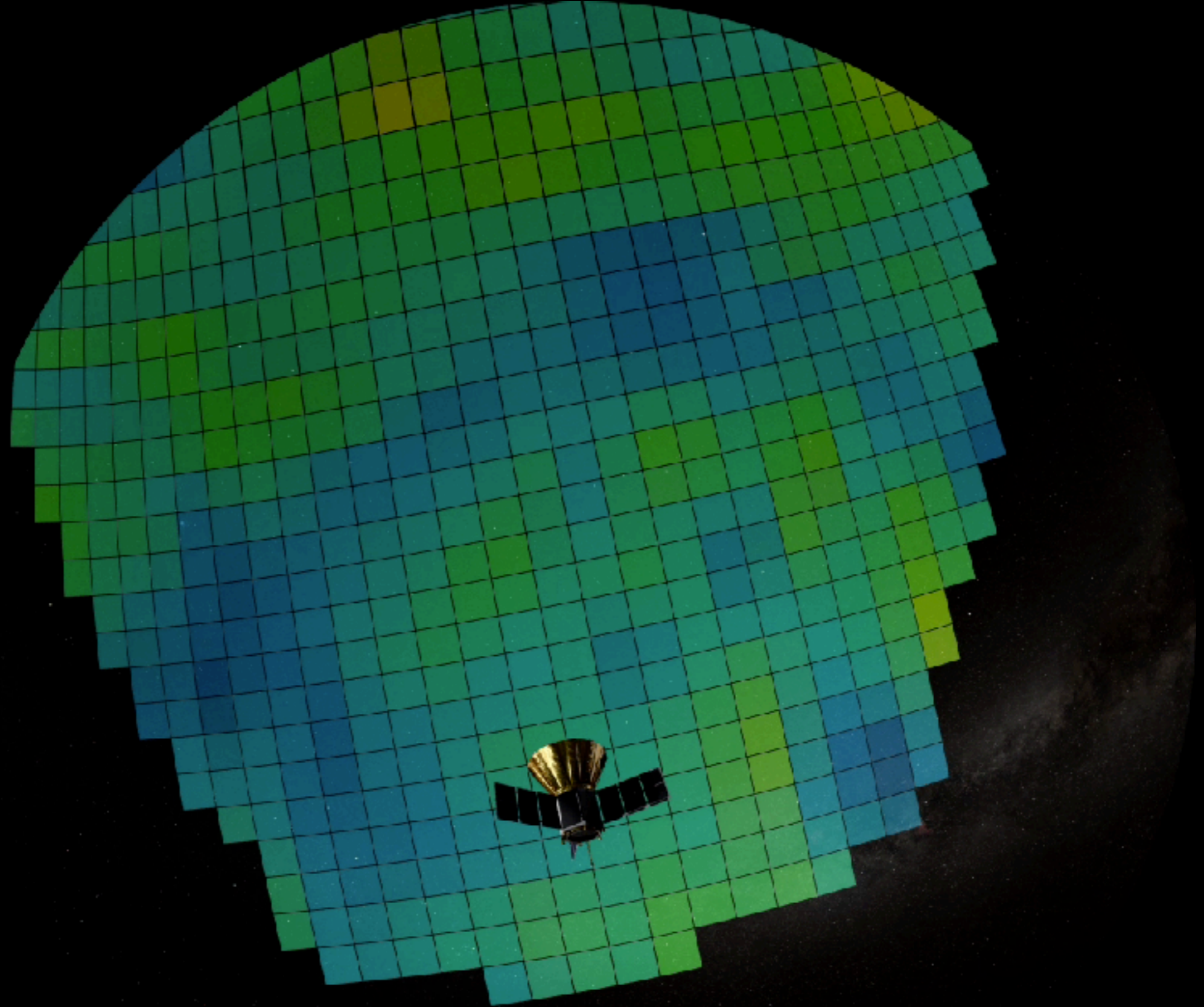


Full-dome movie for planetarium

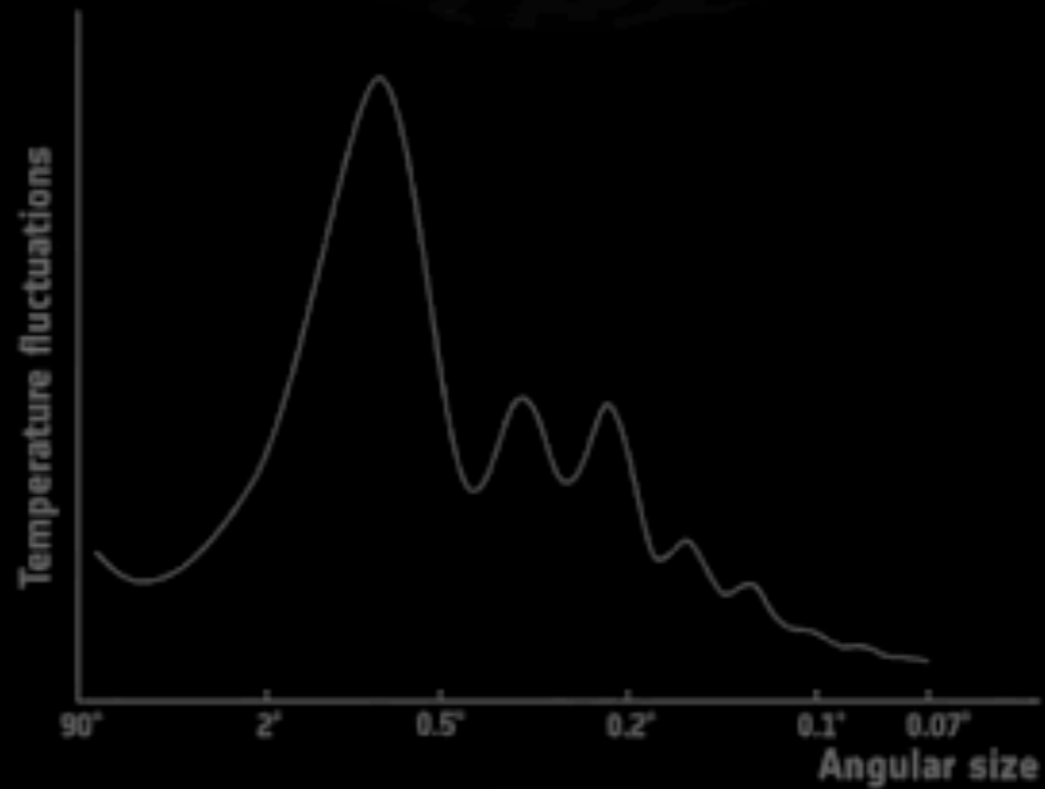
Director: Hiromitsu Kohsaka

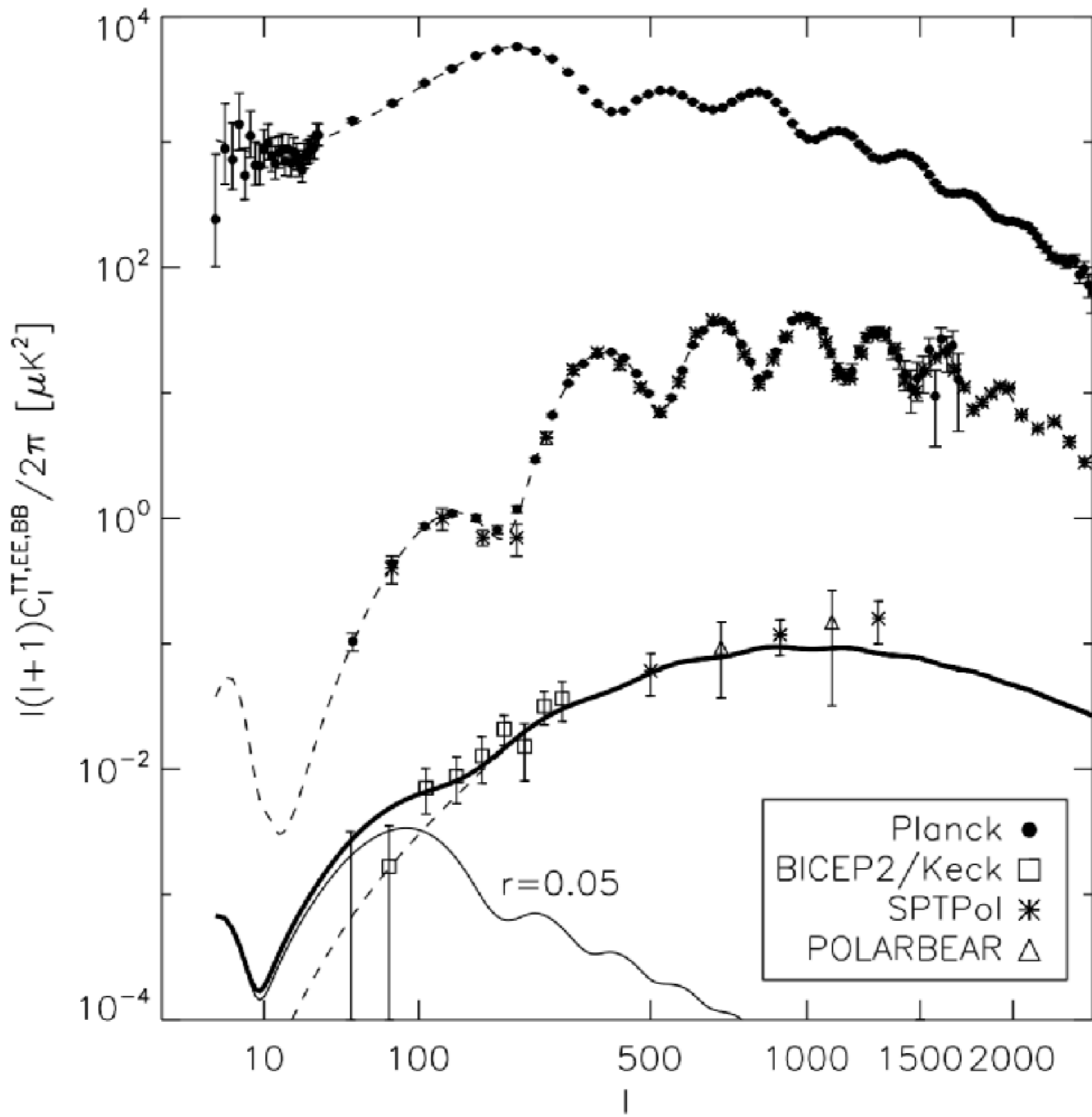


HORIZON :Beyond the Edge of the Visible Universe [Trailer]

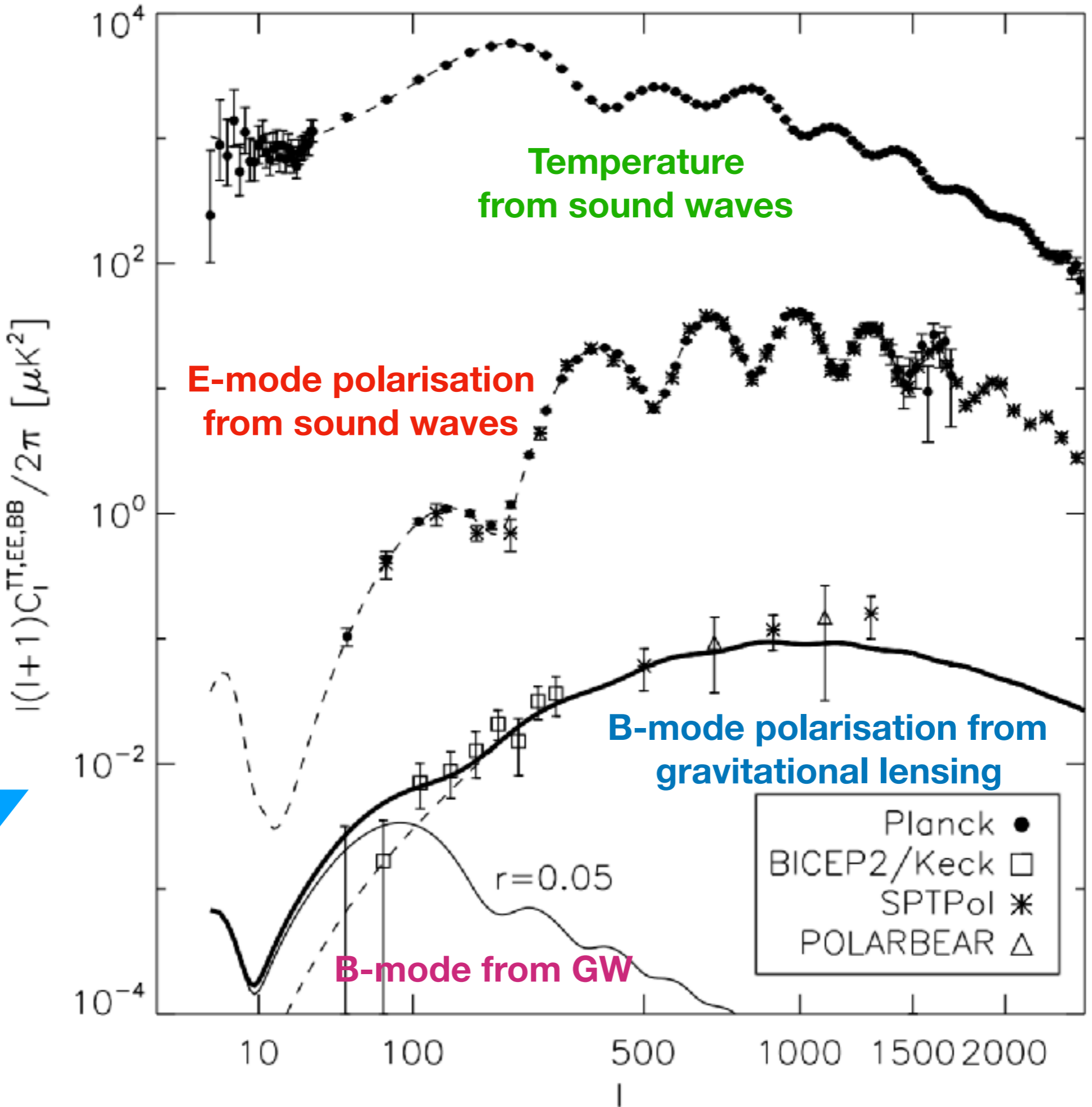
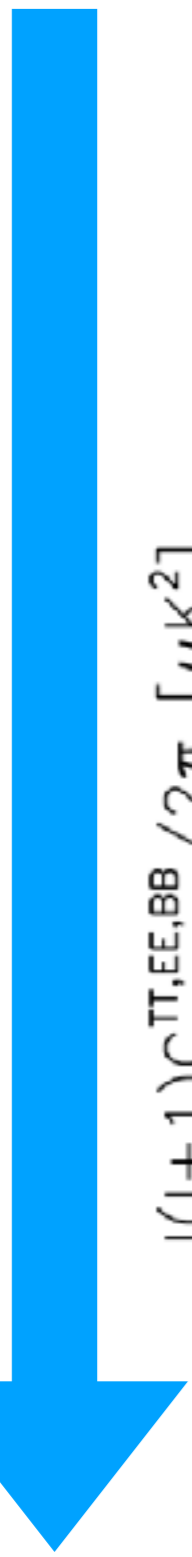


Power spectrum, explained





Seven orders of magnitude in power
in "just" 25 years



CMB-S4

Next Generation CMB Experiment

CMB Stages

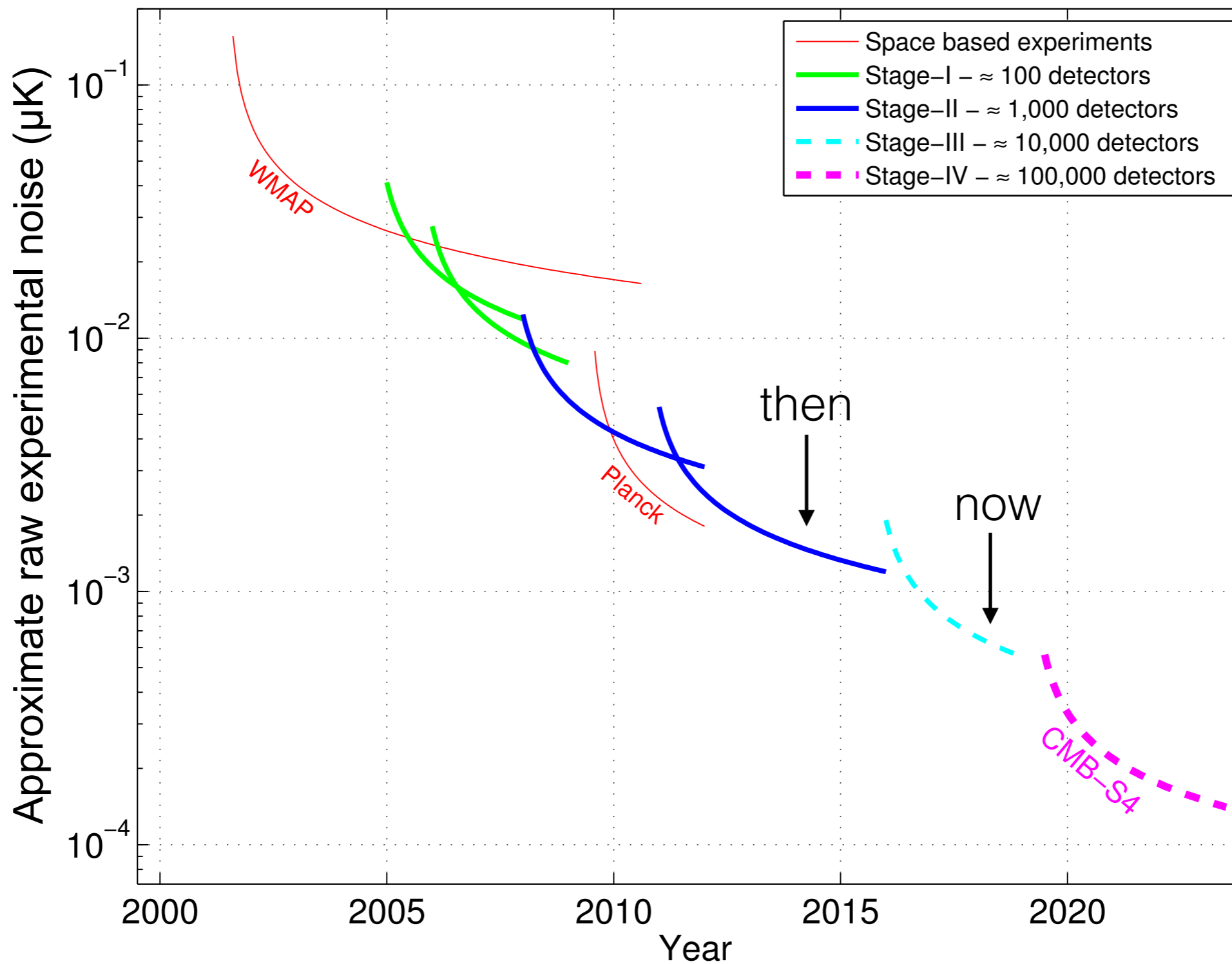
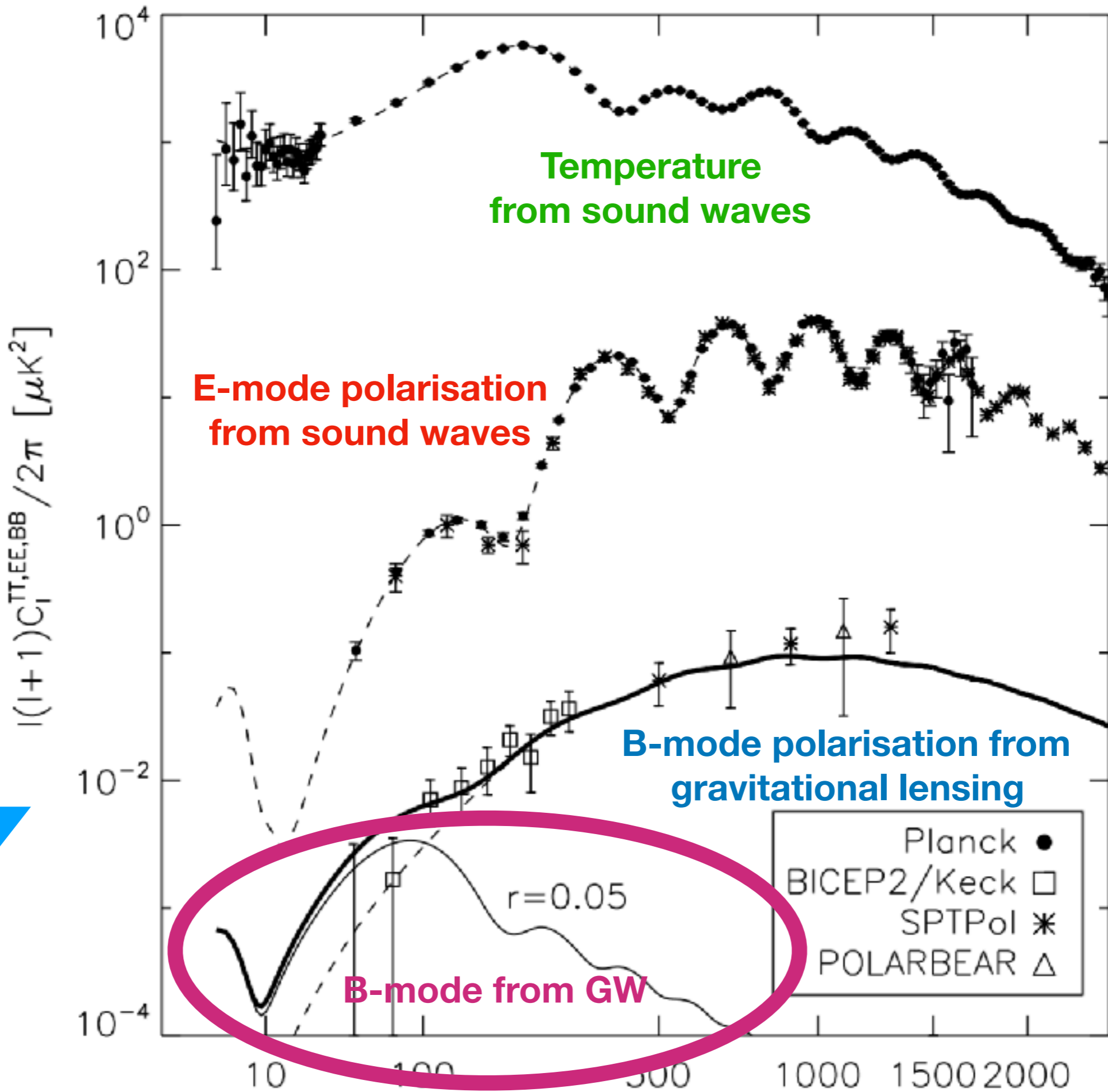
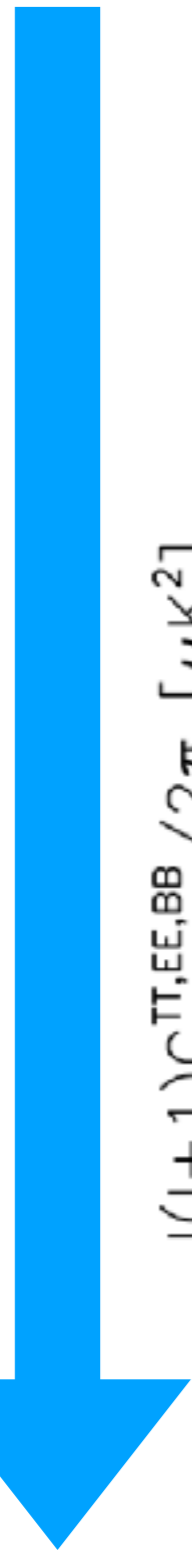


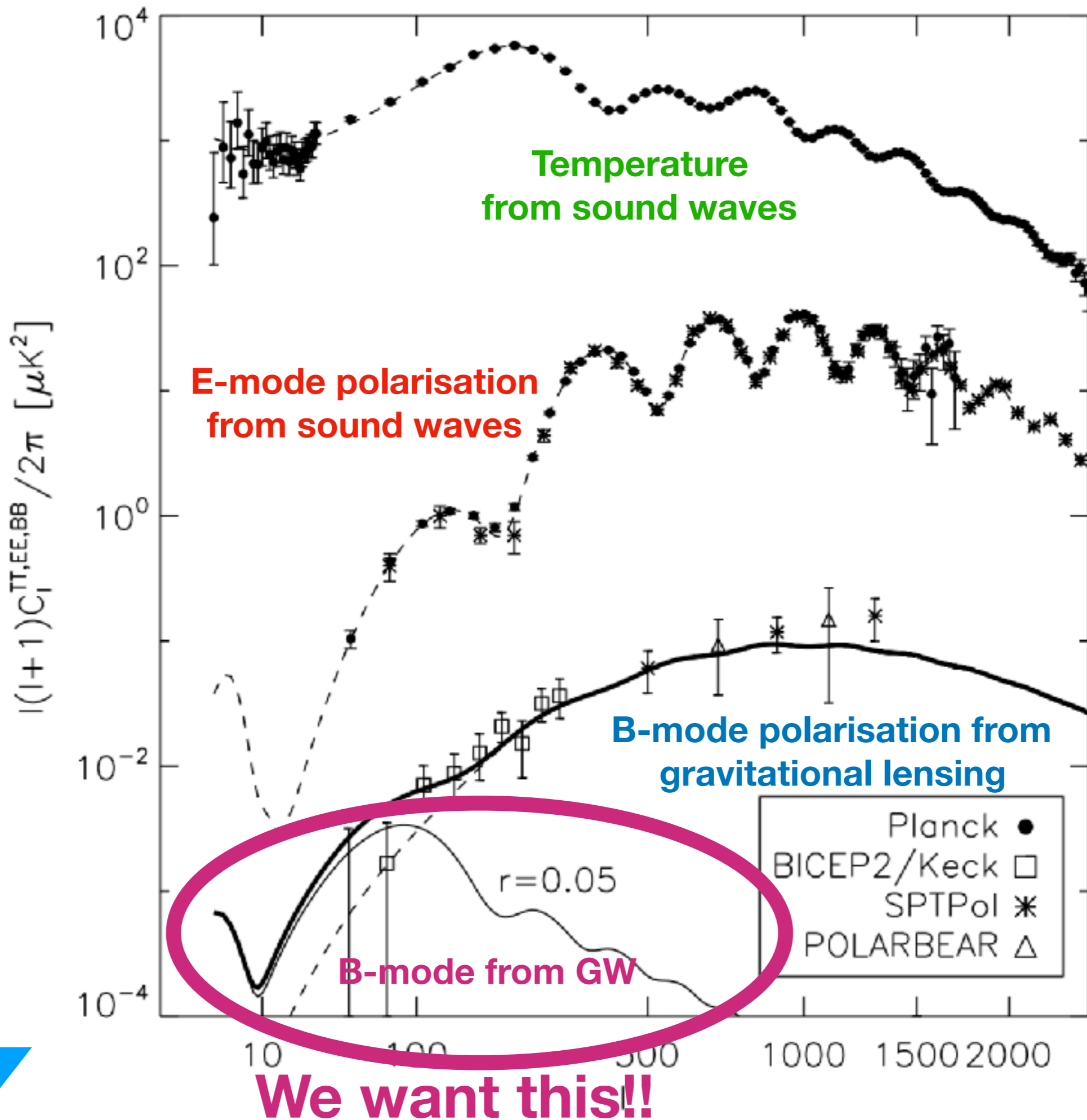
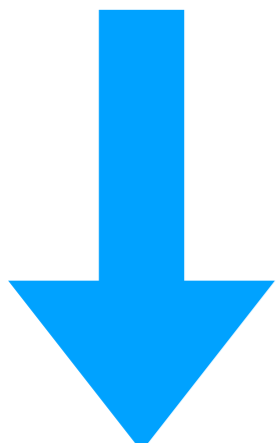
Figure by Clem Pryke for 2013 Snowmass documents

Seven orders of magnitude in power
in "just" 25 years



We want this!!

