



The large scale structure of the Universe as seen by Planck

Aurélien Benoit-Lévy

University College London

On behalf of the Planck Collaboration

XVII. Gravitational lensing by large scale structure

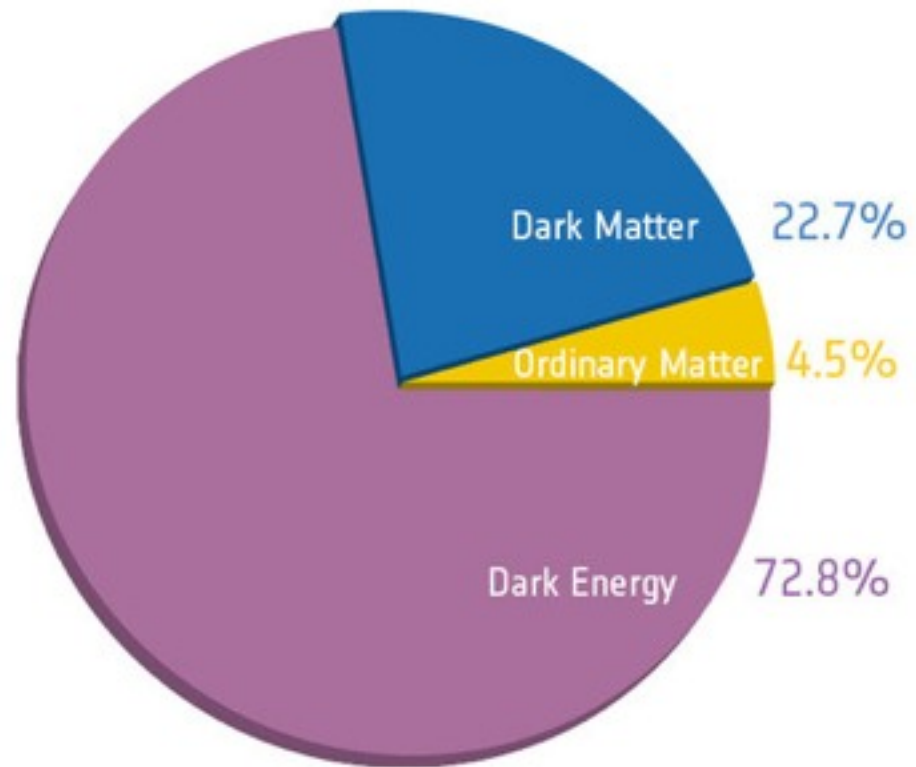
XVI. Cosmological parameters

XVIII. Gravitational lensing - infrared background correlation

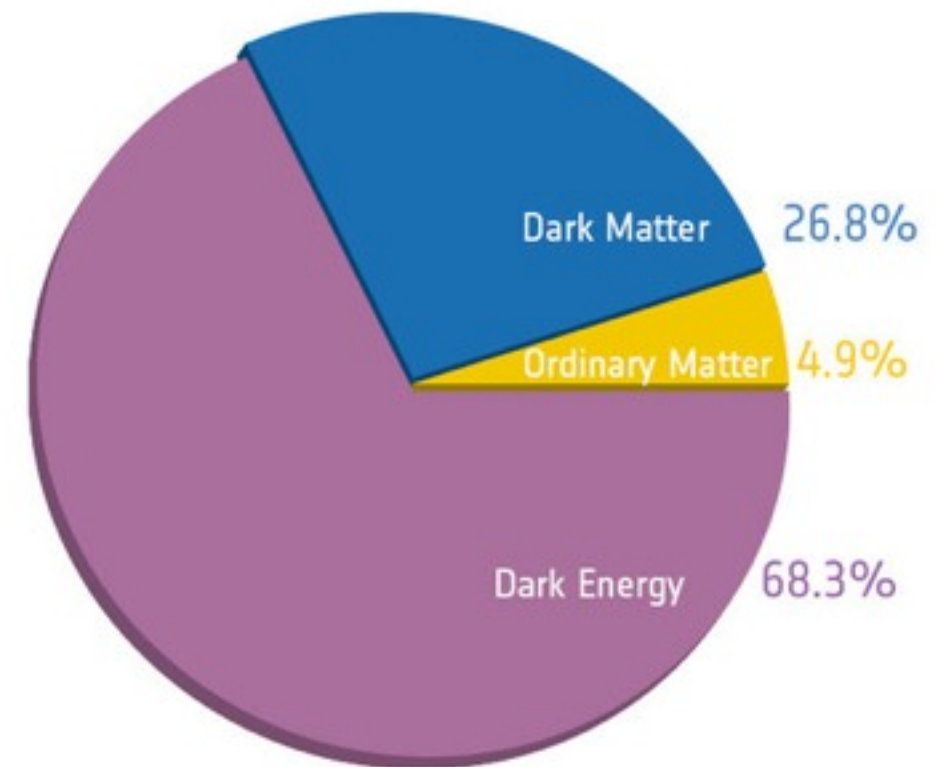
XIX. The integrated Sachs-Wolfe effect



A quick summary of the current status of cosmology



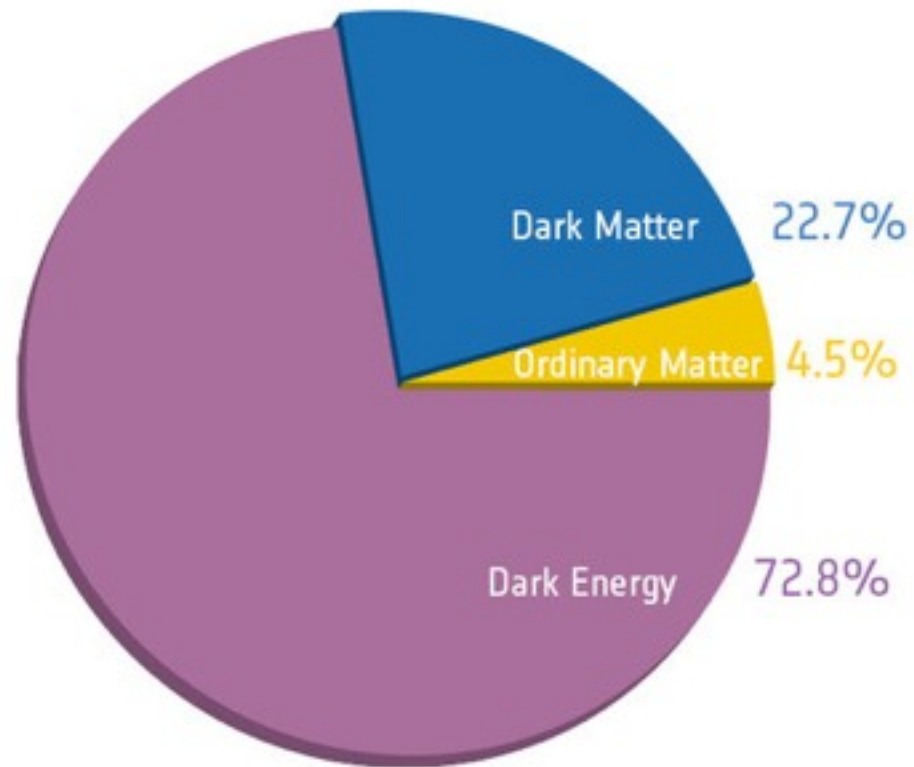
Before Planck



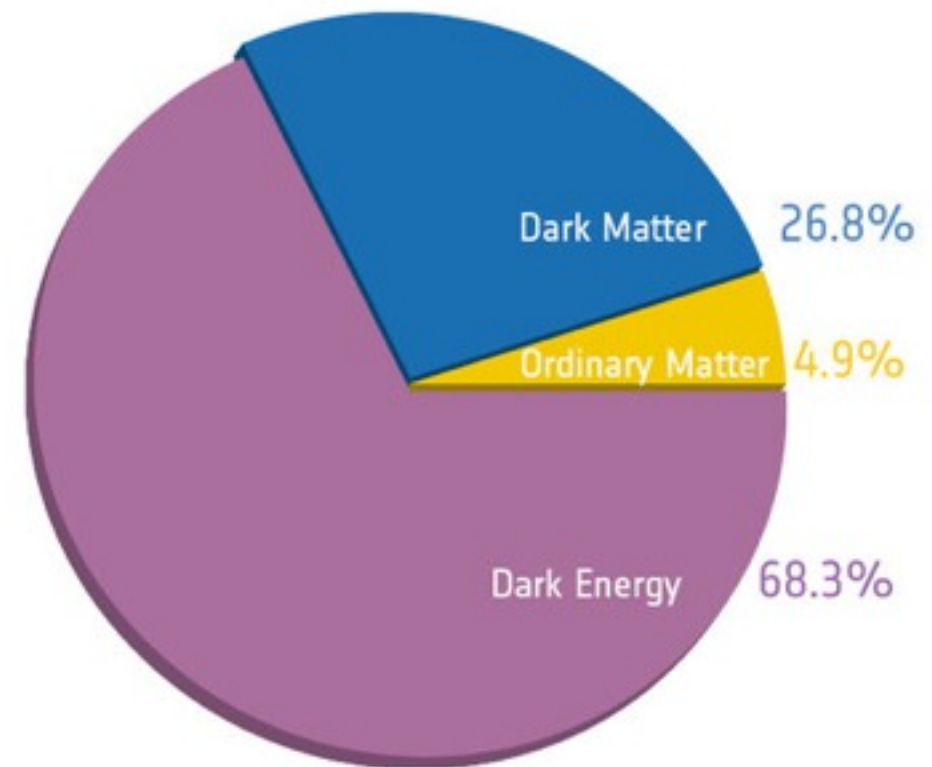
After Planck



A quick summary of the current status of cosmology



Before Planck

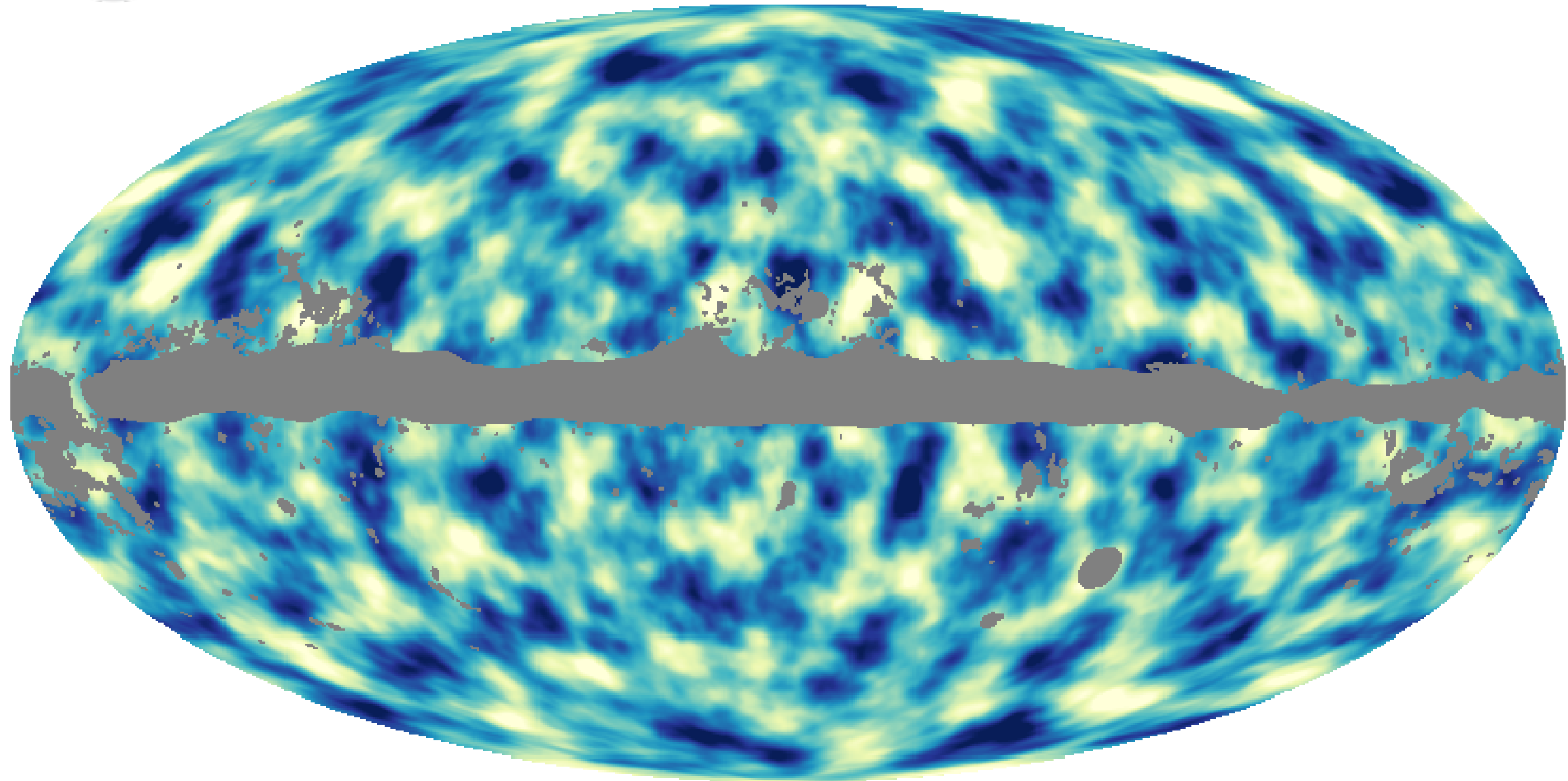


After Planck

We still have no idea what Dark Energy is



The matter in the Universe



Planck picture of the matter distribution at $z \sim 2$



Outline

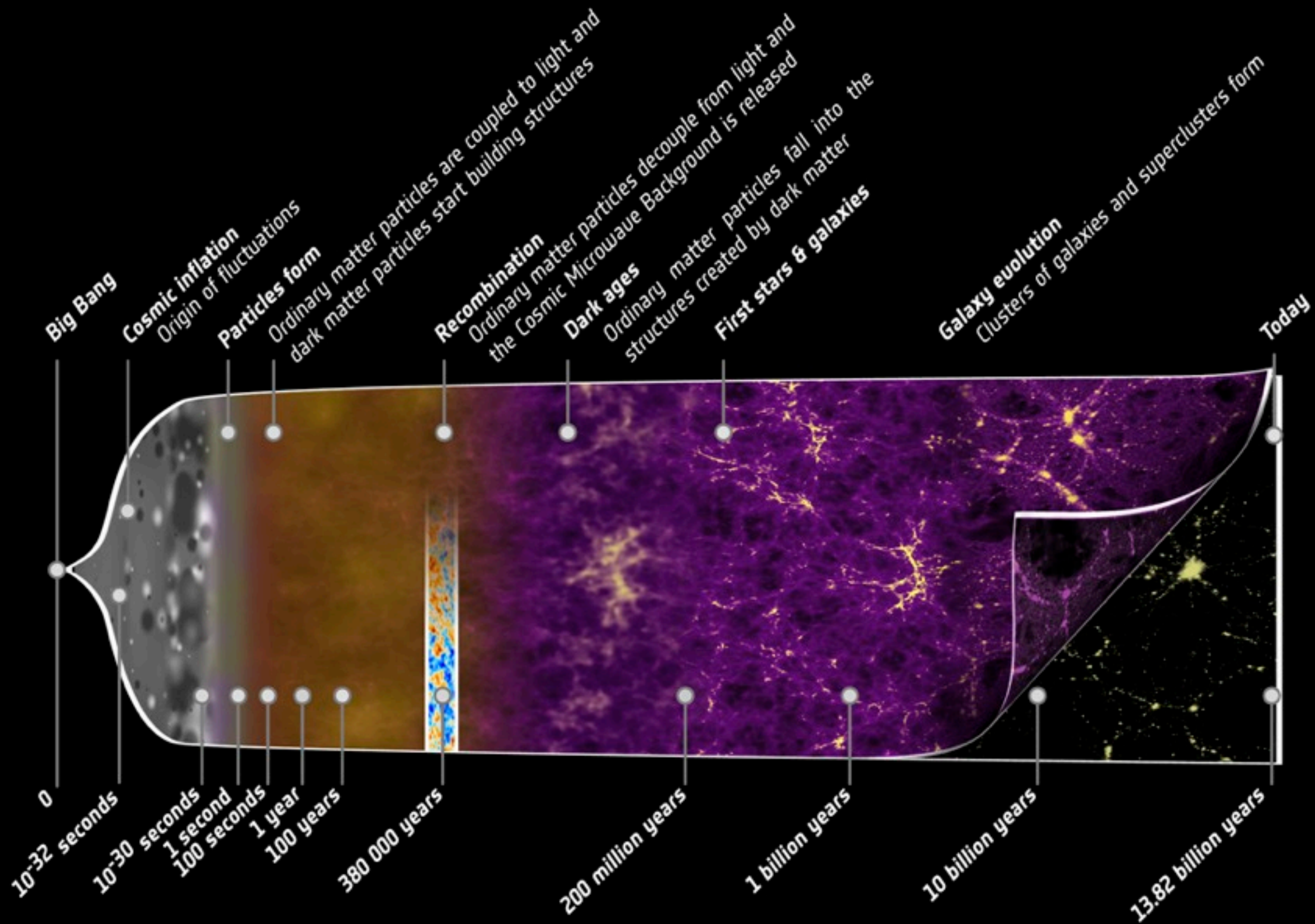
- **A few words on Planck**
- CMB lensing
- Reconstruction from Planck data
- Cosmology from CMB lensing
- Cross-correlations

The scientific results that we present today are a product of the Planck Collaboration, including individuals from more than 100 scientific institutes in Europe, the USA and Canada

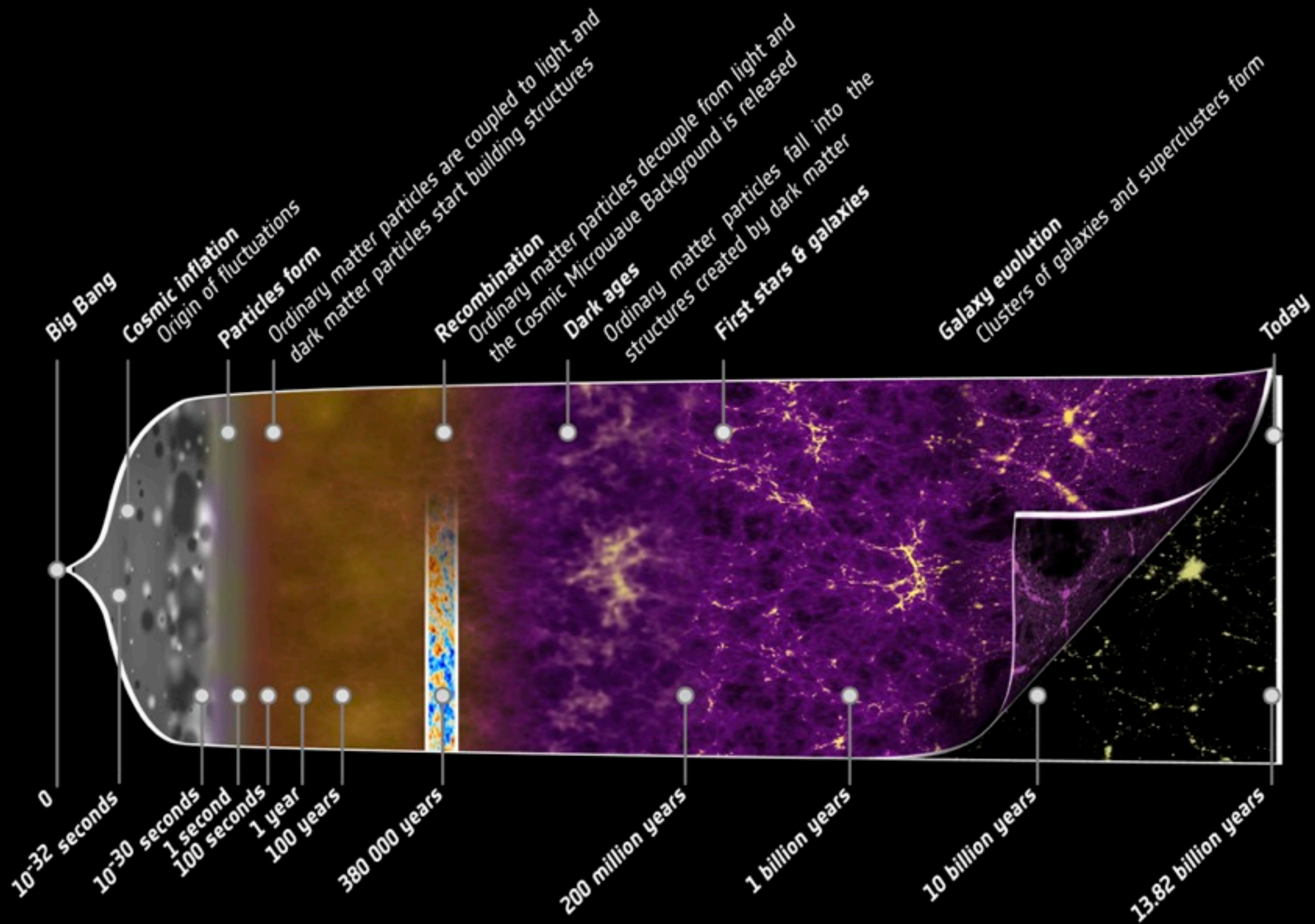


Planck is a project of the European Space Agency, with instruments provided by two scientific Consortia funded by ESA member states (in particular the lead countries: France and Italy) with contributions from NASA (USA), and telescope reflectors provided in a collaboration between ESA and a scientific Consortium led and funded by Denmark.

