

# Nuclear reaction codes development for the particles and nuclei production in meteoroids and planetary atmospheres

Jason Hirtz

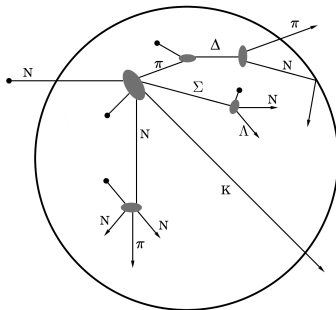
CEA Saclay - 22 November 2019

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- 6 Cosmogenic nuclides production
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# Introduction

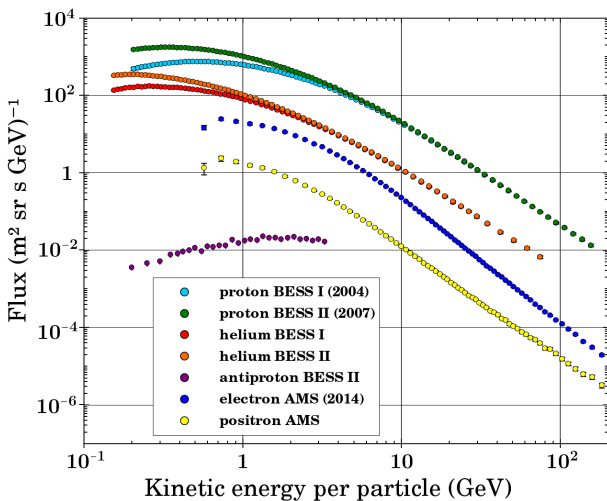
## Main concepts

- Cosmic rays
- Nuclear spallation
- Cosmogenic nuclides



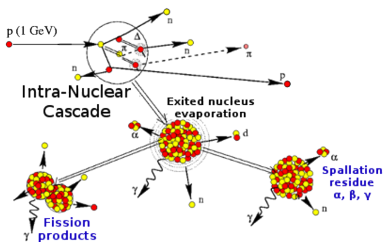
# Cosmic rays

- Protons ( $\sim 90\%$ )
- Alphas ( $\sim 10\%$ )
- Others ( $\sim 1\%$ )



# Nuclear spallation

## Spallation reaction



## Spallation with numbers

- Light projectile ( $p$ ,  $\pi$ ,  $\alpha$ , ...)
- Kinetic energy around the GeV
- Heavy target ( $^{12}\text{C}$ ,  $^{208}\text{Pb}$ , ...)
- Time scale:  $\sim 10^{-22} - 10^{-20} \text{ s}$

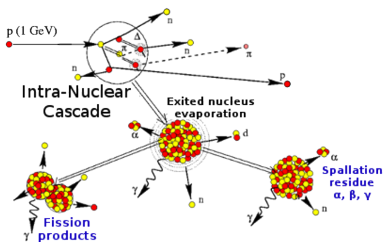
# Nuclear spallation

## Spallation reaction

or

How to transmute lead into gold

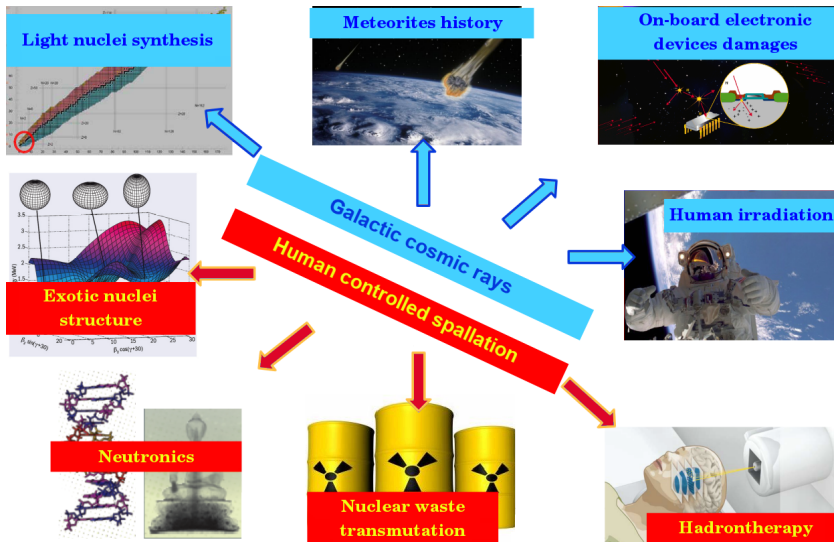
(Did you say cosmochemistry? No! Alchemy!)



## Spallation with numbers

- Light projectile ( $p, \pi, \alpha, \dots$ )
- Kinetic energy around the GeV
- Heavy target ( $^{12}\text{C}, ^{208}\text{Pb}, \dots$ )
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# Spallation applications



# Cosmogenic nuclides

## Dating techniques

- $^{14}\text{C}$



# Cosmogenic nuclides

## Dating techniques

- $^{14}\text{C}/\text{C}$        $\tau \sim 10^3 \text{ years}$
- $^{10}\text{Be}/^{14}\text{C}$        $\tau \sim 10^4 \text{ years}$
- $^{26}\text{Al}/^{21}\text{Ne}$        $\tau \sim 10^6 \text{ years}$
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## Isotope conditions

- Natural abundance low  $\rightarrow$  resolve production vs natural occurrence
- $\Rightarrow$  Order of magnitude of production:  
 $10^4 \text{ atom g}^{-1} \text{ year}^{-1}$  vs  $\mathcal{N}_a$

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- Stable or half-life comparable to the event of interest
- Measurable
- Theoretical understanding of production processes

# Theoretical understanding of cosmogenic nuclide production processes

**Need of improved spallation reaction description**

**Interest in spallation reaction applications**

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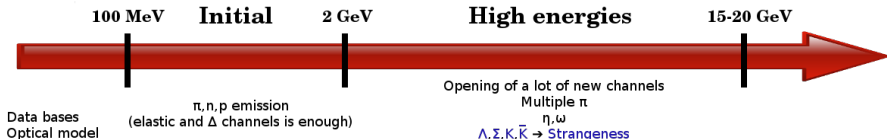
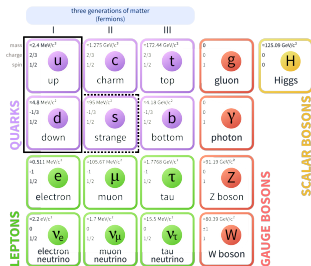
**Need of improved cosmic ray irradiation simulation**

**Interest in cosmic ray behaviour**

# INCL improvement

Improvement of the intra-nuclear cascade simulation code at high energy through a new degree of freedom: Strangeness

## Standard Model of Elementary Particles



# Ingredients

## Old particles

- Nucleons (protons and neutrons)
- Pions ( $\pi^-$ ,  $\pi^0$ , and  $\pi^+$ )
- Deltas ( $\Delta^-$ ,  $\Delta^0$ ,  $\Delta^+$ , and  $\Delta^{++}$ )

## New particles

- Kaons ( $K^0$  and  $K^+$ )
- Antikaons ( $\bar{K}^0$  and  $K^-$ )
- Sigmas ( $\Sigma^-$ ,  $\Sigma^0$ , and  $\Sigma^+$ )
- Lambda ( $\Lambda$ )