Another two orders of magnitude
in the next 10–15 years



JAXA



+ participations from
USA, Canada, Europe

LiteBIRD 2028–

Polarisation satellite dedicated to
measure CMB polarisation from
primordial GW, with a few thousand
TES bolometers in space

JAXA



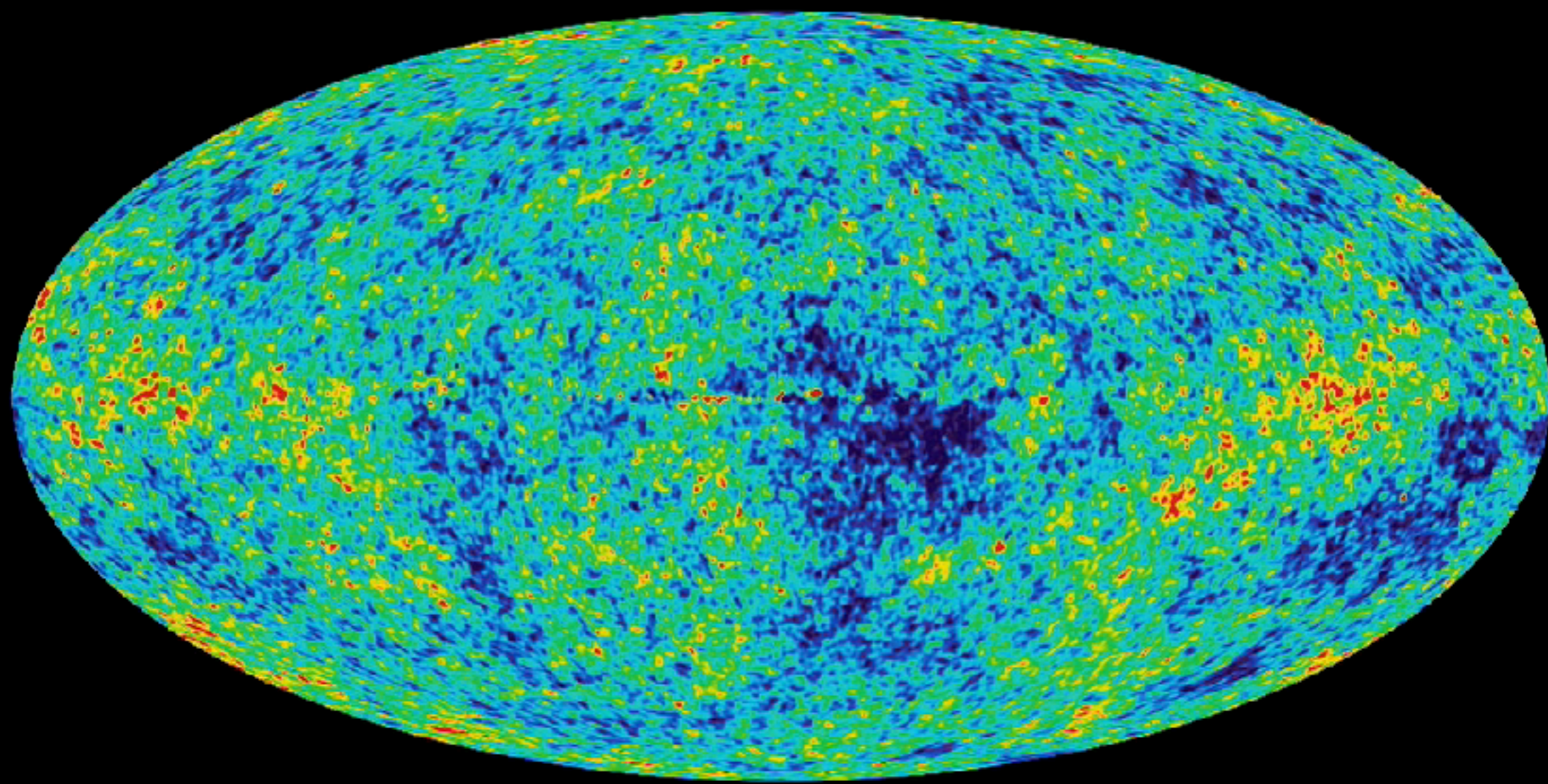
+ participations from
USA, Canada, Europe

LiteBIRD 2028–

Selected!

May 21: JAXA has chosen LiteBIRD
as the strategic large-class mission.

We will go to L2!



A Remarkable Story

- Observations of the cosmic microwave background and their interpretation taught us that **galaxies, stars, planets, and ourselves originated from tiny fluctuations in the early Universe**
- *But, **what generated the initial fluctuations?***

Leading Idea

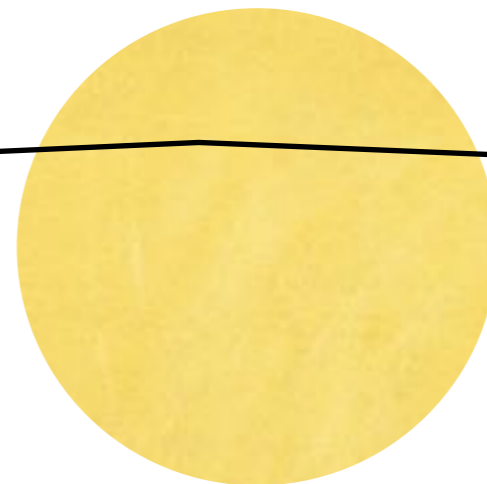
- Quantum mechanics at work in the early Universe
 - “*We all came from quantum fluctuations*”
- But, how did quantum fluctuations on the *microscopic* scales become *macroscopic* fluctuations over large distances?
 - What is the **missing link** between small and large scales?

Cosmic Inflation

Quantum fluctuations on
microscopic scales



Inflation!

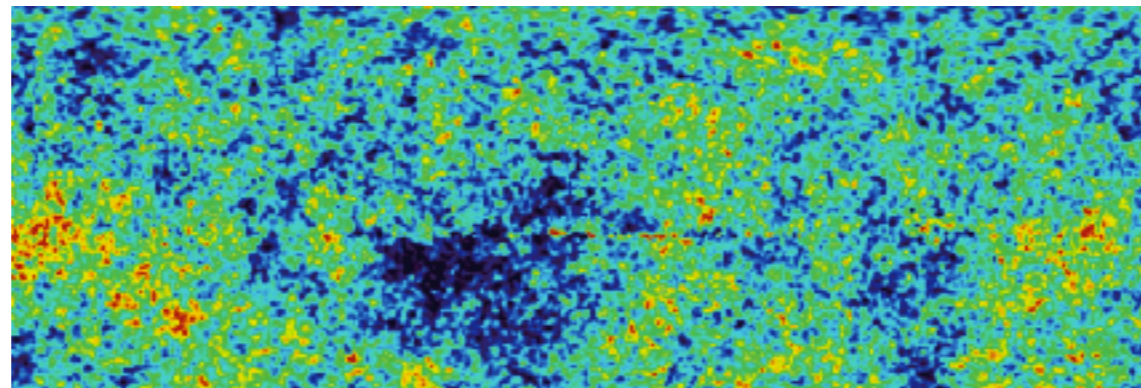
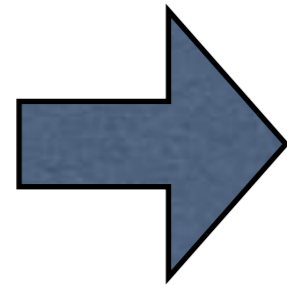


- Exponential expansion (inflation) stretches the wavelength of quantum fluctuations to cosmological scales

Key Predictions

ζ

scalar
mode

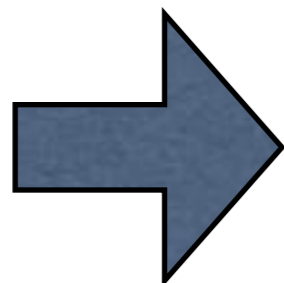


Mukhanov&Chibisov (1981)
Guth & Pi (1982)
Hawking (1982)
Starobinsky (1982)
Bardeen, Steinhardt&Turner (1983)

- Fluctuations we observe today in CMB and the matter distribution originate from quantum fluctuations during inflation

h_{ij}

tensor
mode



Grishchuk (1974)
Starobinsky (1979)

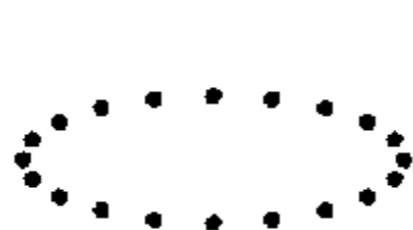
- There should also be *ultra long-wavelength* gravitational waves generated during inflation

We measure distortions in space

- A distance between two points in space

$$d\ell^2 = a^2(t) [1 + 2\zeta(\mathbf{x}, t)] [\delta_{ij} + h_{ij}(\mathbf{x}, t)] dx^i dx^j$$

- ζ : “curvature perturbation” (scalar mode)
 - Perturbation to the determinant of the spatial metric
- h_{ij} : “gravitational waves” (tensor mode)
 - Perturbation that does not alter the determinant



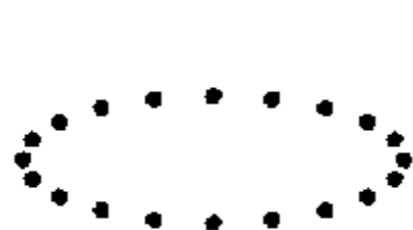
$$\sum_i h_{ii} = 0$$

We measure distortions in space

- A distance between two points in space

$$d\ell^2 = \underbrace{a^2(t)}_{\text{scale factor}} [1 + 2\zeta(\mathbf{x}, t)] [\delta_{ij} + h_{ij}(\mathbf{x}, t)] dx^i dx^j$$

- ζ : “curvature perturbation” (scalar mode)
 - Perturbation to the determinant of the spatial metric
- h_{ij} : “gravitational waves” (tensor mode)
 - Perturbation that does not alter the determinant



$$\sum_i h_{ii} = 0$$

Finding Inflation

- Inflation is the accelerated, quasi-exponential expansion. Defining the Hubble expansion rate as $H(t)=d\ln(a)/dt$, we must find

$$\frac{\ddot{a}}{a} = \dot{H} + H^2 > 0 \quad \longrightarrow \quad \epsilon \equiv -\frac{\dot{H}}{H^2} < 1$$

- For inflation to explain flatness of spatial geometry of our observable Universe, we need to have a **sustained** period of inflation. This implies $\epsilon=O(N^{-1})$ or smaller, where N is the number of e-folds of expansion counted from the end of inflation:

$$N \equiv \ln \frac{a_{\text{end}}}{a} = \int_t^{t_{\text{end}}} dt' H(t') \approx 50$$

Have we found inflation?

- *Have we found $\varepsilon \ll 1$?*

$$\varepsilon \equiv -\frac{\dot{H}}{H^2}$$

- To achieve this, we need to map out **H(t)**, and show that it does not change very much with time
 - **We need the “Hubble diagram” during inflation!**

Fluctuations are proportional to H

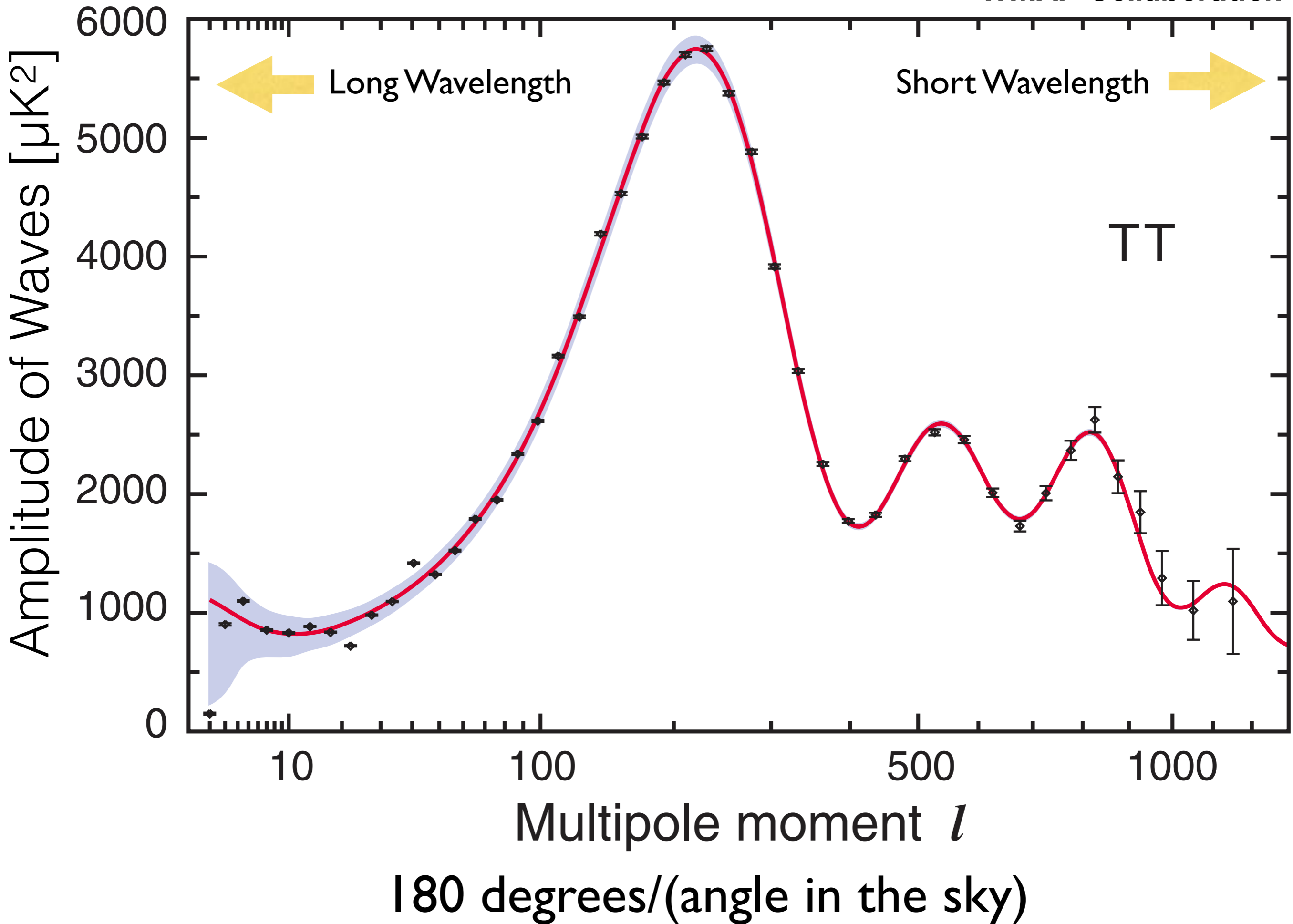
- Both scalar (ζ) and tensor (h_{ij}) perturbations are proportional to H
- Consequence of the uncertainty principle
- [energy you can borrow] \sim [time you borrow] $^{-1} \sim H$
- **THE KEY:** The earlier the fluctuations are generated, the more its wavelength is stretched, and thus the bigger the angles they subtend in the sky. **We can map $H(t)$ by measuring CMB fluctuations over a wide range of angles**

Fluctuations are proportional to H

- **We can map $H(t)$ by measuring CMB fluctuations over a wide range of angles**
 1. We want to show that the amplitude of CMB fluctuations does not depend very much on angles
 2. Moreover, since inflation must end, H would be a decreasing function of time. It would be fantastic to show that the amplitude of CMB fluctuations actually **DOES** depend on angles such that the small scale has ***slightly*** smaller power

Data Analysis

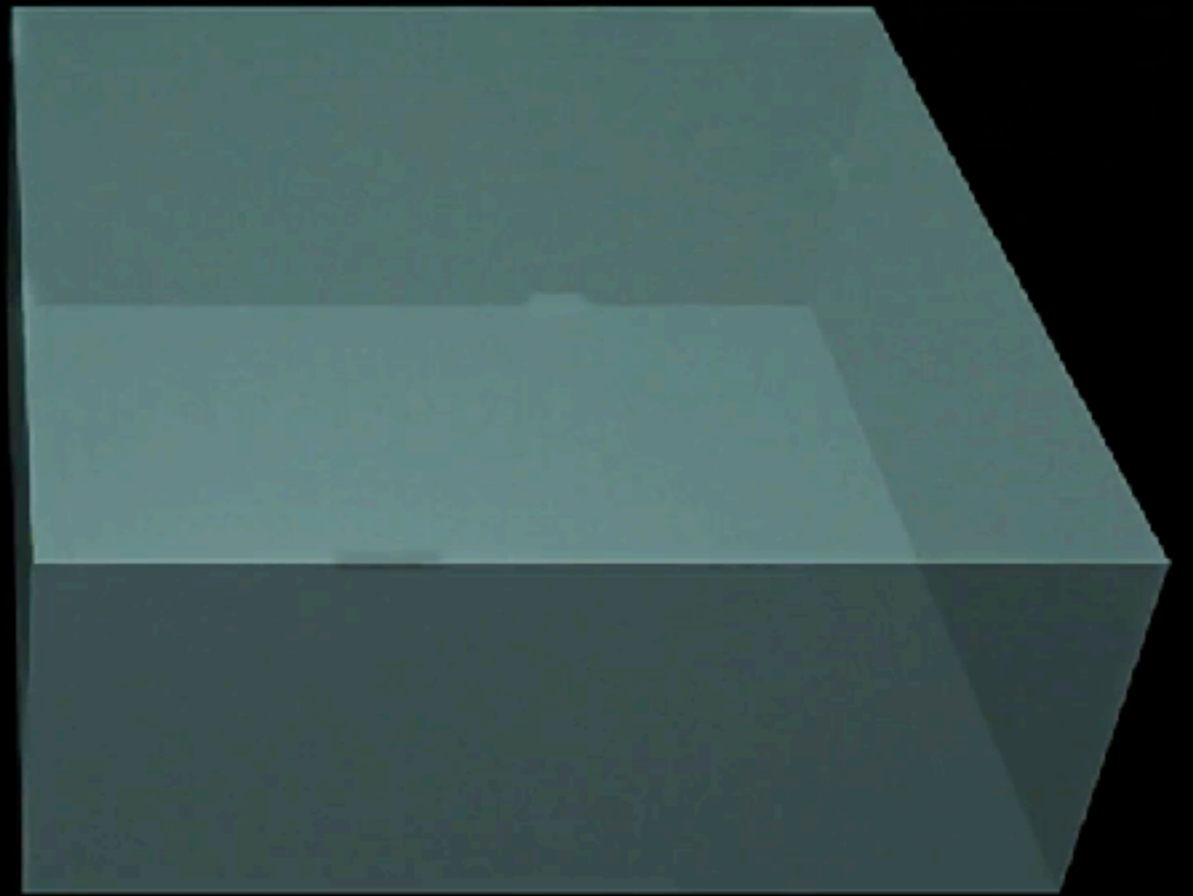
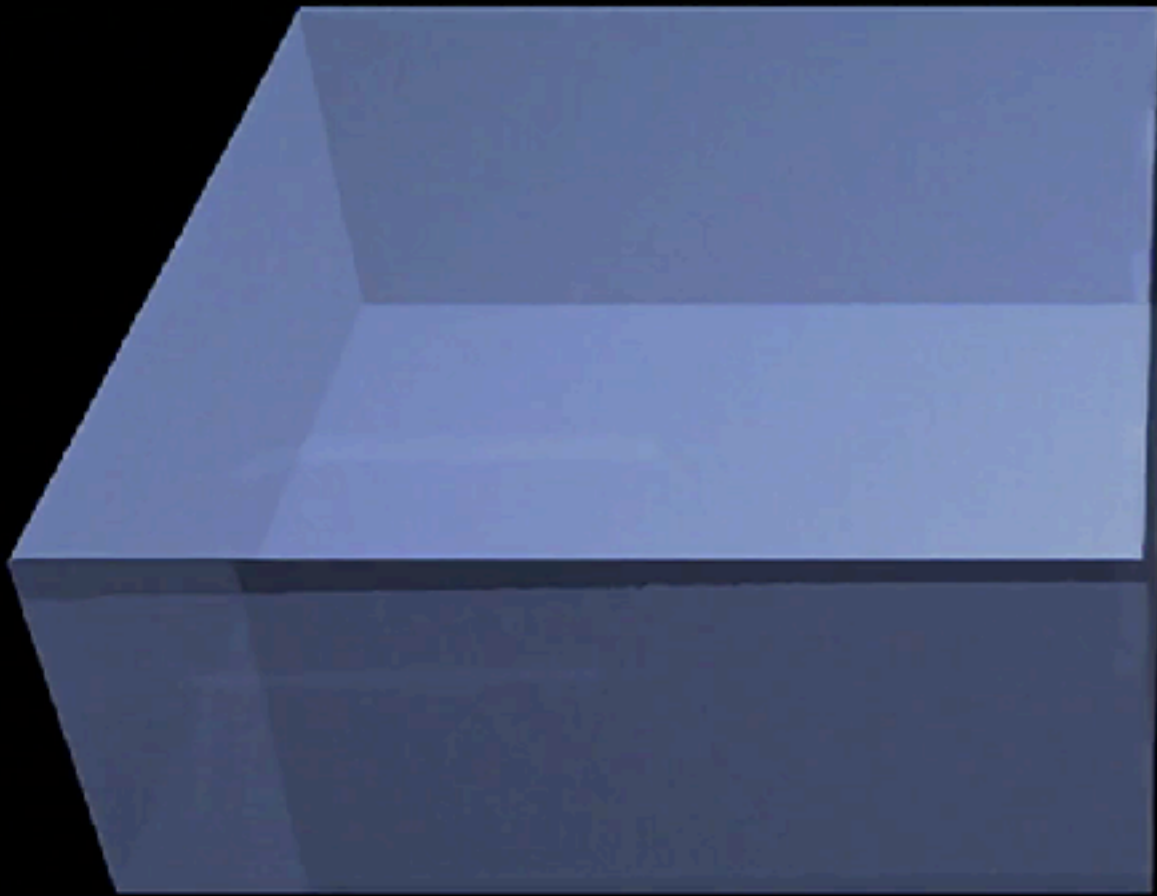
- Decompose temperature fluctuations in the sky into a set of waves with various wavelengths
- Make a diagram showing the strength of each wavelength