A (very) schematic history of our Universe



A (very) schematic history of our Universe



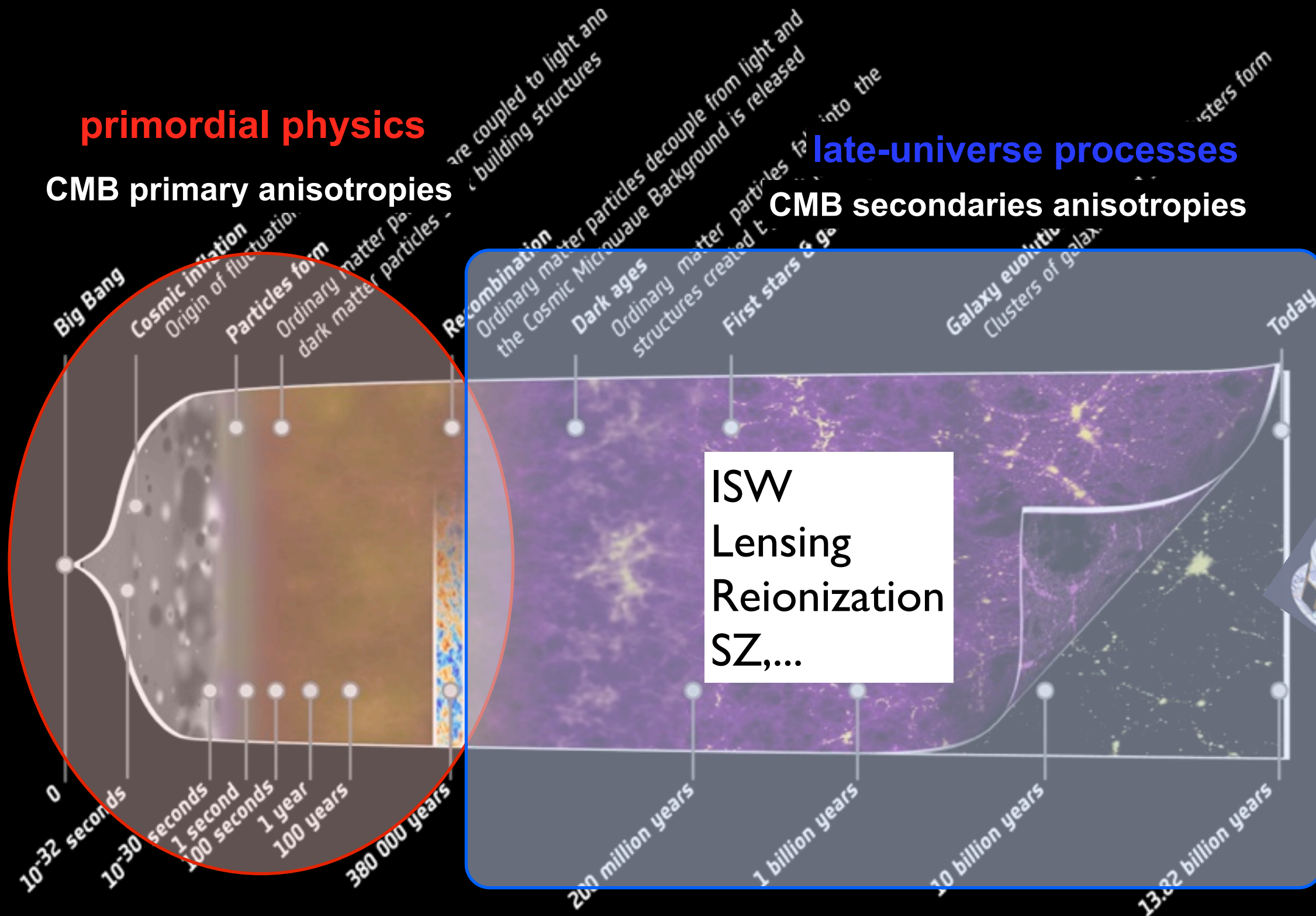
CMB: central observation in cosmology

primordial physics

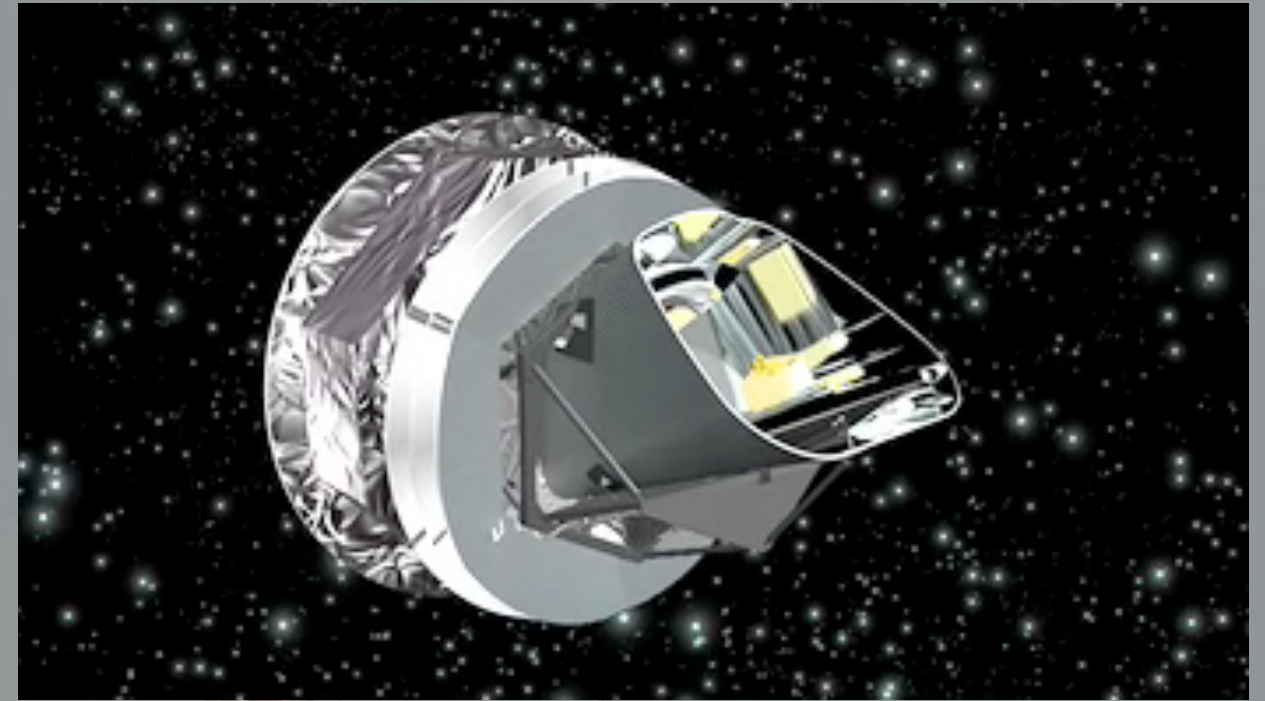
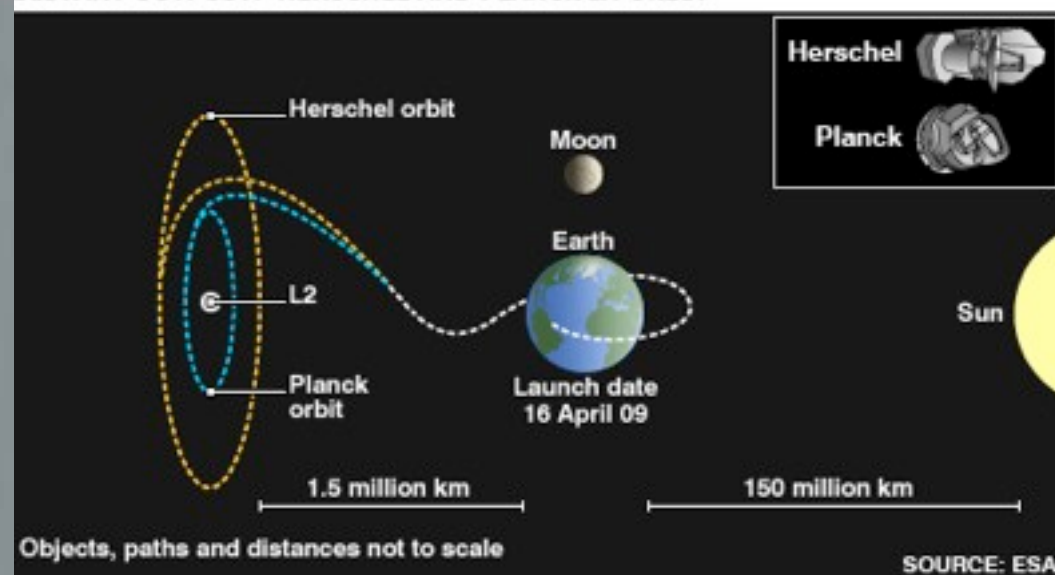
CMB primary anisotropies

late-universe processes

CMB secondaries anisotropies



DISTANT OUTPOST: HERSCHEL AND PLANCK IN ORBIT

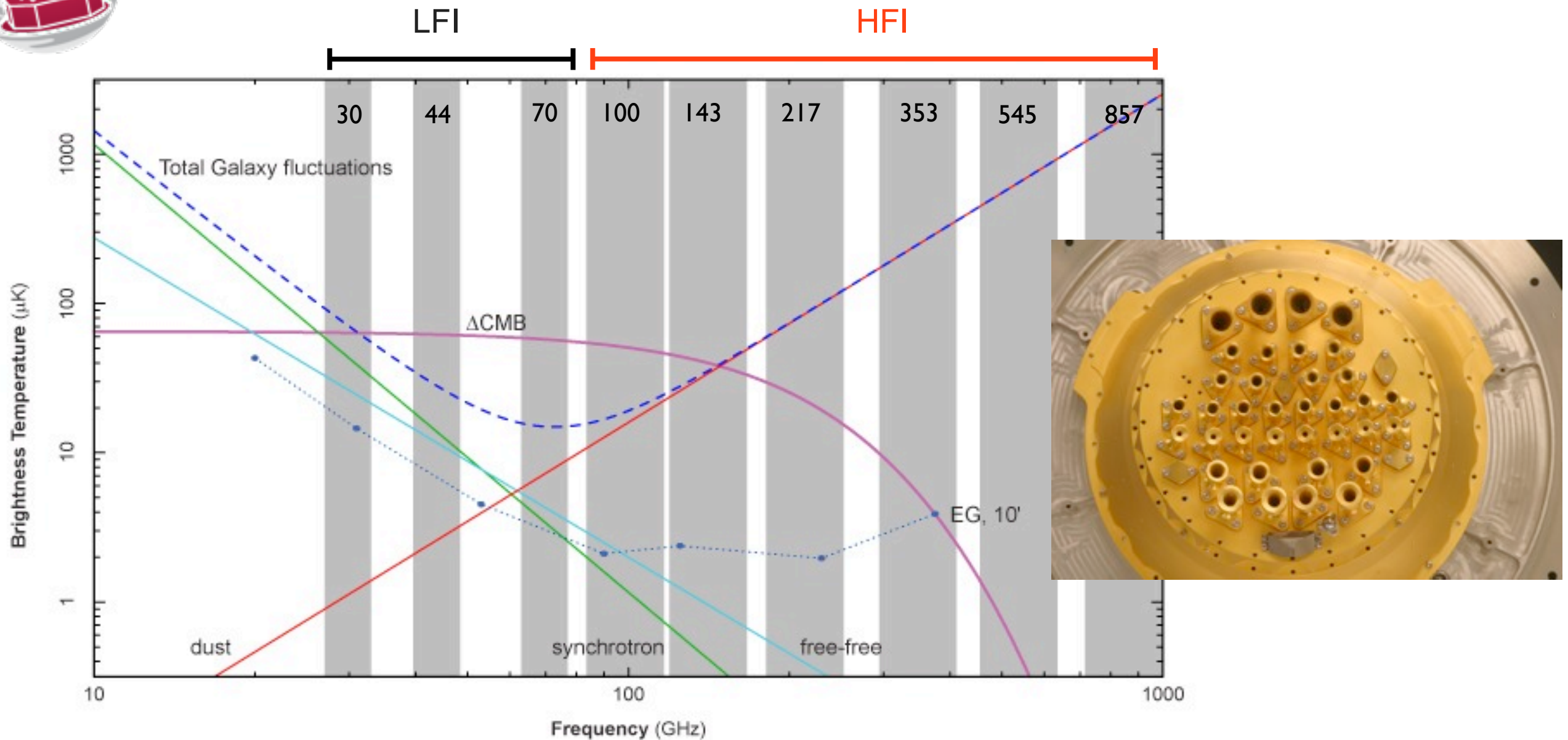


- Proposed to ESA in 1993, selected in 1996
- Launched on May 14th 2009
- First complete coverage of sky in June 2010
- Nominal mission completed in November 2010
- End of light (HFI) January 14th 2012. 32 months after launch
- March 2013: First cosmological data release
- August 2013: Departure manoeuvre from L2. 1554 days of mission. 8 LFI surveys
- Full release in 2014

Ariane 5 ECA Launch • HERSCHEL – PLANCK - May 14, 2009



Planck frequency coverage



PLANCK	LFI			HFI					
Center Freq (GHz)	30	44	70	100	143	217	353	545	857
Angular resolution (FWHM arcmin)	33	24	14	10	7.1	5.0	5.0	5	5
Sensitivity in I [$\mu\text{K.deg}$] [$\sigma_{\text{pix}} \Omega_{\text{pix}}^{1/2}$]	3.0	3.0	3.0	1.1	0,7	1.1	3.3	33	3.0