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## Particle properties

- Mass
- Half life
- Decay channel
- Nuclear potential

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## Cross sections

- Production
- Interaction
- Absorption

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## Cross sections

- Production
- Interaction
- Absorption

## Angular distributions

- Energy
- Direction

# Cross sections to parametrise

$NN \rightarrow N\Lambda K$	$\pi N \rightarrow \Lambda K$	$NK \rightarrow NK$	$N\bar{K} \rightarrow N\bar{K}$
$\rightarrow N\Sigma K$	$\rightarrow \Sigma K$	$\rightarrow NK\pi$	$\rightarrow \Lambda\pi$
$\rightarrow N\Lambda K\pi$	$\rightarrow \Lambda K\pi$	$\rightarrow NK\pi\pi$	$\rightarrow \Sigma\pi$
$\rightarrow N\Sigma K\pi$	$\rightarrow \Sigma K\pi$	$N\Lambda \rightarrow N\Lambda$	$\rightarrow N\bar{K}\pi$
$\rightarrow N\Lambda K\pi\pi$	$\rightarrow \Lambda K\pi\pi$	$\rightarrow N\Sigma$	$\rightarrow \Lambda\pi\pi$
$\rightarrow N\Sigma K\pi\pi$	$\rightarrow \Sigma K\pi\pi$	$N\Sigma \rightarrow N\Lambda$	$\rightarrow \Sigma\pi\pi$
$\rightarrow N\bar{K}\pi\pi$	$\rightarrow N\bar{K}\pi\pi$	$\rightarrow N\Sigma$	$\rightarrow N\bar{K}\pi\pi$

**Initial set: ~400 channels**

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$\rightarrow N\Sigma K\pi$	$\rightarrow \Sigma K\pi$	$N\Lambda \rightarrow N\Lambda$	$\rightarrow N\bar{K}\pi$
$\rightarrow N\Lambda K\pi\pi$	$\rightarrow \Lambda K\pi\pi$	$\rightarrow N\Sigma$	$\rightarrow \Lambda\pi\pi$
$\rightarrow N\Sigma K\pi\pi$	$\rightarrow \Sigma K\pi\pi$	$N\Sigma \rightarrow N\Lambda$	$\rightarrow \Sigma\pi\pi$
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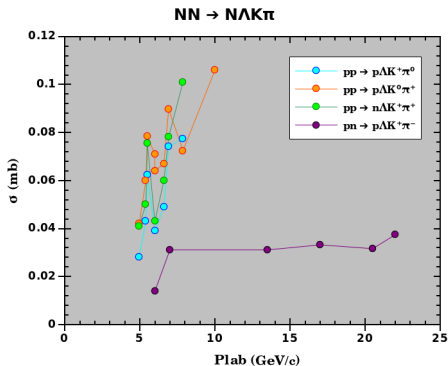
Initial set: ~400 channels

$\Delta N \rightarrow N\Lambda K$	$NN \rightarrow K + X$
$\rightarrow N\Sigma K$	
$\rightarrow \Delta\Lambda K$	$\pi N \rightarrow K + X$
$\rightarrow \Delta\Sigma K$	
$\rightarrow N\bar{K}\pi\pi$	

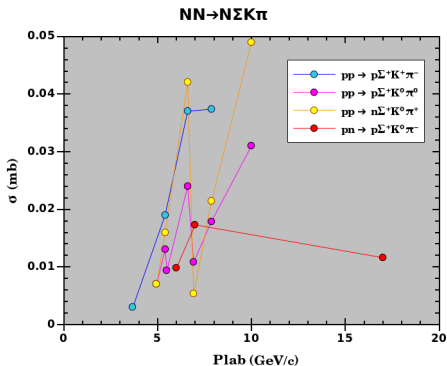
Second set: No data but needed. → Thousands of new channels.

# Sparse data

10 channels, 29 data points



26 channels, 43 data points



Data for 17% of the channels of the first set, including the above channels.  
(0% for the second set)

# Data completion

## First set

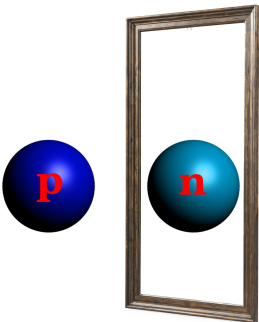
- Experimental data

17%

# Data completion

## First set

- Experimental data 17%
- Bystricky procedure 18% **total: 35%**



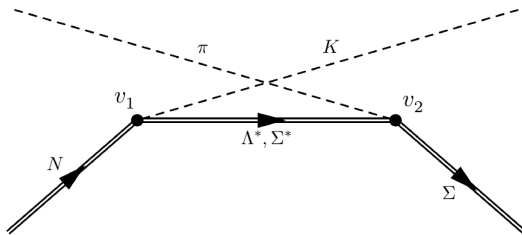
Symmetries between the channels



# Data completion

## First set

- **Experimental data** **17%**
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- **Hadron exchange model** **37%** **total: 72%**



## Symmetries between the Feynman diagrams

# Data completion

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- **Models-hypotheses-approximations** **28%** **total: 100%**

# Data completion

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**Second set: Models-hypotheses-approximations 100%**

**J. Hirtz, J.C. David, et al., Eur. Phys. J. Plus 133:436 (2018)**

# Angular distributions

**Angular distributions:**  
the direction and the energy of the particles in the final state

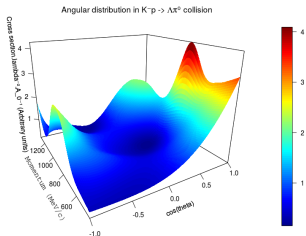
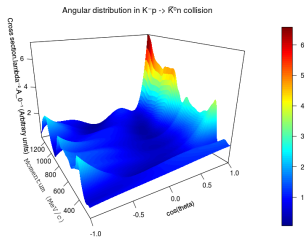
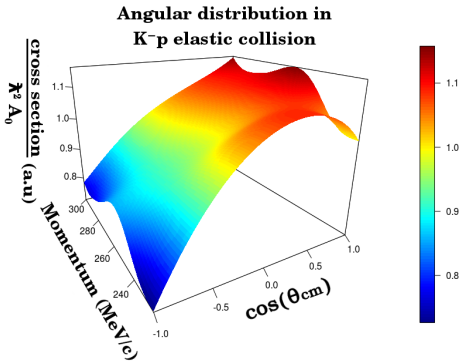
# Angular distributions

**Angular distributions:**  
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**Use of phase space generators when no experimental data**

**A refine model when possible**

# Angular distribution



J. Hirtz, J.C. David, et al., Eur. Phys. J. Plus 133:436 (2018)

# Variance reduction scheme

**Strangeness production represents 0.014% (0.15%) of the total cross section in p-p collision at kinetic energies of 2(3) GeV.**

**Computational time problem**

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(plus a lot of mathematics)

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**How to use the scheme?**

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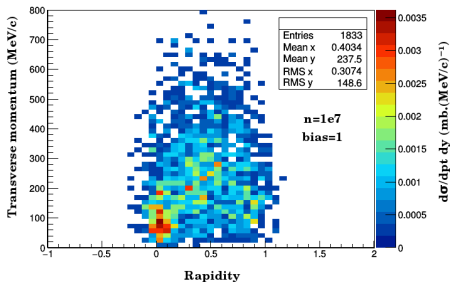
## How to use the scheme?