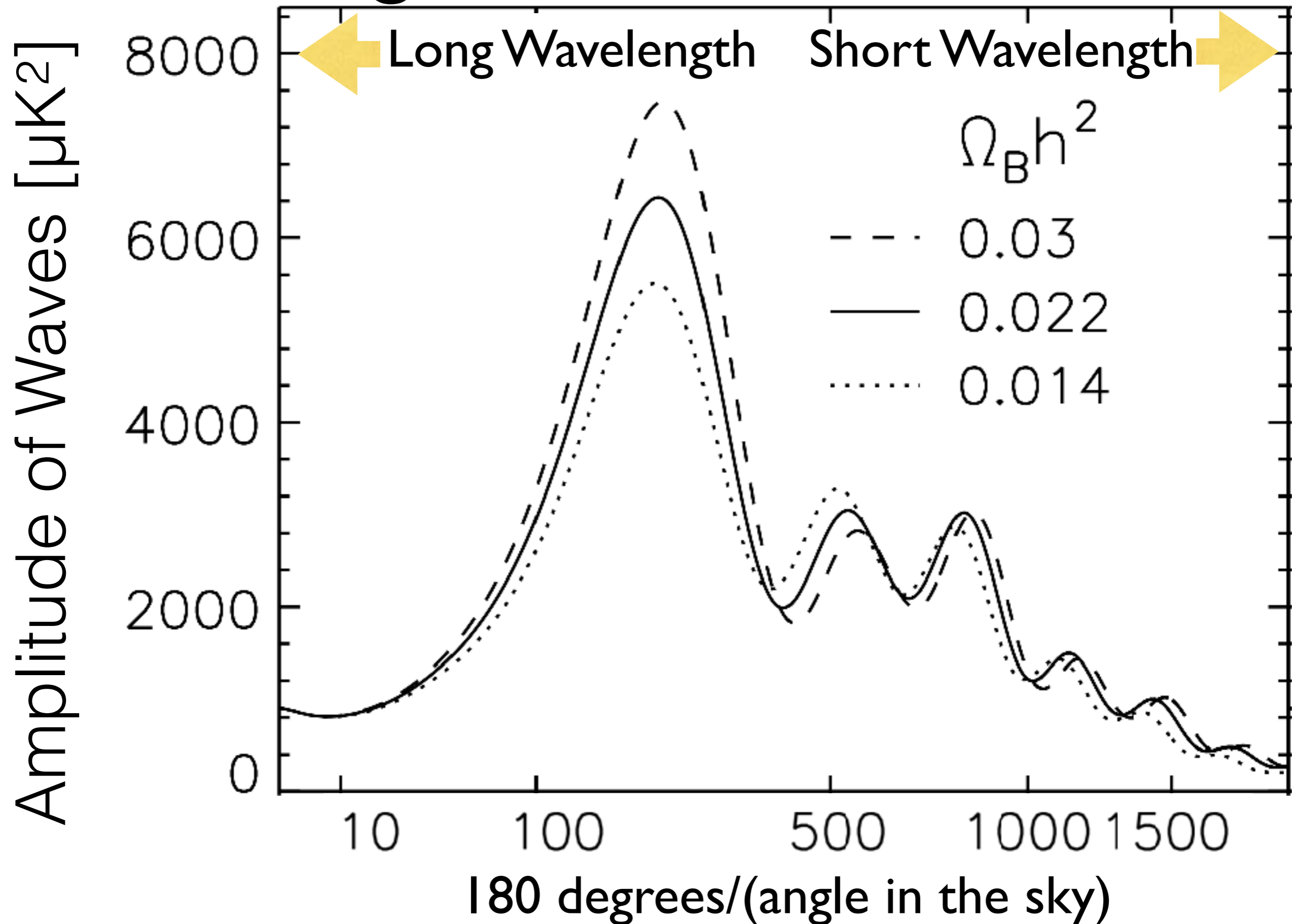


Soupe Miso Cosmique

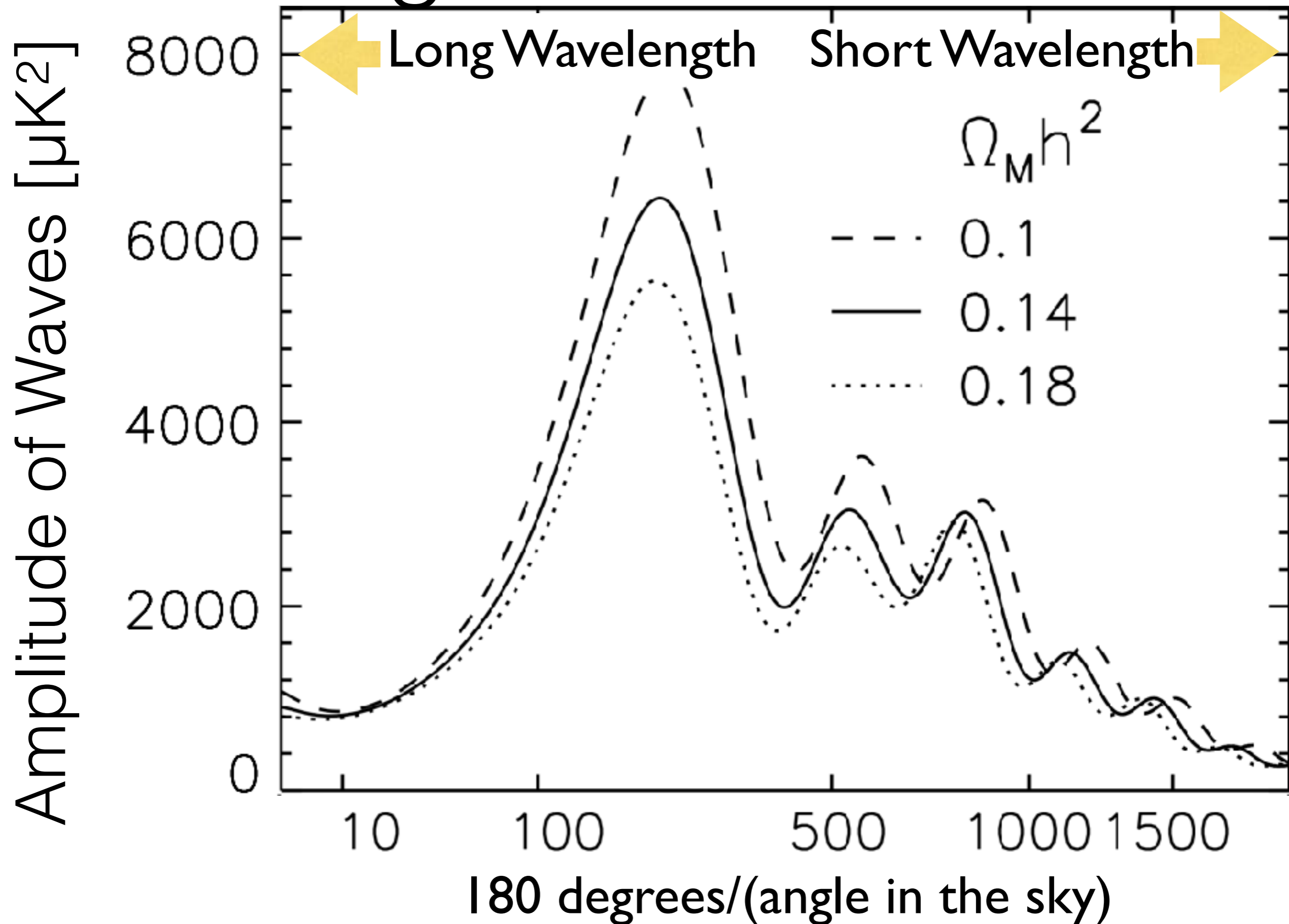
- When matter and radiation were hotter than 3000 K, matter was completely ionised. The Universe was filled with plasma, which behaves just like a soup
- Think about a Miso soup (if you know what it is). Imagine throwing Tofus into a Miso soup, while changing the density of Miso
- And imagine watching how ripples are created and propagate throughout the soup



Measuring Abundance of H&He

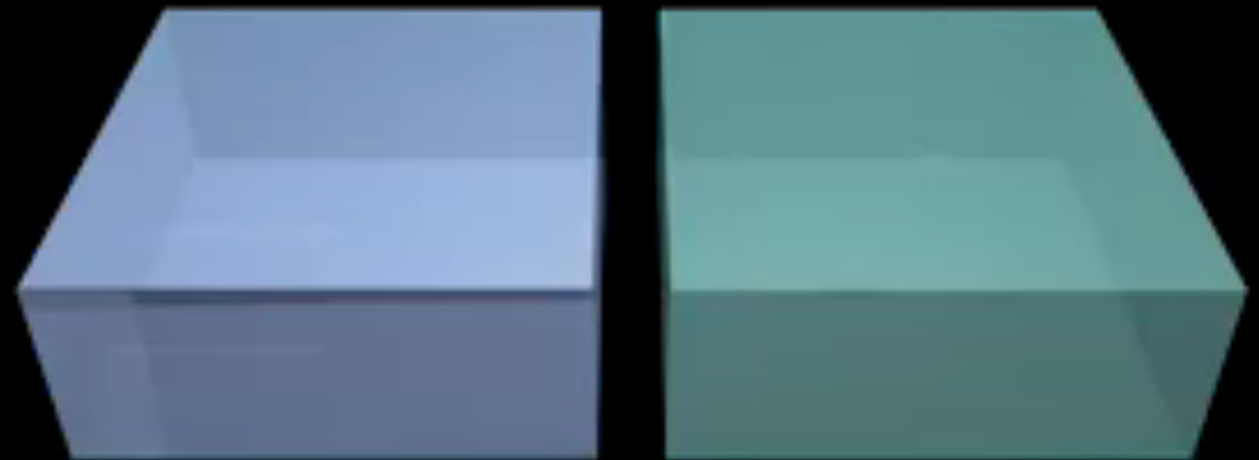


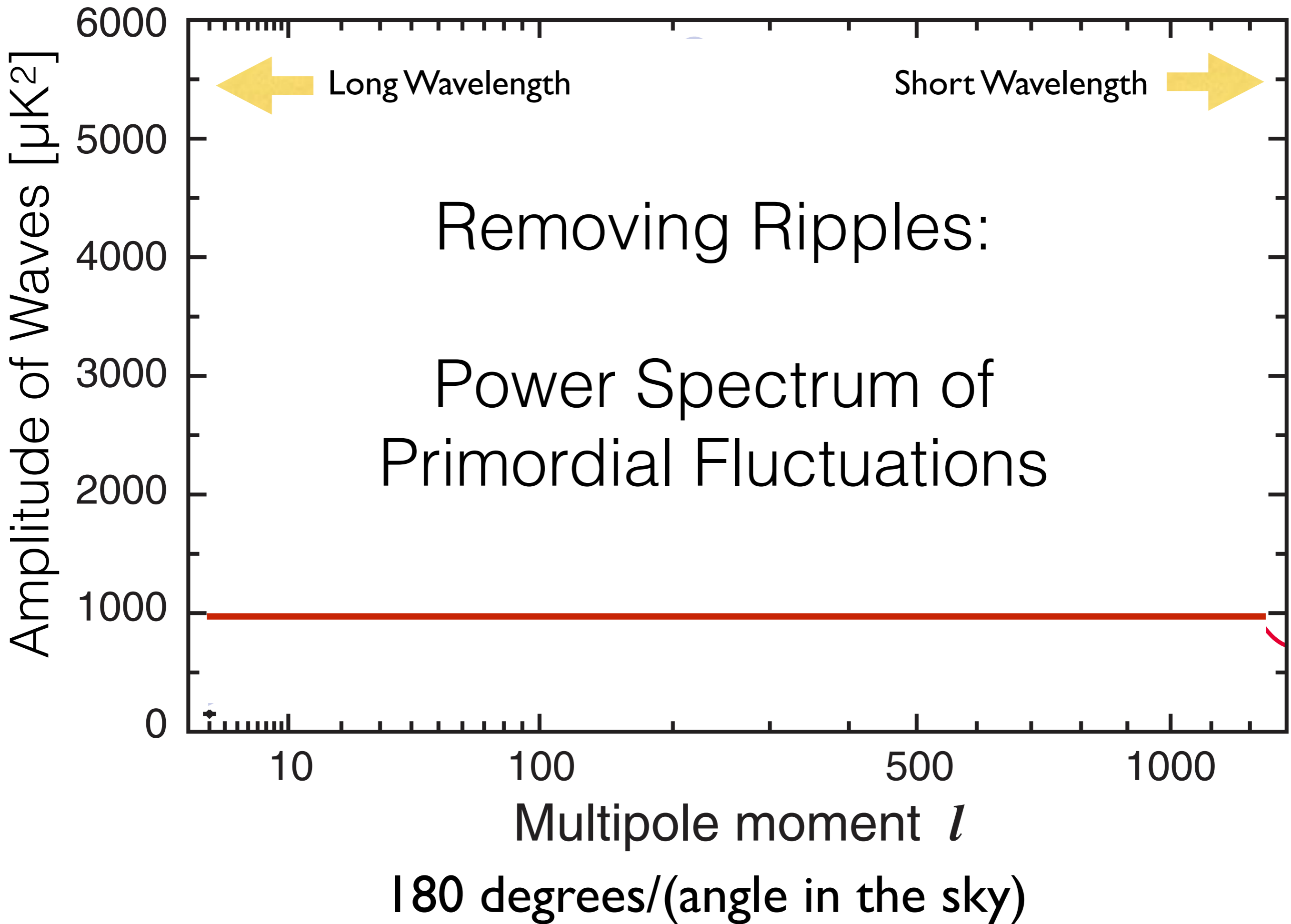
Measuring Total Matter Density

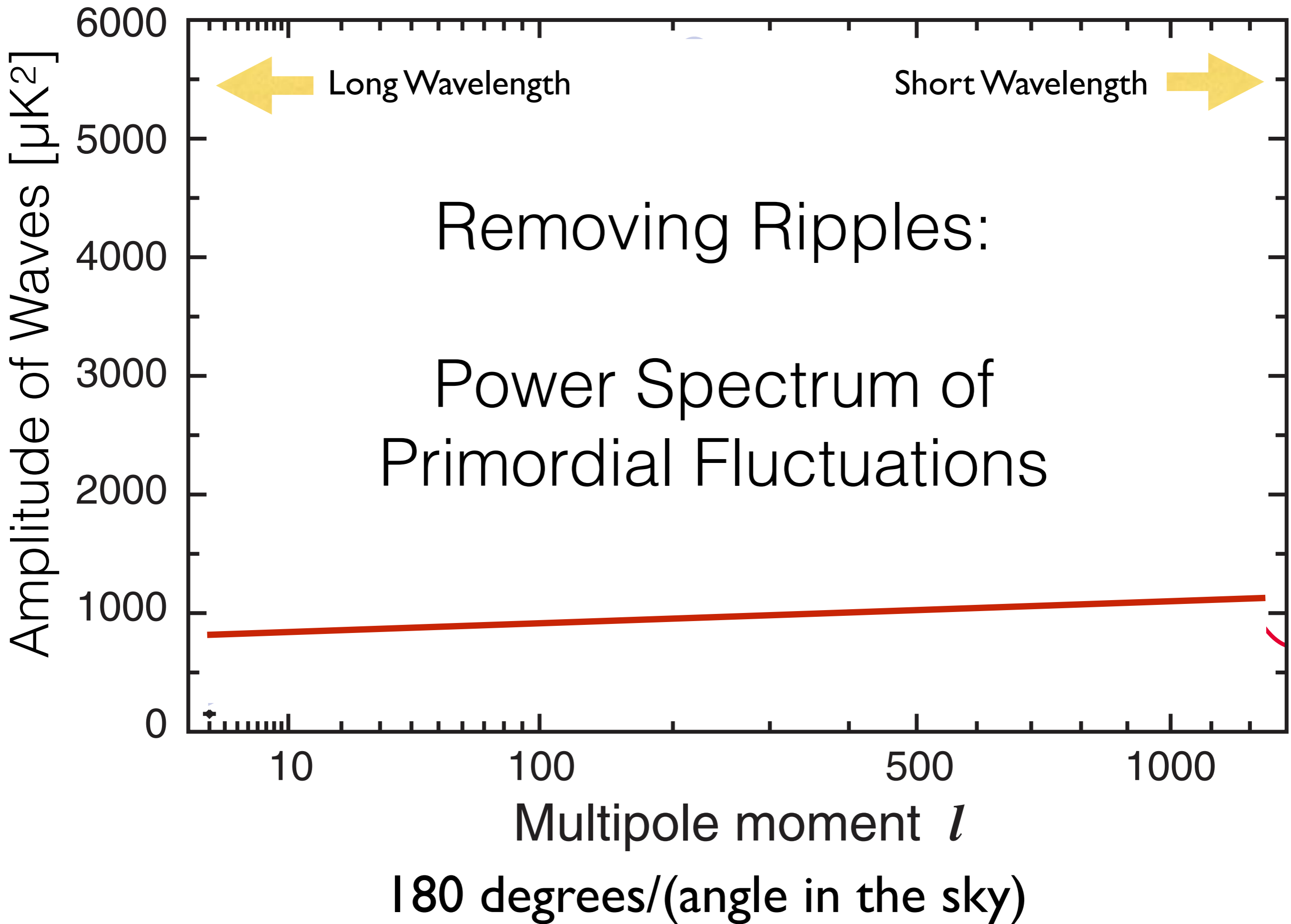


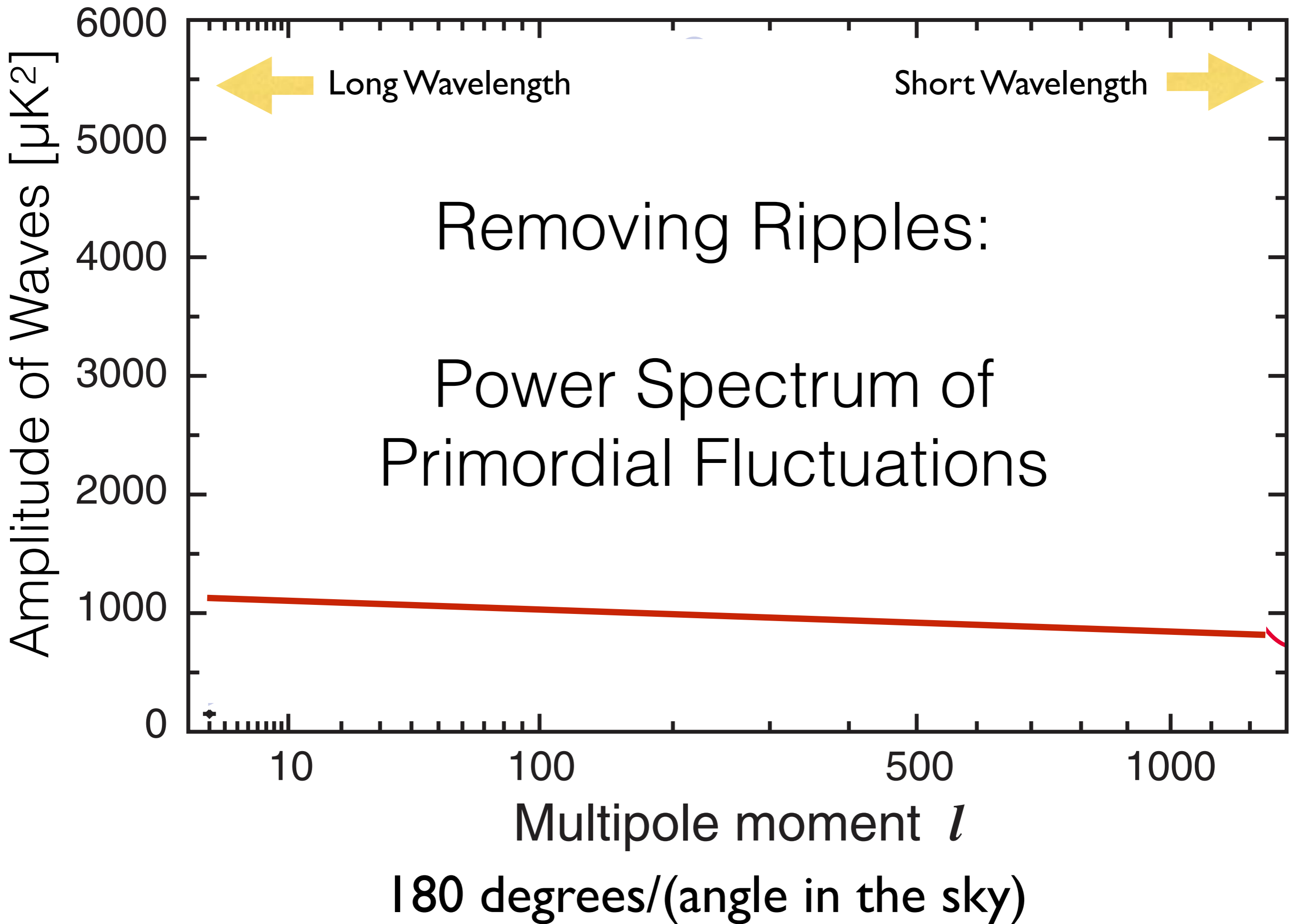
Origin of Fluctuations

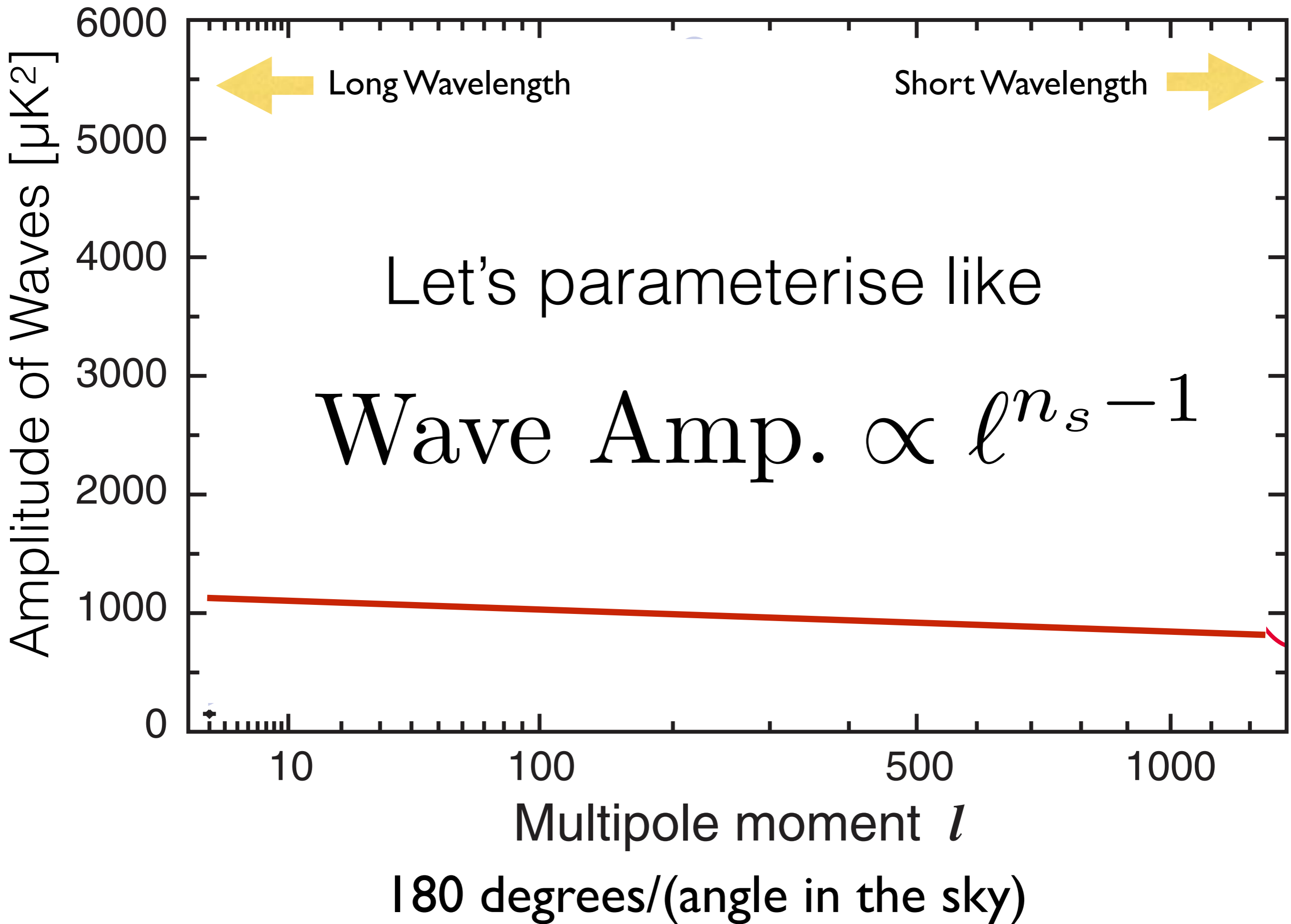
- Who dropped those Tofus into the cosmic Miso soup?