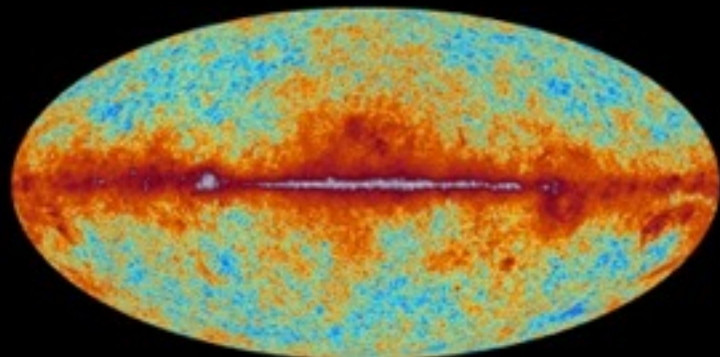


Planck frequency coverage

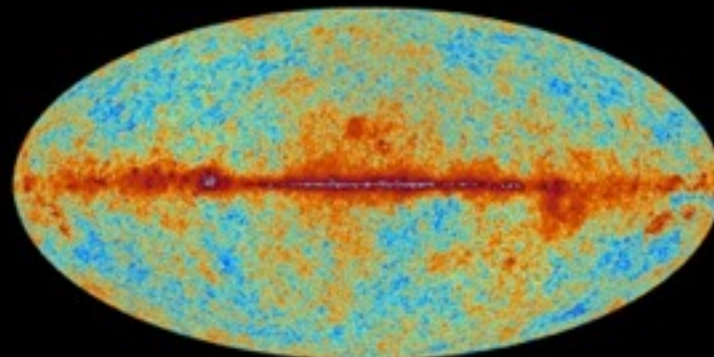


planck

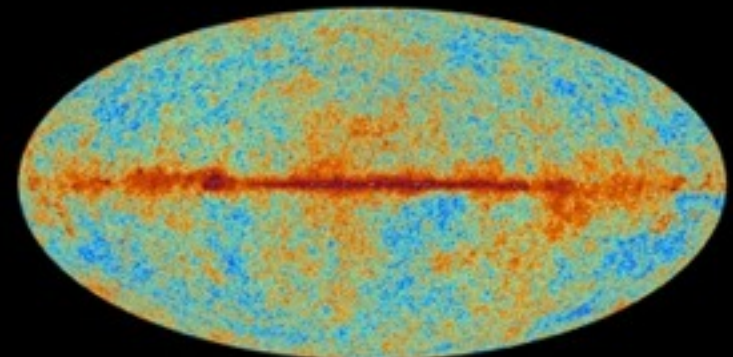
The sky as seen by Planck



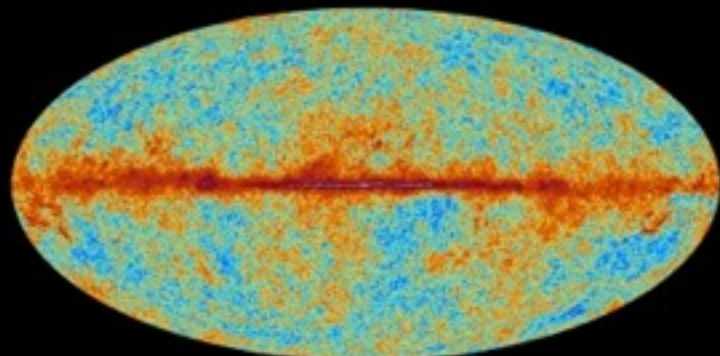
30 GHz



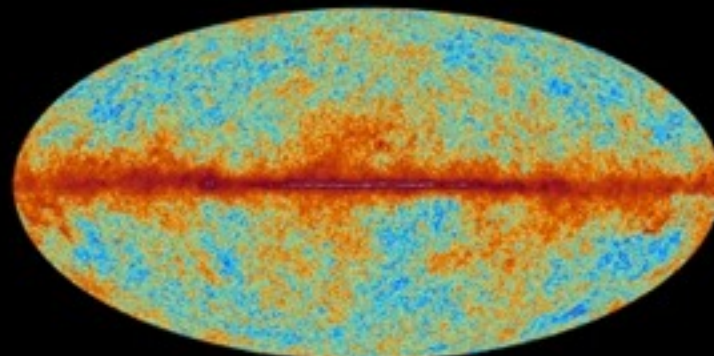
44 GHz



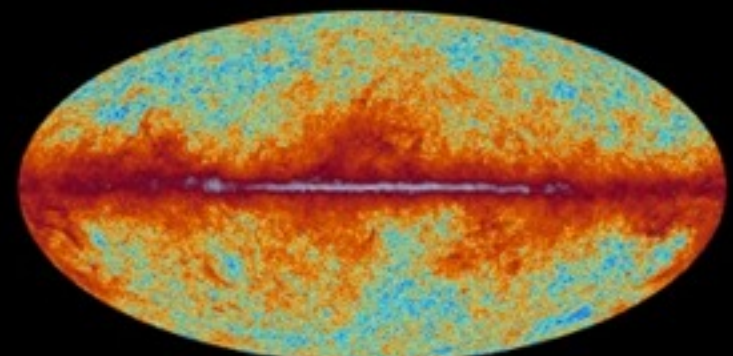
70 GHz



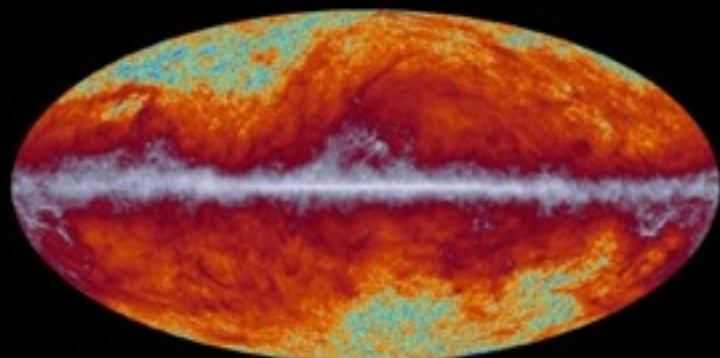
100 GHz



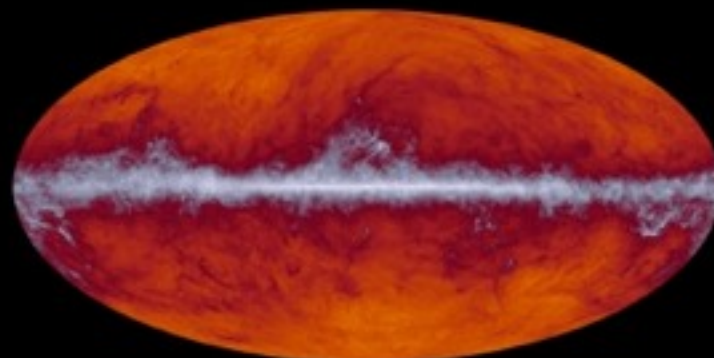
143 GHz



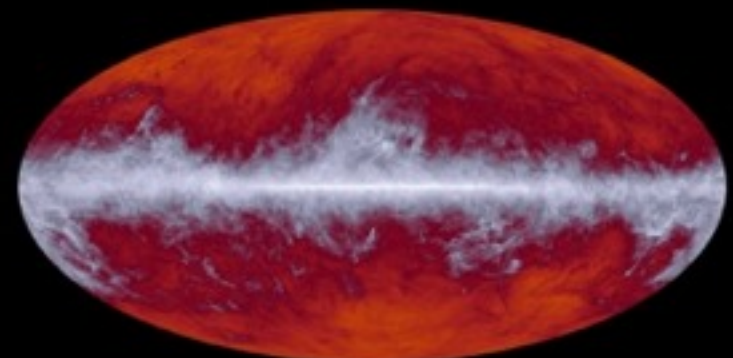
217 GHz



353 GHz



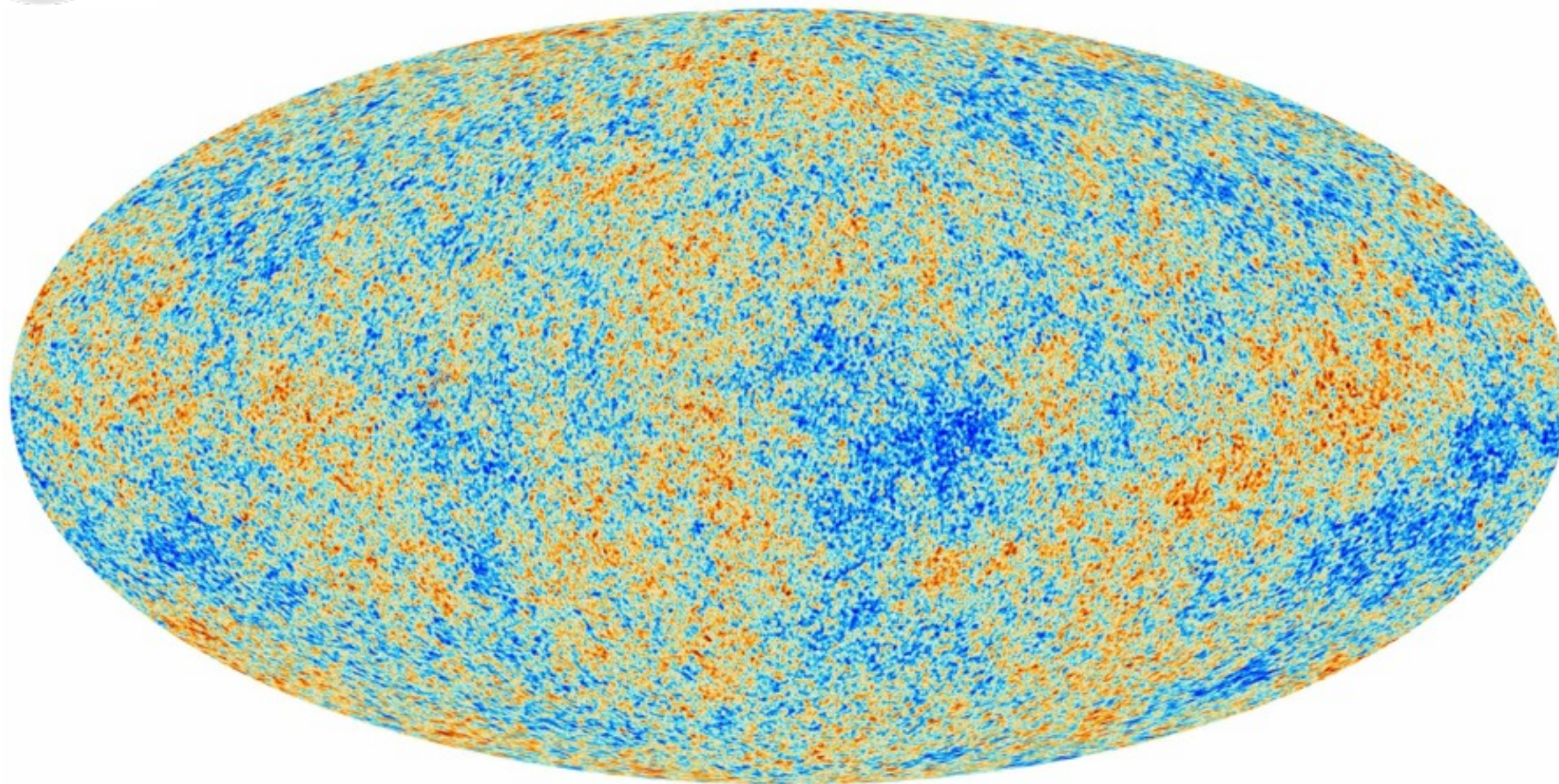
545 GHz



857 GHz



Full-sky temperature map



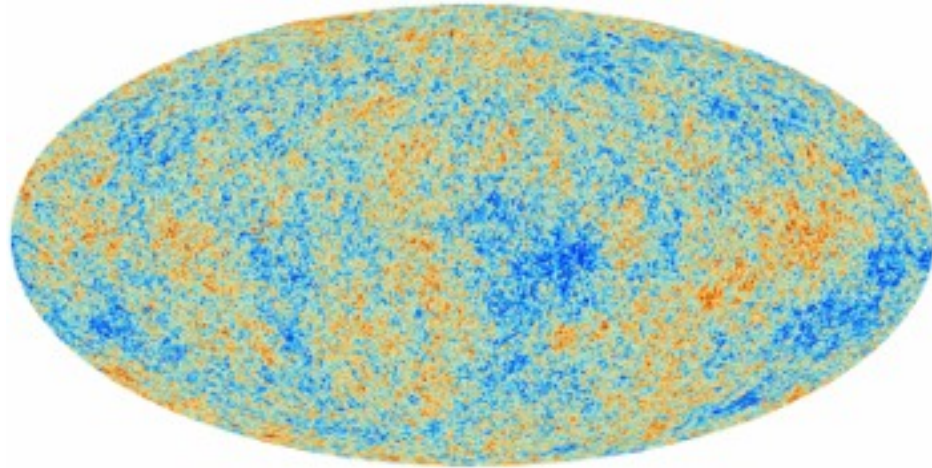
- 3% sky fraction filled with Gaussian constrained realisations
-



Cosmic Microwave Background

- Decompose the temperature on the sphere $T(\hat{n}) \longrightarrow T_{\ell m}$