**The user requires an increase of the statistics by a factor 10 and the scheme increases the statistics by a factor 10 and tells you how to weight the results**

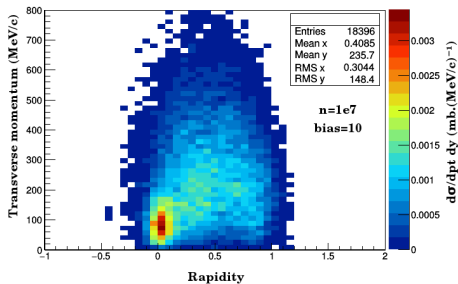
# Efficiency

## $\Lambda$ production in $p(1.7 \text{ GeV}) + \text{Ca}$ collision

Before

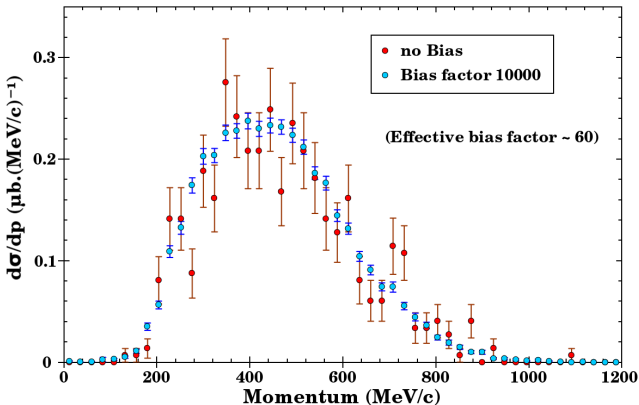


After



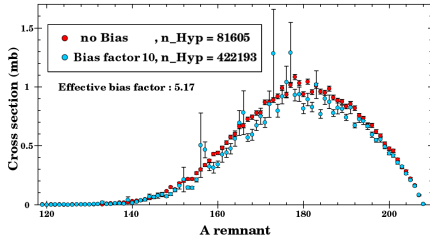
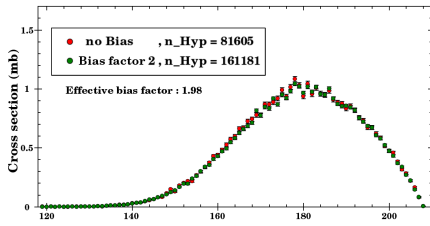
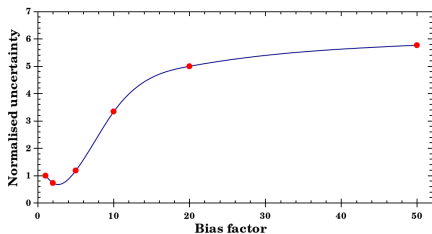
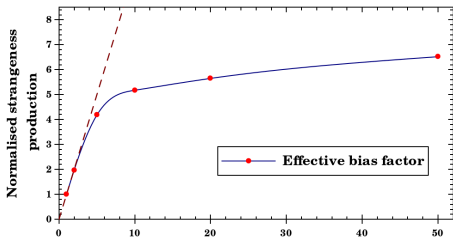
# Physical limits

$K^+$  momentum in  $p(1.6 \text{ GeV}) + ^{12}\text{C}$  with  $10^7$  events



# Borderline cases

$p(10 \text{ GeV}) + {}^{208} \text{Pb}$  ( $10^7$  shots)



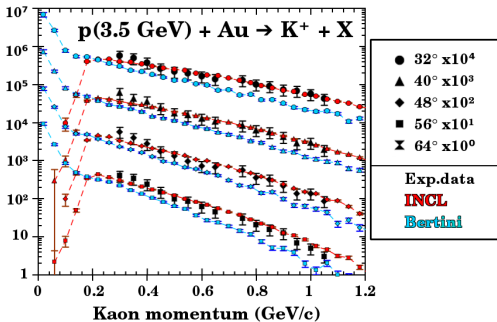
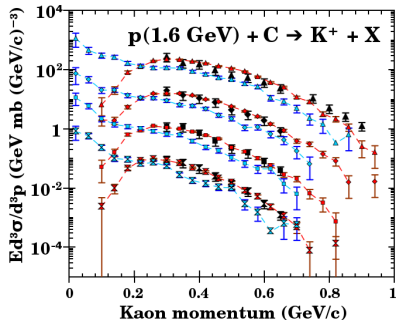
# INCL++6 results

**Time to control the results!**



# KaoS experiment

(W. Scheinast et al., PRL 96, 072301 (2006))



## Good points

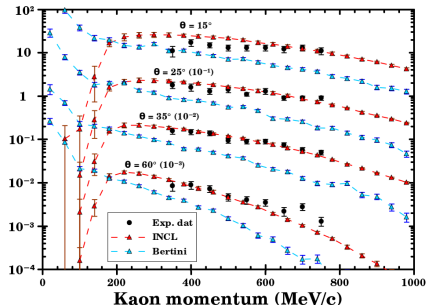
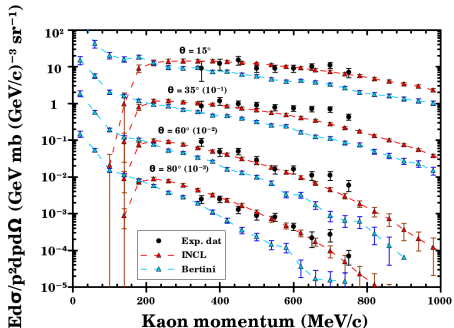
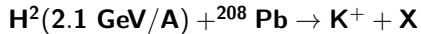
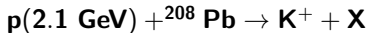
Excellent agreement with experimental data

## Observations

Threshold very different compared to the Bertini model because of repulsive K<sup>+</sup>'s potential

# LBL experiment

S. Schnetzer et al., Phys. Rev. C 40, 640(1989)



## Observations

- Results globally fine for proton as well as for deuteron induced reaction

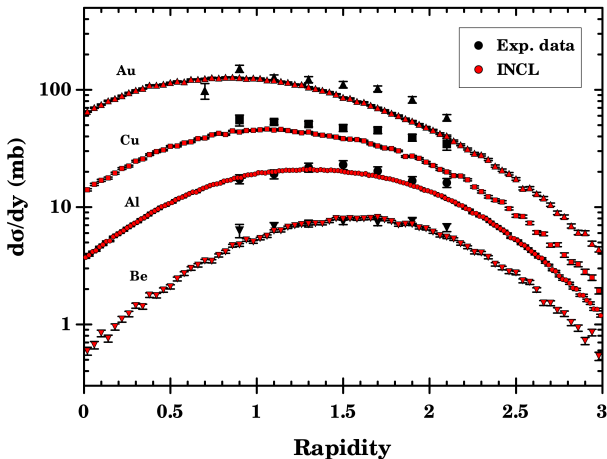
## E-802 experiment

E-802 Collaboration Phys. Rev. D 45, 3906 (1992)

## Observations

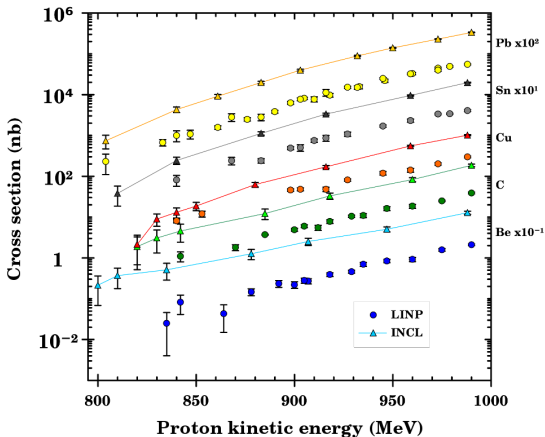
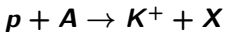
Relatively good results  
at high energy  
Promising for cosmic ray  
applications

$$p(14.6 \text{ GeV}/c) + A \rightarrow K^+ + X$$



# LINP experiment

V.P. Koptev et al., Zh. Eksp. Teor. Fiz. 94,1-14 (1988)



## Remark

- Threshold  $pp \rightarrow p\Lambda K^+$   
1580 MeV

## Observations

- Factor 4 with experimental data
- Far sub-threshold
  - Use of biasing (speed up by a factor 1 000)
  - Other models cannot produce results in a reasonable time