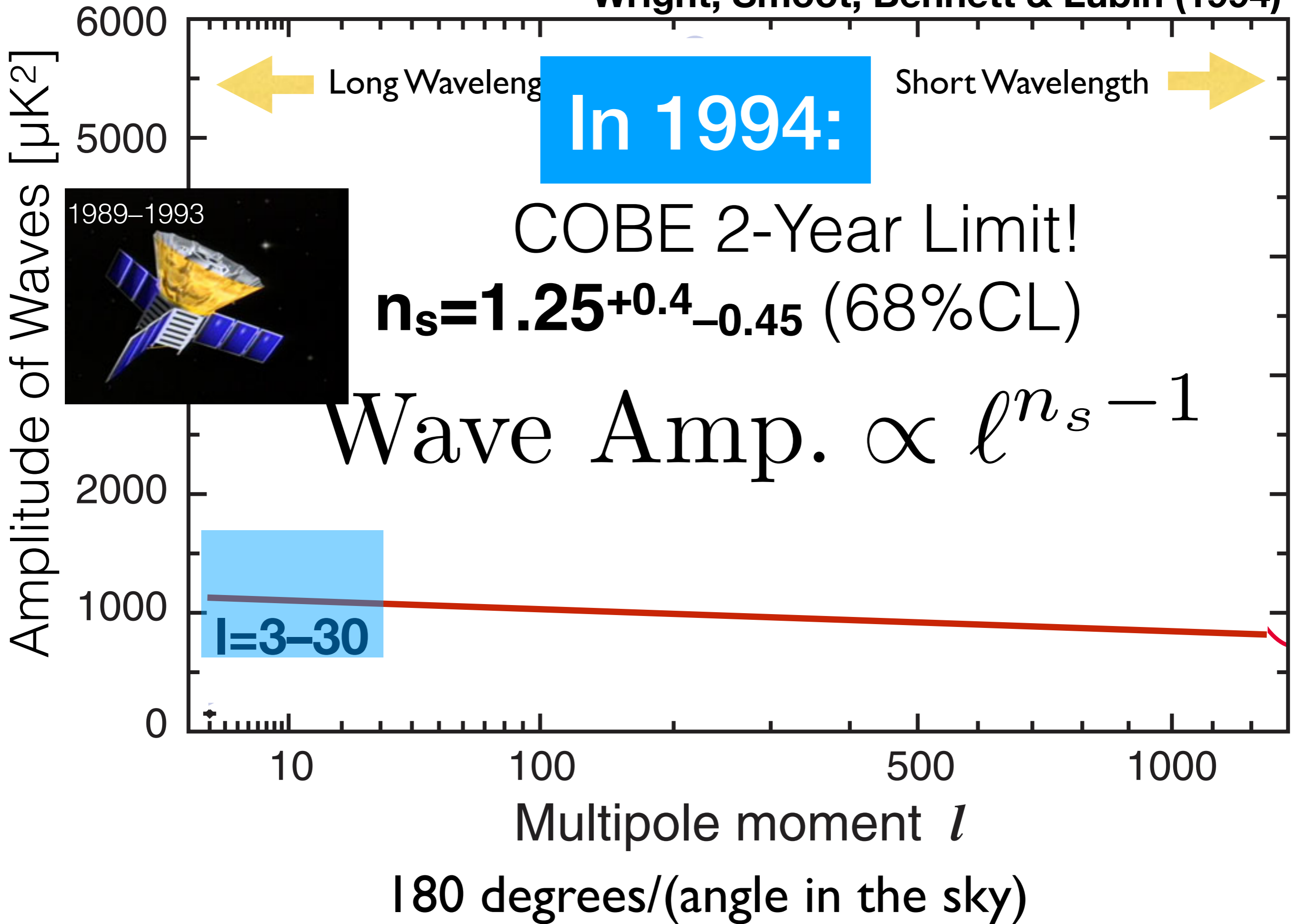


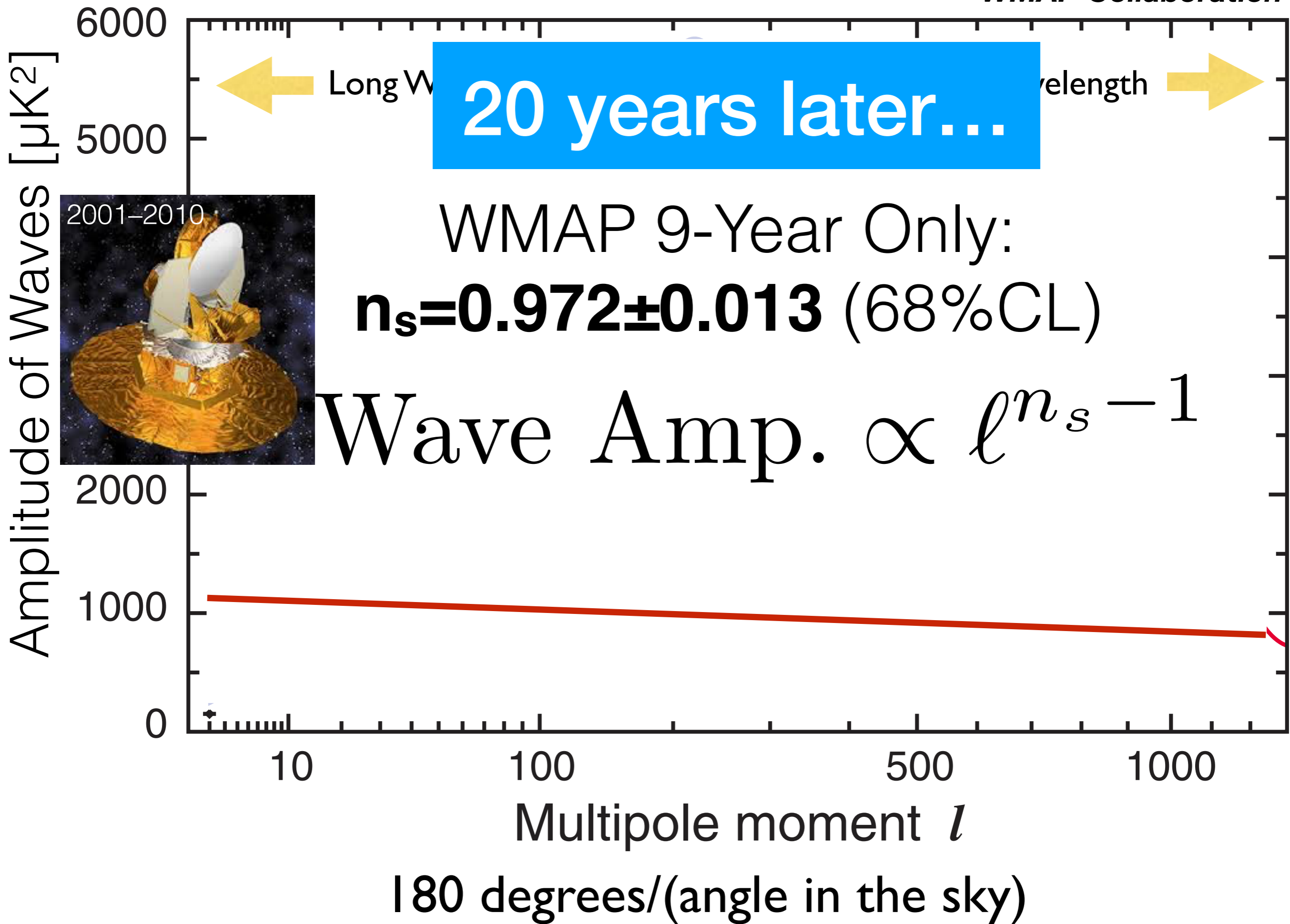












Angular scale

WMAP Collaboration

90°

2°

0.5°

0.2°

0.1°

Amplitude of ΔC_{ℓ}^2

2001–2010

South Pole Telescope
[10-m in South Pole]

$n_s = 0.965 \pm 0.010$

Atacama Cosmology Telescope
[6-m in Chile]

100

10

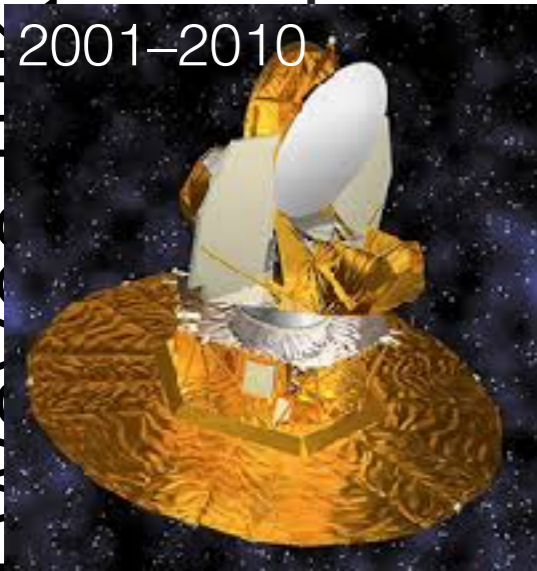
100

500

1000

2000

Multipole moment l



Angular scale

WMAP Collaboration

90°

2°

0.5°

0.2°

0.1°

Amplitude of ΔC_{ℓ}^2

2001–2010

South Pole Telescope
[10-m in South Pole]

$n_s = 0.961 \pm 0.008$

~5 σ discovery of $n_s < 1$ from the
CMB data combined with the
distribution of galaxies

Atacama Cosmology Telescope
[6-m in Chile]

100

10

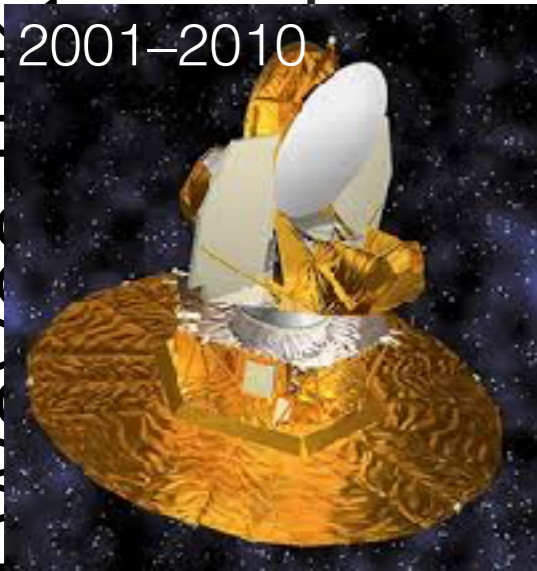
100

500

1000

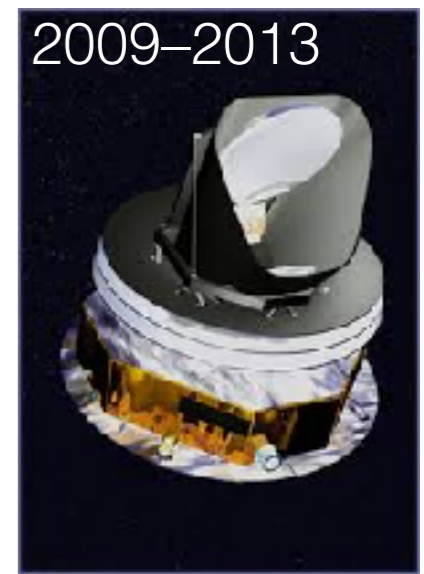
2000

Multipole moment l



Residual Amplitude of Waves [μK^2]

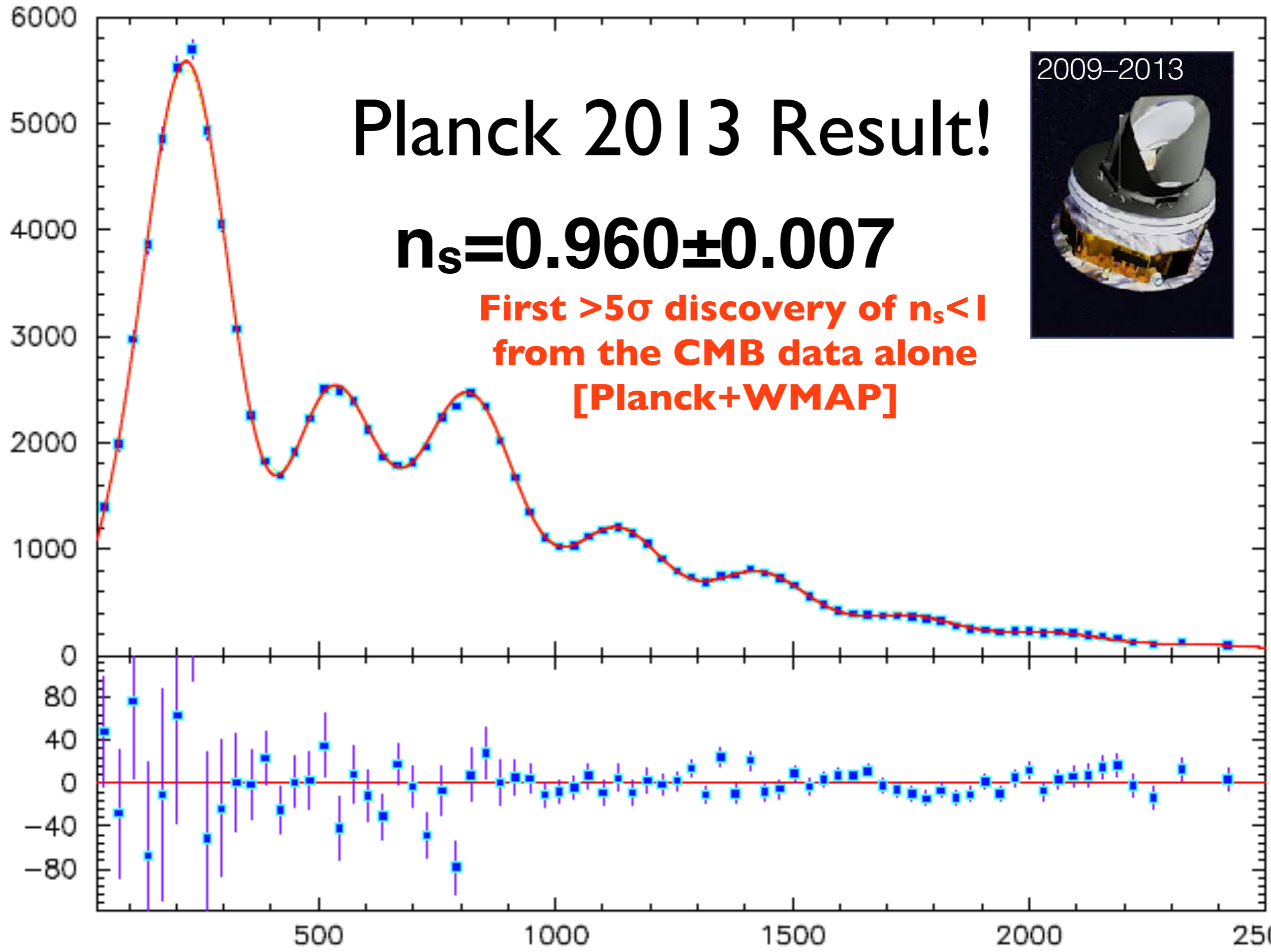
2009–2013



Planck 2013 Result!

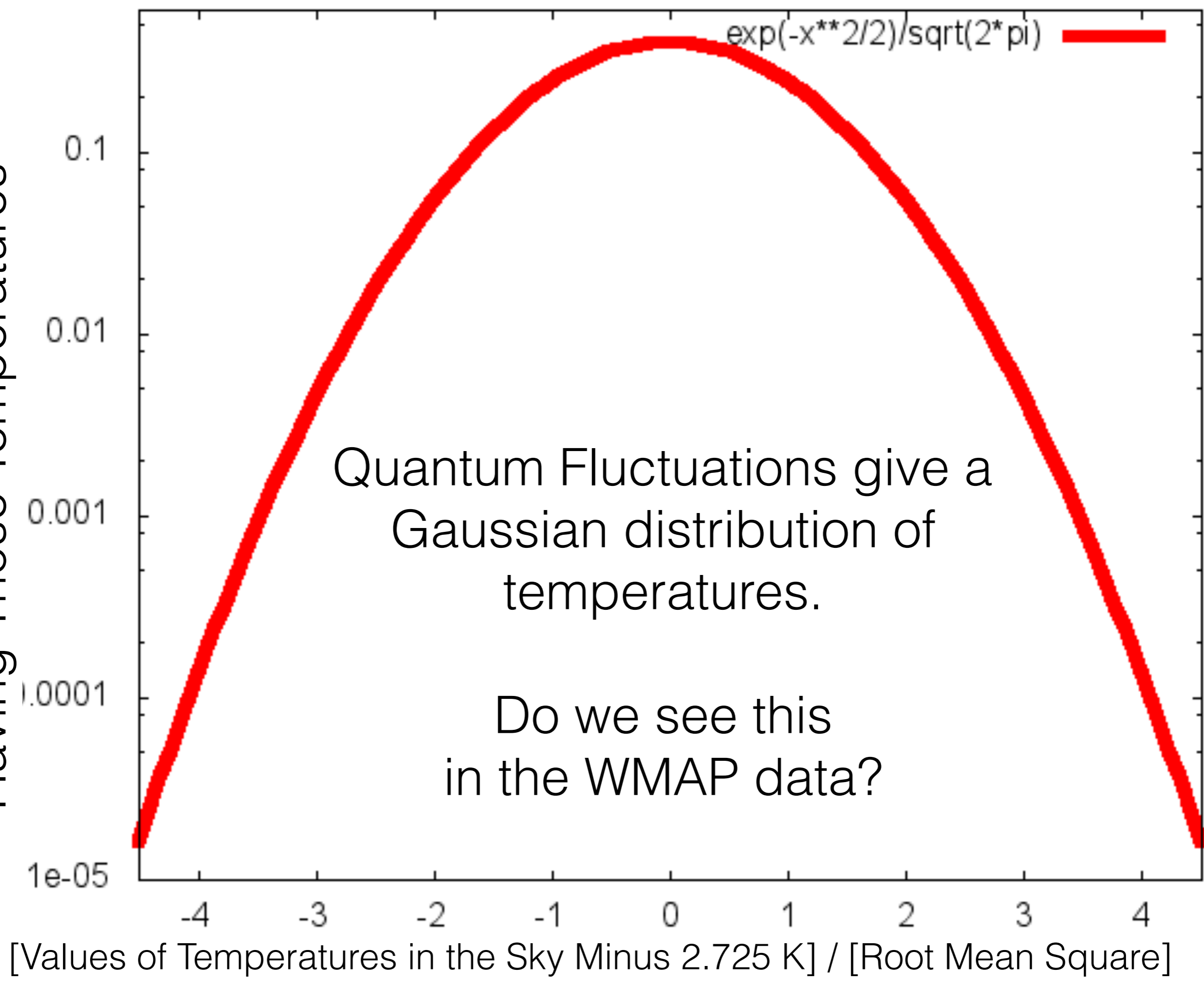
$$n_s = 0.960 \pm 0.007$$

First $>5\sigma$ discovery of $n_s < 1$
from the CMB data alone
[Planck+WMAP]



l 80 degrees/(angle in the sky)

Fraction of the Number of Pixels
Having Those Temperatures



Fraction of the Number of Pixels
Having Those Temperatures

WMAP Collaboration

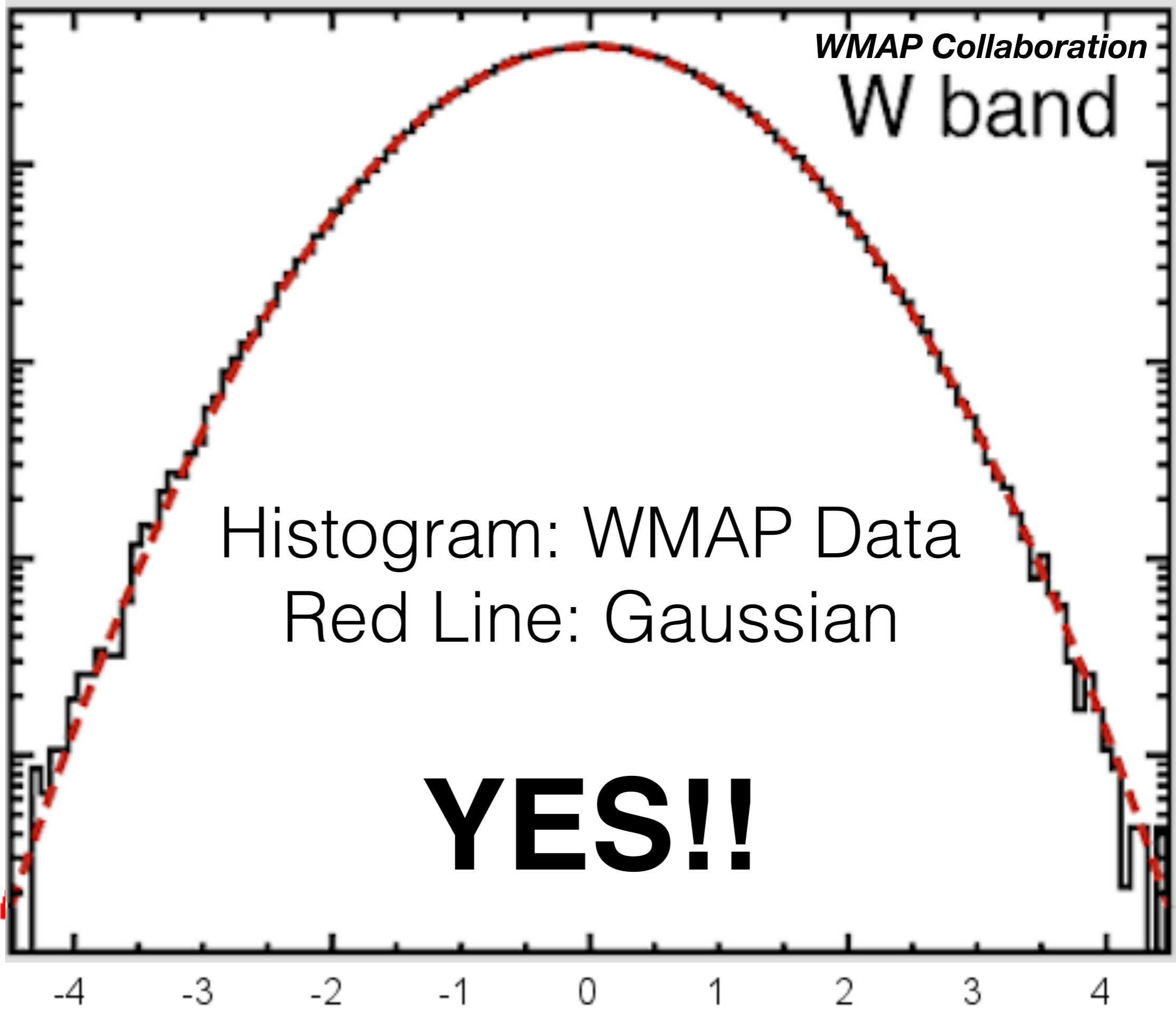
W band

0.1
0.01
0.001
0.0001
1e-05

Histogram: WMAP Data
Red Line: Gaussian

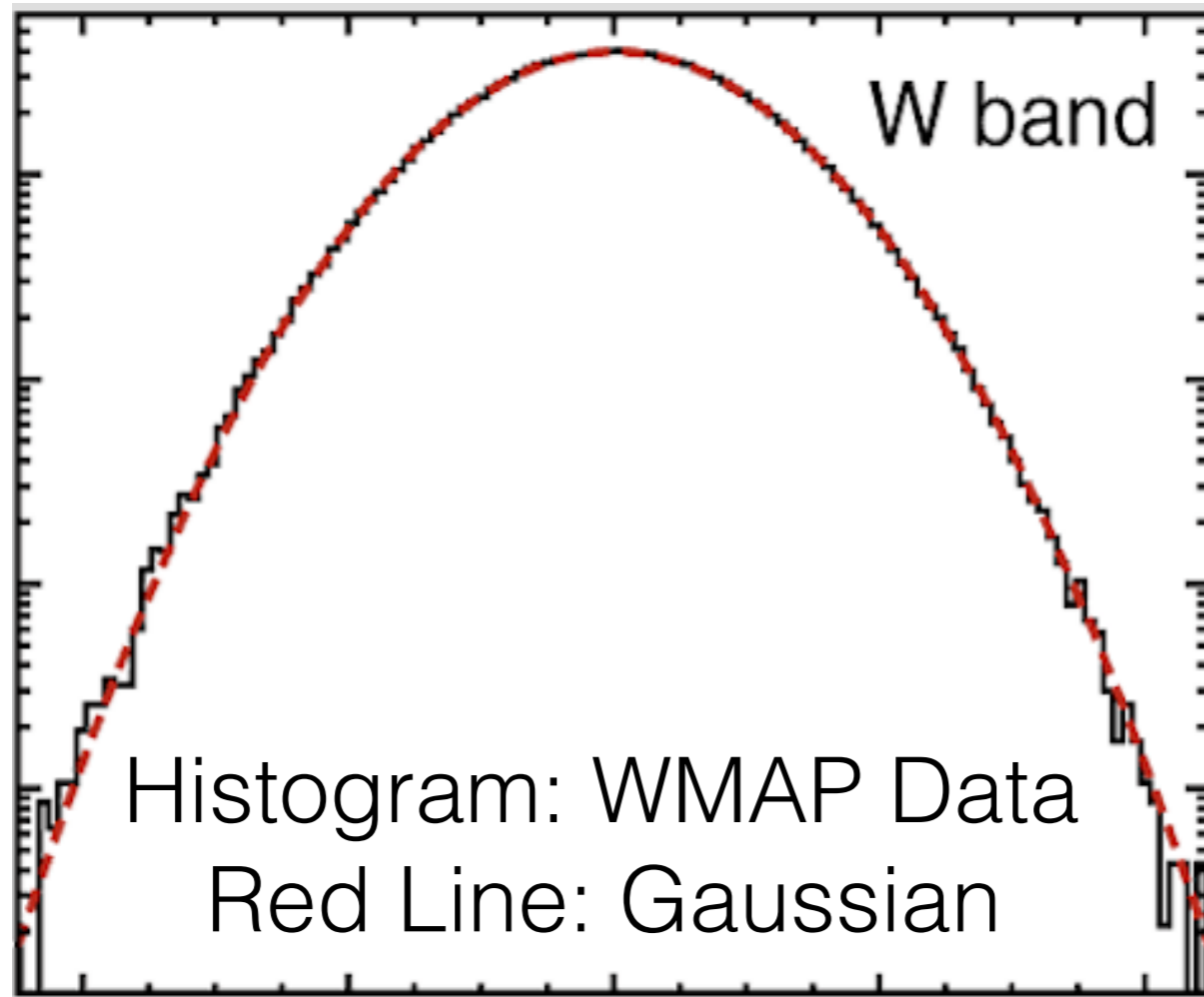
YES!!

[Values of Temperatures in the Sky Minus 2.725 K] / [Root Mean Square]



Testing Gaussianity

Fraction of the Number of Pixels
Having Those Temperatures



[Values of Temperatures in the Sky Minus
2.725 K]/ [Root Mean Square]

- Since a Gauss distribution is symmetric, it must yield a vanishing **3-point function**

$$\langle \delta T^3 \rangle \equiv \int_{-\infty}^{\infty} d\delta T P(\delta T) \delta T^3$$

- More specifically, we measure this by averaging the product of temperatures at three different locations in the sky

$$\langle \delta T(\hat{n}_1) \delta T(\hat{n}_2) \delta T(\hat{n}_3) \rangle$$

Lack of non-Gaussianity

- The WMAP data show that the distribution of temperature fluctuations of CMB is very precisely Gaussian
 - with an upper bound on a deviation of **0.2%** (95%CL)

$$\zeta(\mathbf{x}) = \zeta_{\text{gaus}}(\mathbf{x}) + \frac{3}{5} f_{\text{NL}} \zeta_{\text{gaus}}^2(\mathbf{x}) \text{ with } f_{\text{NL}} = 37 \pm 20 \text{ (68\% CL)}$$

WMAP 9-year Result

- The Planck data improved the upper bound by an order of magnitude: deviation is **<0.03%** (95%CL)

$$f_{\text{NL}} = 0.8 \pm 5.0 \text{ (68\% CL)}$$

Planck 2015 Result

So, have we found inflation?