$T(\hat{n})$



$T_{\ell m}$

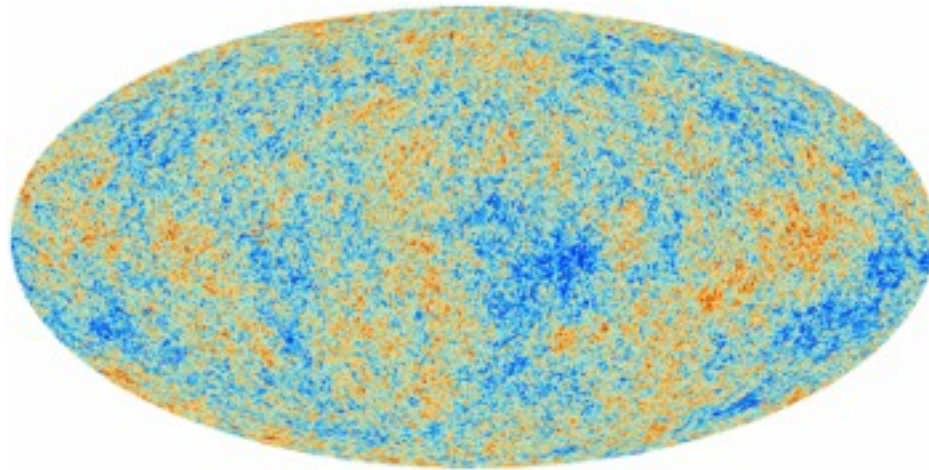
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3.48160018e-07 +5.48607128e-07j,  
8.64414116e-07 +1.58062970e-06j,  
2.32962756e-07 +1.72990879e-07j,  
2.07366735e-07 -1.48637056e-06j,  
1.33636760e-06 +1.44430207e-06j,  
-1.33047477e-06 +1.49222938e-06j,  
2.01588688e-07 +1.39367943e-08j,  
1.20185303e-06 -1.04105033e-06j,  
-1.88960308e-06 -2.69868746e-07j,  
1.06239463e-06 +4.31127048e-07j,  
3.98739296e-07 +1.19163879e-07j,  
-1.24503110e-06 -1.93401840e-06j,  
5.68052758e-07 +6.49802586e-08j,  
5.05386856e-07 -2.28955226e-07j,  
-2.60272490e-07 +2.21246718e-06j,  
-1.11889361e-06 +1.87312956e-06j,  
9.72080476e-07 -6.89214224e-07j,  
3.26351028e-07 +1.08530943e-06j,  
2.14977119e-06 -9.44341599e-07j,
```



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2.14977119e-06 -9.44341599e-07j,
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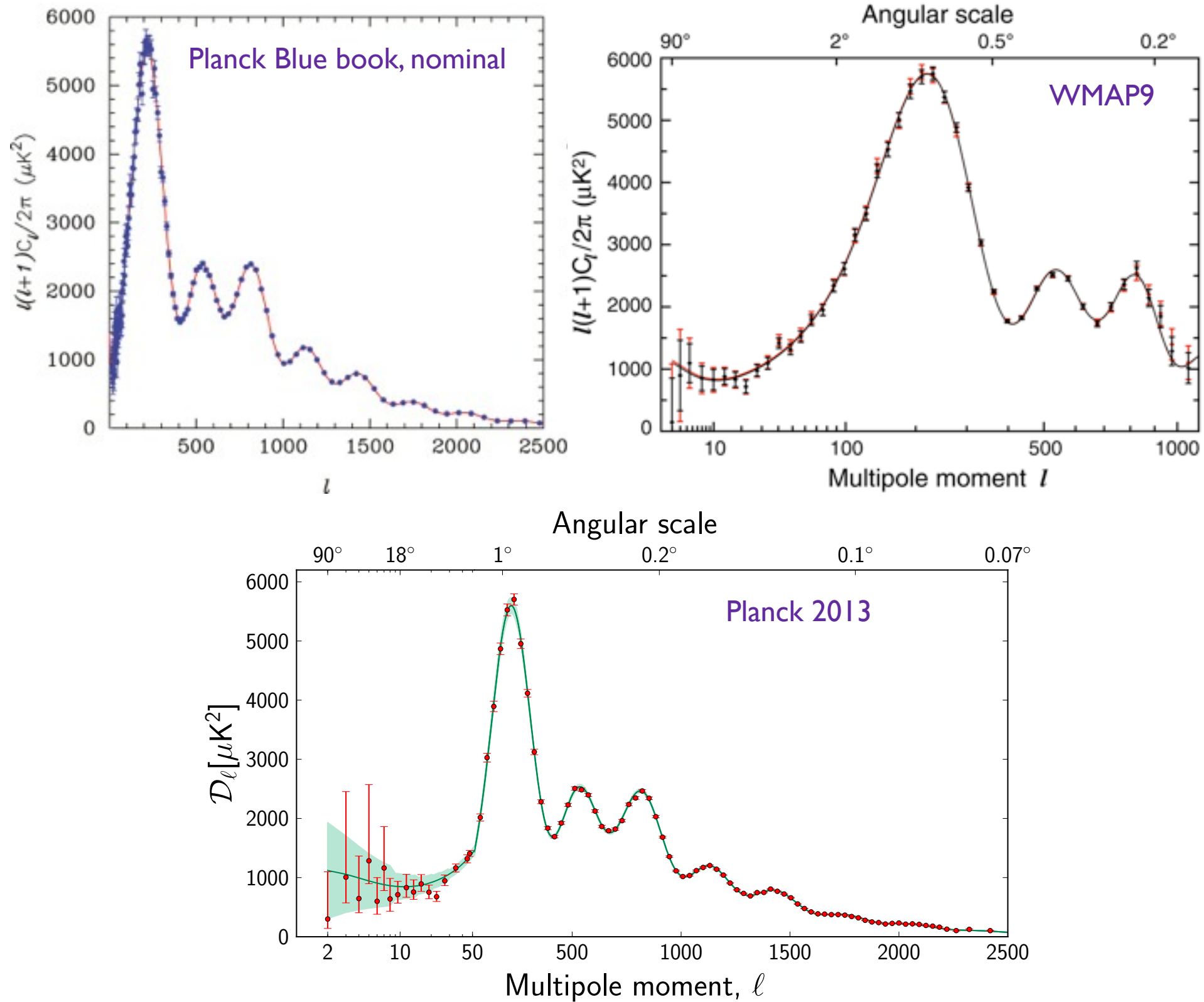
- CMB is (almost) Gaussian: all the information is in the variance $\langle t_{\ell m} t_{\ell' m'}^* \rangle = C_{\ell}$

Power spectrum can be computed: e.g. CAMB

Can be measured from observations: e.g. pseudo-Cl's $\hat{C}_{\ell} = \frac{1}{2\ell + 1} \sum_{m=-\ell}^{\ell} |T_{\ell m}|^2$



Cosmic Microwave Background



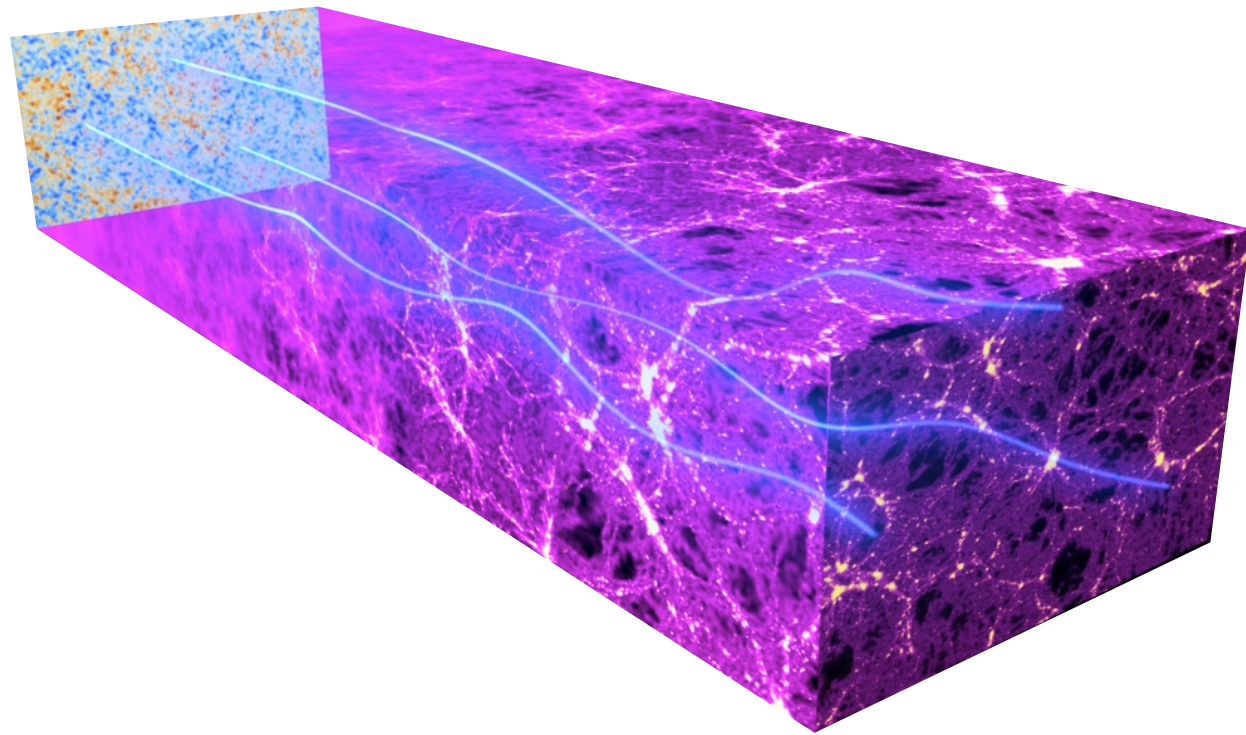


Outline

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- **CMB lensing**
- Reconstruction from Planck data
- Cosmology from CMB lensing
- Cross-correlations



CMB lensing



Typical deflection $\delta\beta$ sourced by potential Ψ

$$\Psi \sim 2 \cdot 10^{-5}$$

$$\delta\beta \sim 10^{-4}$$

Potential well size ~ 300 Mpc

Distance to last scattering surface $\sim 14\,000$ Mpc

Photons encounter ~ 50 potential wells

r.m.s deflection

$$50^{1/2} * 10^{-4} \sim 2 \text{ arcmin}$$

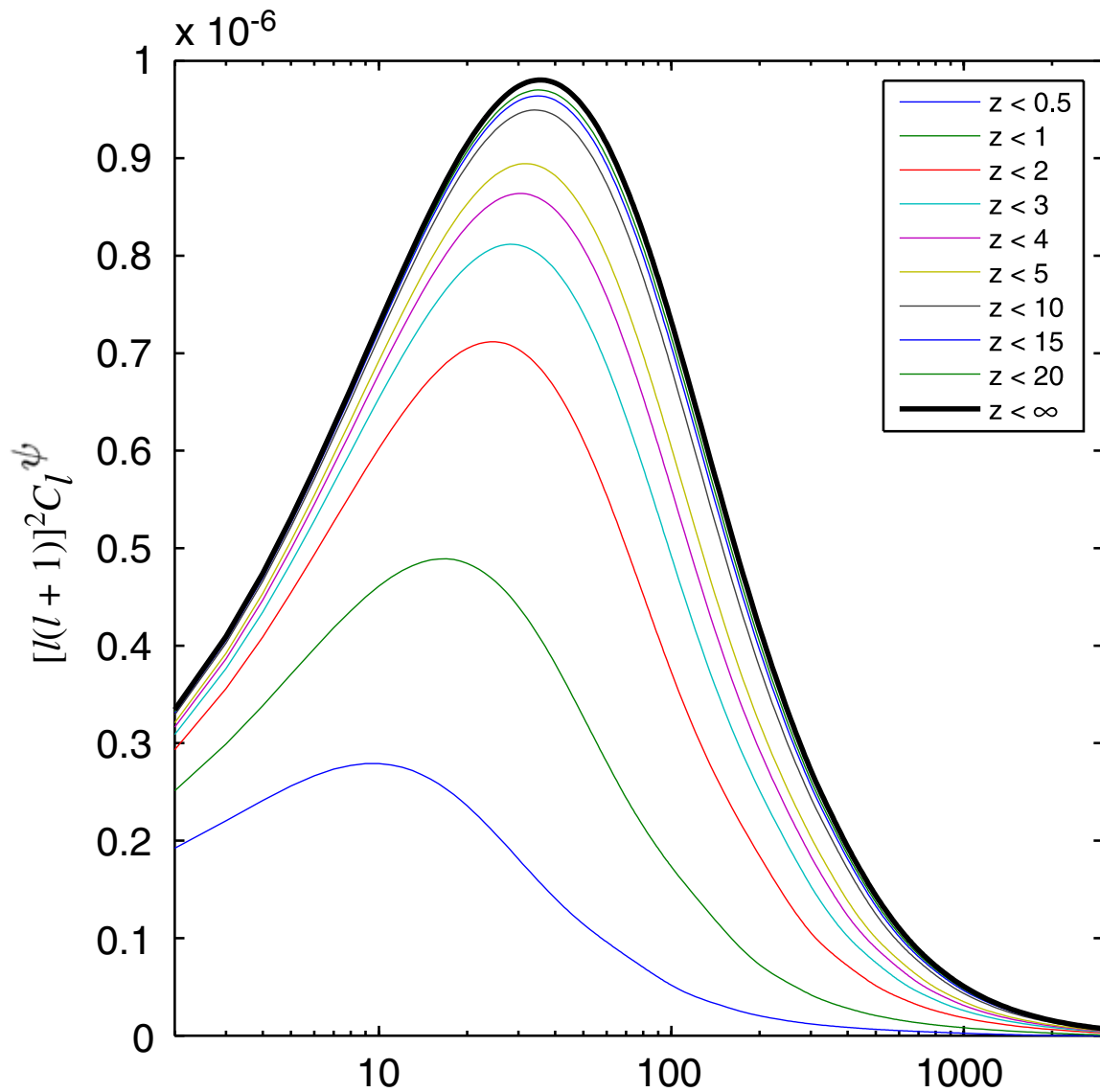