# CosmicTransmutation

**Simulation of spallation reactions improved**

**New version implemented in the Geant4 toolkit (open source)**

**Time to simulate cosmic ray irradiation**

**Creation of a new program: CosmicTransmutation (Geant4 based)**

# Objectives

## Observables

- Cosmogenic nuclide production rates
- Light particle fluxes ( $p$ ,  $n$ ,  $\alpha$ )

## Meteoroids (asteroids, moons)

- Shape
- Composition
- Size

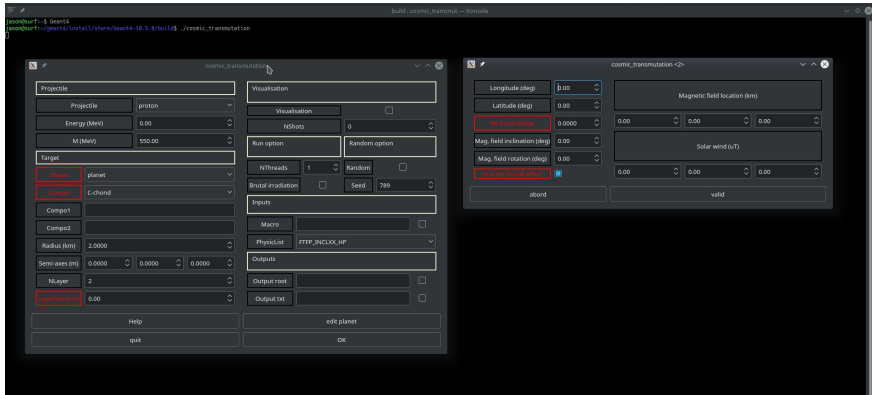
## Planets

- Planet size
- Atmosphere size, composition, density profile
- **Magnetic field**

## Requirements

- User-friendly
- Simple input and output
- Code documentation for analyses

# User-friendly interface



## Interface

- A few steps to run the program
- Simple definition of input parameters
- Able to tell the user if something is wrong or if an input file is missing

# Simple output

## Different type of output as a function of the needs

### Data file

- Small output file
- Automatically normalised results
- Only the fluxes of light particles

### ROOT file

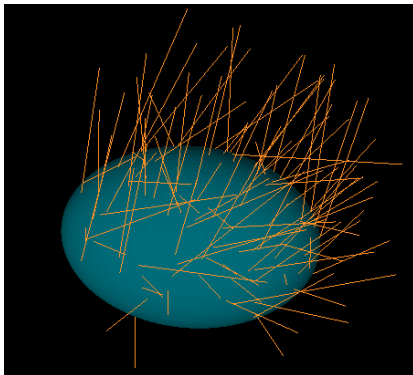
- All the information
- Possibility to cross observables
- More complex to manipulate



# Development

## Algorithms - interface

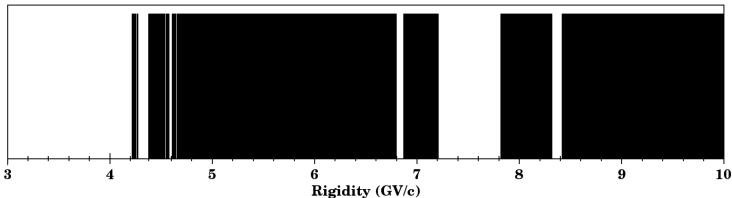
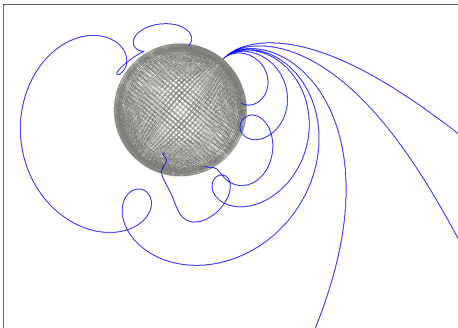
- Uniform irradiation (symmetries)
- User defined compositions
- etc...



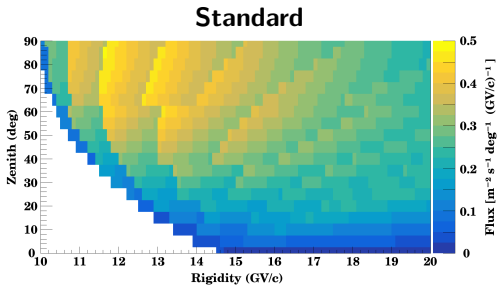
# Planets and magnetospheres

## Algorithms

- 2 phases
- Reverse kinematic calculations
- Map of allowed trajectories (Longitude, Latitude, Zenith, Azimuth, Rigidity)



# Cut-off maps

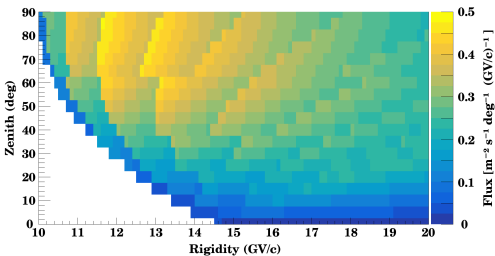


## New considerations

- Structure of the penumbra

# Cut-off maps

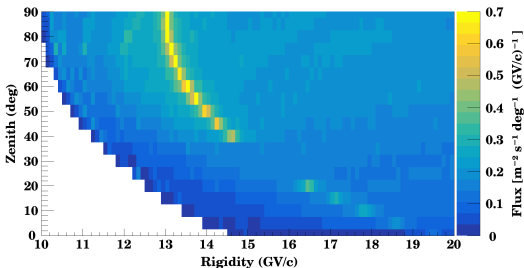
## Standard



## New considerations

- Structure of the penumbra
  - Consideration of focusing and dispersion
- Funnel effect**

## Funnel



# CosmicTransmutation results

**Time to control the results! (Again)**

# Meteoroids

## What to compare with?

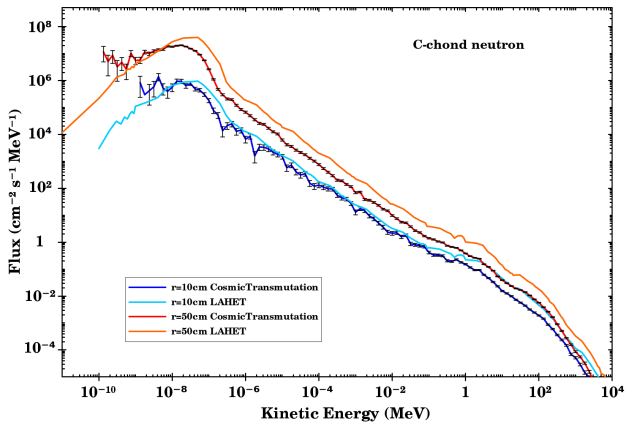
### Cosmogenic nuclide production rate

- What we try to understand
- Models use fluxes to calculate cosmogenic nuclide production

### Particle fluxes

- No experimental data
- Other models

# Neutron flux - Surface



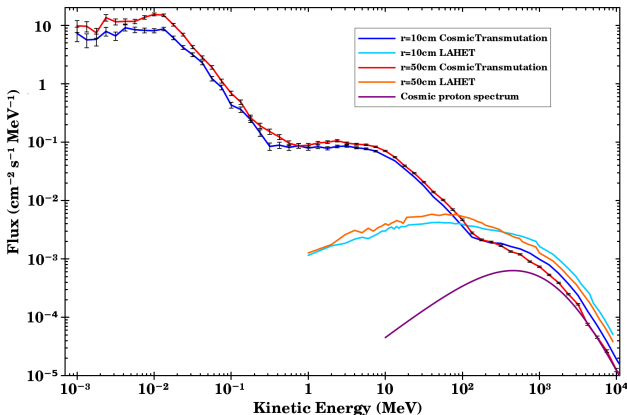
## Observations

- Factor 2 below LAHET
- Likely an error of normalisation
- Shapes similar

# Proton flux - Surface

## Observations

- Factor 2 below LAHET
- Confirmation error of normalisation
- High energy flux corresponds to the cosmic ray spectrum
- High energies (INC): similar shapes
- Low and intermediate energies: very different