- Single-field slow-roll inflation looks remarkably good:
 - **Super-horizon fluctuation**
 - **Adiabaticity**
 - **Gaussianity**
 - **$n_s < 1$**
- What more do we want? **Gravitational waves**. Why?
 - Because the “*extraordinary claim requires extraordinary evidence*”

Gravitational waves as the quantum vacuum fluctuation in spacetime

- Quantising the gravitational waves in de Sitter space in **vacuum**

$$\square h_{ij} = 0$$

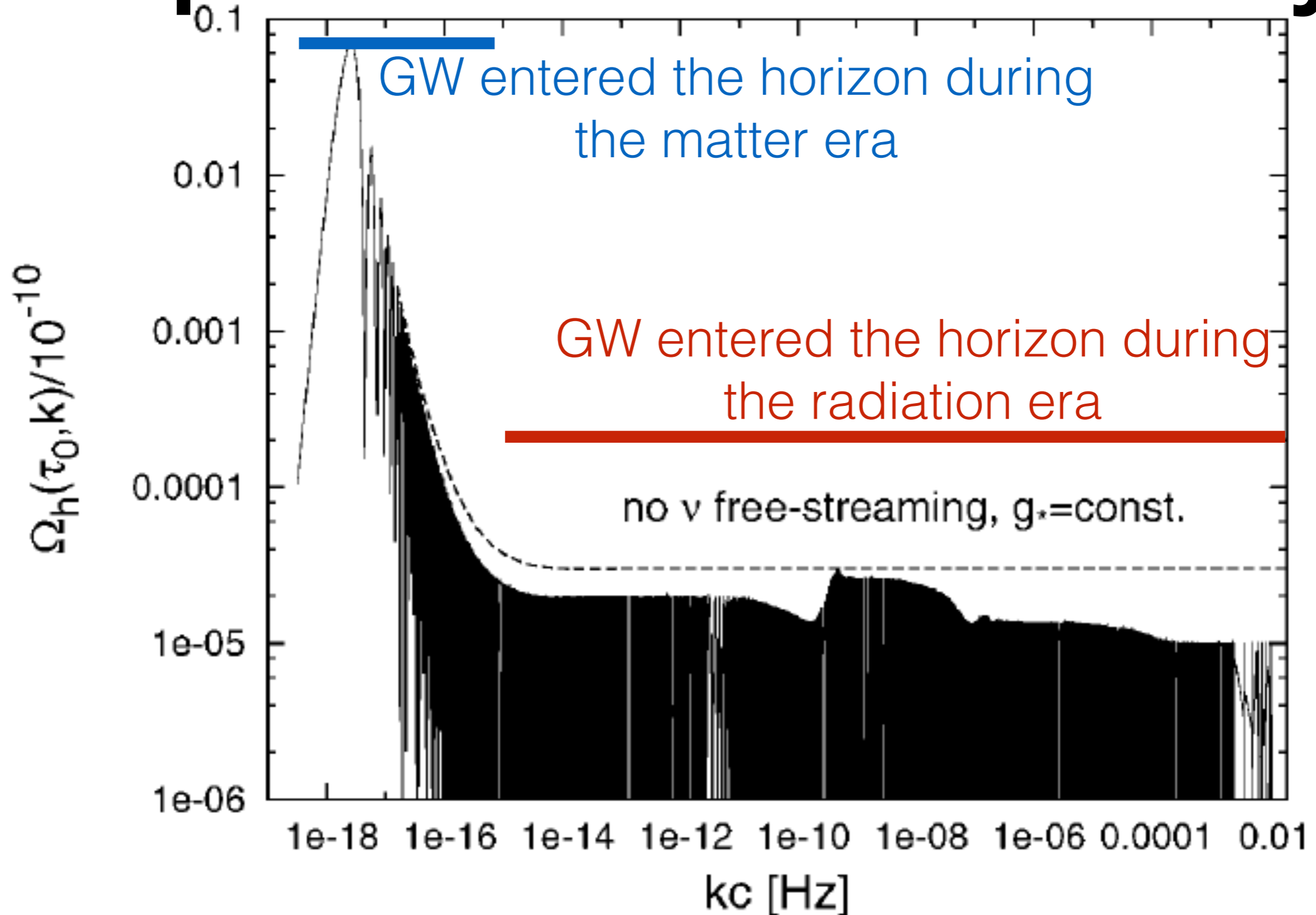
gives

$$k^3 \langle h_{ij}(\mathbf{k}) h^{ij*}(\mathbf{k}') \rangle$$

$$= (2\pi)^3 \delta_D(\mathbf{k} - \mathbf{k}') \frac{8}{M_{\text{pl}}^2} \left(\frac{H}{2\pi} \right)^2$$

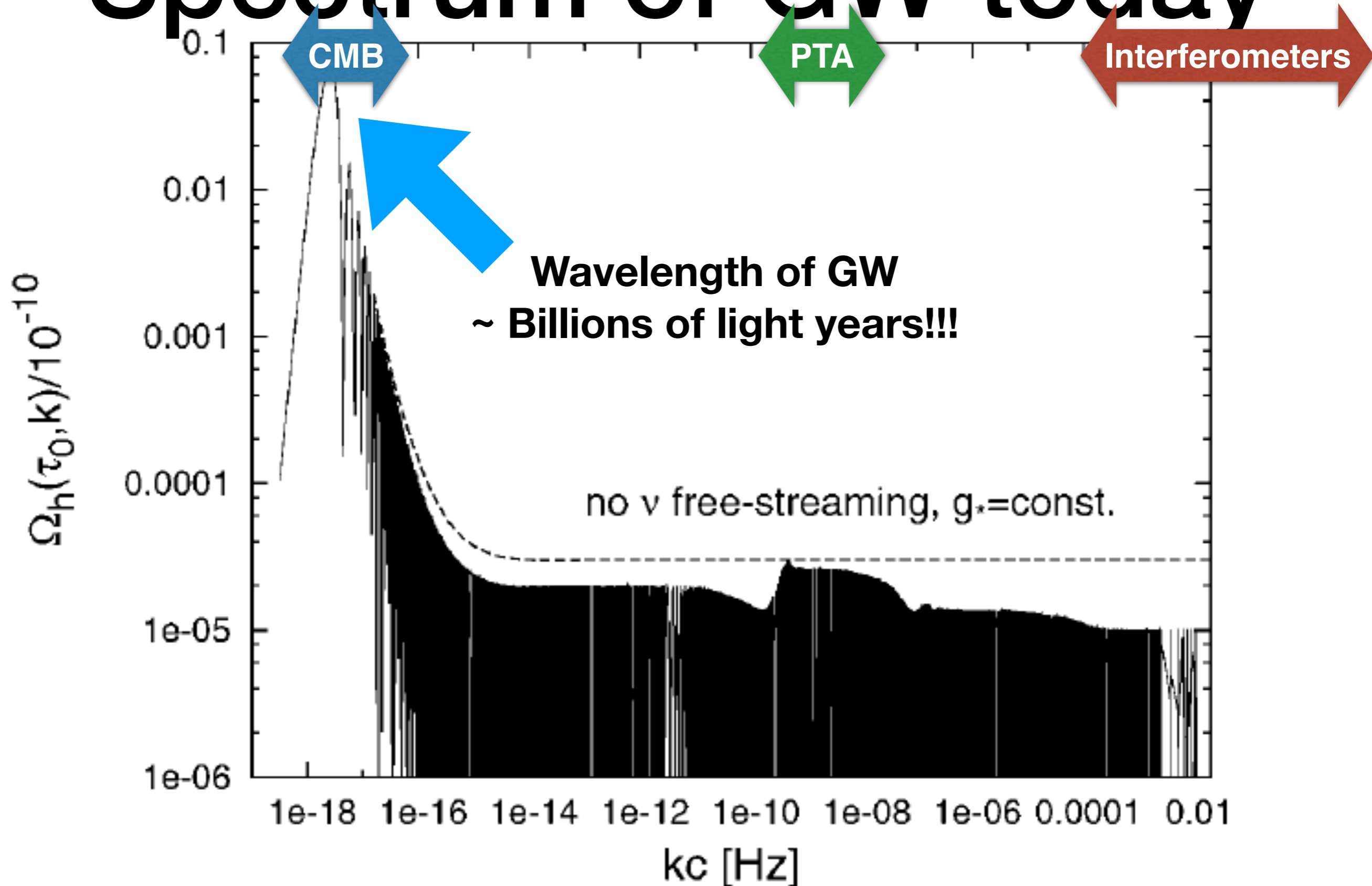
scale-invariant spectrum

Theoretical energy density Spectrum of GW today



Theoretical energy density

Spectrum of GW today



Measuring GW

- GW changes distances between two points

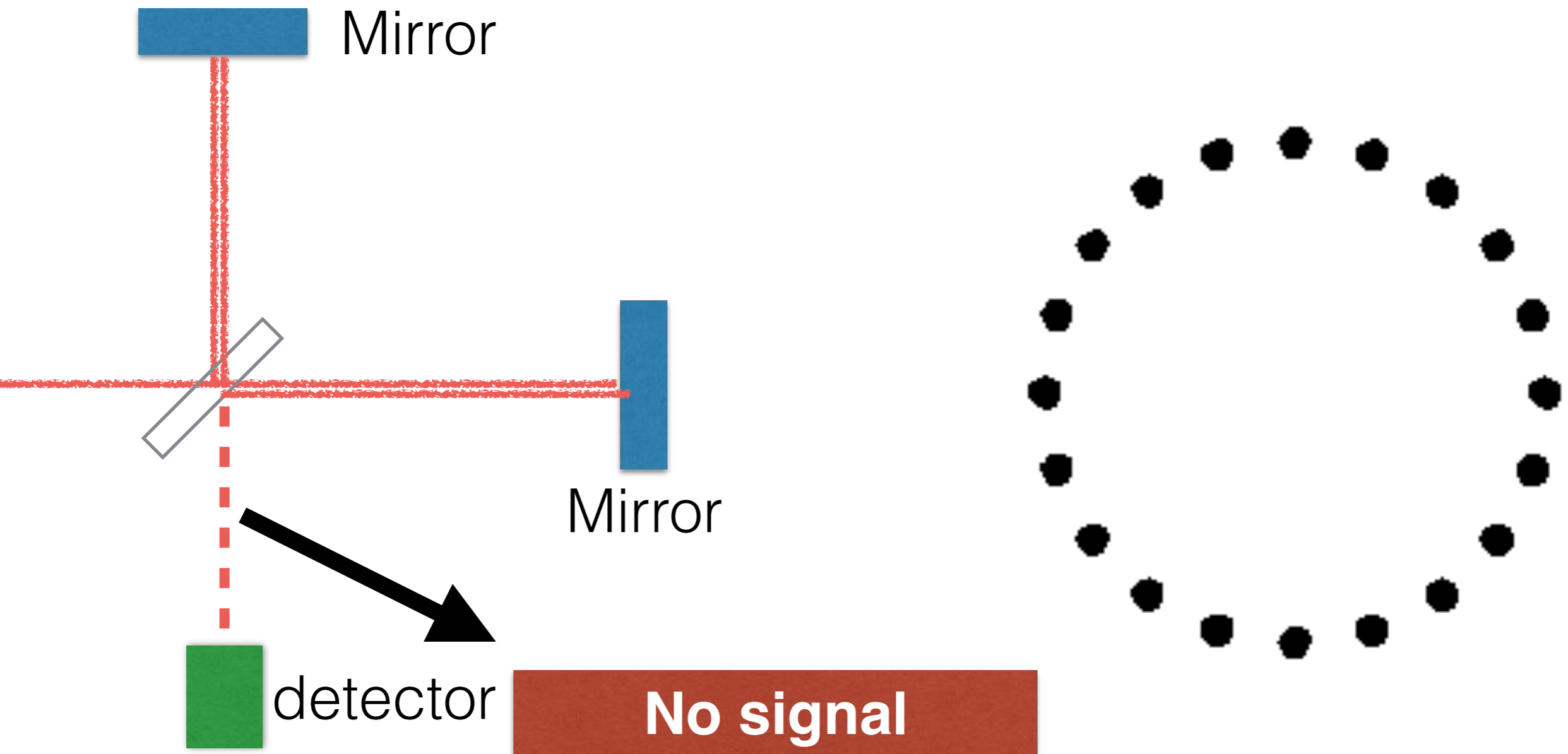
$$d\ell^2 = d\mathbf{x}^2 = \sum_{ij} \delta_{ij} dx^i dx^j$$



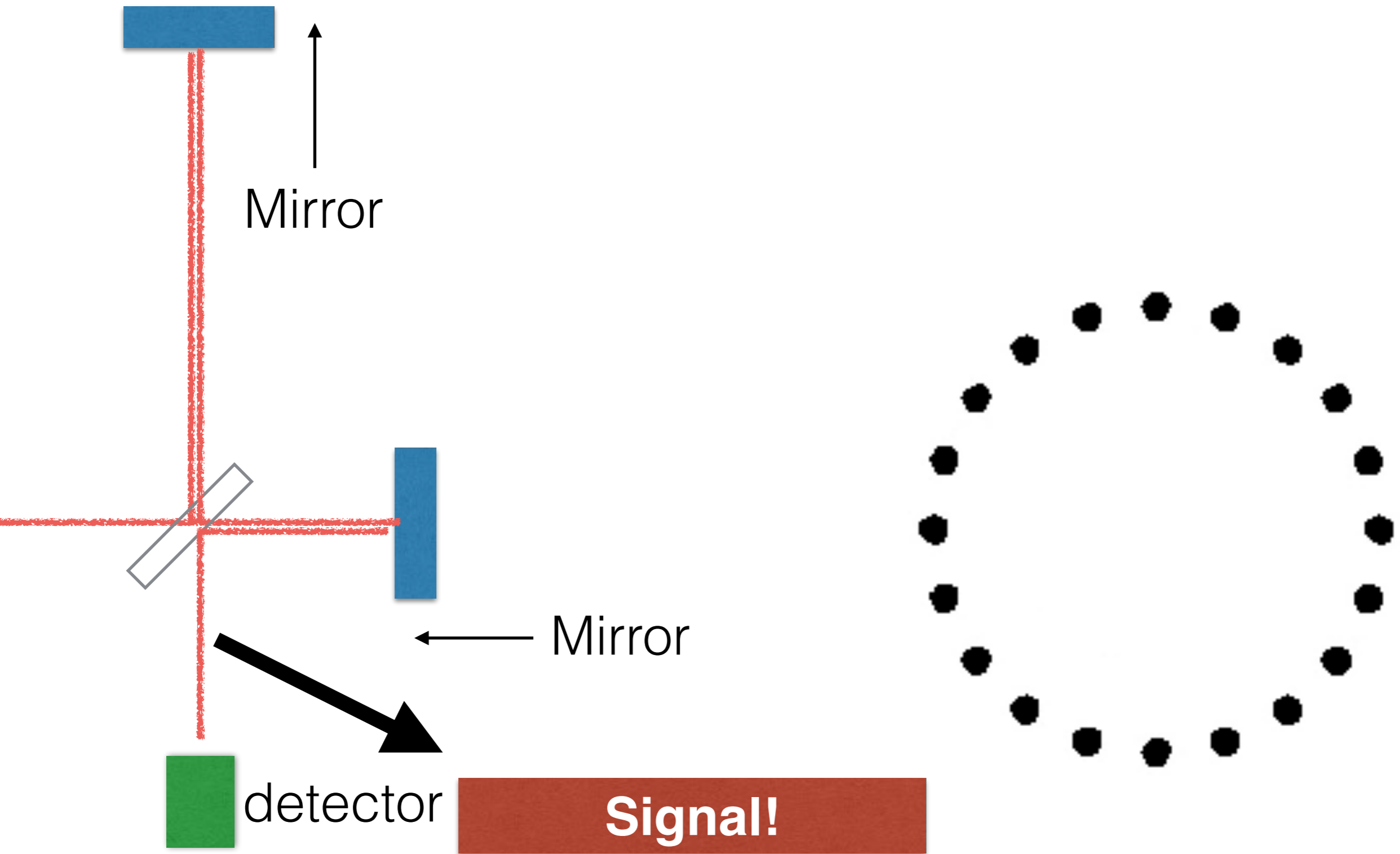
$$d\ell^2 = \sum_{ij} (\delta_{ij} + \underline{h_{ij}}) dx^i dx^j$$



Laser Interferometer



Laser Interferometer



LIGO detected GW from a binary blackholes, with the wavelength of thousands of kilometres

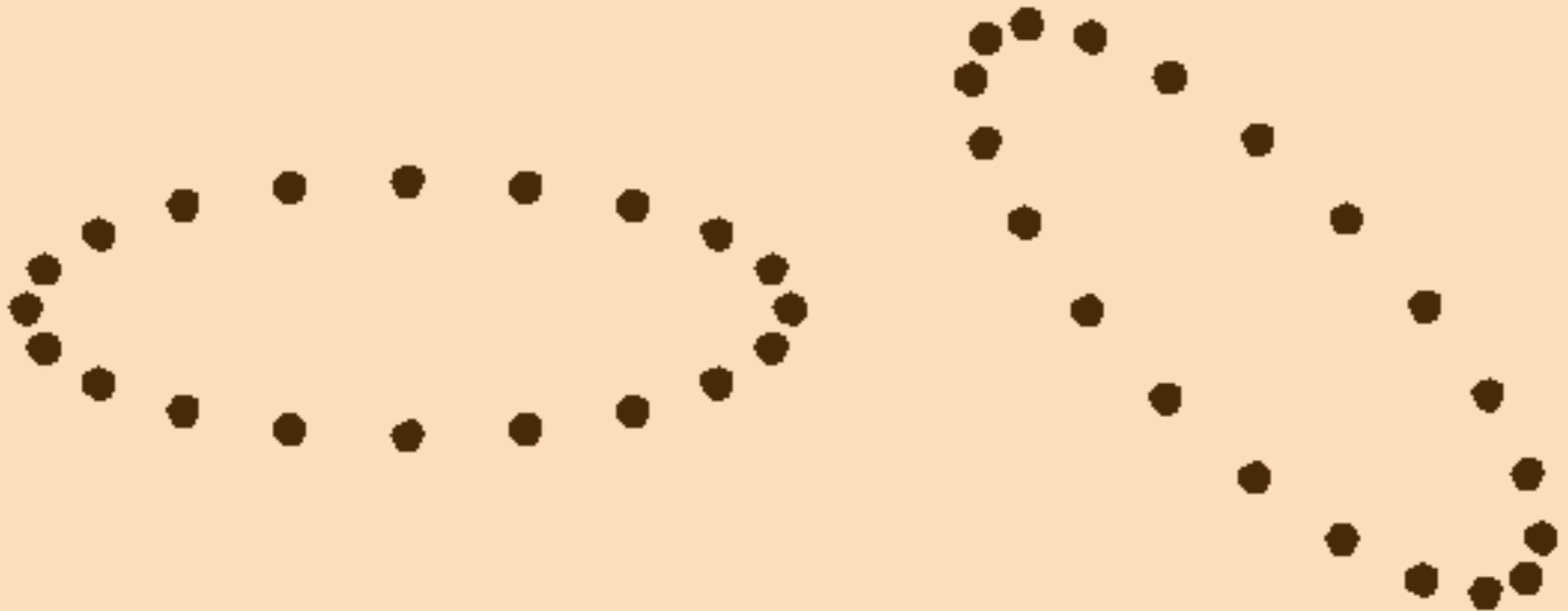
But, the primordial GW affecting the CMB has a wavelength of **billions of light-years!!** How do we find it?