$$\Theta[\hat{\mathbf{n}}] = \tilde{\Theta}[\hat{\mathbf{n}} + \nabla\phi(\hat{\mathbf{n}})]$$

$$\phi(\hat{\mathbf{n}}) = -2 \int_0^{\chi_*} d\chi \frac{f_K(\chi_* - \chi)}{f_K(\chi_*)f_K(\chi)} \Psi(\chi\hat{\mathbf{n}}; \eta_0 - \chi).$$

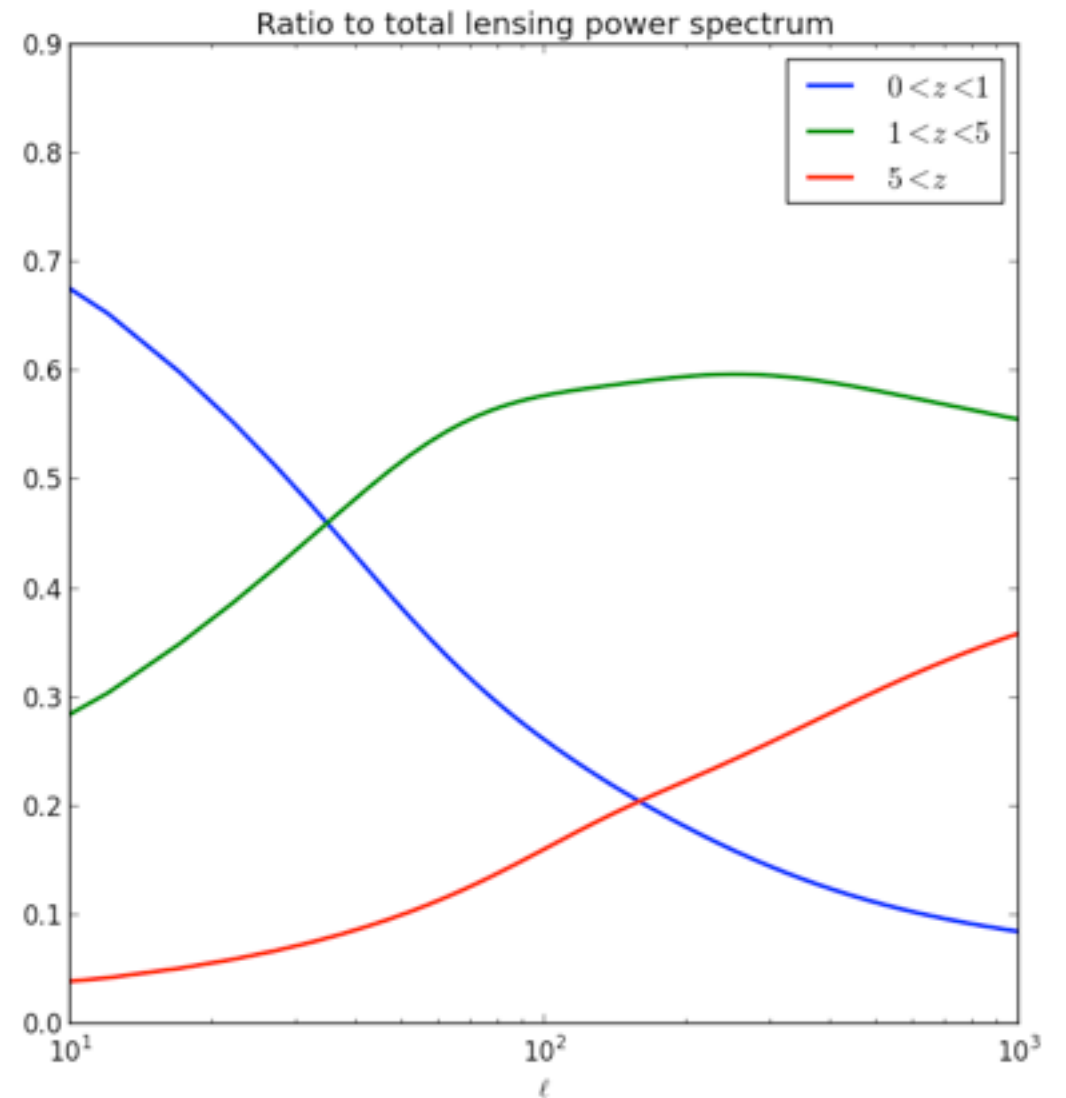


The lensing potential

$$\phi(\hat{n}) = -2 \int_0^{\chi_*} d\chi \frac{f_K(\chi_* - \chi)}{f_K(\chi_*)f_K(\chi)} \Psi(\chi \hat{n}; \eta_0 - \chi).$$



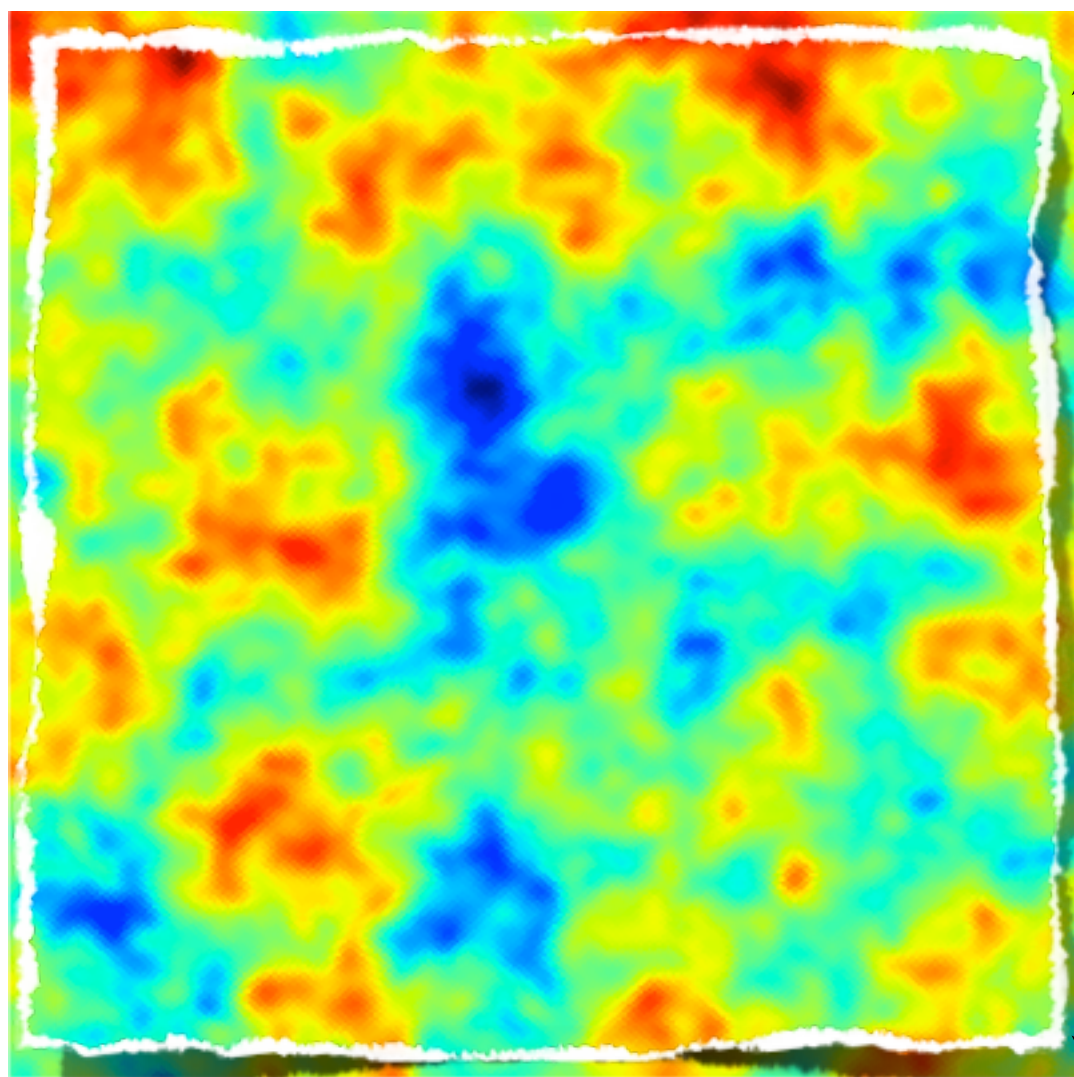
Lewis & Challinor, 2006





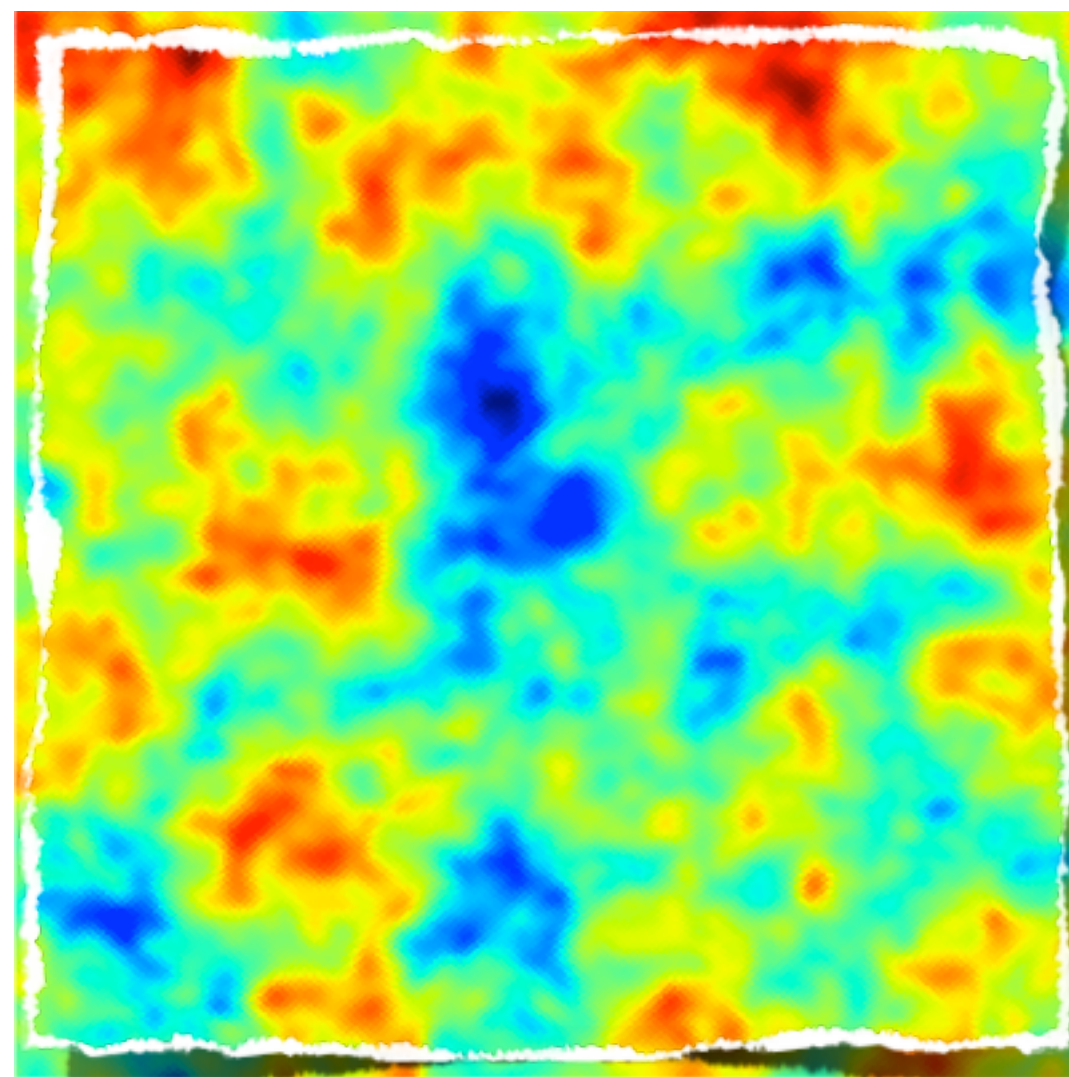
CMB lensing

Deflections are about 2 arcmin



Unlensed

6°

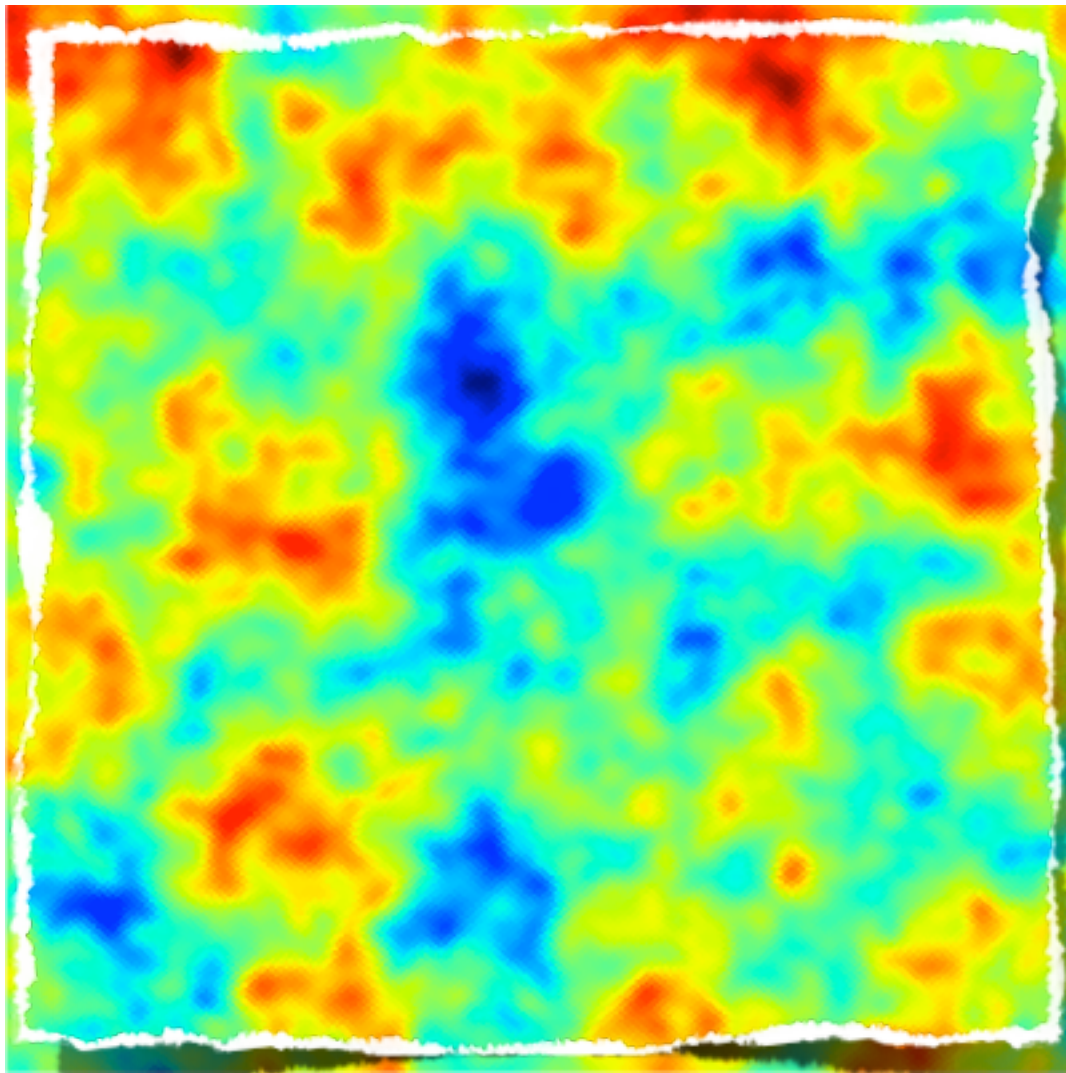


Lensed



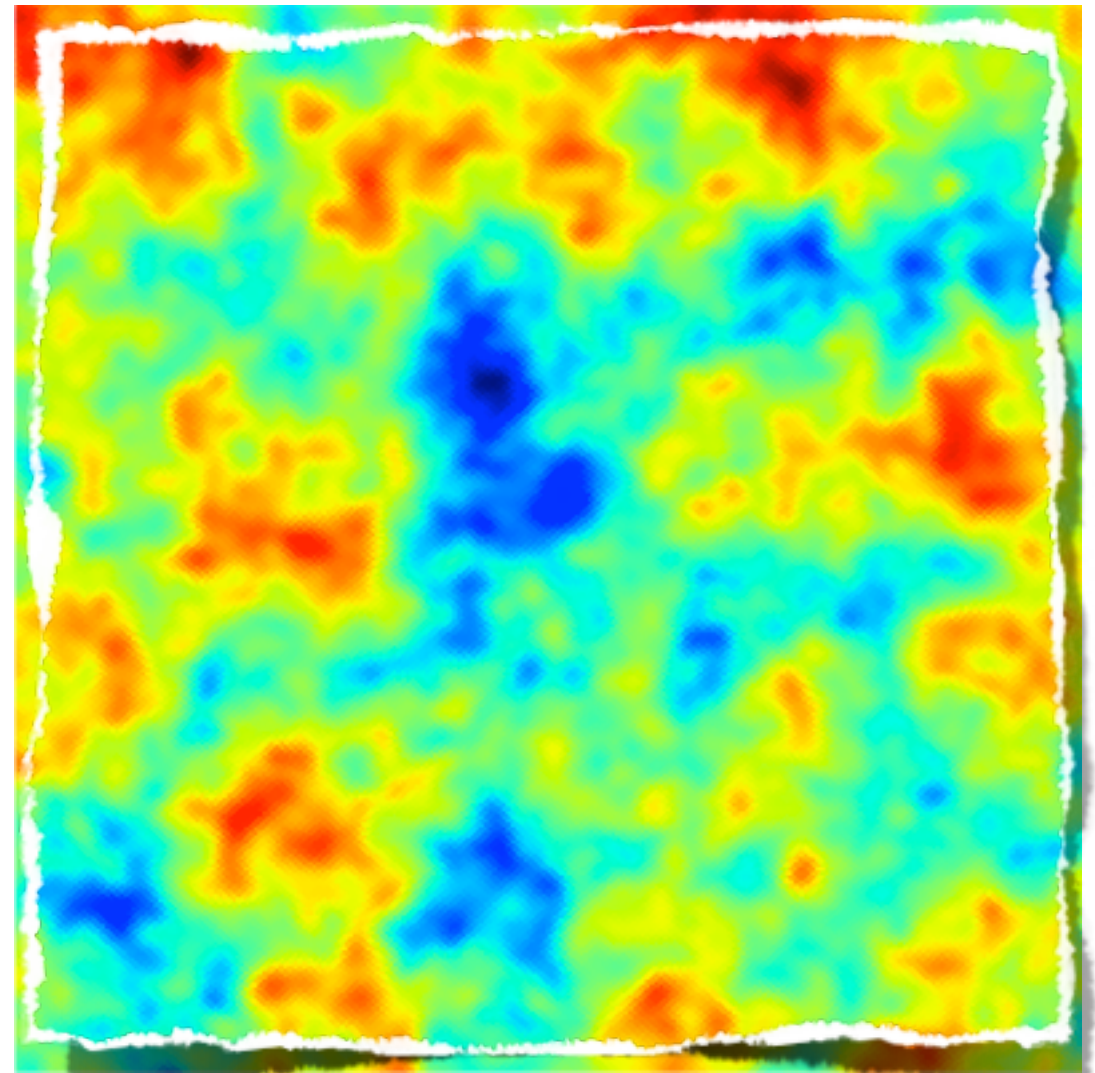
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6°

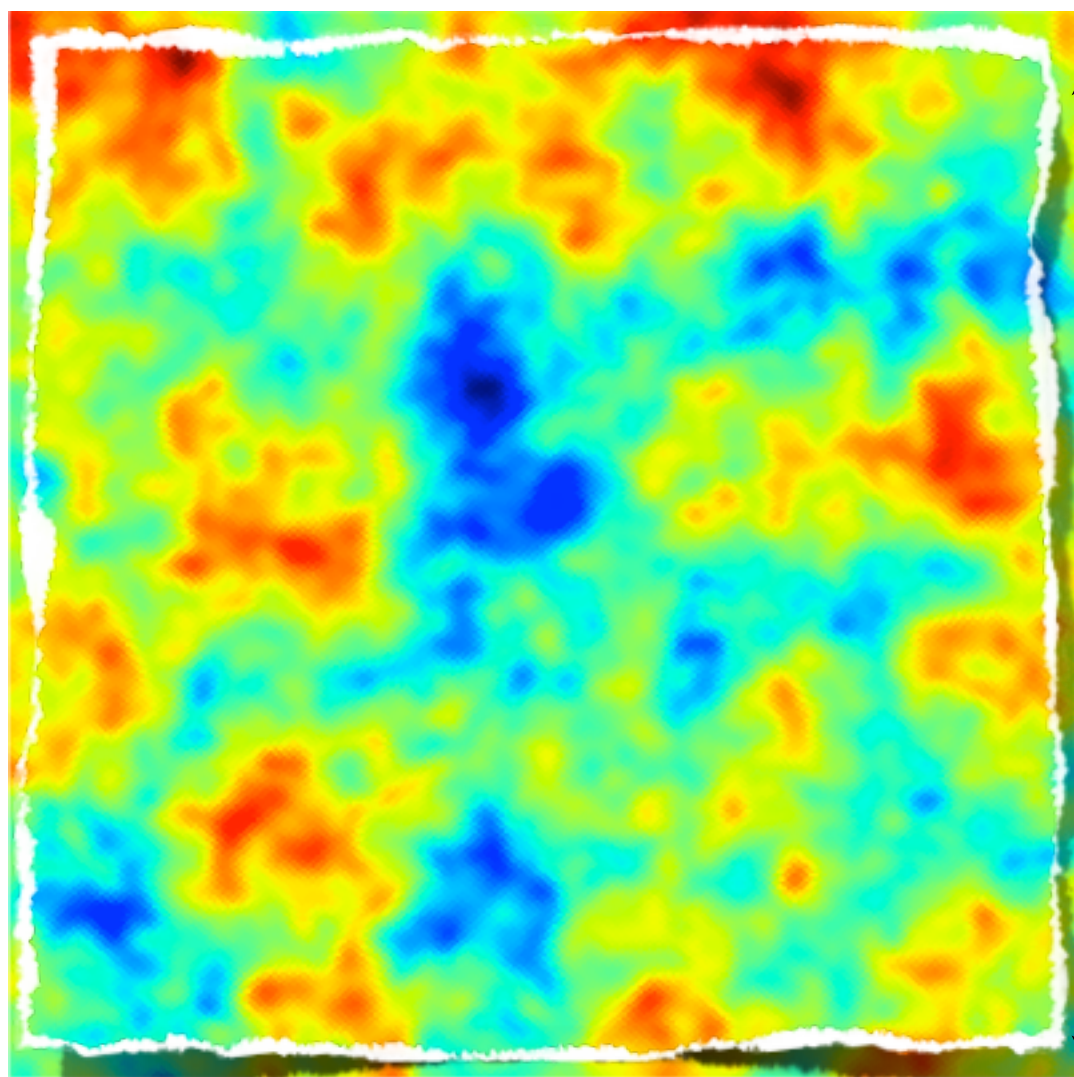


Unlensed



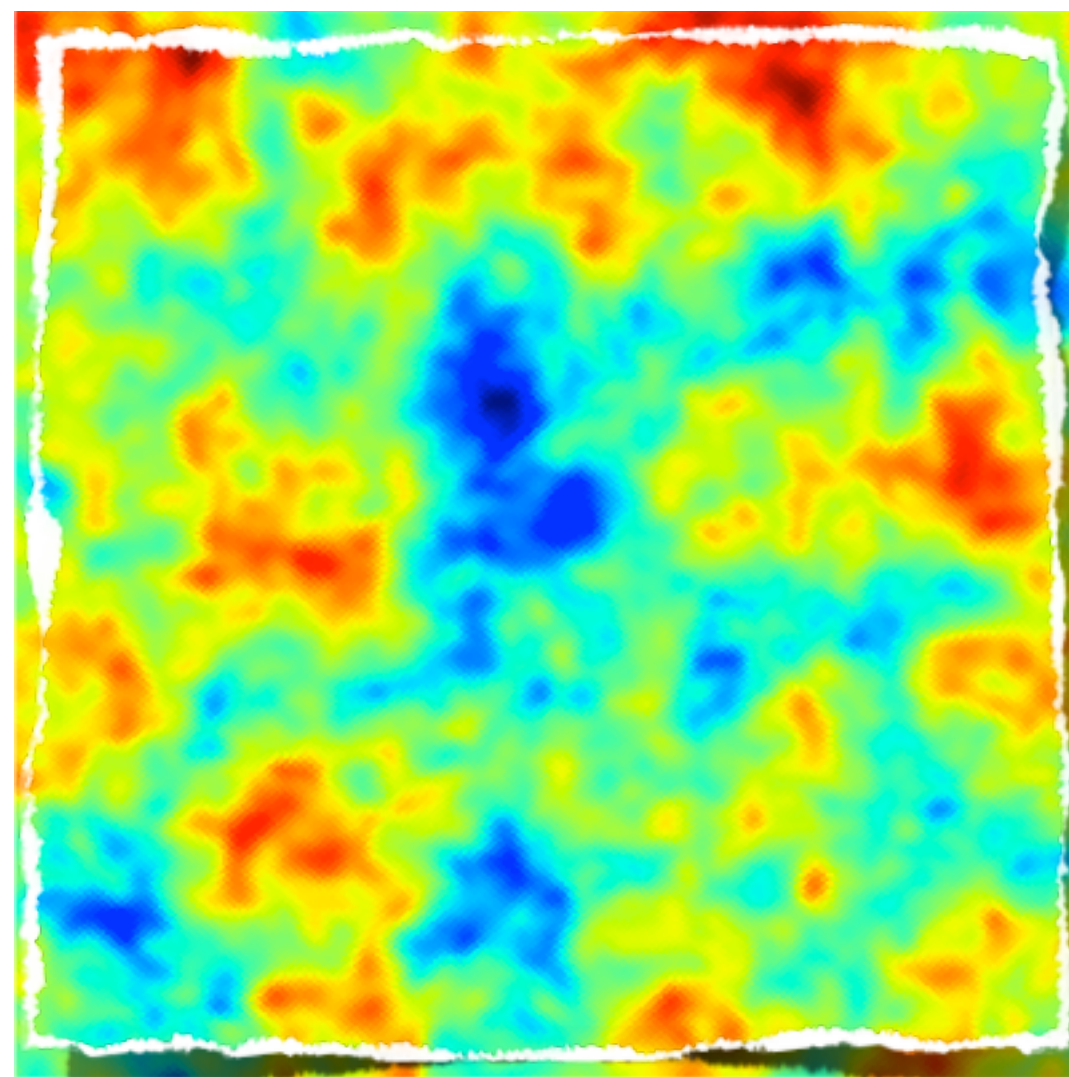
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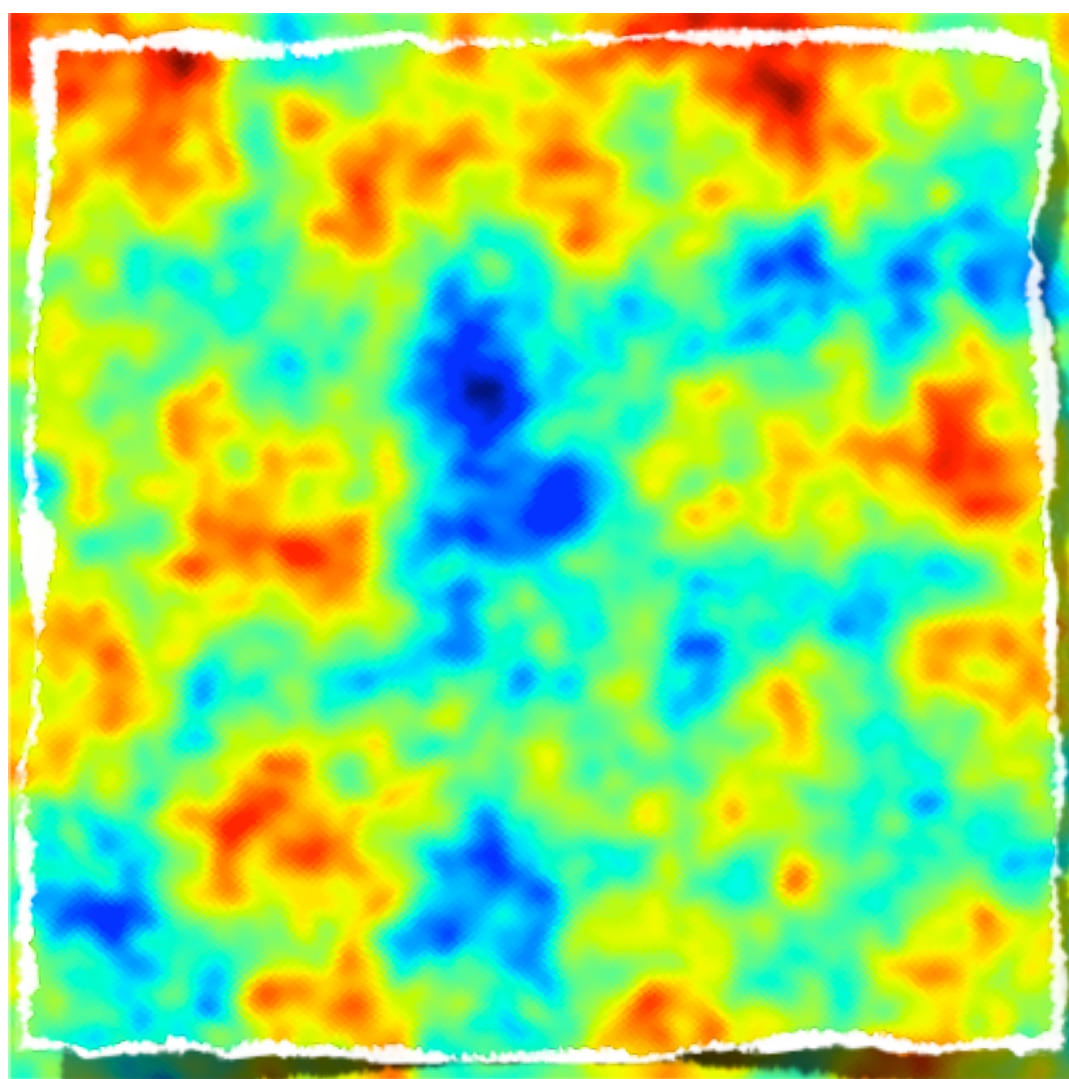


Lensed



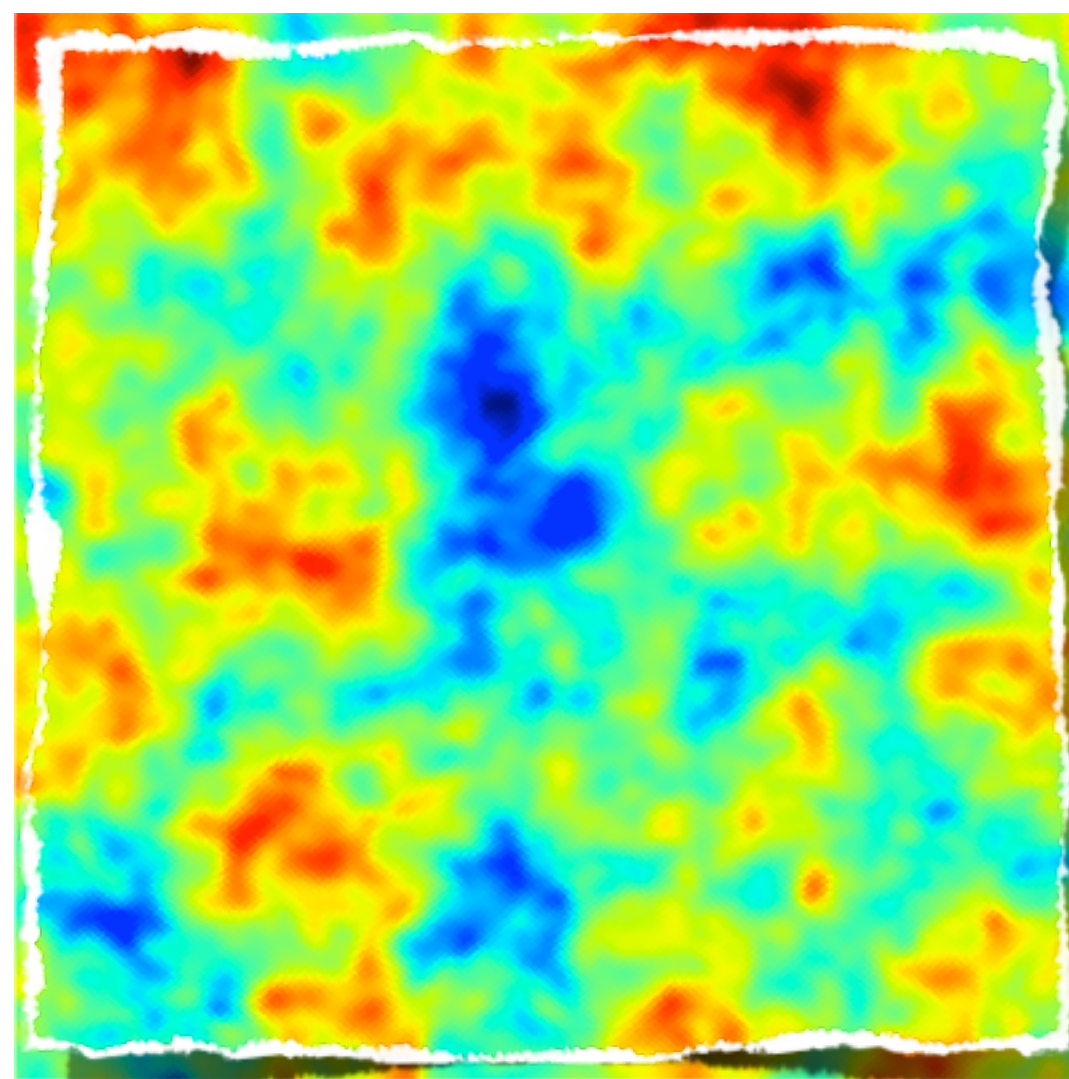
CMB lensing

Deflections are about 2 arcmin



Unlensed

6°



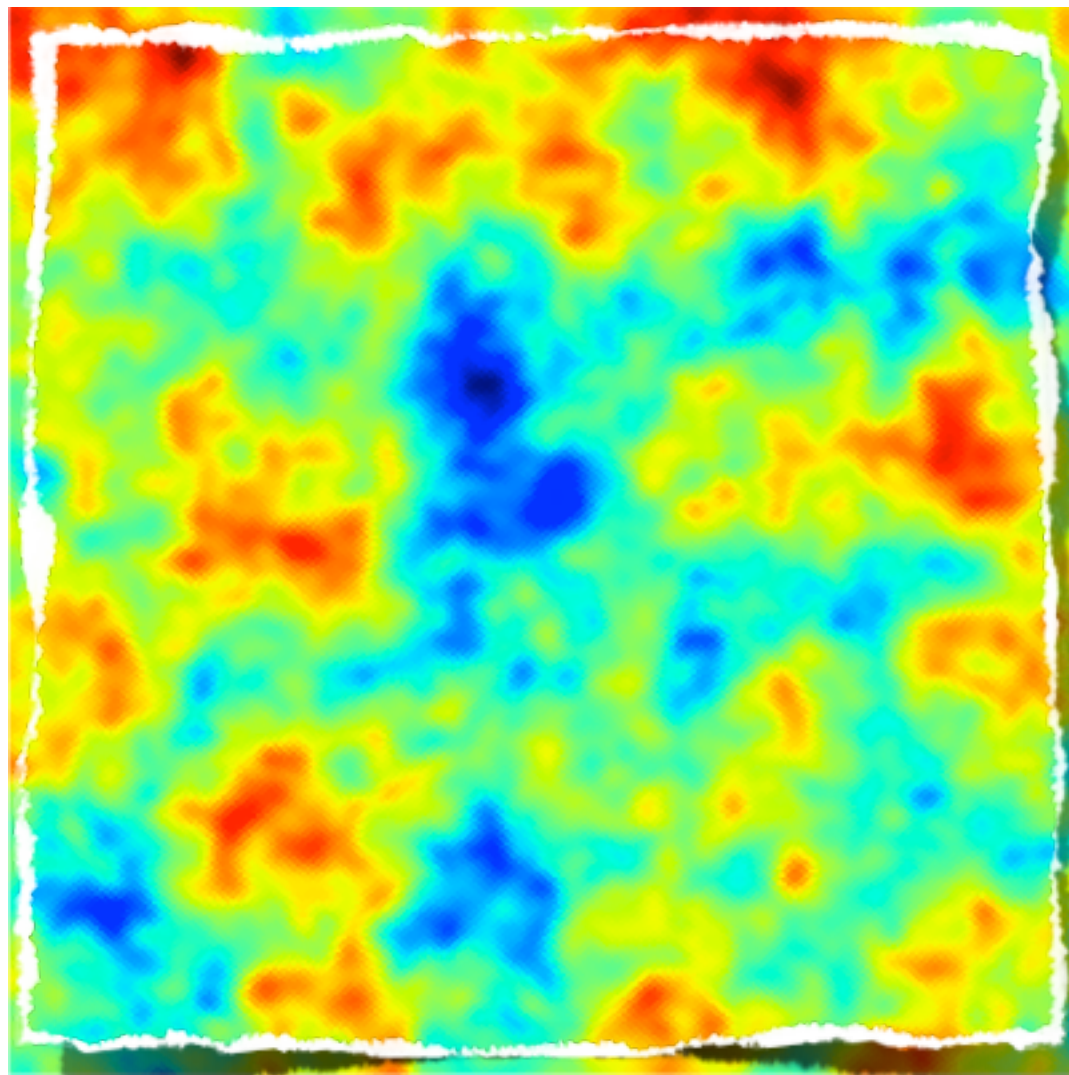
Lensed

Deflections are correlated on the degree scale



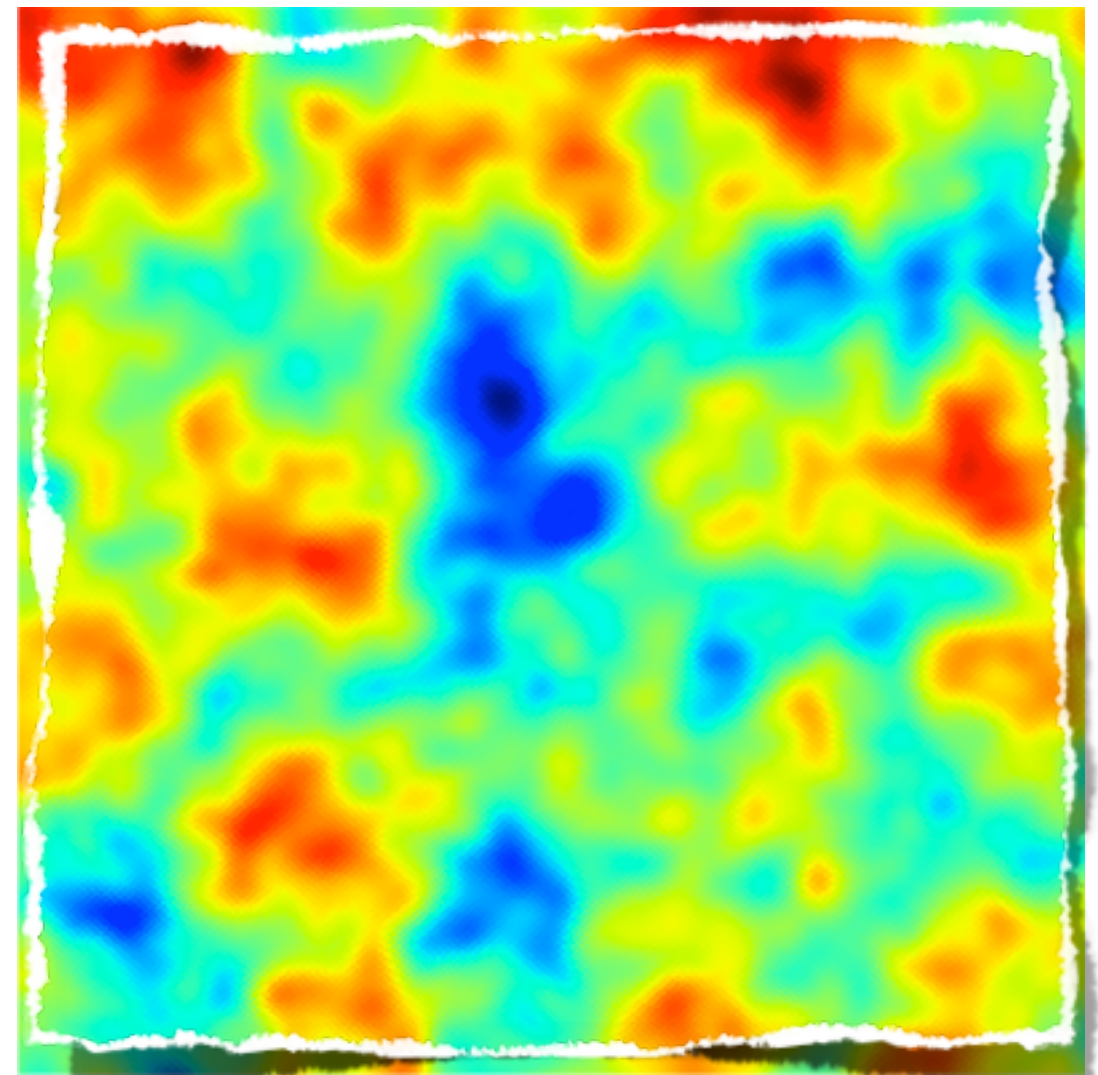
CMB lensing

Deflections are about 2 arcmin



Unlensed

6°



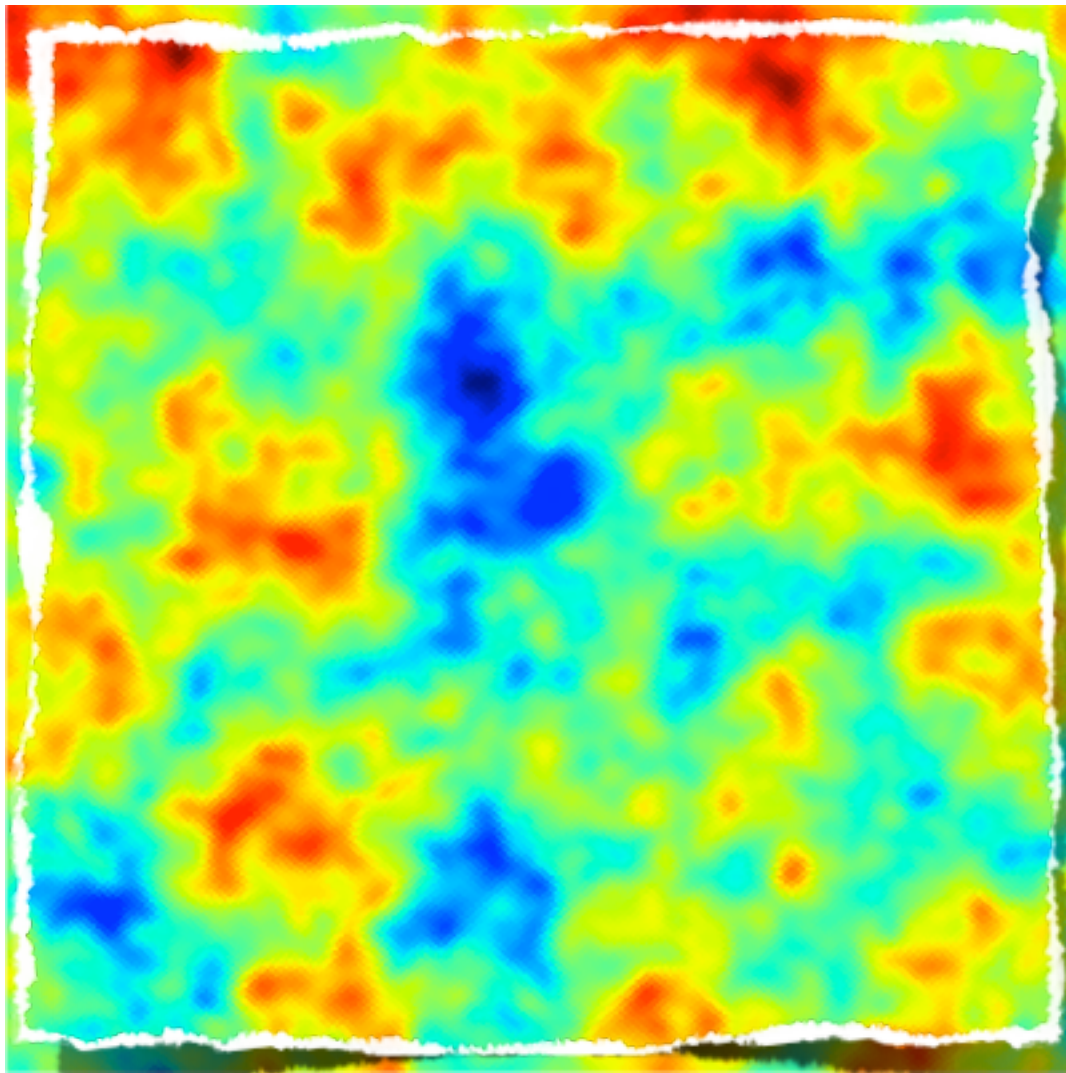
Lensed,
beamed

Deflections are correlated on the degree scale



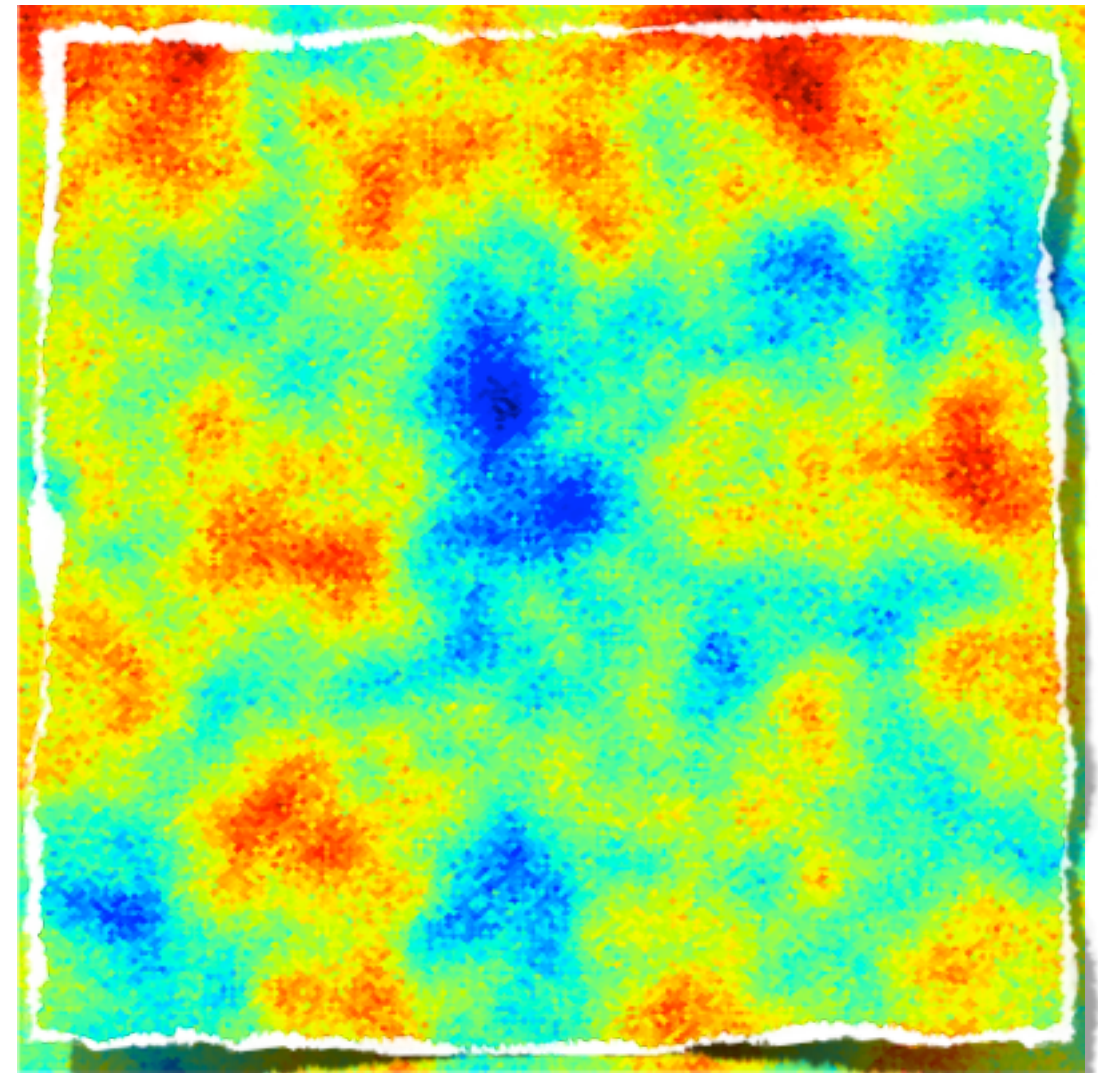
CMB lensing

Deflections are about 2 arcmin



Unlensed

6°



Lensed,
beamed, noised

Deflections are correlated on the degree scale



Impact on CMB

- CMB lensing induces temperature-gradient correlations

$$\Theta[\hat{\mathbf{n}}] = \tilde{\Theta}[\hat{\mathbf{n}} + \nabla\phi(\hat{\mathbf{n}})] \approx \tilde{\Theta}[\hat{\mathbf{n}}] + \nabla\phi[\hat{\mathbf{n}}] \nabla\tilde{\Theta}[\hat{\mathbf{n}}] + \dots$$



Impact on CMB