# Planetary atmospheres

## What to compare with?

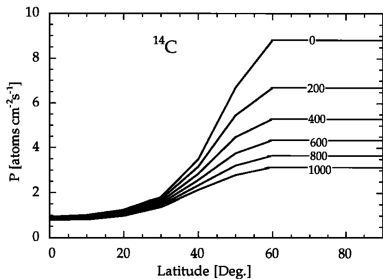
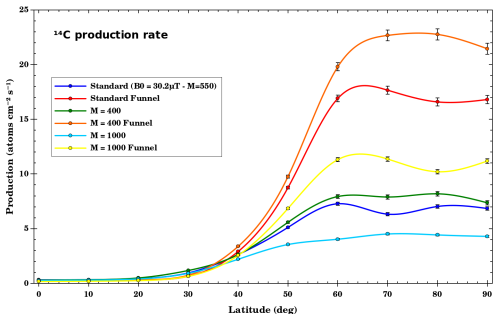
### Particle fluxes

- Experimental data: Input data or unmeasured
- Models: No data found + funnel effect

### Cosmogenic nuclide production rate

- Experimental data: hard to measure, atmosphere aerodynamics
- Models: funnel effect should not be considered to be comparable

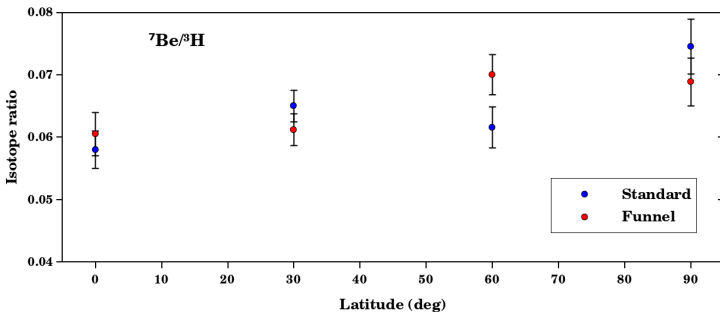
# Solar modulation parameter



## Without funnel vs Masarik and Beer

- Similar shapes
  - 40% above
- alpha particles ( $\sim 10\%$  of the cosmic ray spectrum; made of 4 nucleons)

# Cosmogenic nuclide ratios



## Observations

- Isotope ratio can change with a modification of the irradiation spectrum
- No observation of isotope ratio modification due to the funnel effect

# Conclusion

## Successful implementation of strangeness in INCL

- Improved simulation at high energy
- New fields of simulation opened
- Very good results for most of the observables studied
- Bonus: Variance reduction scheme

## Creation of CosmicTransmutation

- State-of-the-art simulation models used
- New features: alpha particles, ellipsoidal meteorite, penumbra structure, funnel effect, ...

## Future and perspective

- Study of the impact of funnel effect (cosmic ray flux, cosmogenic nuclides)
- Date things!

# Conclusion

*The End*



# Backup



# Isospin symmetry - Bystricky procedure

$$\frac{d\sigma}{d\Omega} = \frac{1}{64\pi^2 s^2} \frac{P_f}{P_i} |\mathcal{M}_{fi}|^2 \quad \rightarrow \quad \sigma \propto |\mathcal{M}_{fi}|^2$$

$$\mathcal{M}(NN \rightarrow NN \ x\pi) = (\langle NN| \otimes \langle x\pi|) M |NN\rangle$$

Superposition of state

$$\Rightarrow \langle I_1^{(1)} I_3^{(1)} I_2^{(2)} I_3^{(2)} | M | I_1^i I_3^i \rangle = CG M_{I_1^{(1)} I_2^{(2)} I_i}$$

Equations of the type  $\sigma_1 = ax + by$ ,  $\sigma_2 = cx + dy$ , ...

$$\begin{aligned} \mathcal{M}(\text{Initial state} \rightarrow x_N N \ x_\pi \pi \ x_Y Y \ x_K K \ x_{\bar{K}} \bar{K}) \\ = (\langle x_N N | \otimes \langle x_\pi \pi | \otimes \langle x_Y Y | \otimes \langle x_K K | \otimes \langle x_{\bar{K}} \bar{K} |) M | \text{Initial state} \rangle \\ = (\langle \text{system1} | \otimes \langle \text{system2} |) M | \text{Initial state} \rangle \end{aligned}$$



# Isospin symmetry - Bystricky results

$$\sigma(pp \rightarrow p\Sigma^+ K^0) = \sigma(nn \rightarrow n\Sigma^- K^+)$$

$$\begin{aligned} &\sigma(pn \rightarrow p\Sigma^- K^+) + \sigma(pp \rightarrow n\Sigma^+ K^+) + \sigma(pp \rightarrow p\Sigma^+ K^0) \\ &= 2\sigma(pn \rightarrow p\Sigma^0 K^0) + 2\sigma(pp \rightarrow p\Sigma^0 K^+) \end{aligned}$$

**Data for 17% → 35% of the channels.**

# Isospin projection

$$|pp\rangle = |1\ 1\rangle$$

$$|pn\rangle = \frac{\sqrt{2}}{2} |1\ 0\rangle + \frac{\sqrt{2}}{2} |0\ 0\rangle$$

$$|np\rangle = \frac{\sqrt{2}}{2} |1\ 0\rangle - \frac{\sqrt{2}}{2} |0\ 0\rangle$$

$$|nn\rangle = |1\ -1\rangle$$

$$|p\Sigma^+\rangle = |3/2\ 3/2\rangle$$

$$|p\Sigma^0\rangle = \sqrt{\frac{2}{3}} |3/2\ 1/2\rangle - \sqrt{\frac{1}{3}} |1/2\ 1/2\rangle$$

$$|p\Sigma^-\rangle = \sqrt{\frac{1}{3}} |3/2\ -1/2\rangle - \sqrt{\frac{2}{3}} |1/2\ -1/2\rangle$$

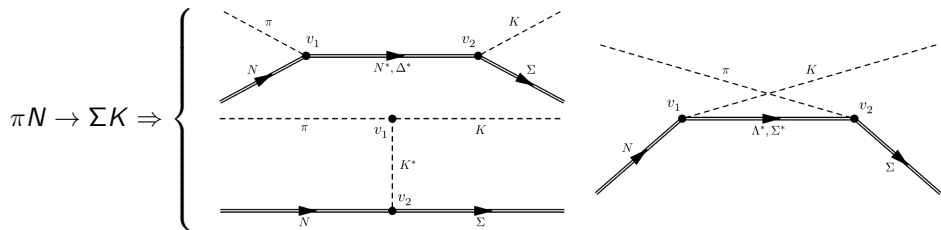
$$|n\Sigma^+\rangle = \sqrt{\frac{1}{3}} |3/2\ 1/2\rangle + \sqrt{\frac{2}{3}} |1/2\ 1/2\rangle$$

$$|n\Sigma^0\rangle = \sqrt{\frac{2}{3}} |3/2\ -1/2\rangle + \sqrt{\frac{1}{3}} |1/2\ -1/2\rangle$$

$$|n\Sigma^-\rangle = |3/2\ -3/2\rangle$$

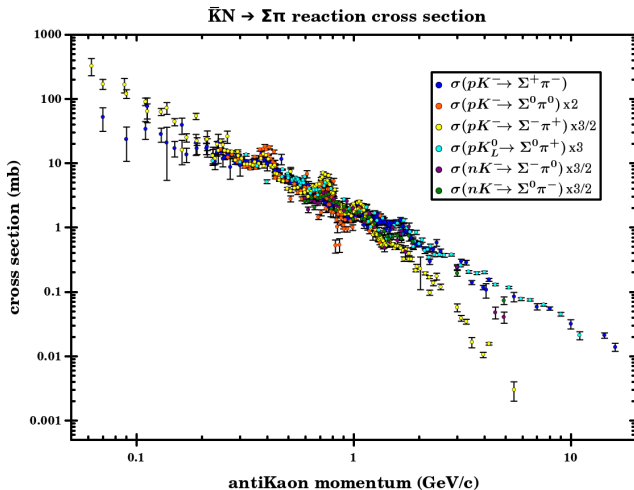
# Isospin symmetry - Hadron Exchange Model