Detecting GW by CMB

Isotropic electro-magnetic fields

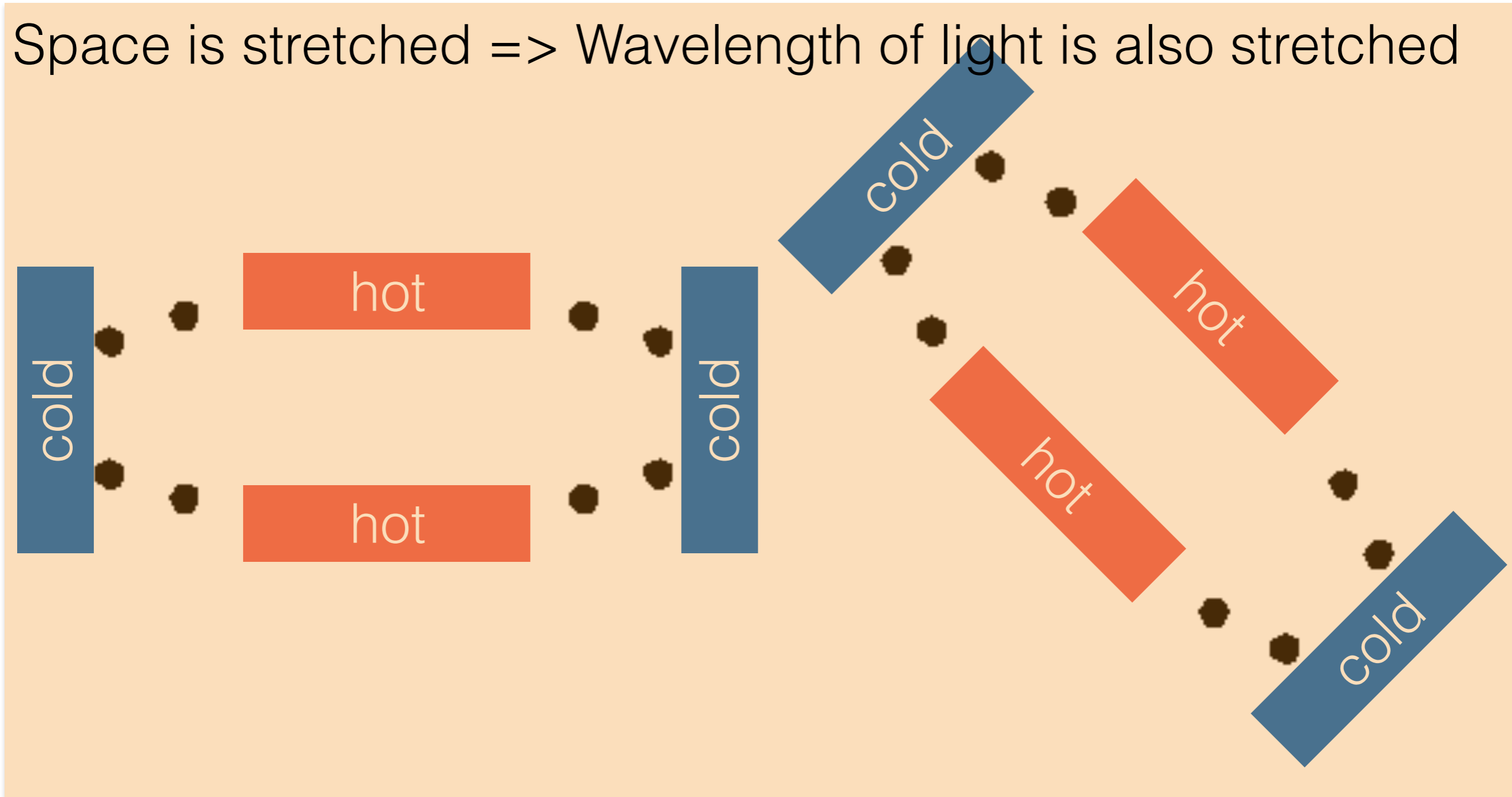
Detecting GW by CMB

GW propagating in isotropic electro-magnetic fields



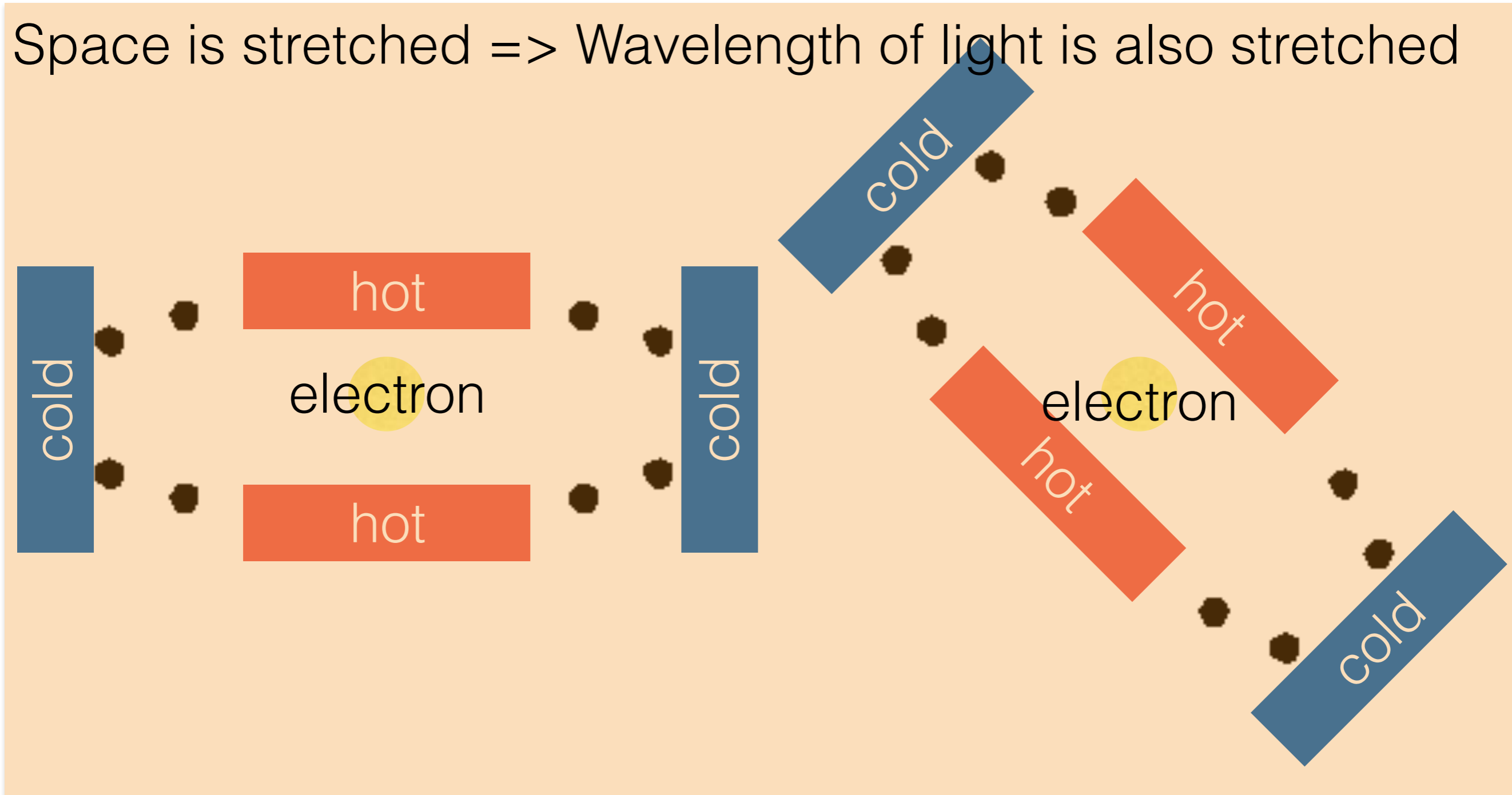
Detecting GW by CMB

Space is stretched => Wavelength of light is also stretched



Detecting GW by CMB Polarisation

Space is stretched => Wavelength of light is also stretched



Detecting GW by CMB Polarisation

Space is stretched => Wavelength of light is also stretched

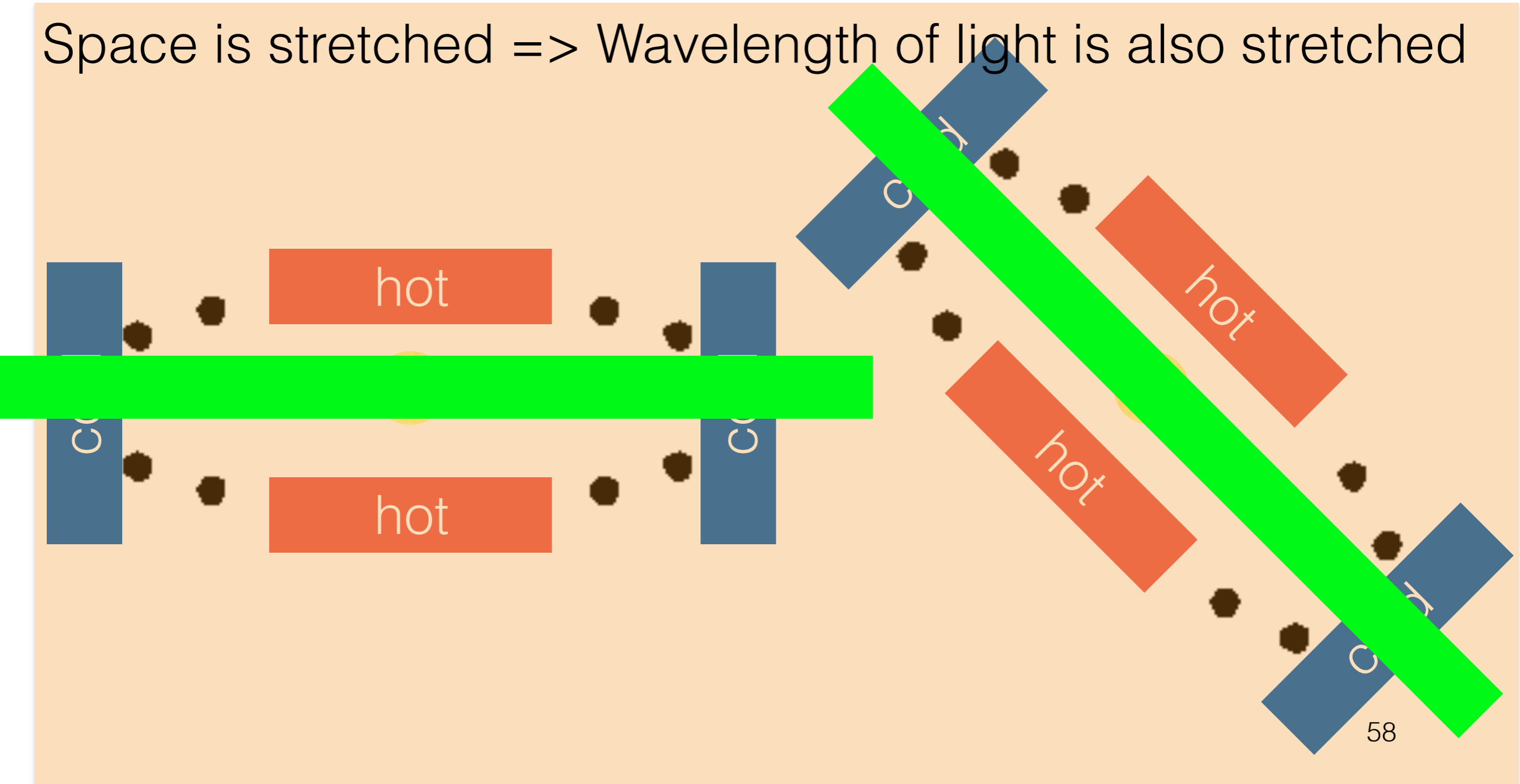


Photo Credit: TALEX



horizontally polarised

Photo Credit: TALEX

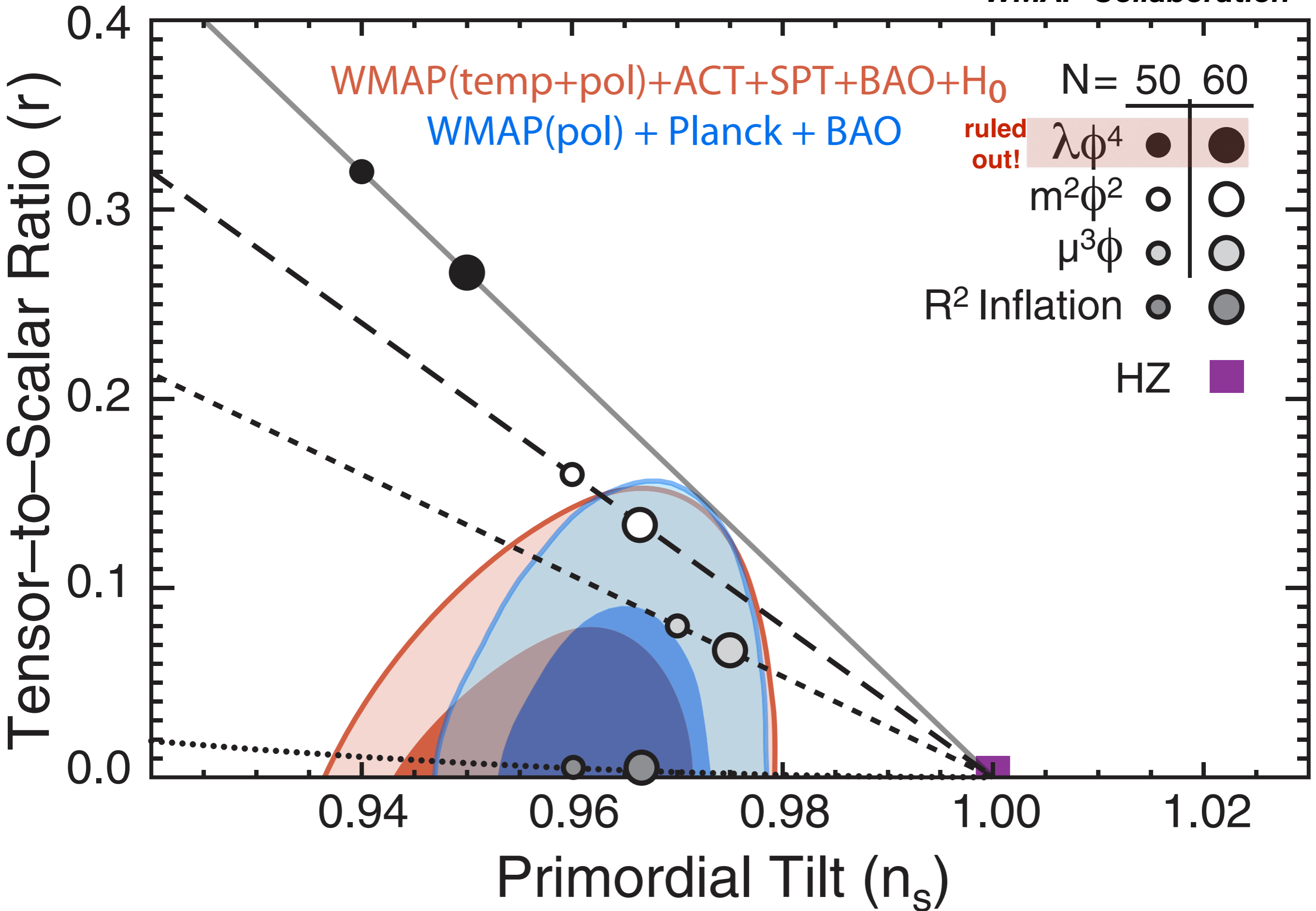


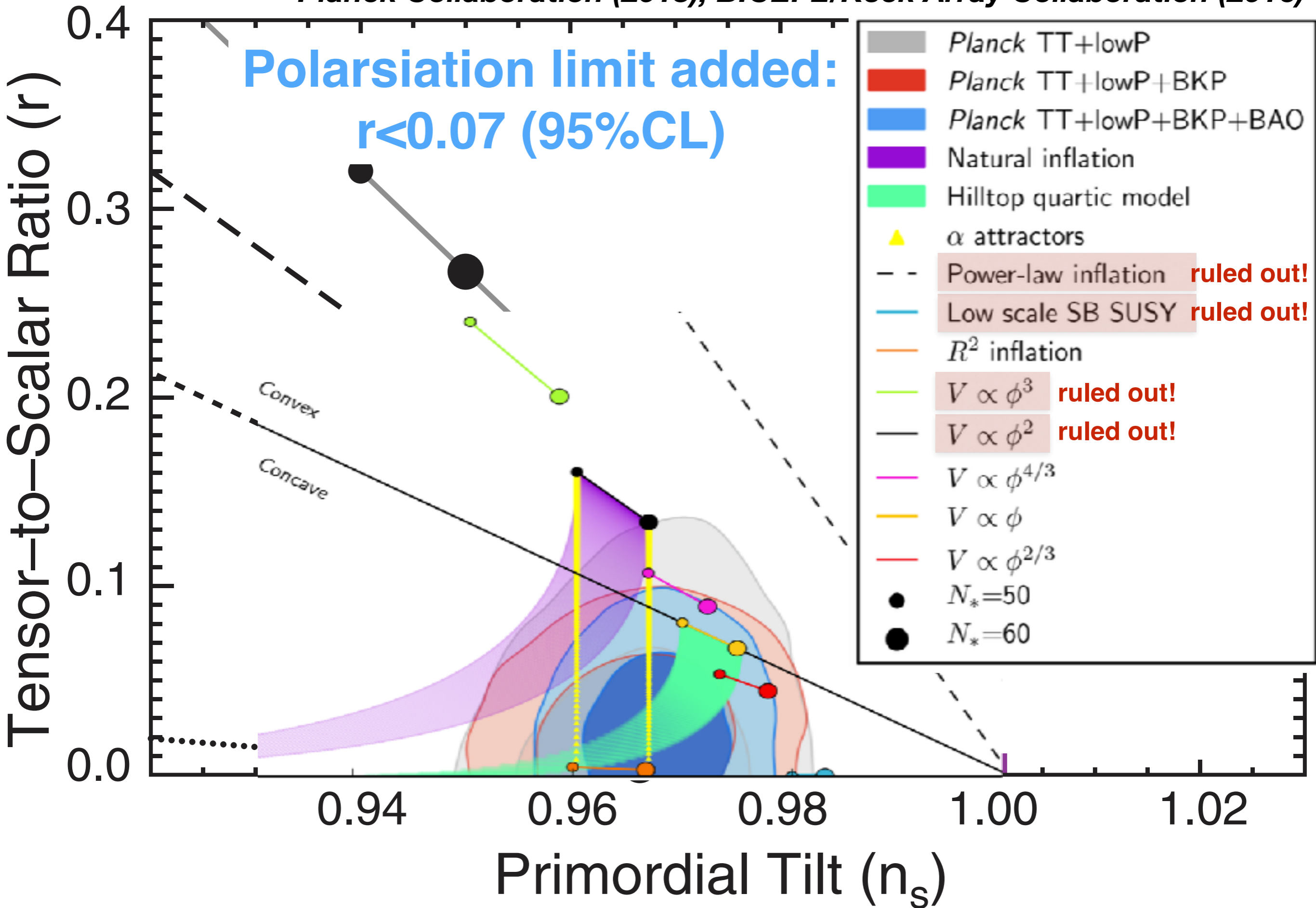
Tensor-to-scalar Ratio

$$r \equiv \frac{\langle h_{ij} h^{ij} \rangle}{\langle \zeta^2 \rangle}$$

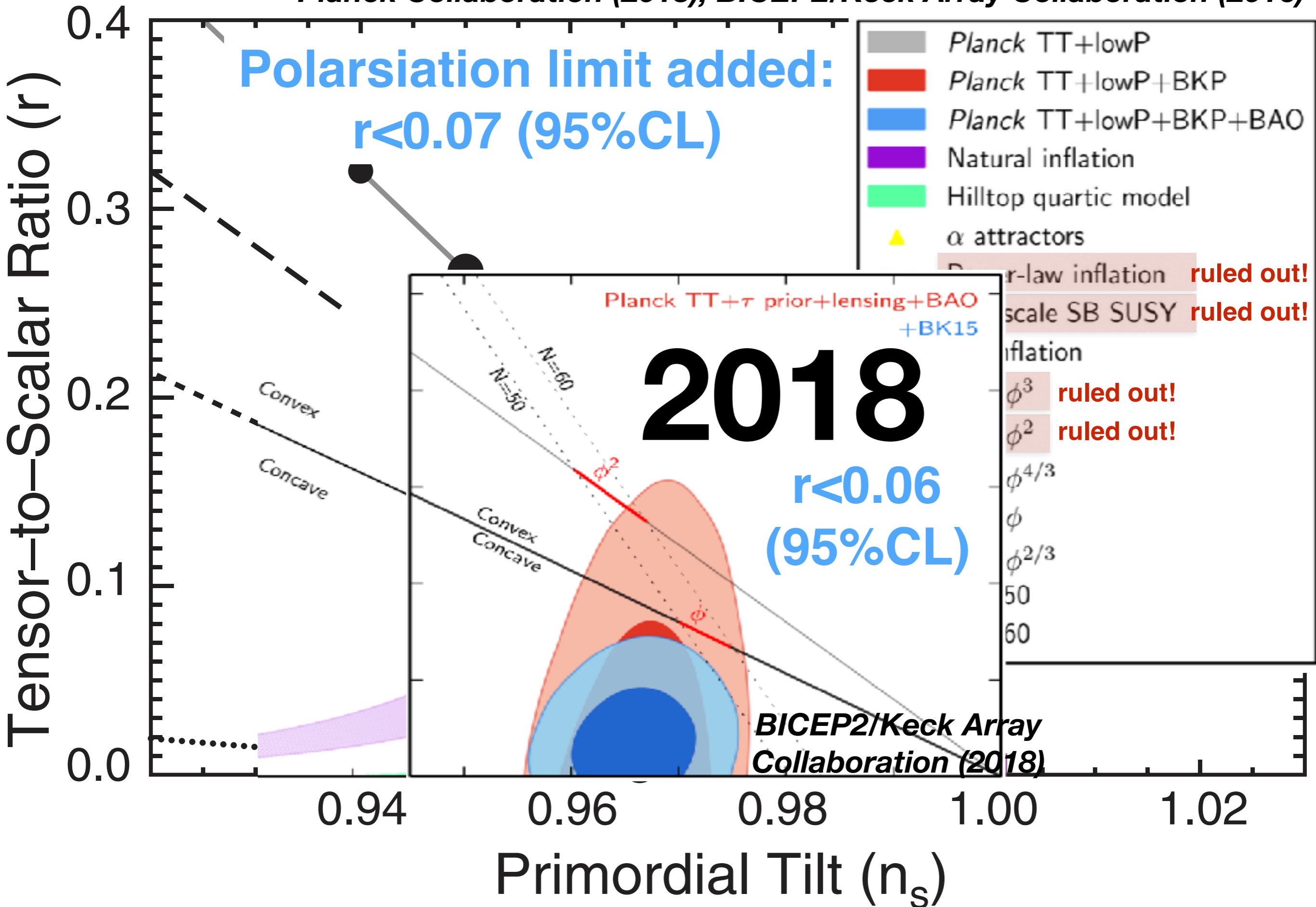
- We really want to find this! The current upper bound is **$r < 0.06$** (95%CL)

BICEP2/Keck Array Collaboration (2018)





Planck Collaboration (2015); BICEP2/Keck Array Collaboration (2016)



JAXA



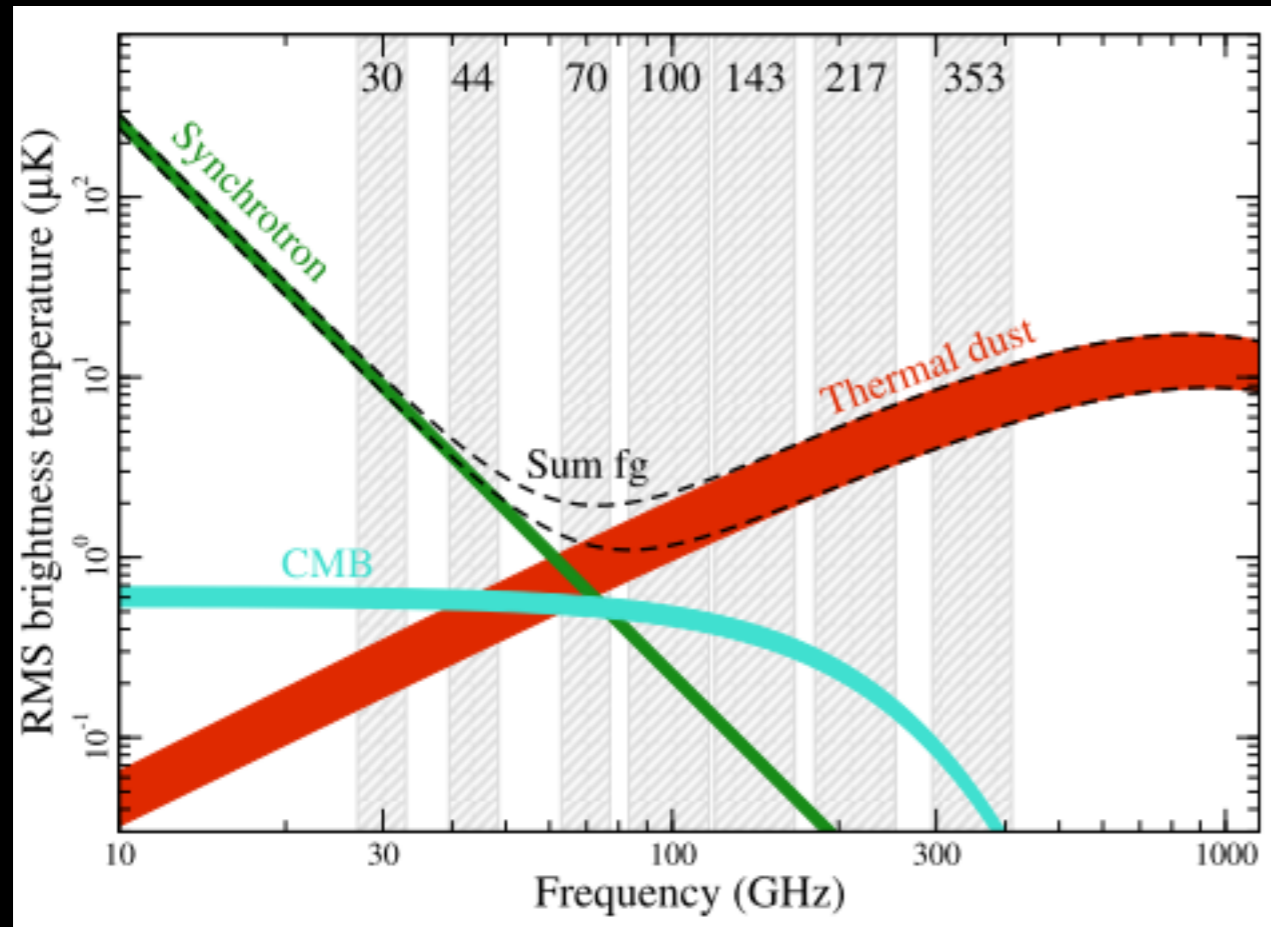
+ participations from
USA, Canada, Europe

LiteBIRD
2028–

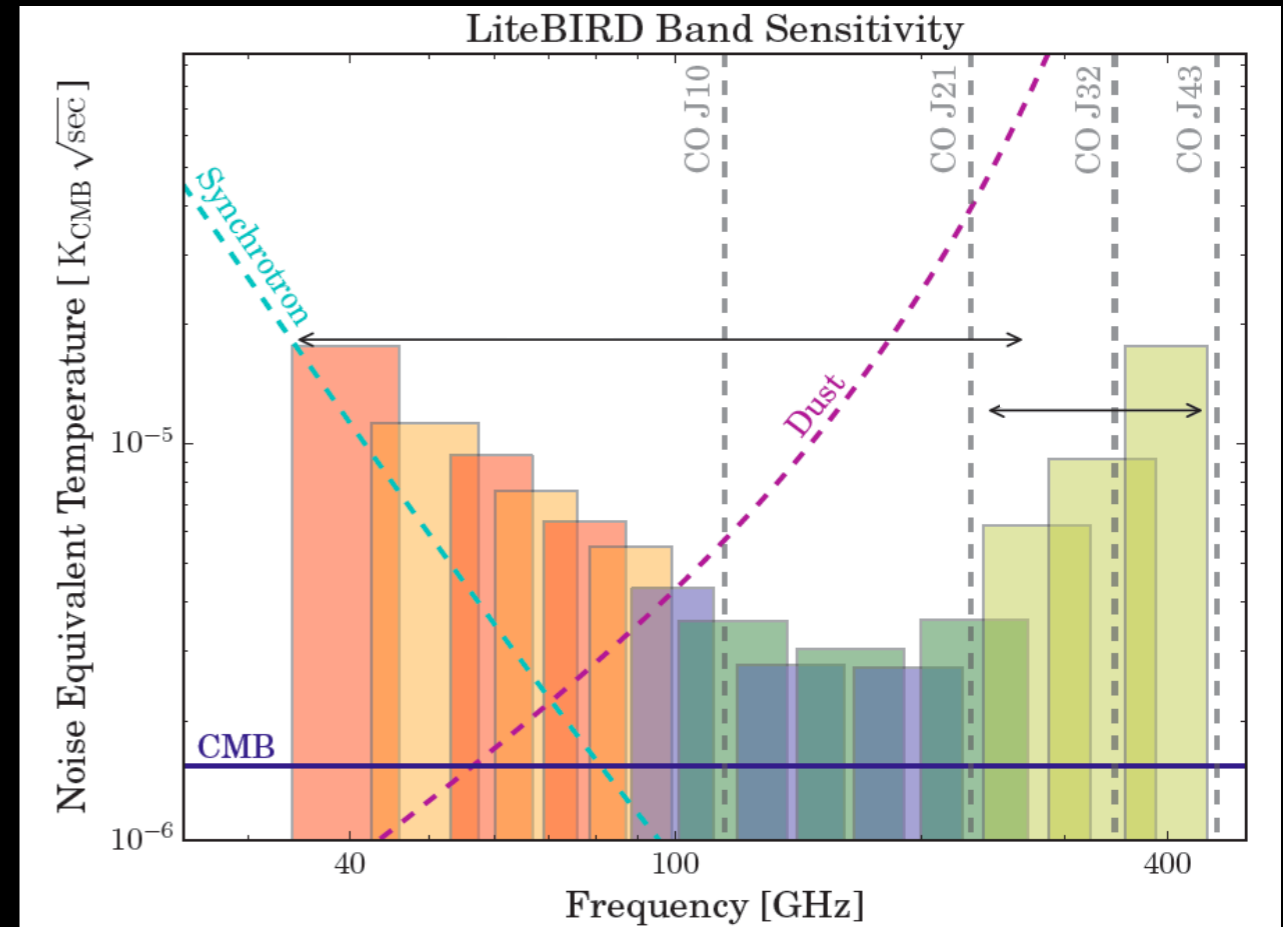
Selected!