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$$\Theta[\hat{\mathbf{n}}] = \tilde{\Theta}[\hat{\mathbf{n}} + \nabla\phi(\hat{\mathbf{n}})] \approx \tilde{\Theta}[\hat{\mathbf{n}}] + \nabla\phi[\hat{\mathbf{n}}] \nabla\tilde{\Theta}[\hat{\mathbf{n}}] + \dots$$

- CMB lensing induces statistical anisotropies

$$\langle T_{l_1 m_1} T_{l_2 m_2}^* \rangle = C_{l_1} \delta_{l_1 l_2} \delta_{m_1 m_2}$$



Impact on CMB

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$$\langle T_{\ell_1 m_1} T_{\ell_2 m_2}^* \rangle = C_{\ell_1} \delta_{\ell_1 \ell_2} \delta_{m_1 m_2} + \sum_{LM} \sum_{\ell_1 m_1, \ell_2 m_2} (-1)^M \begin{pmatrix} \ell_1 & \ell_2 & L \\ m_1 & m_2 & -M \end{pmatrix} W_{\ell_1 \ell_2 L}^\phi \phi_{LM}$$



Impact on CMB

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$$\Theta[\hat{\mathbf{n}}] = \tilde{\Theta}[\hat{\mathbf{n}} + \nabla\phi(\hat{\mathbf{n}})] \approx \tilde{\Theta}[\hat{\mathbf{n}}] + \nabla\phi[\hat{\mathbf{n}}] \nabla\tilde{\Theta}[\hat{\mathbf{n}}] + \dots$$

- CMB lensing induces statistical anisotropies

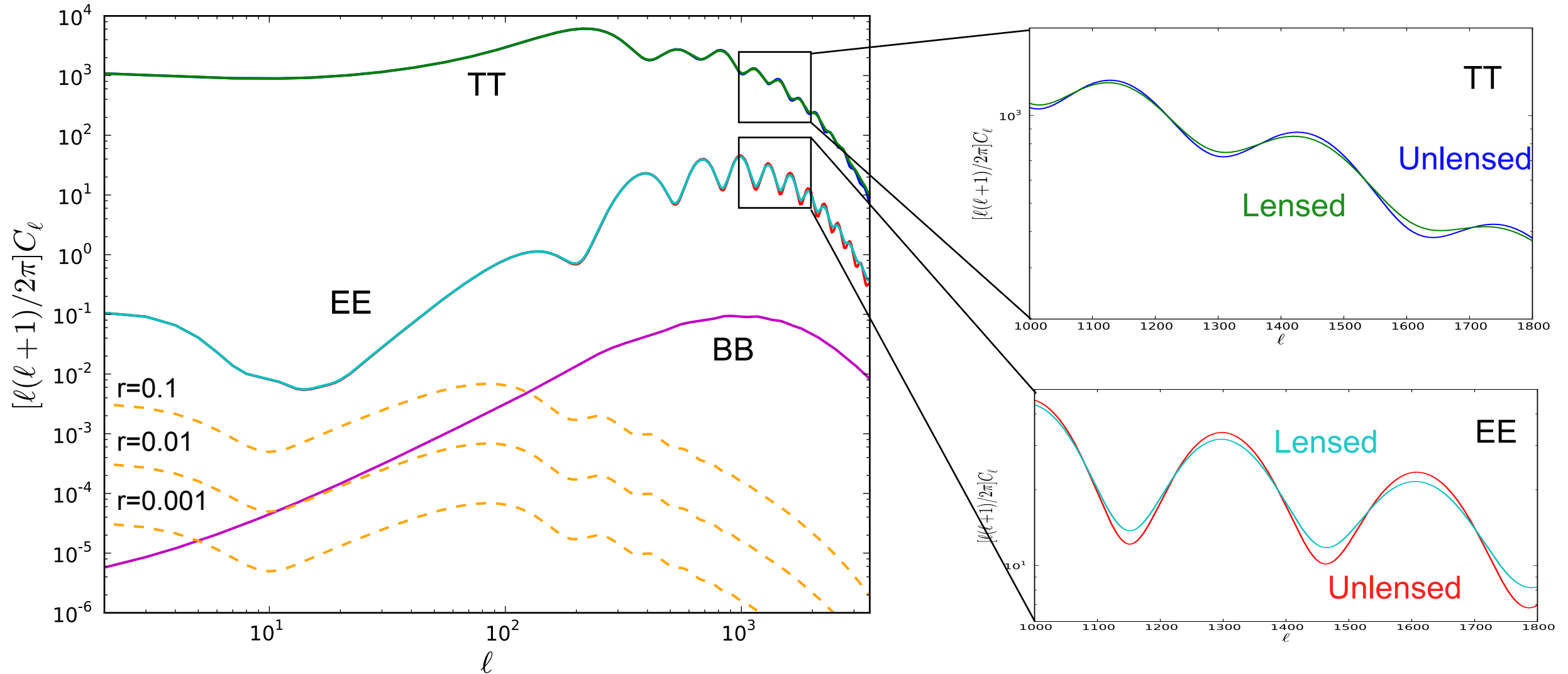
$$\langle T_{\ell_1 m_1} T_{\ell_2 m_2}^* \rangle = C_{\ell_1} \delta_{\ell_1 \ell_2} \delta_{m_1 m_2} + \sum_{LM} \sum_{\ell_1 m_1, \ell_2 m_2} (-1)^M \begin{pmatrix} \ell_1 & \ell_2 & L \\ m_1 & m_2 & -M \end{pmatrix} W_{\ell_1 \ell_2 L}^\phi \phi_{LM}$$

$$W_{\ell_1 \ell_2 L}^\phi = -\sqrt{\frac{(2\ell_1 + 1)(2\ell_2 + 1)(2L + 1)}{4\pi}} \sqrt{L(L + 1)\ell_1(\ell_1 + 1)} \\ \times C_{\ell_1}^{TT} \left(\frac{1 + (-1)^{\ell_1 + \ell_2 + L}}{2} \right) \begin{pmatrix} \ell_1 & \ell_2 & L \\ 1 & 0 & -1 \end{pmatrix} + (\ell_1 \leftrightarrow \ell_2). \quad (6)$$



Impact on anisotropies power spectra

$$C_\ell \sim (1 - \alpha_\ell)\tilde{C}_\ell + \sum_{\ell_1 \ell_2} C_{\ell_1}^{\phi\phi} \tilde{C}_{\ell_2} F_{\ell\ell_1\ell_2}$$

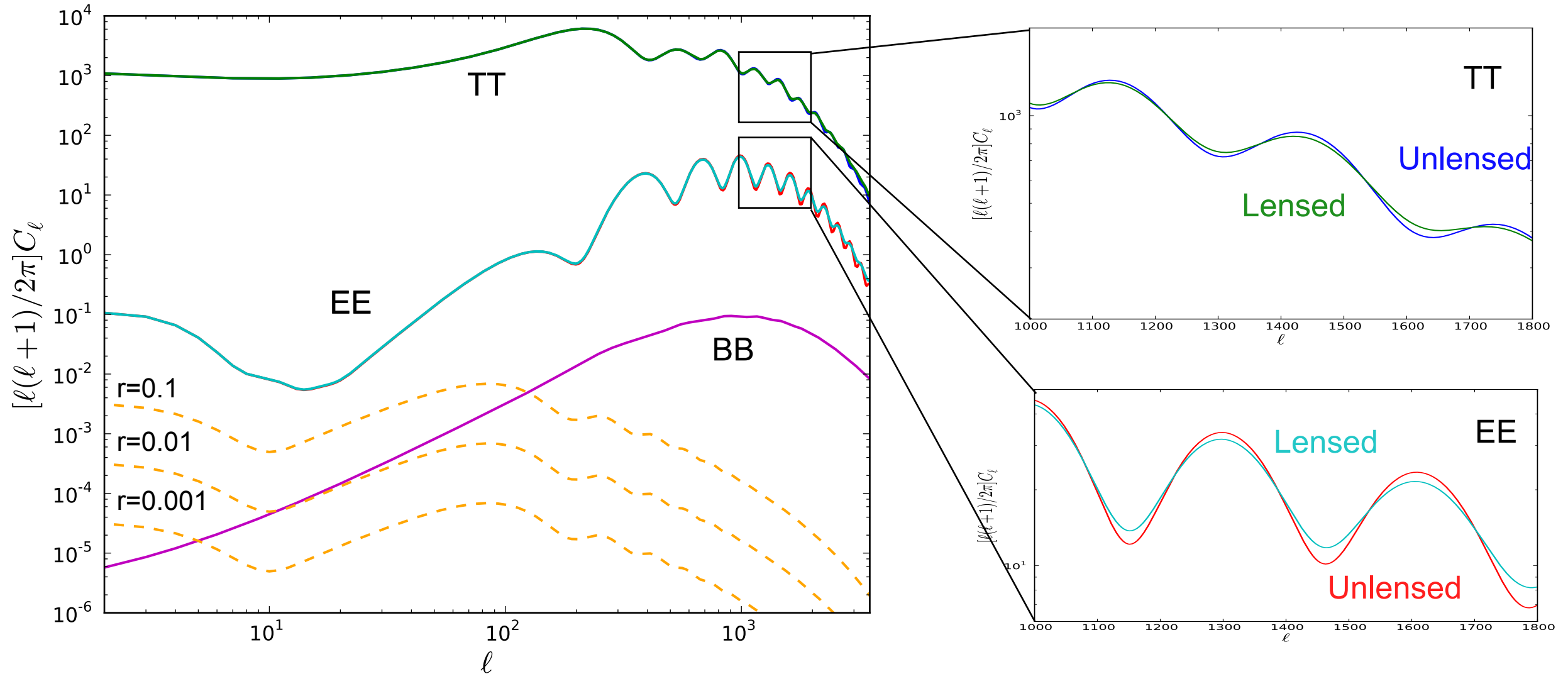


**1) Lensing can also be detected in TT
~10 sigma with Planck2013**



Impact on anisotropies power spectra