Zoom from reactions level to Feynman diagrams level.  
More powerful but need more hypotheses.



$$\begin{aligned} \sigma(\pi N \rightarrow \Sigma K) = & a_K^2 \int |\mathfrak{M}_K|^2 d\Omega + a_\Lambda^2 \int |\mathfrak{M}_\Lambda|^2 d\Omega + a_\Sigma^2 \int |\mathfrak{M}_\Sigma|^2 d\Omega \\ & + a_N^2 \int |\mathfrak{M}_N|^2 d\Omega + a_\Delta^2 \int |\mathfrak{M}_\Delta|^2 d\Omega. \end{aligned}$$

# Isospin symmetry - HEM results



Data for 35%  $\rightarrow$  72% of the channels.

# Model, Hypotheses, and approximations

**Still 28% of the channels without possible parametrisation. All important!**

$$\sigma_{NN \rightarrow N\Lambda K\pi}(\sqrt{s}) = 3 \sigma_{NN \rightarrow N\Lambda K}(\sqrt{s}) \times \frac{\sigma_{NN \rightarrow NN\pi\pi}(\sqrt{s} - 540)}{\sigma_{NN \rightarrow NN\pi}(\sqrt{s} - 540)}$$

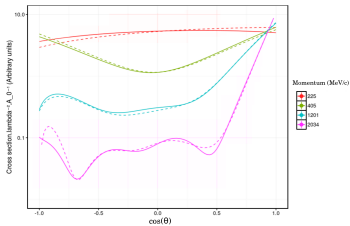
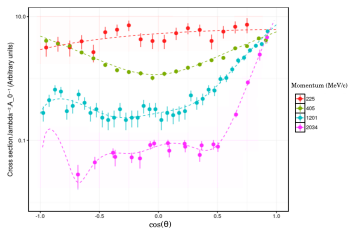
$$\sigma_{NN \rightarrow N\Sigma K\pi}(\sqrt{s}) = 3 \sigma_{NN \rightarrow N\Sigma K}(\sqrt{s}) \times \frac{\sigma_{NN \rightarrow NN\pi\pi}(\sqrt{s} - 620)}{\sigma_{NN \rightarrow NN\pi}(\sqrt{s} - 620)}$$

$$\sigma_{NN \rightarrow N\Lambda K\pi\pi}(\sqrt{s}) = \sigma_{NN \rightarrow N\Lambda K\pi}(\sqrt{s}) \times \frac{\sigma_{NN \rightarrow NN\pi\pi}(\sqrt{s} - 675)}{\sigma_{NN \rightarrow NN\pi}(\sqrt{s} - 675)}$$

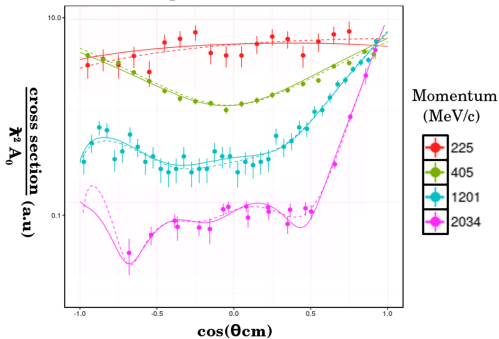
$$\sigma_{NN \rightarrow N\Sigma K\pi\pi}(\sqrt{s}) = \sigma_{NN \rightarrow N\Sigma K\pi}(\sqrt{s}) \times \frac{\sigma_{NN \rightarrow NN\pi\pi}(\sqrt{s} - 755)}{\sigma_{NN \rightarrow NN\pi}(\sqrt{s} - 755)}$$

**Data for 100% of the channels! This is what I fought...**

# Angular distributions

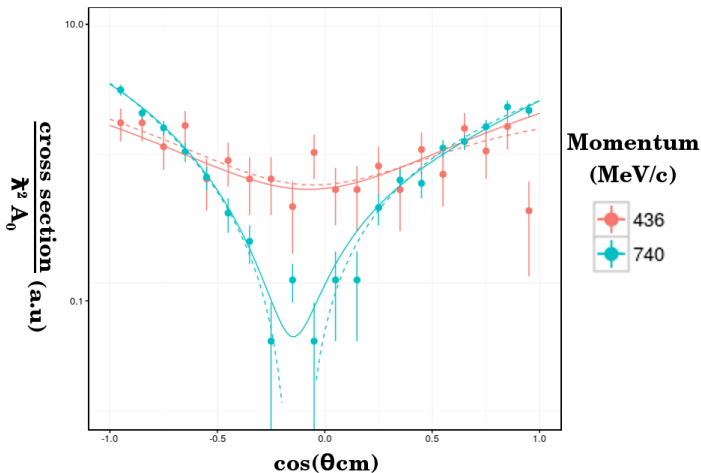


## Angular distribution in $K^-p$ elastic collision

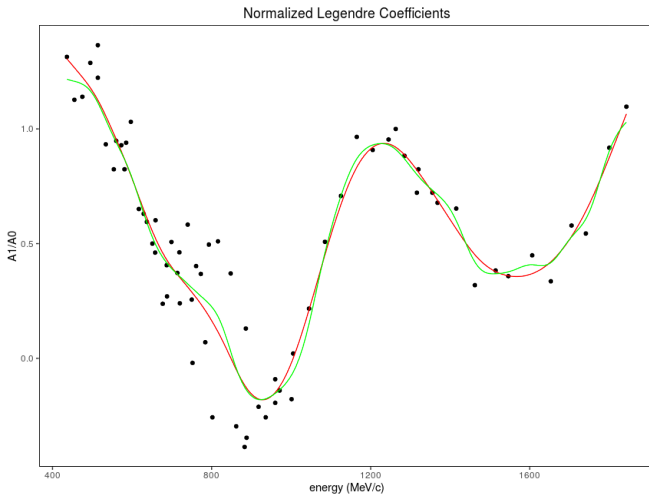


# Negative density of probability

## Angular distribution in $K^-p \rightarrow \Sigma^- \pi^+$ collision

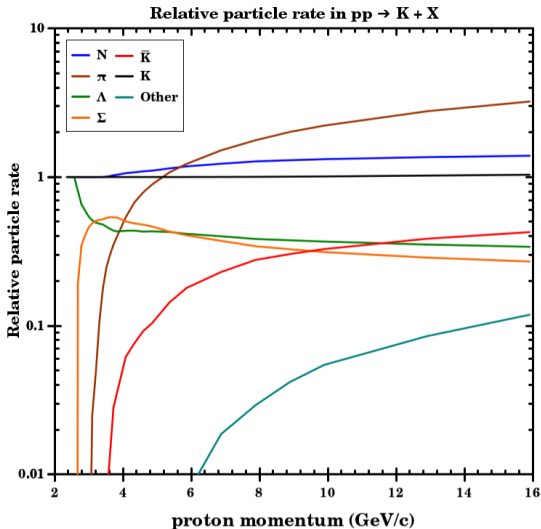


# Smoothing splines vs Nadaraya-Watson kernel regression



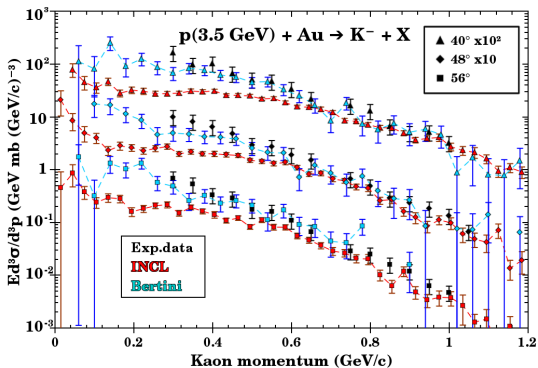


# Fritiof rates



## KaoS Experiment

(W. Scheinast et al., PRL 96, 072301 (2006))