Target: $\delta r < 0.001$ (68%CL)

Foreground Removal



Polarized galactic emission (Planck X)

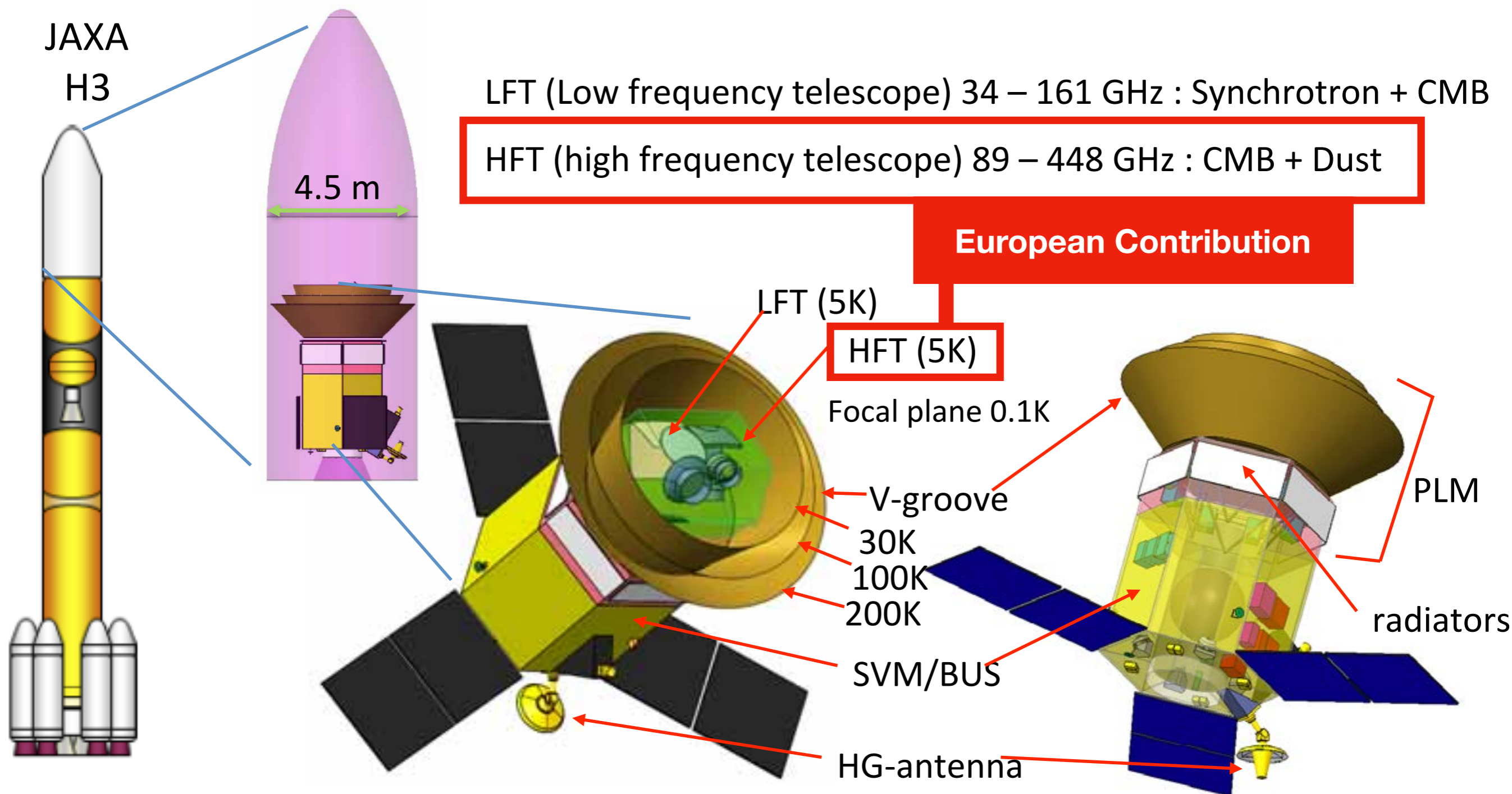
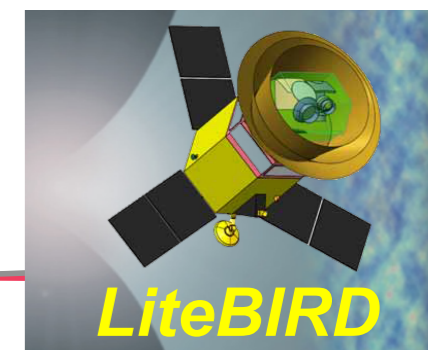


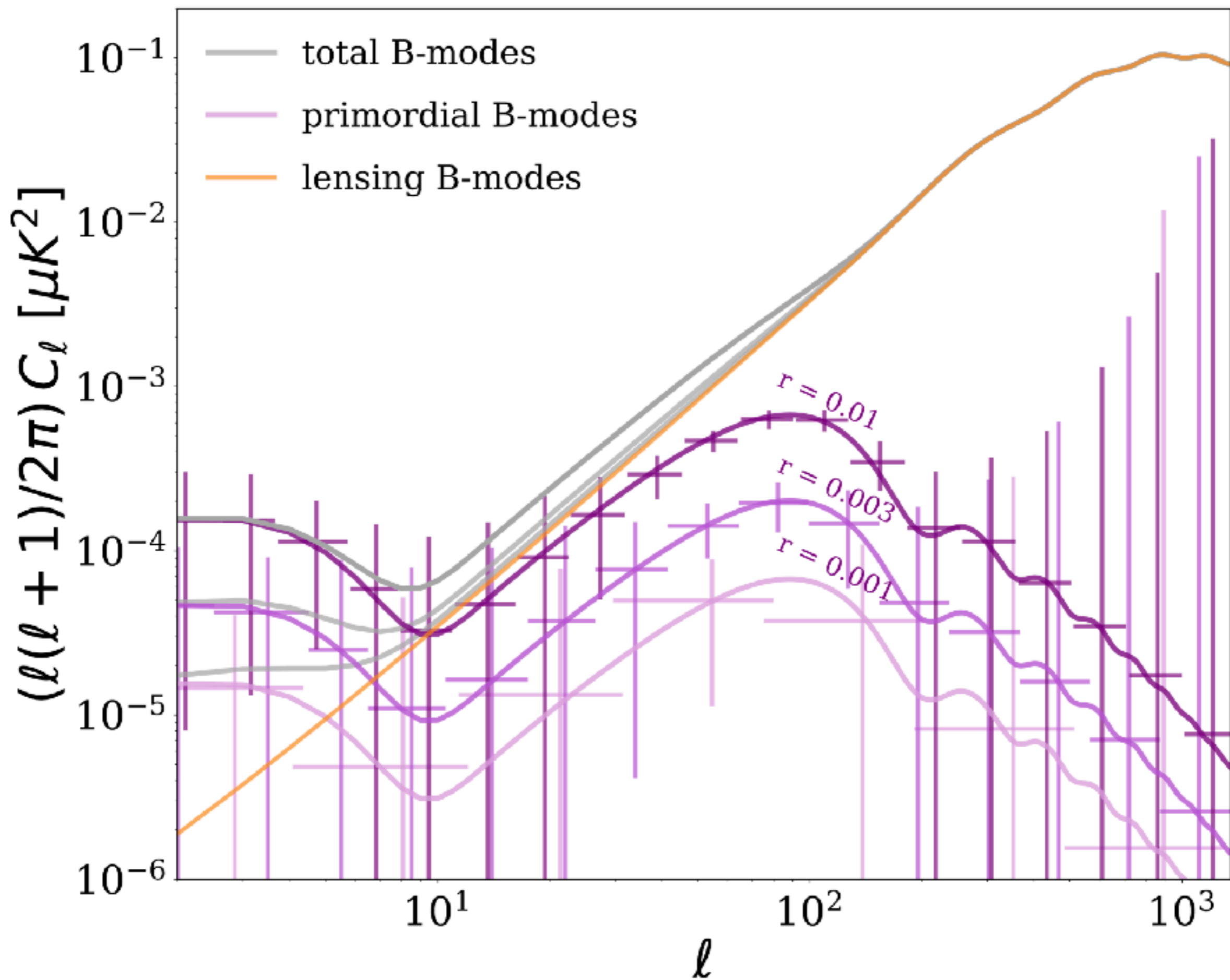
LiteBIRD: 15 frequency bands

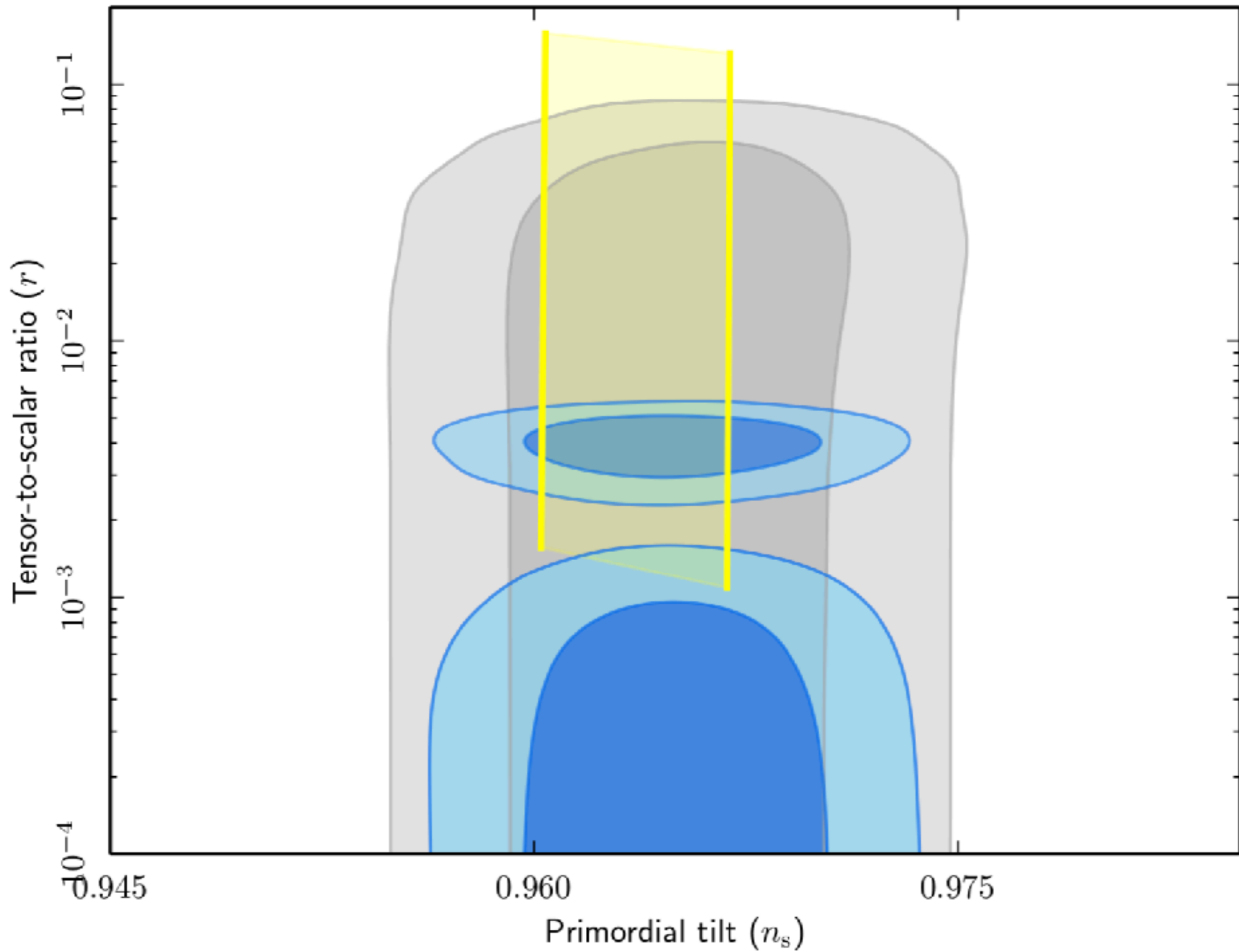
- Polarized foregrounds
 - Synchrotron radiation and thermal emission from inter-galactic dust
 - Characterize and remove foregrounds
- 15 frequency bands between 40 GHz - 400 GHz
 - Split between Low Frequency Telescope (LFT) and High Frequency Telescope (HFT)
 - LFT: 40 GHz – 235 GHz
 - HFT: 280 GHz – 400 GHz

Slide courtesy Toki Suzuki (Berkeley)

LiteBIRD Spacecraft







Summary

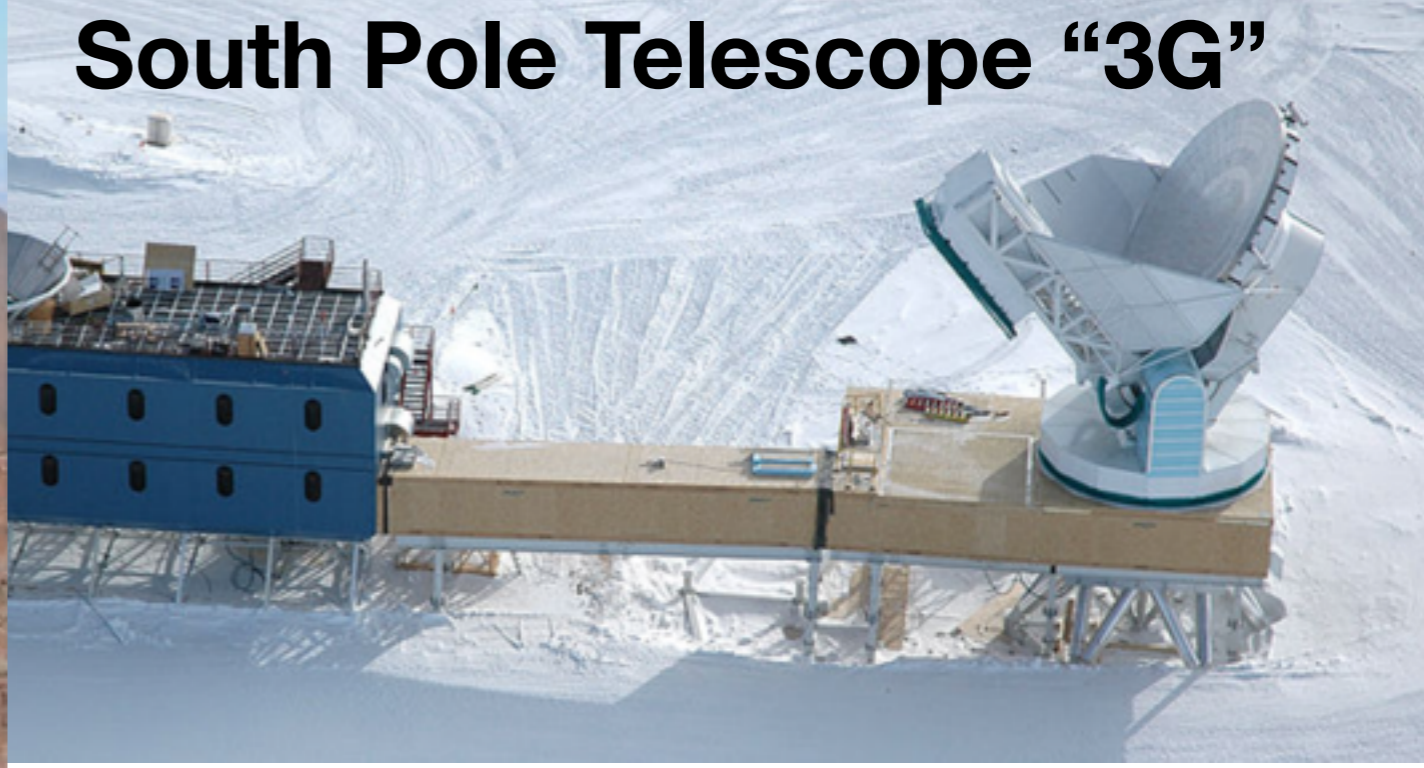
- Inflation looks pretty good: passed all the tests using the scalar (density) perturbation
- **Next frontier**: Using CMB polarisation to find GWs from inflation. **Critical test of the physics of inflation!**
- With *LiteBIRD* we plan to reach $r \sim 10^{-3}$, i.e., 100 times better than the current bound

Ground-based Experiments

Advanced Atacama Cosmology Telescope

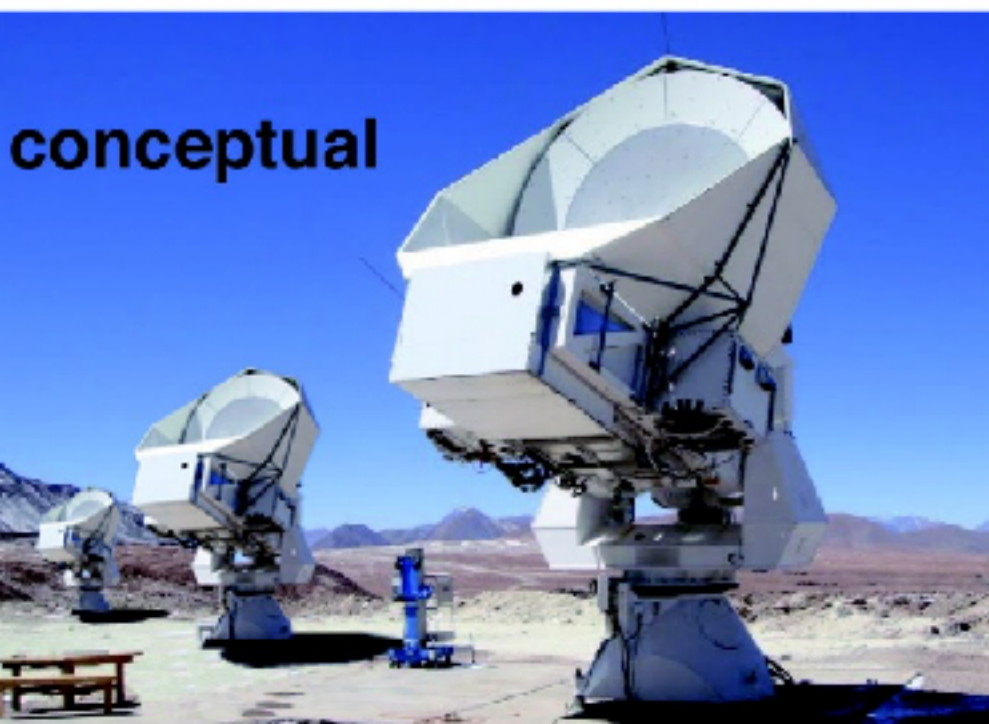


South Pole Telescope “3G”



What comes next?