$$C_\ell \sim (1 - \alpha_\ell)\tilde{C}_\ell + \sum_{\ell_1\ell_2} C_{\ell_1}^{\phi\phi}\tilde{C}_{\ell_2}F_{\ell\ell_1\ell_2}$$



**2) Multipoles become correlated.
Lensing induced non-Gaussian covariance**

ABL, Smith, Hu 2012



Lensing reconstruction

- CMB lensing induces statistical anisotropies

$$\langle T_{\ell_1 m_1} T_{\ell_2 m_2}^* \rangle = C_{\ell_1} \delta_{\ell_1 \ell_2} \delta_{m_1 m_2} + \sum_{LM} \sum_{\ell_1 m_1, \ell_2 m_2} (-1)^M \begin{pmatrix} \ell_1 & \ell_2 & L \\ m_1 & m_2 & -M \end{pmatrix} W_{\ell_1 \ell_2 L}^{\phi} \phi_{LM}$$

- Quadratic estimator on the full sky

$$\bar{x}_{LM} = \frac{1}{2} \sum_{\ell_1 m_1, \ell_2 m_2} (-1)^M \begin{pmatrix} \ell_1 & \ell_2 & L \\ m_1 & m_2 & -M \end{pmatrix} W_{\ell_1 \ell_2 L}^x \bar{T}_{\ell_1 m_1}^{(1)} \bar{T}_{\ell_2 m_2}^{(2)}$$

Okamoto & Hu, 2003



Lensing reconstruction

- CMB lensing induces statistical anisotropies

$$\langle T_{\ell_1 m_1} T_{\ell_2 m_2}^* \rangle = C_{\ell_1} \delta_{\ell_1 \ell_2} \delta_{m_1 m_2} + \sum_{LM} \sum_{\ell_1 m_1, \ell_2 m_2} (-1)^M \begin{pmatrix} \ell_1 & \ell_2 & L \\ m_1 & m_2 & -M \end{pmatrix} W_{\ell_1 \ell_2 L}^{\phi} \phi_{LM}$$

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Okamoto & Hu, 2003

Filtered temperature. Multiple choices.

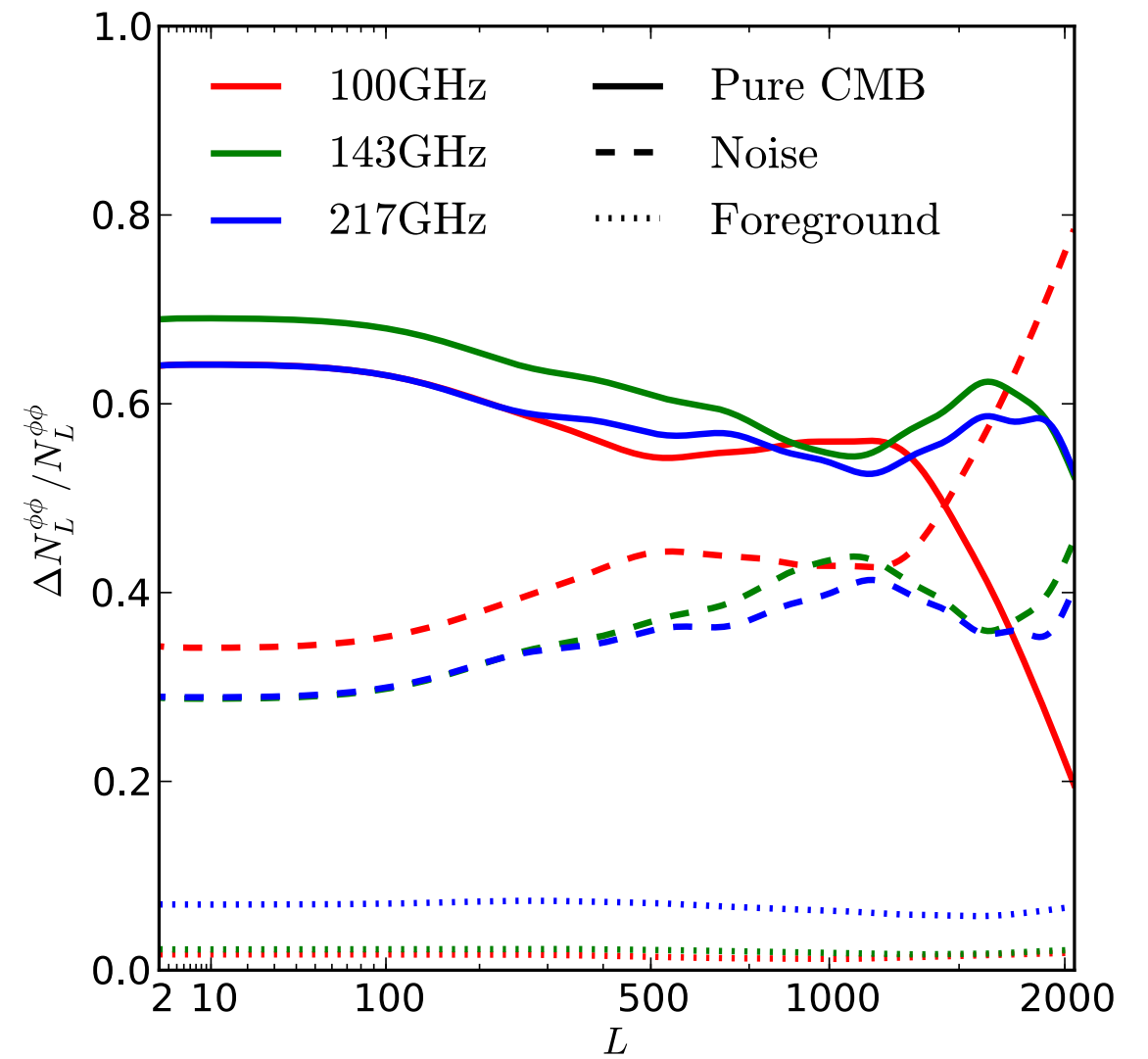
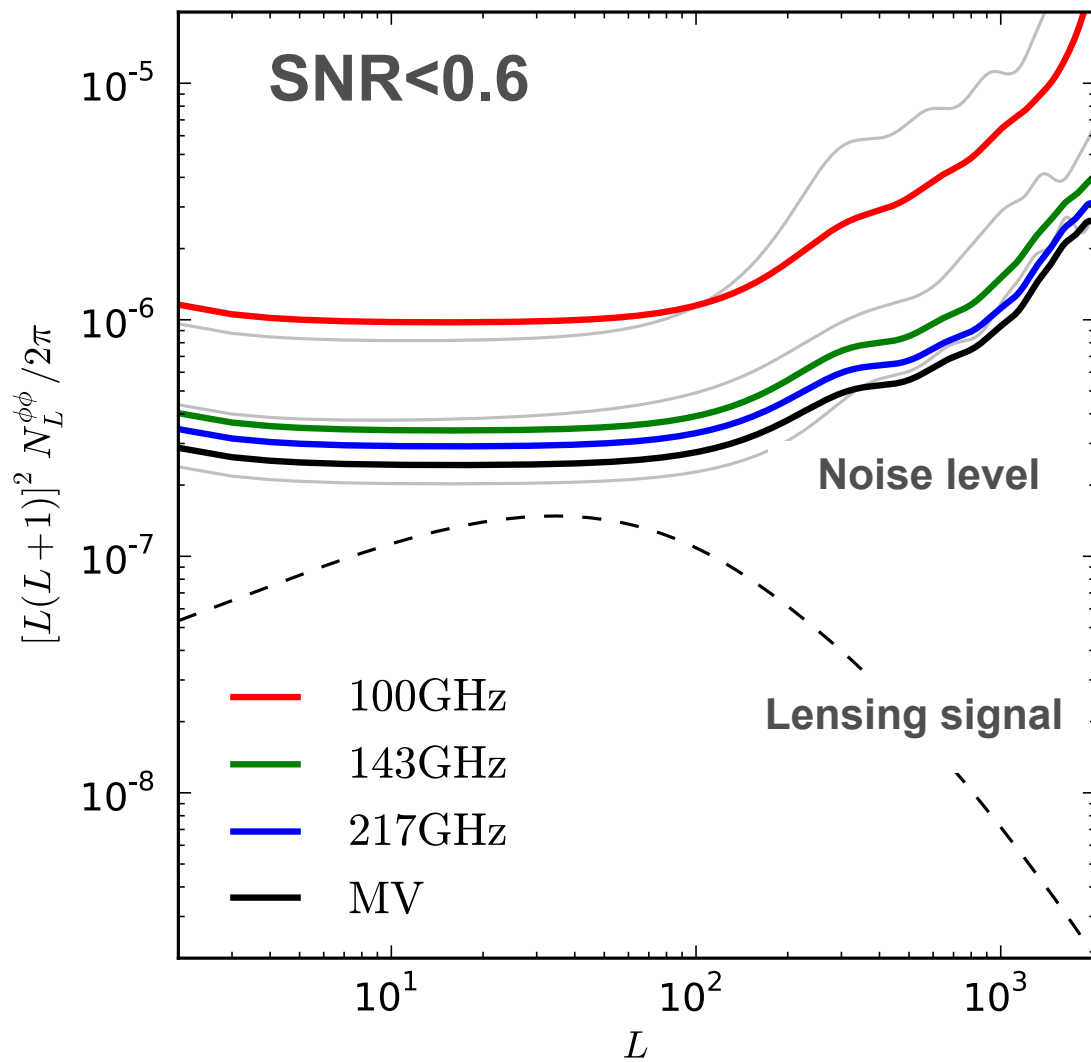
Typically: T_1 is inverse-variance filtered, and T_2 is Wiener filtered

Estimator is unbiased (in the absence of real-life issues), but noisy



CMB lensing reconstruction

$$\text{var}(\hat{\phi}) \sim \langle \hat{\phi} \hat{\phi}^* \rangle \sim \langle \text{TTTT} \rangle \sim C_{\ell}^{\phi\phi} + N_{\ell}^0$$





Outline

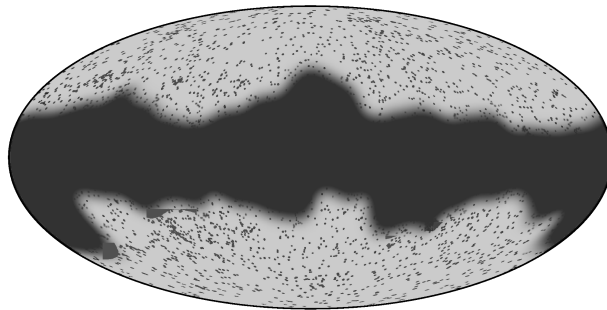
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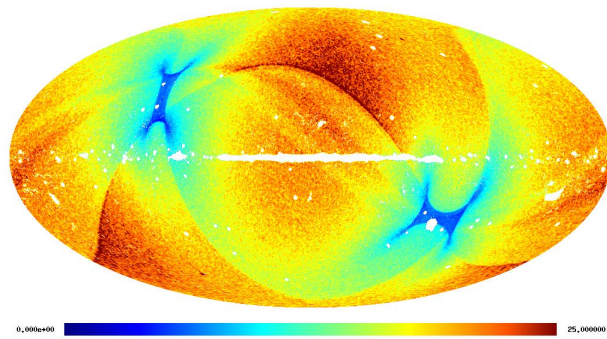
CMB lensing reconstruction

Other sources of statistical anisotropies

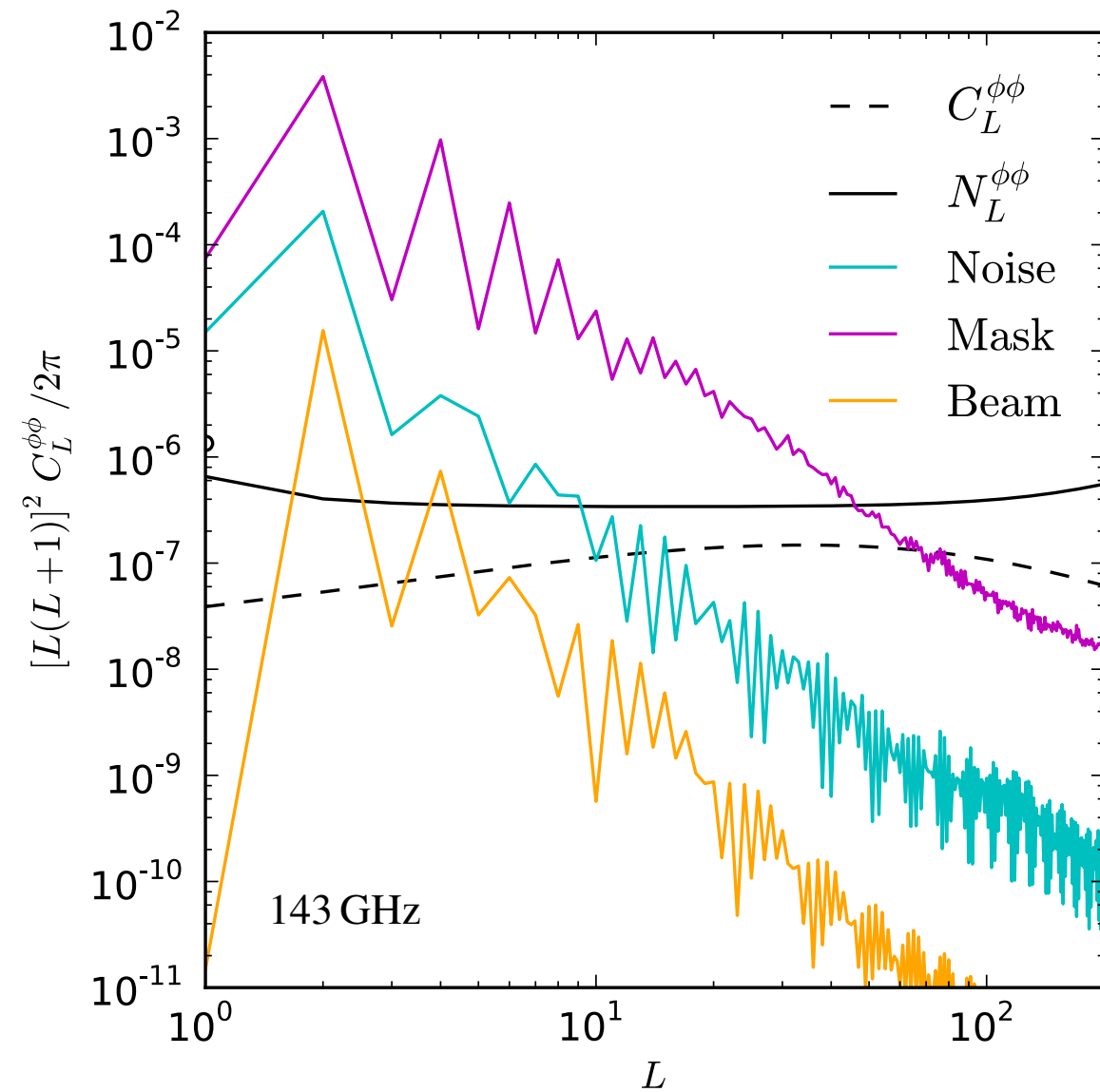