A word about  $K^-$  production

Relatively bad results, notably at low energy

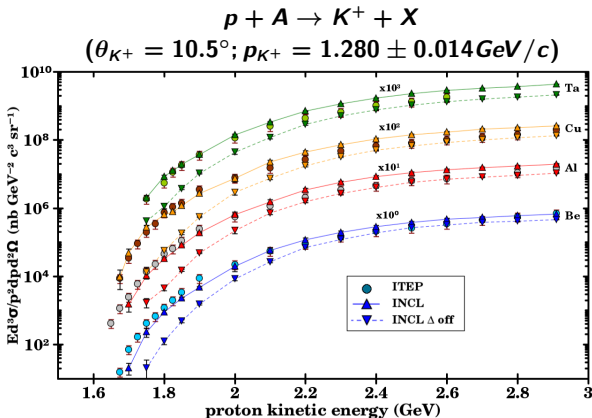
→ Possible explanation: missing channels.  $\bar{K}$  production in strangeness exchange reaction not taken into account (e.g.  $\Lambda N \rightarrow NN\bar{K}$ )

# ITEP experiment

A test for unmeasured cross sections

## Observations

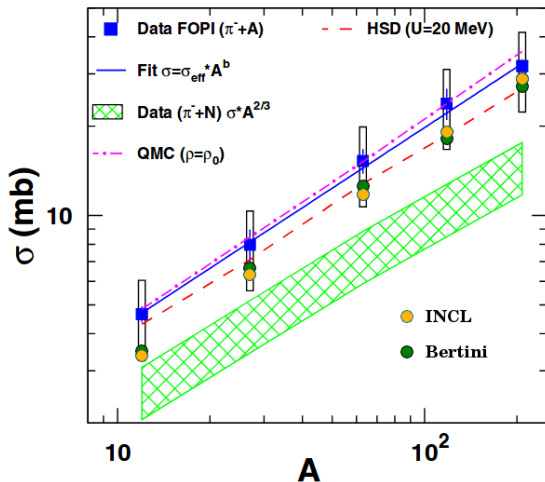
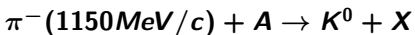
- Results correct in the threshold region
- Huge impact of  $\Delta$ -induced reactions



A. V. Akindinov et al., JETP Letters, Vol. 72, No. 3, 2000, pp. 100-105

## FOPI experiment

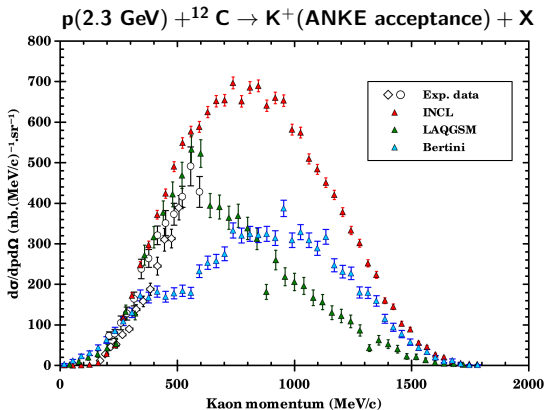
M. L. Benabderrahmane et al., Phys. Rev. Lett. 102, 182501



## Observations

- Within the systematic errors
- INCL slope  $\propto A^{3/4}$   
FOPI slope  $\propto A^{2/3}$

# ANKE experiment



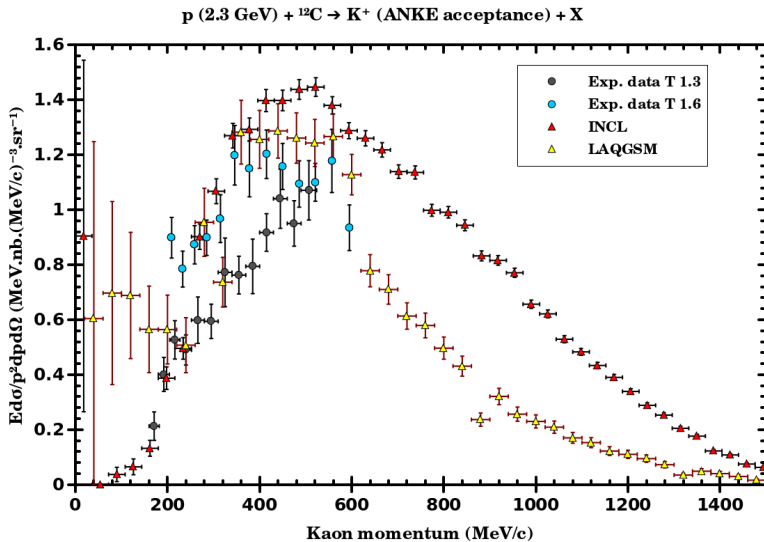
## Observations

- Good threshold simulation
- Prediction very different of LAQGSM at energies higher than 600 MeV/c

M. Büscher et al., Eur.Phys. J. A 22, 301-317(2004)

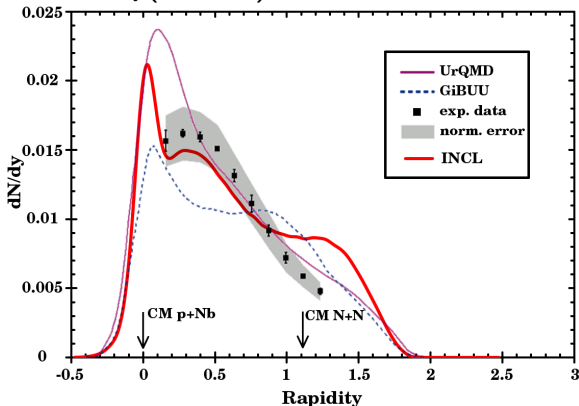
Thanks Nikolai Mokhov for LAQGSM data

# ANKE invariant cross section



HADES - The  $\Lambda$ 

HADES Collaboration, Eur. Phys. J. A (2014) 50:81

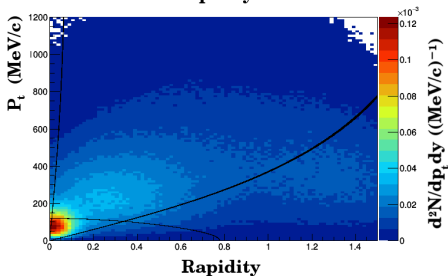
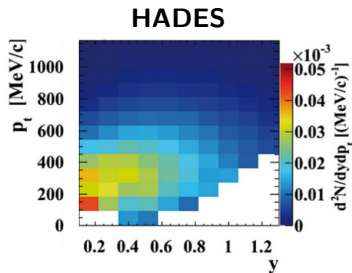
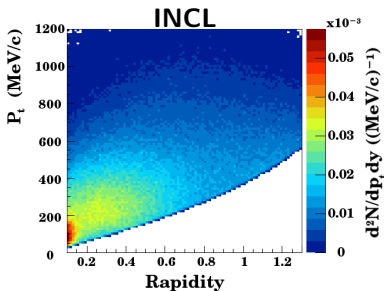
 $p(3.5 \text{ GeV}) + \text{Nb} \rightarrow \Lambda + X$ 