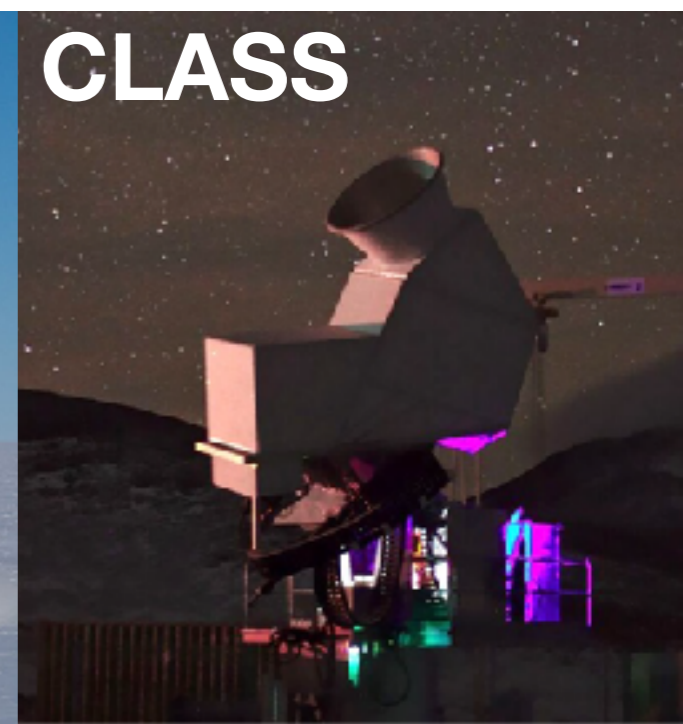
The Simons Array



BICEP/Keck Array



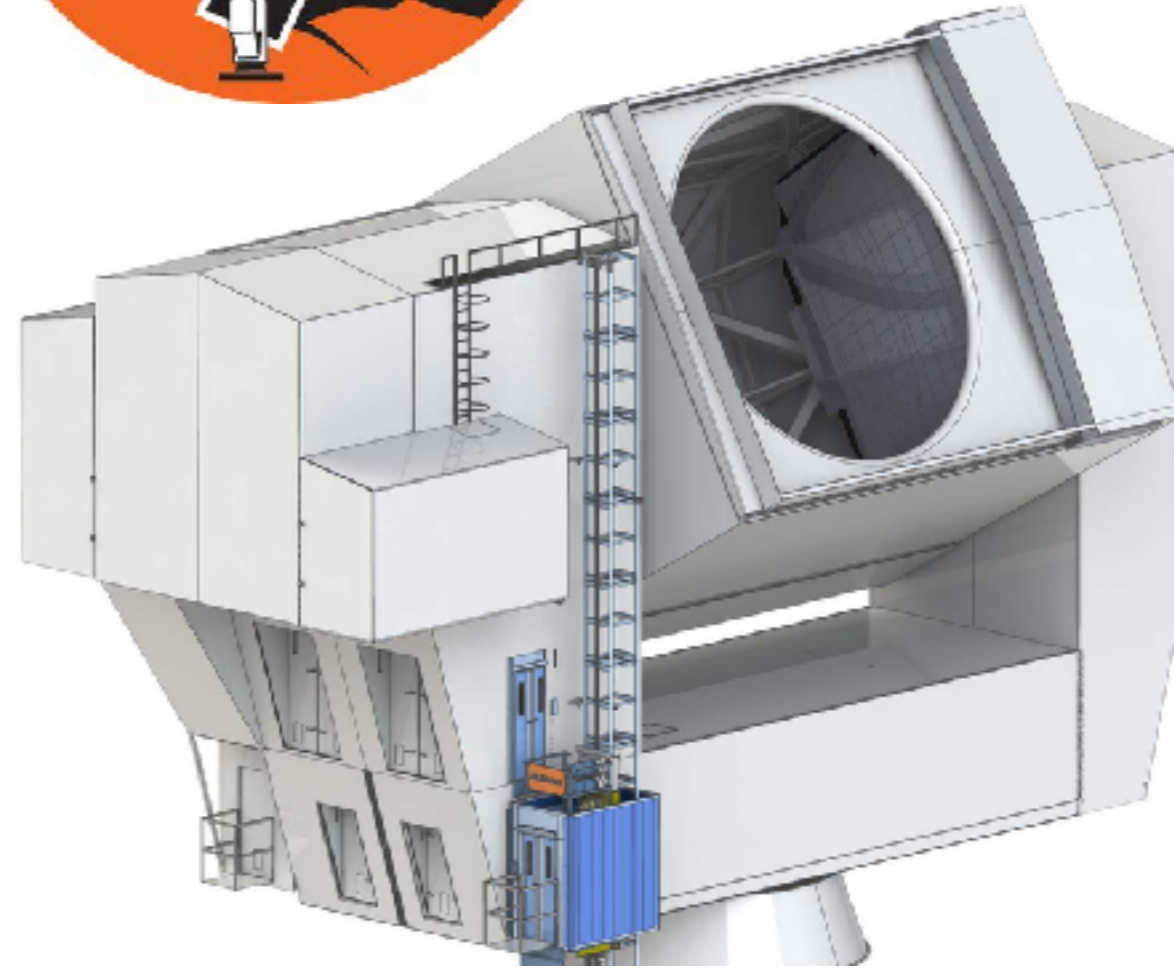
CLASS



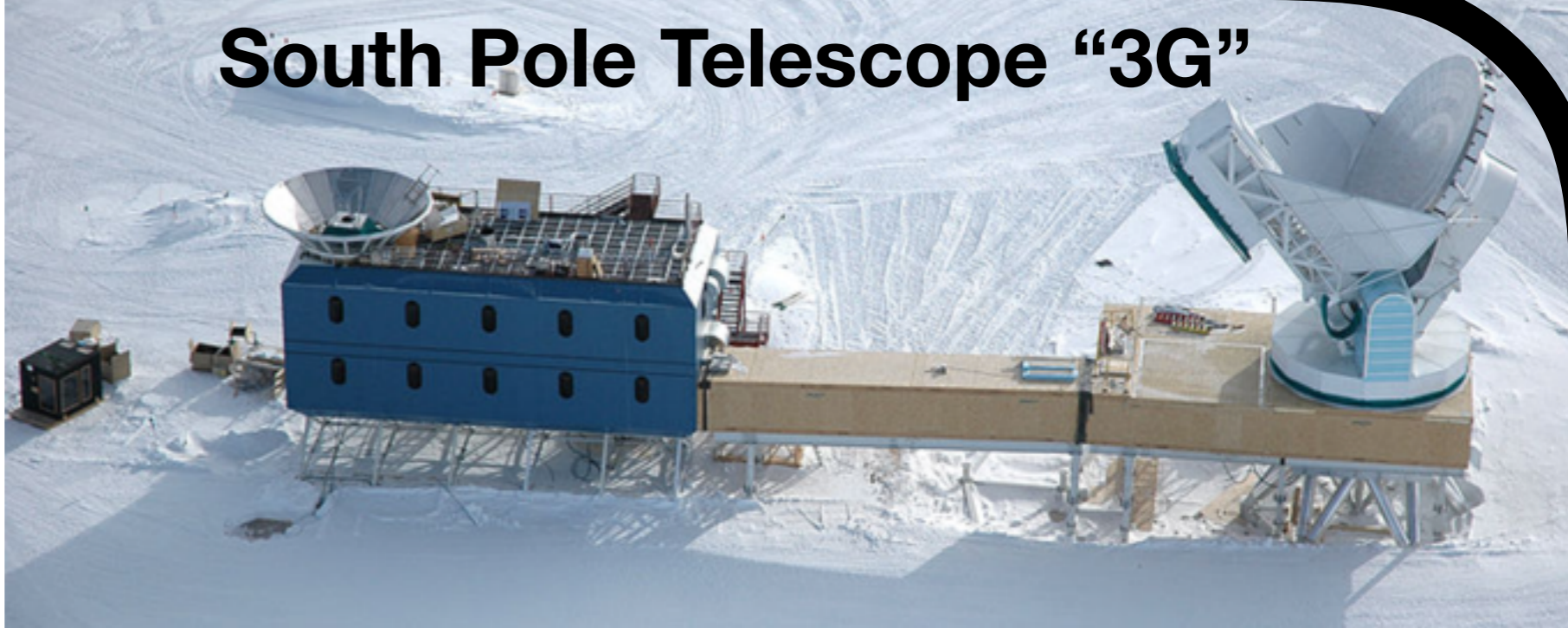
Advanced Atacama Cosmology Telescope



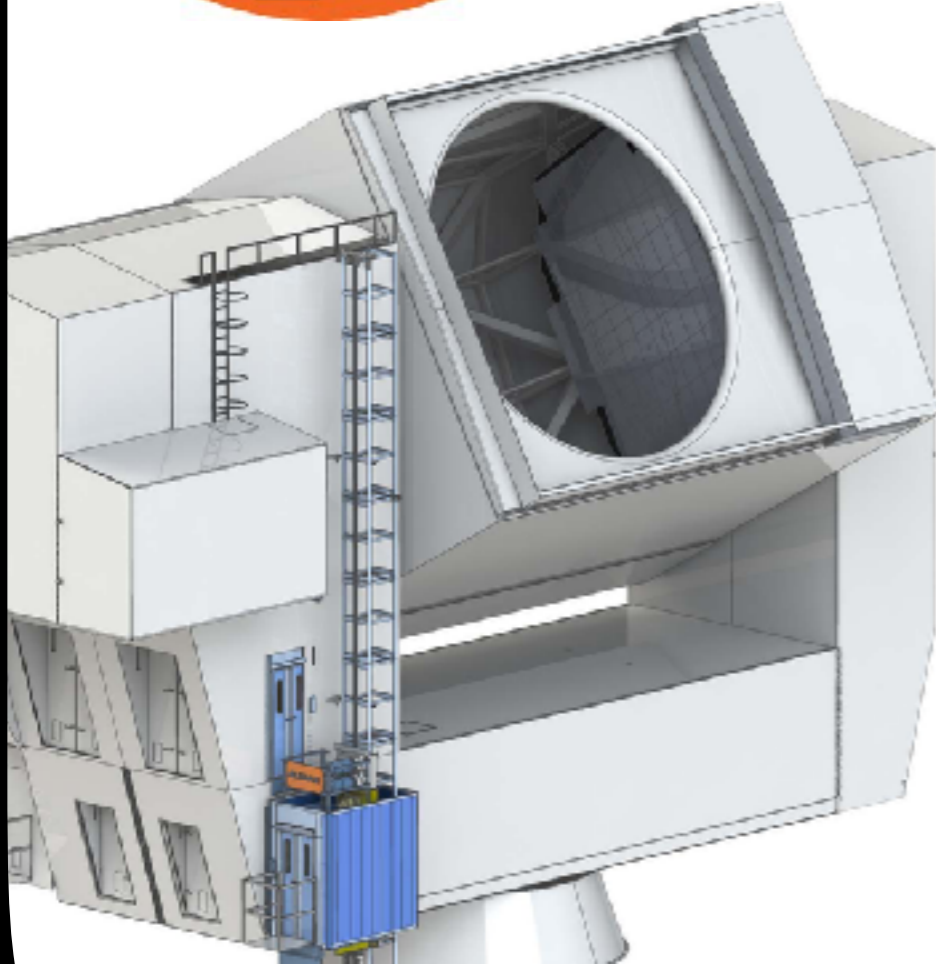
The Simons Array



conceptual

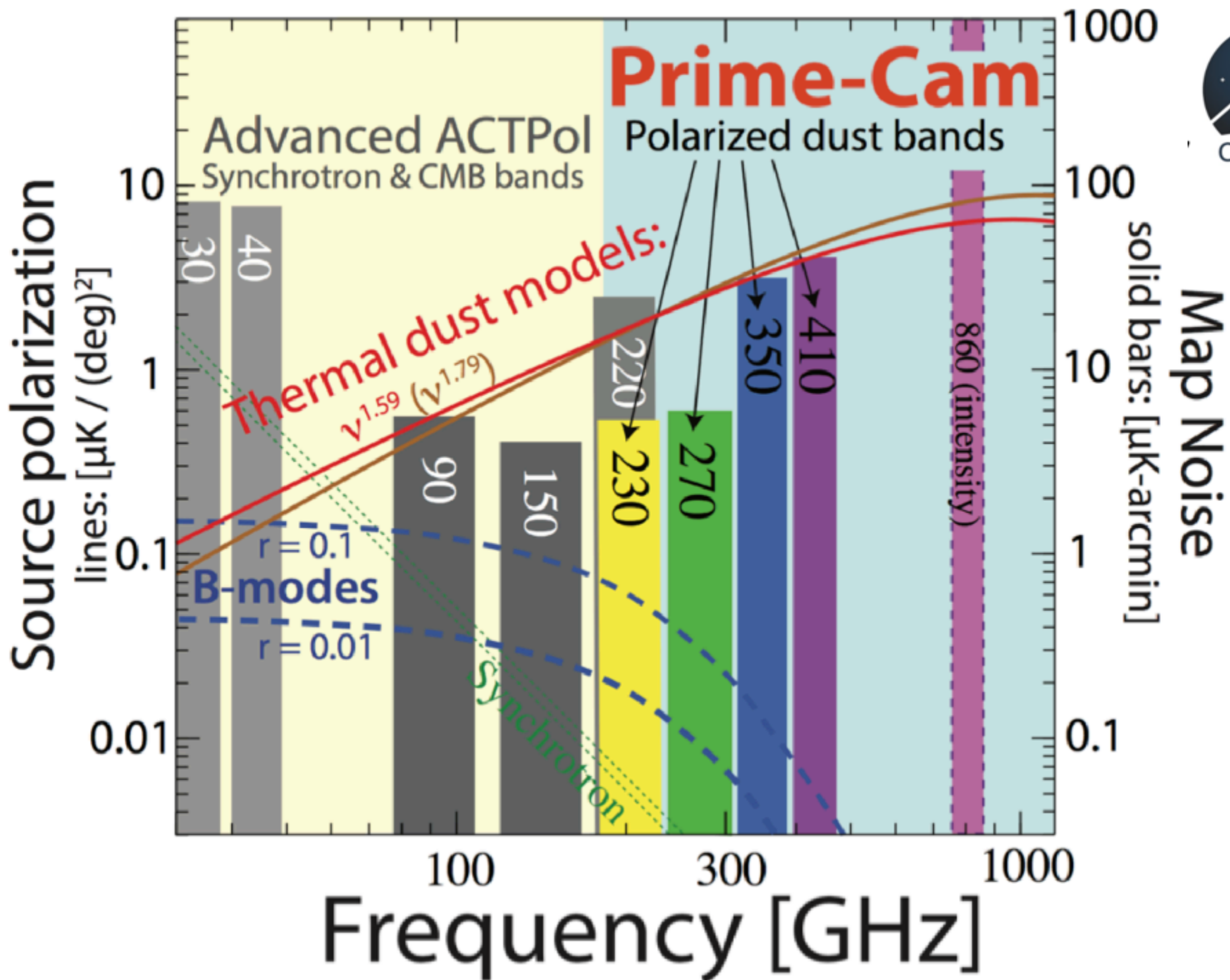


CMB-S4(?)



The Biggest Enemy: Polarised Dust Emission

- The upcoming data will **NOT** be limited by statistics, but by systematic effects such as the Galactic contamination
- **Solution**: Observe the sky at multiple frequencies, especially at high frequencies (>300 GHz)
- This is challenging, unless we have a superb, high-altitude site with low water vapour
- **CCAT-p!**



Frank Bertoldi's slide from the Florence meeting

Where is CCAT-p?

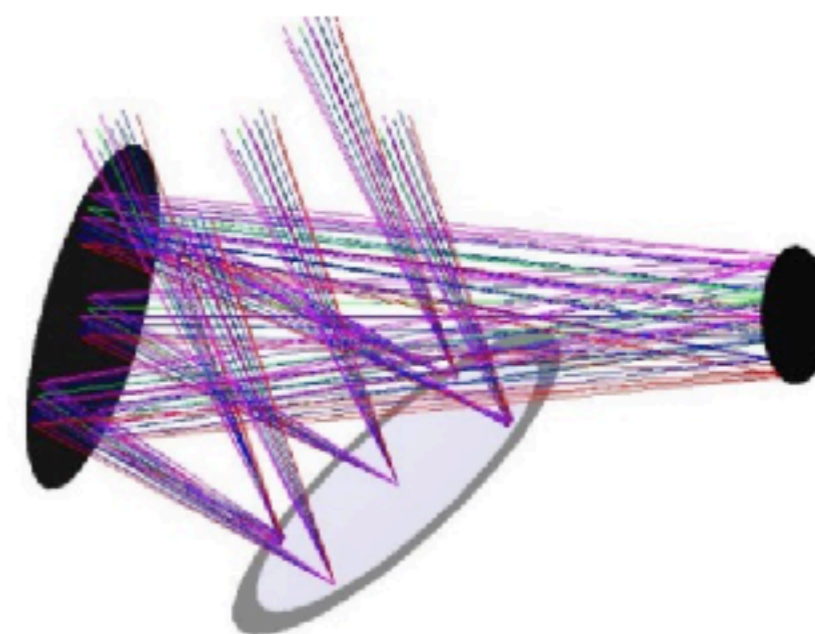
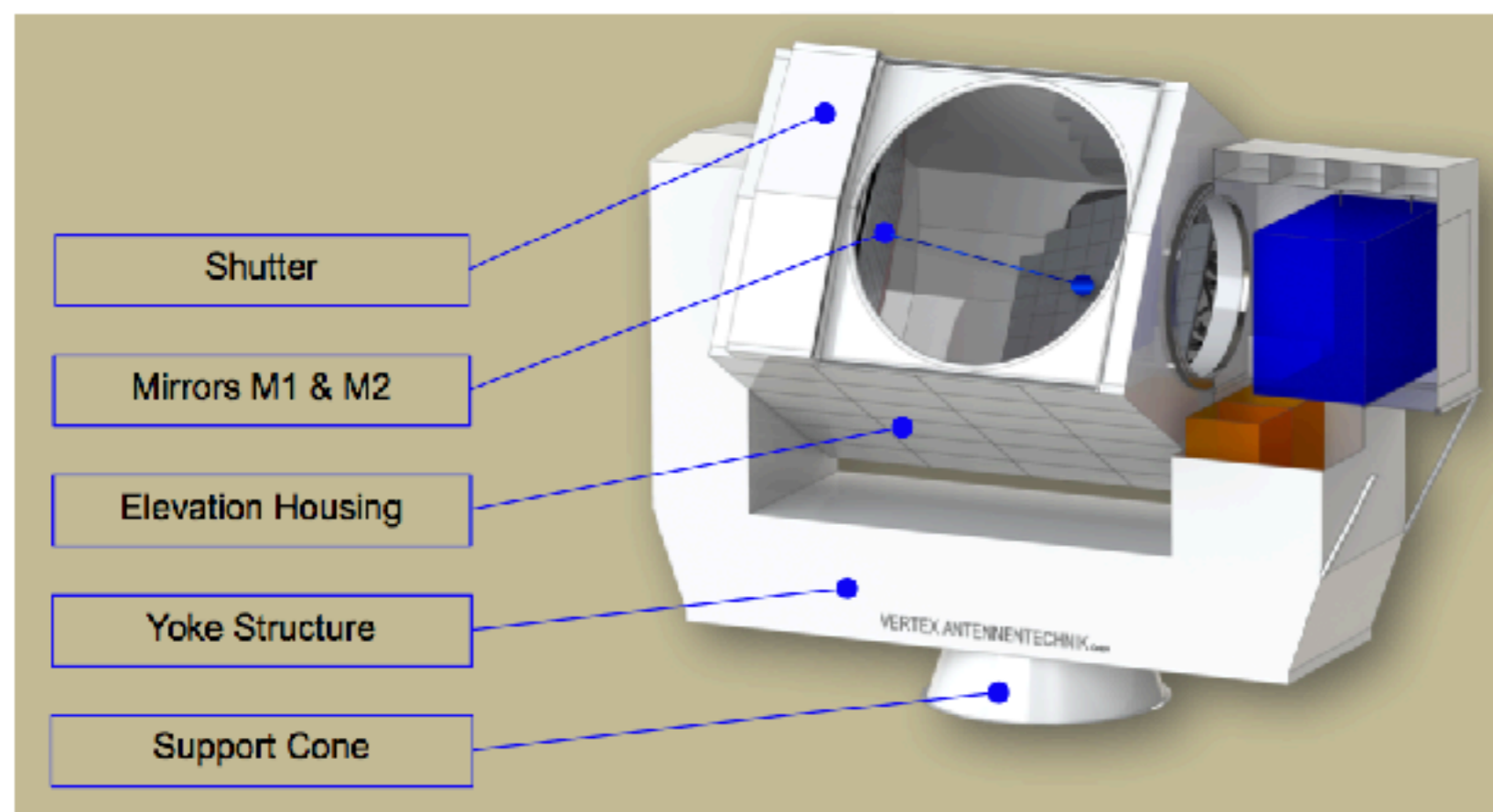
Cerro Chajnantor at 5600 m w/ TAO





What is CCAT-p?

CCAT-prime is a high surface accuracy / throughput 6 m submm (0.3-3mm) telescope



Cornell U. + German consortium + Canadian consortium + ...

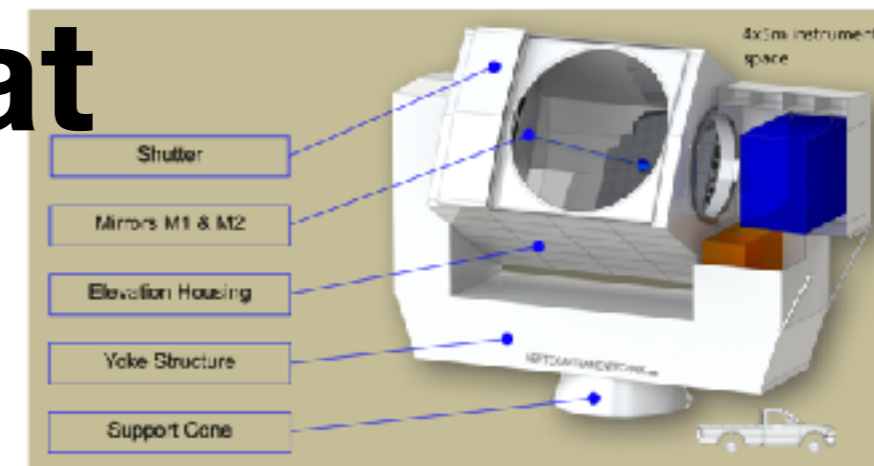
A Game Changer

- **CCAT-p**: 6-m, Cross-dragone design, on Cerro Chajnantor (5600 m)

- **Germany makes great telescopes!**

CCAT-prime

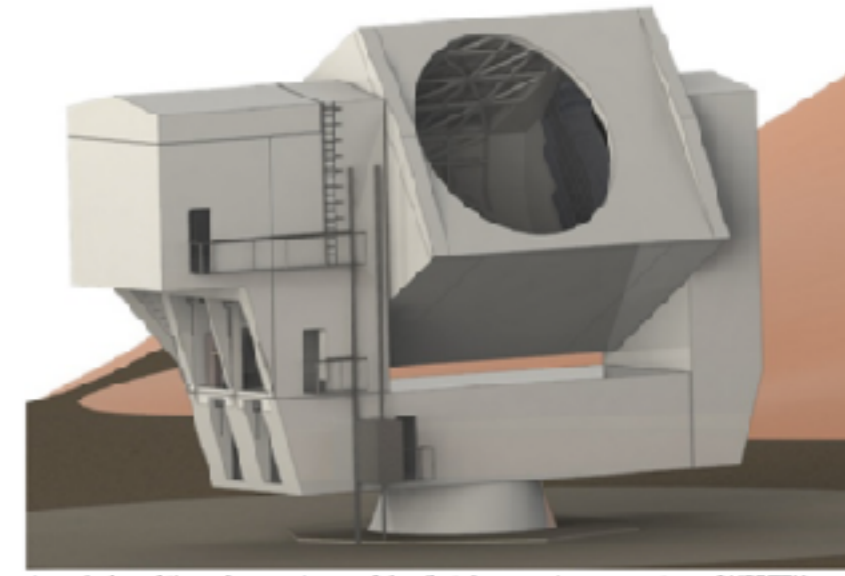
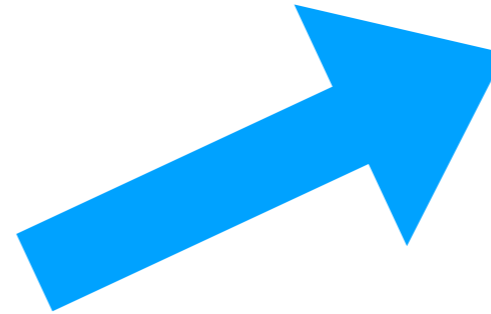
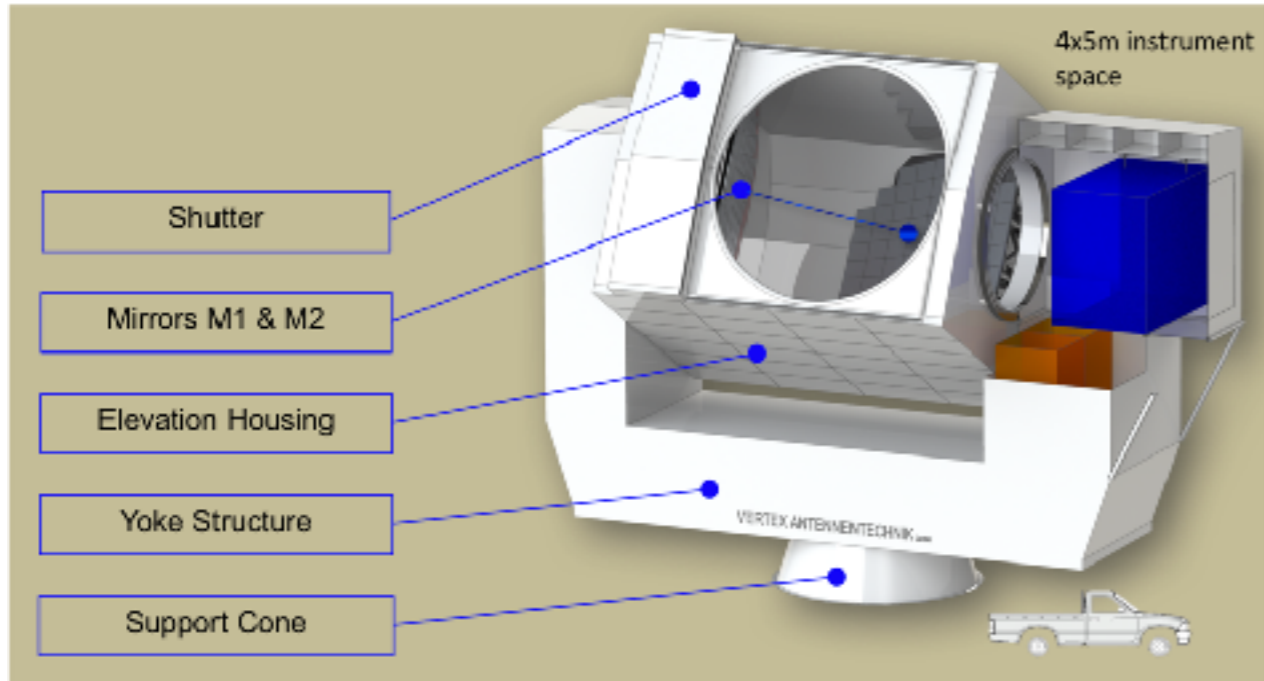
designed and built by Vertex Antennentechnik GmbH, Duisburg



- Design study completed, and the contract has been signed by “VERTEX Antennentechnik GmbH”
 - CCAT-p is a great opportunity for Germany to make significant contributions towards the CMB S-4 landscape (both US and Europe) by providing telescope designs and the “lessons learned” with prototypes.

CCAT-prime

designed and built by Vertex Antennentechnik GmbH, Duisburg



A rendering of the unique and powerful radio telescope. Image courtesy of VERTEX ANTENNENTECHNIK.

Simons Observatory (USA)

in collaboration

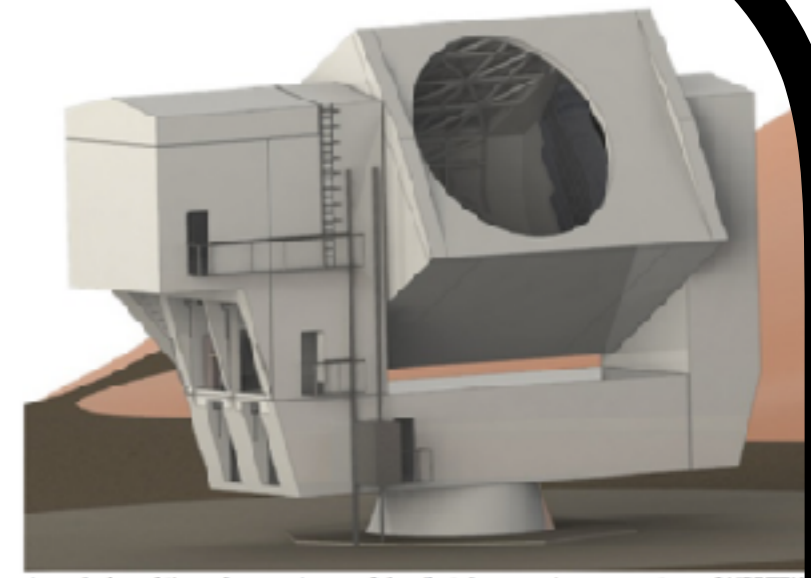
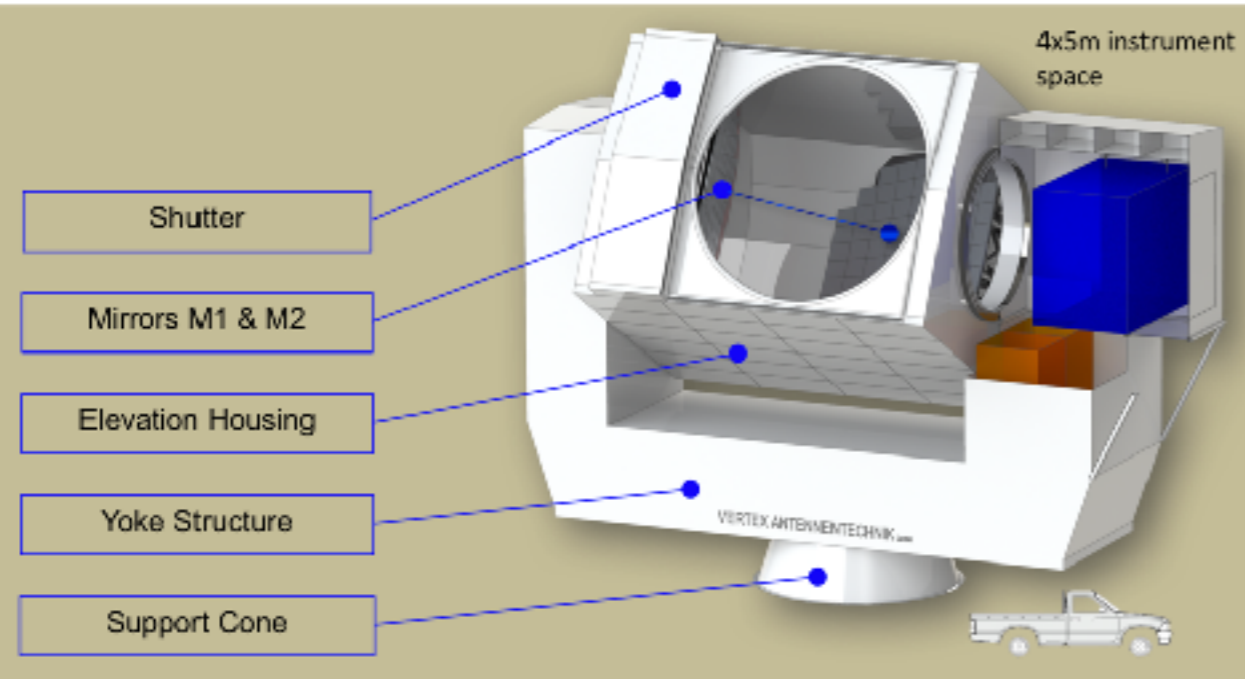


South Pole?

This could be “CMB-S4”

CCAT-prime

designed and built by Vertex Antennentechnik GmbH, Duisburg



A rendering of the unique and powerful radio telescope. Image courtesy of VERTEX ANTENNENTECHNIK.

**Simons Observatory
(USA)**

in collaboration



South Pole?

But, wait a minute...

Are GWs from vacuum fluctuation in spacetime, or from sources?

$$\square h_{ij} = -16\pi G \pi_{ij}$$

- **Homogeneous solution:** “GWs from vacuum fluctuation”
- **Inhomogeneous solution:** “GWs from sources”
 - Scalar and vector fields cannot source tensor fluctuations at linear order (possible at non-linear level)
Many papers by Sorbo, Peloso, and others
 - SU(2) gauge field can!

Maleknejad & Sheikh-Jabbari (2013); Dimastrogiovanni & Peloso (2013);
Adshead, Martinec & Wyman (2013); Obata & Soda (2016); ...

Final Remark

$$\square h_{ij} = -16\pi G \pi_{ij}$$

- We have ignored the source term during inflation, and considered only the vacuum fluctuation. Is this justified? **Maybe not!**

- *Further reading:*

- B. Thorne et al., Phys. Rev. D, 97, 043506 (2018), arXiv: 1707.03240
- A. Agrawal et al., Phys. Rev. D, 97, 103526 (2018), arXiv: 1707.03023
- A. Maleknejad & E. Komatsu, JHEP, 05, 174 (2019), arXiv: 1808.09076

Effect of π_{ij}