## Observations

- Good reproduction in the region  $[0.15-0.9]$  (Amplitude, shape)
- Bump around  $CM N+N$

HADES - The  $\Lambda$ 

HADES Collaboration, Eur. Phys. J. A (2014) 50:81



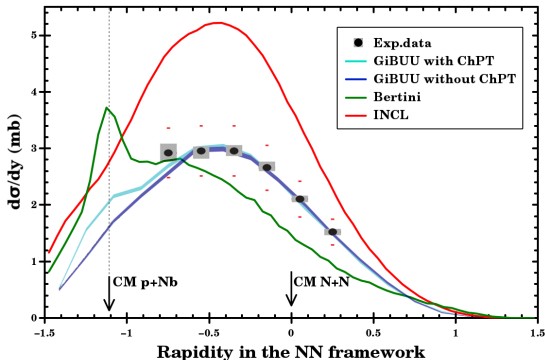
## Observations

- Consistent with experimental data
- Tension with the extrapolation



# HADES experiment - The $K_S^0$

$$p(3.5\text{GeV}) + \text{Nb} \rightarrow K_S^0 + X$$



HADES Collaboration, T.Gaitanos and J. Weil,  
Phys. Rev. C 90, 054906 (2014)

## Observations

- Same experiment as the previous one but results very different
- Reaction cross section:  
HADES -  $848 \pm 127 \text{ mb}$ ,  
INCL -  $1047.87 \text{ mb}$ ,  
Bertini -  $1164 \text{ mb}$

## Remark

GiBUU has been rescaled  
Impossible to make proper  
comparisons

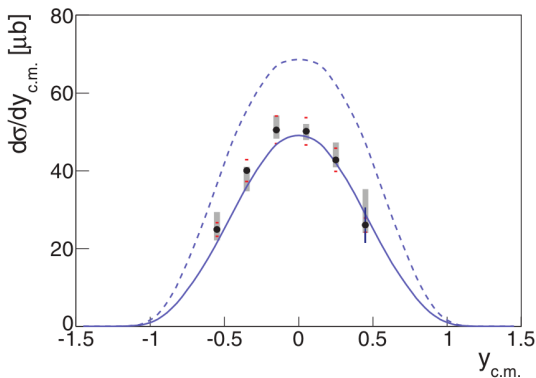


FIG. 4. (Color online)  $K_s^0$  rapidity distribution in  $p + p$  collisions (black circles) and GiBUU transport model simulations (dashed curve—original resonance model [30], solid curve—modified resonance model; see text).

# Simple input - Irradiation flux

Only one input parameter to fully define proton and alpha spectra:  
The solar modulation parameter  $M$

proton

$$J_p(T, M) = c_p \times \frac{T (T + 2m_p c^2) (T + 780 \times e^{-2.5 \cdot 10^{-4} \times T} + M)^{-2.65}}{(T + M) (T + 2m_p c^2 + M)}$$

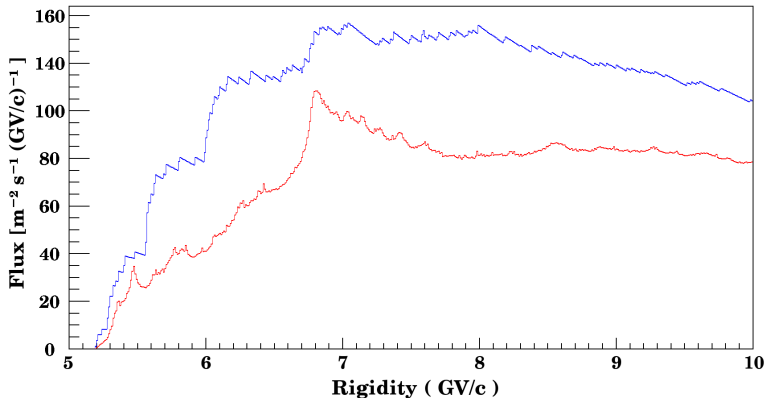

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alpha (new)

$$J_\alpha(T, K) = \frac{c_\alpha \times T^K \times (T + 2m_\alpha c^2)}{(T + 700)(T + 2m_\alpha c^2 + 700)(T + 312500 T^{-2.5} + 700)^{1.65+K}}$$

$$K = (1.786 \cdot 10^{-3} \times M) - 0.1323$$

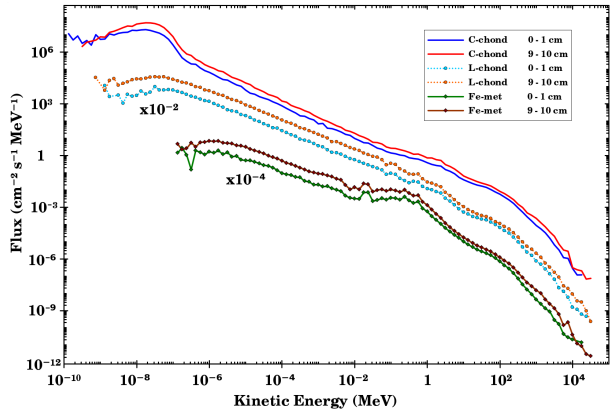
# Cut-off effects



## New effects

- Modified irradiation flux
- Modified ratio  $p/\alpha$  particles

# Meteoroid types

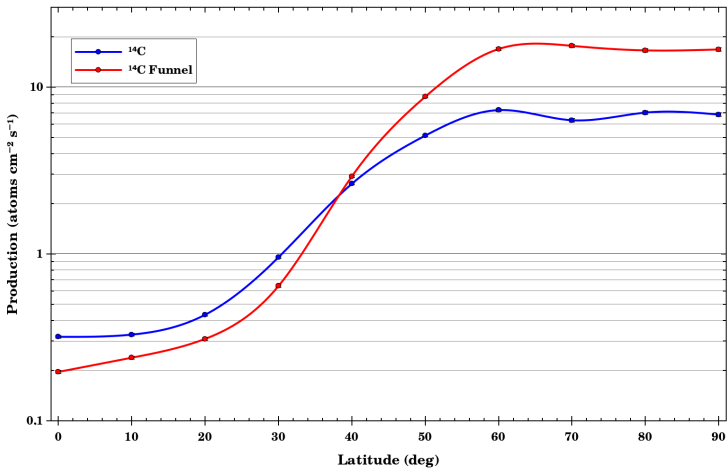


### Observations

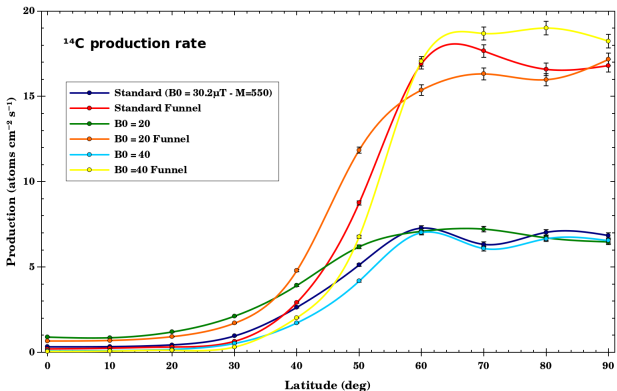
- Increased flux at 10 cm
- Higher neutron flux with heavier elements
- Composition influence the spectrum shape

# Funnel effect

## Cosmic Transmutation vs Cosmic Transmutation



# Magnetic field intensity



## Observations

- Higher magnetic field increases the particle flux at the poles (higher focusing)

# Test Funnel algorithm