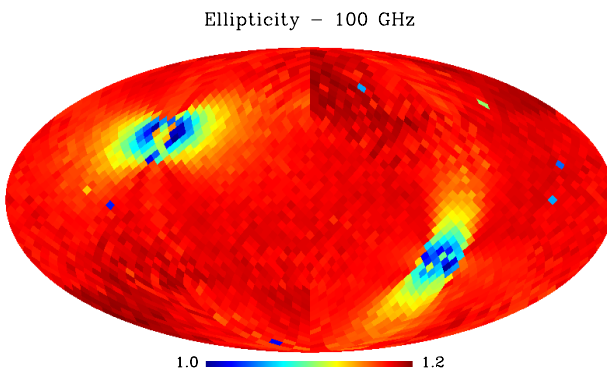
Galactic + PS mask



Inh. noise



Beam ellipticity





CMB lensing reconstruction

$$\hat{\phi}_{LM}^x = \frac{1}{\mathcal{R}_L^{x\phi}} \left(\bar{x}_{LM} - \bar{x}_{LM}^{MF} \right).$$

$$\bar{x}_{LM} = \frac{1}{2} \sum_{\ell_1 m_1, \ell_2 m_2} (-1)^M \begin{pmatrix} \ell_1 & \ell_2 & L \\ m_1 & m_2 & -M \end{pmatrix} W_{\ell_1 \ell_2 L}^x \langle \bar{T}_{\ell_1 m_1}^{(1)} \bar{T}_{\ell_2 m_2}^{(2)} \rangle.$$

$$\bar{\phi}_{\ell m} = [(C^{-1}T)\nabla(SC^{-1}T)]_{\ell m}$$

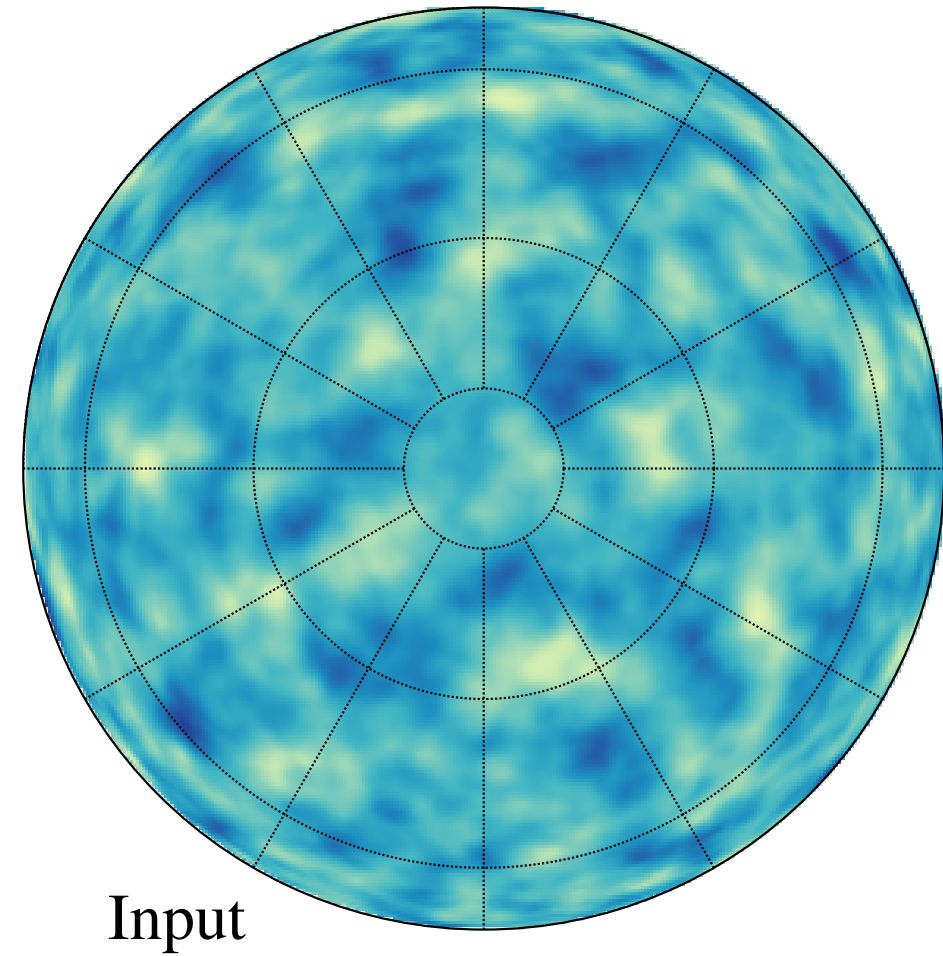
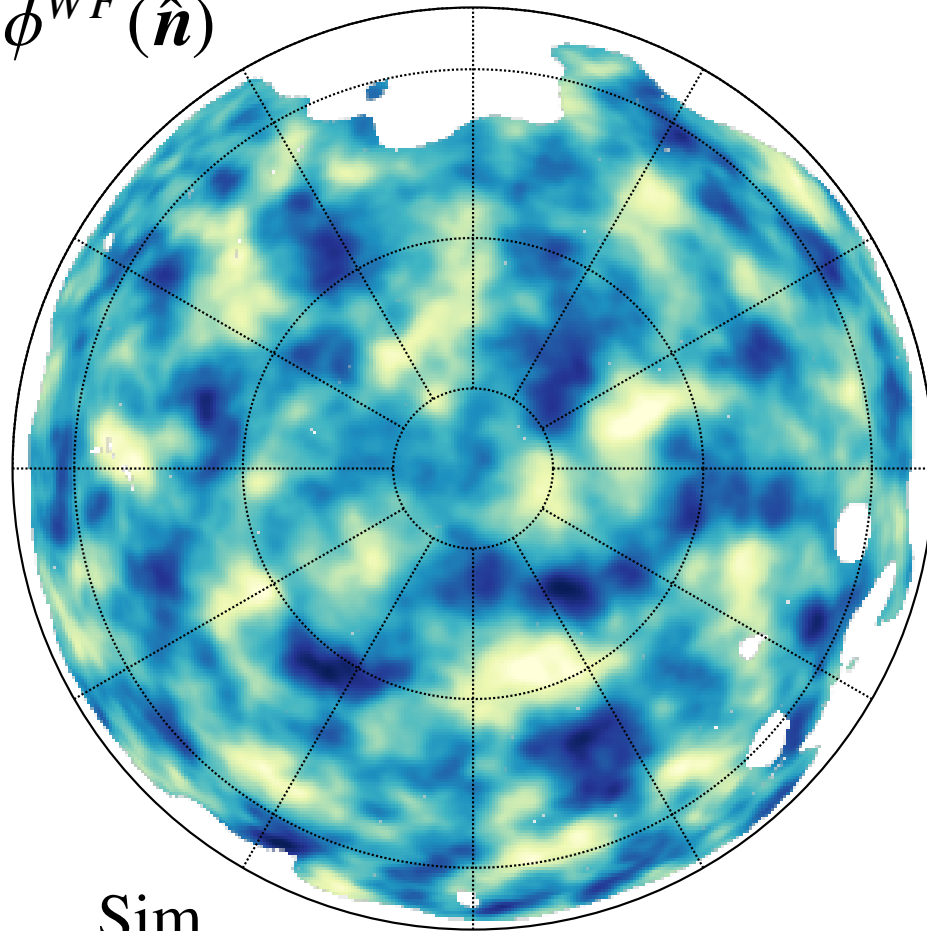
$$\bar{T}_{\ell m} = [S + N]^{-1} T_{\ell m} \approx [C_{\ell}^{TT} + C_{\ell}^{NN}]^{-1} T_{\ell m} = F_{\ell} T_{\ell m} \quad \mathcal{R}_L^{x\phi} = \frac{1}{(2L+1)} \sum_{\ell_1 \ell_2} \frac{1}{2} W_{\ell_1 \ell_2 L}^x W_{\ell_1 \ell_2 L}^{\phi} F_{\ell_1}^{(1)} F_{\ell_2}^{(2)}.$$

- Take two temperature maps and inverse-variance filter them
- Multiply one by the temperature power spectrum and differentiate it
- Multiply it with the first filtered map
- Do the same on a set of realistic simulations
- Take the difference and normalize to get unbiased estimator



CMB lensing reconstruction

$$\phi^{WF}(\hat{n})$$

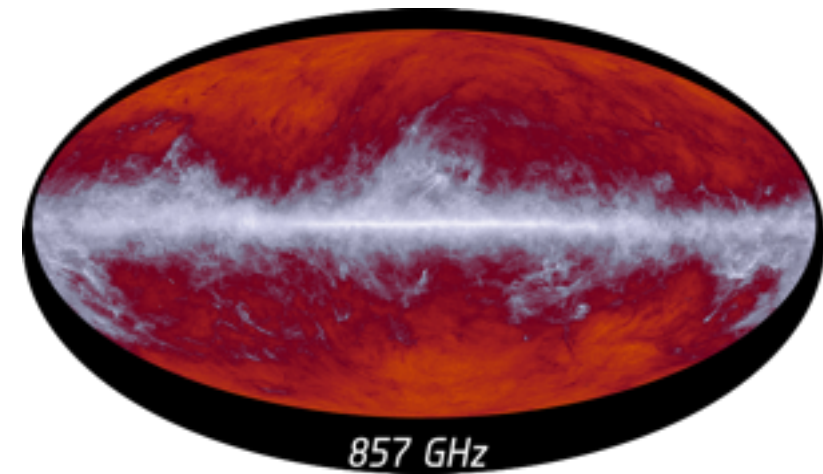
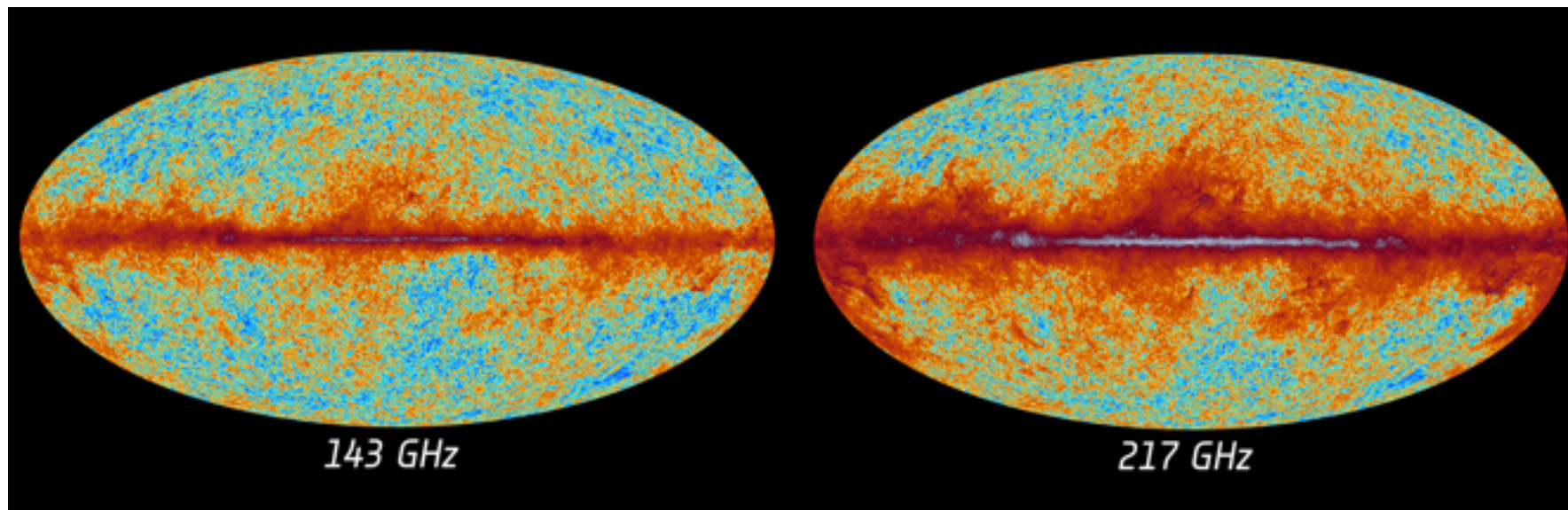


Reconstruction on a realistic Planck simulation



Best reconstruction

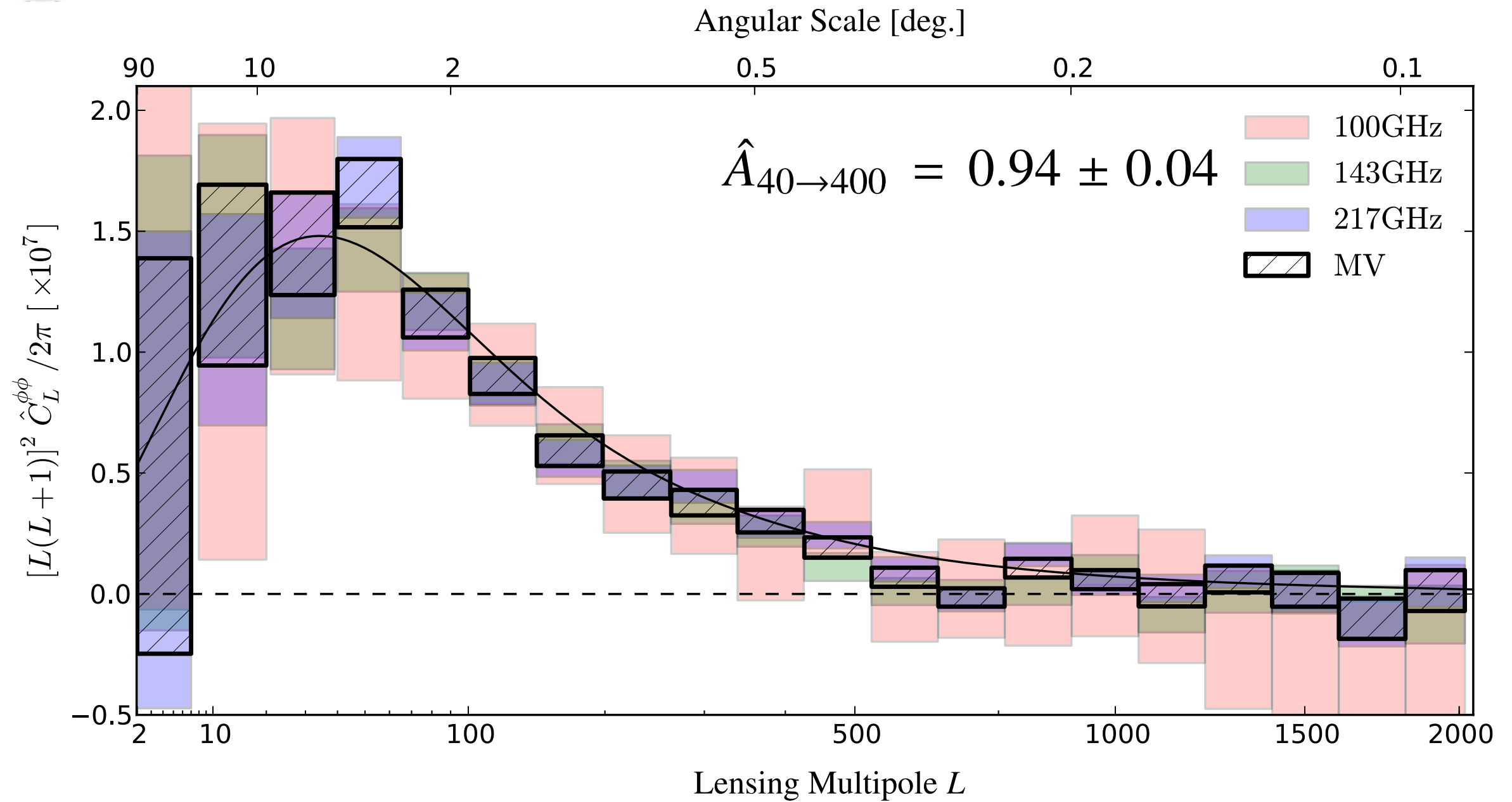
- Minimum-variance combination of 143GHz & 217 GHz



- 857 GHz map used as a template for dust cleaning
- 30 % Galactic mask +CO+ point sources
- 5° apodization (for lensing power spectrum estimation)

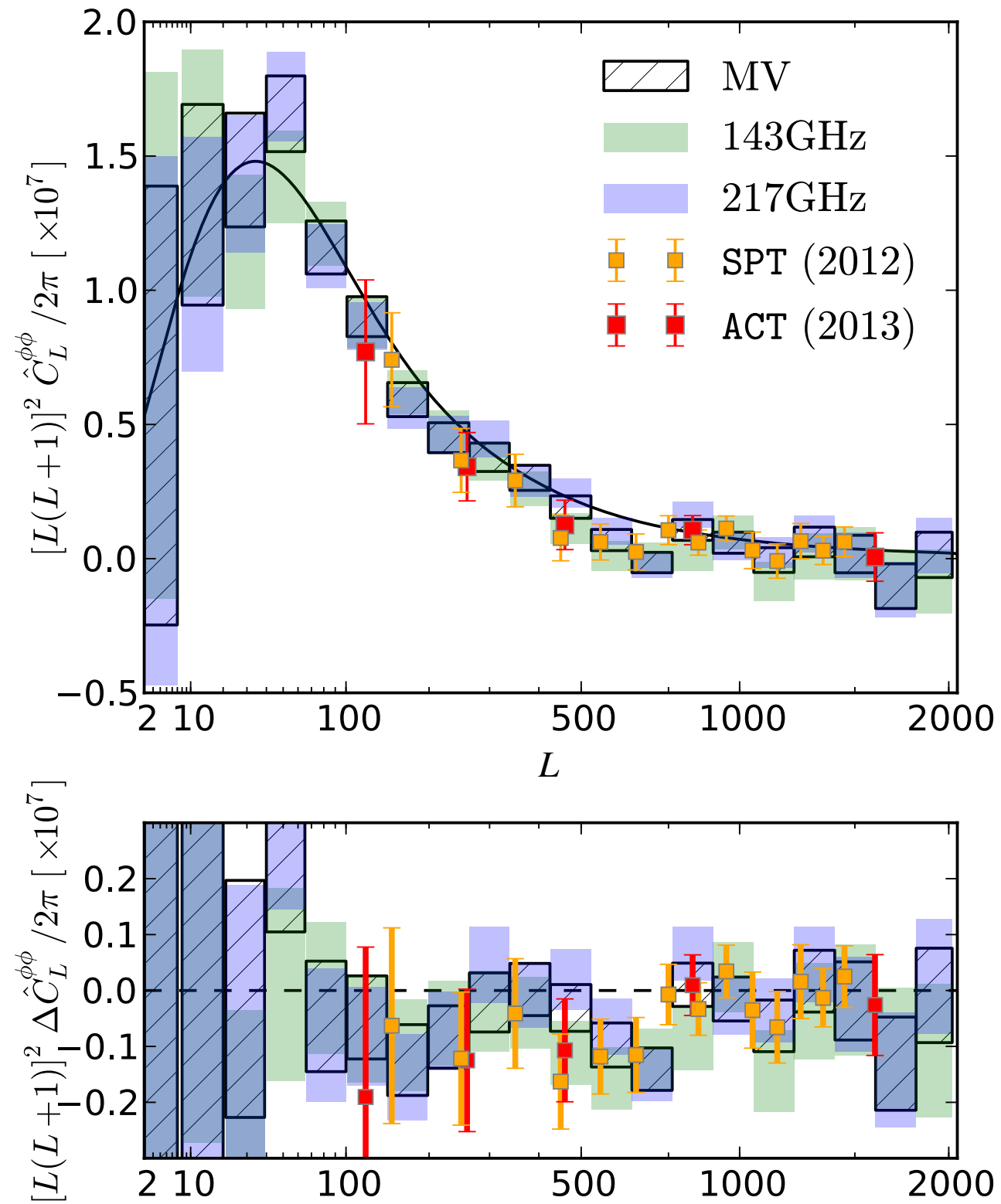


Best reconstruction





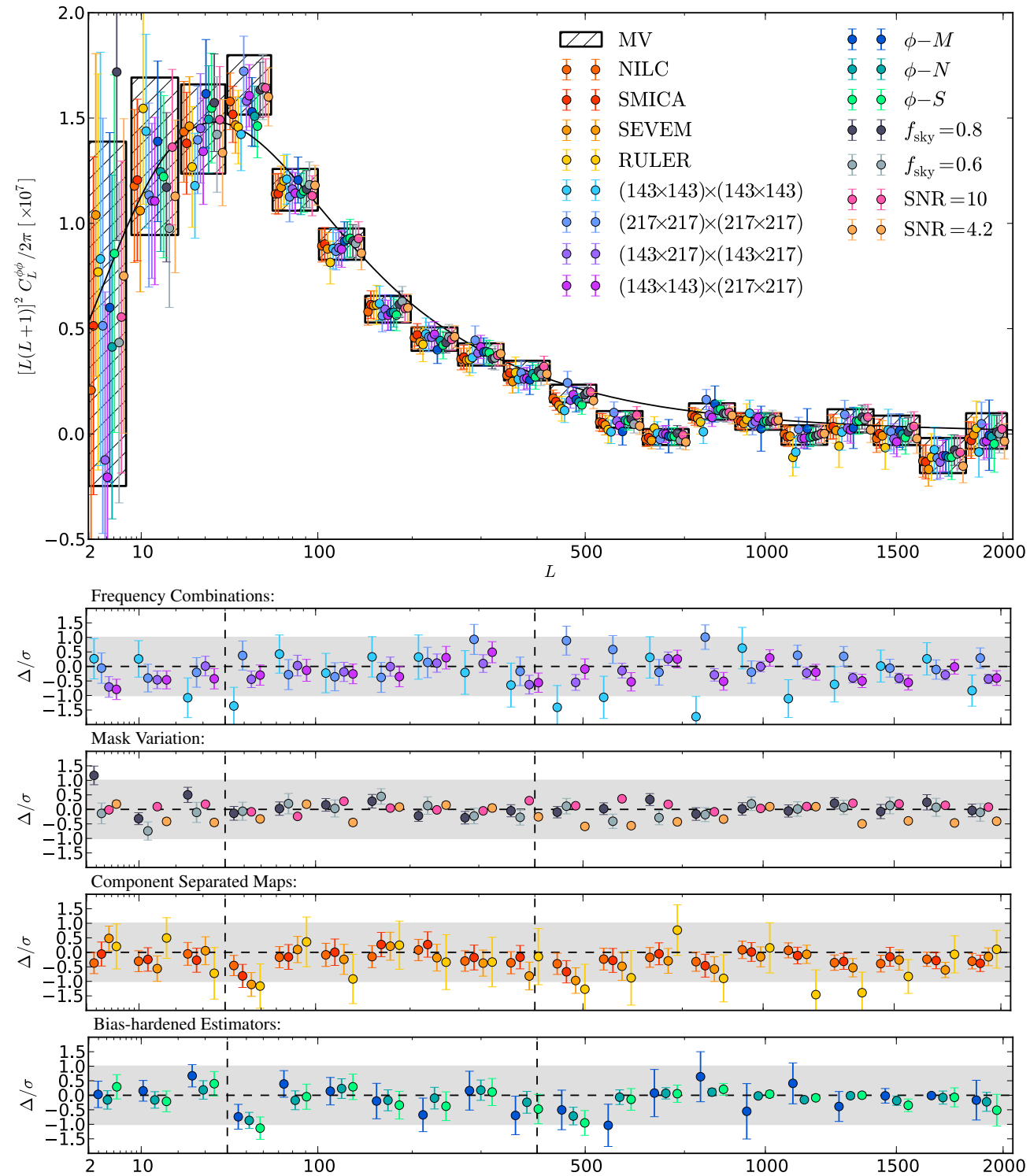
Comparison to other surveys



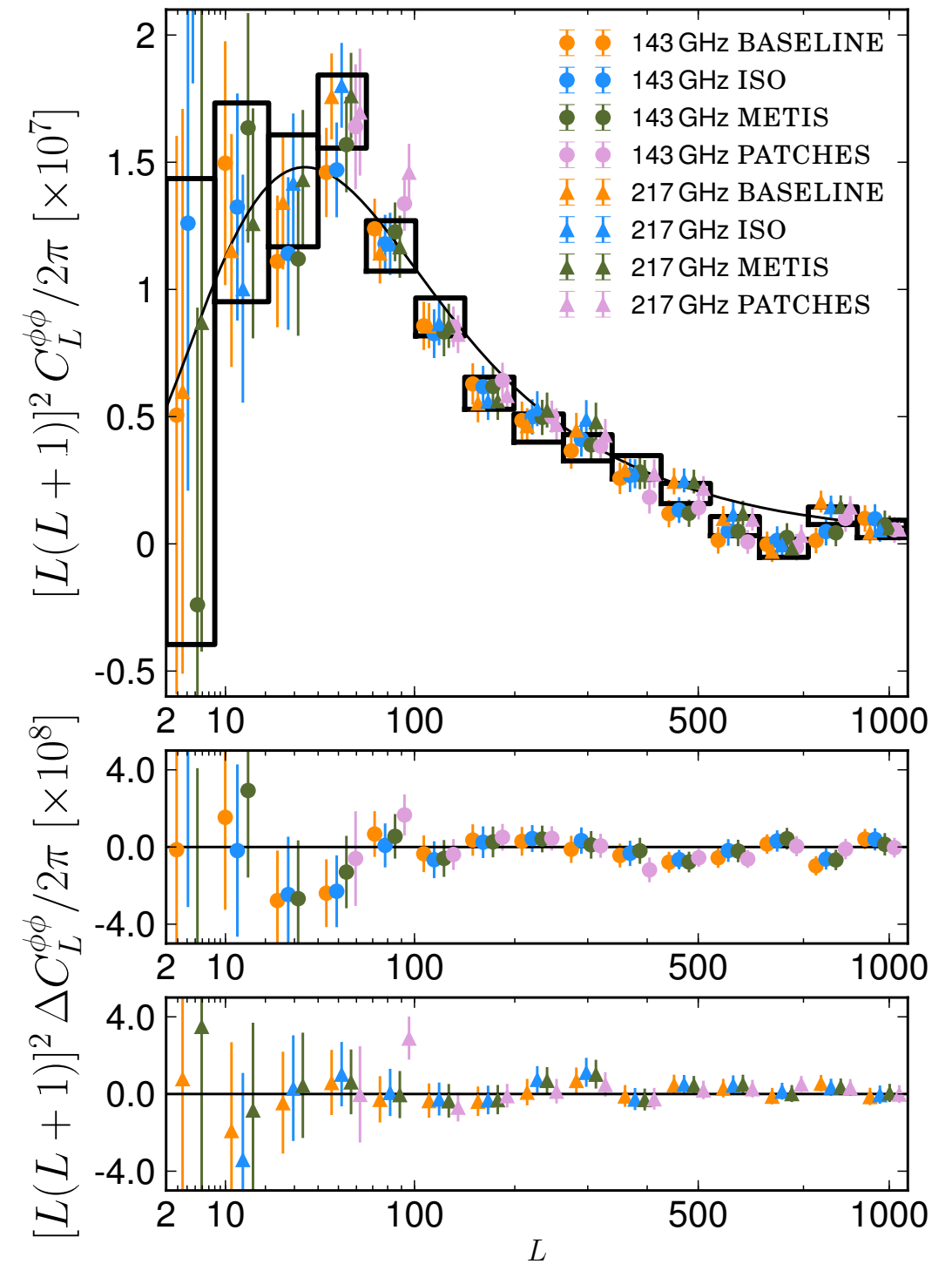


Tests

Testing foreground contamination



Testing the filter & implementation



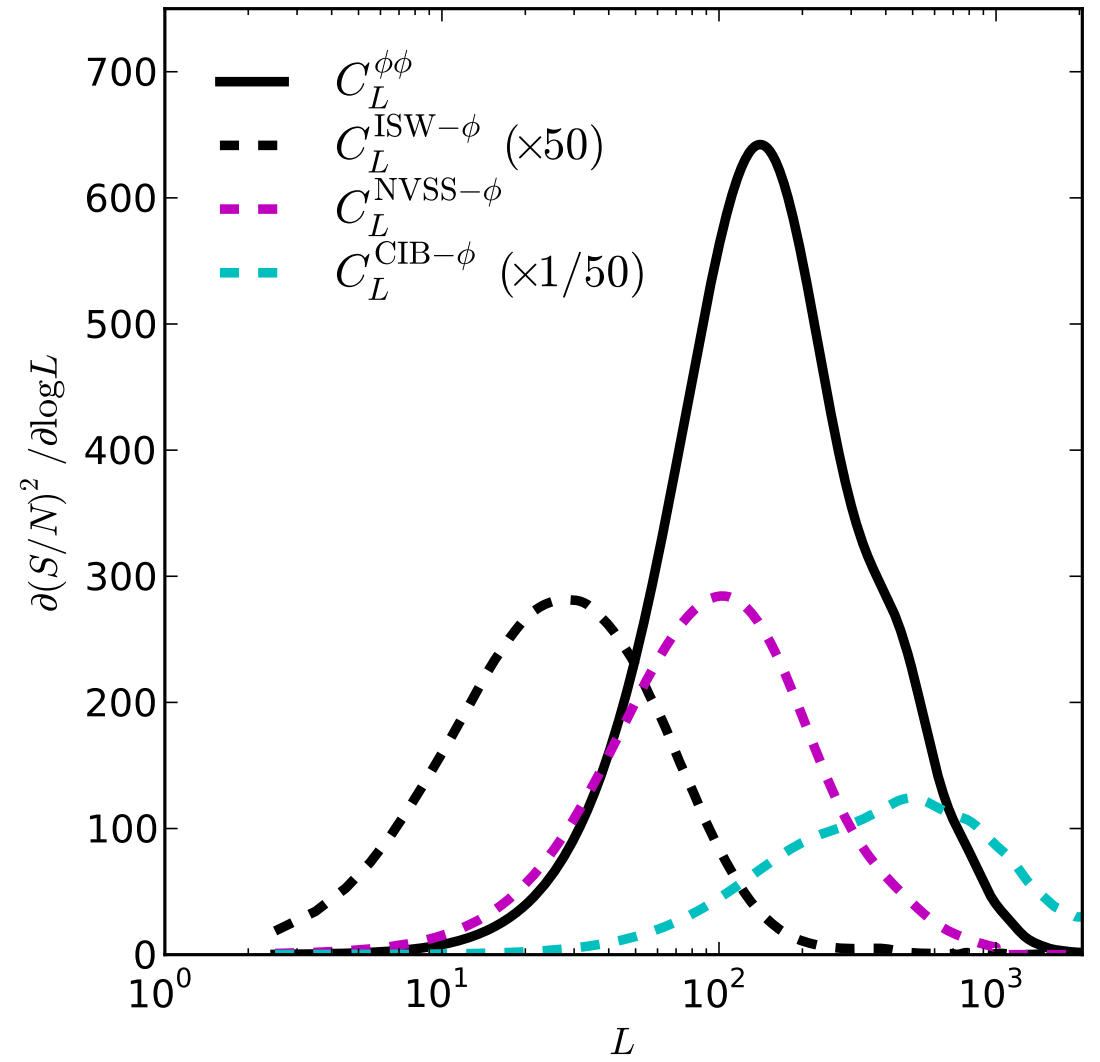
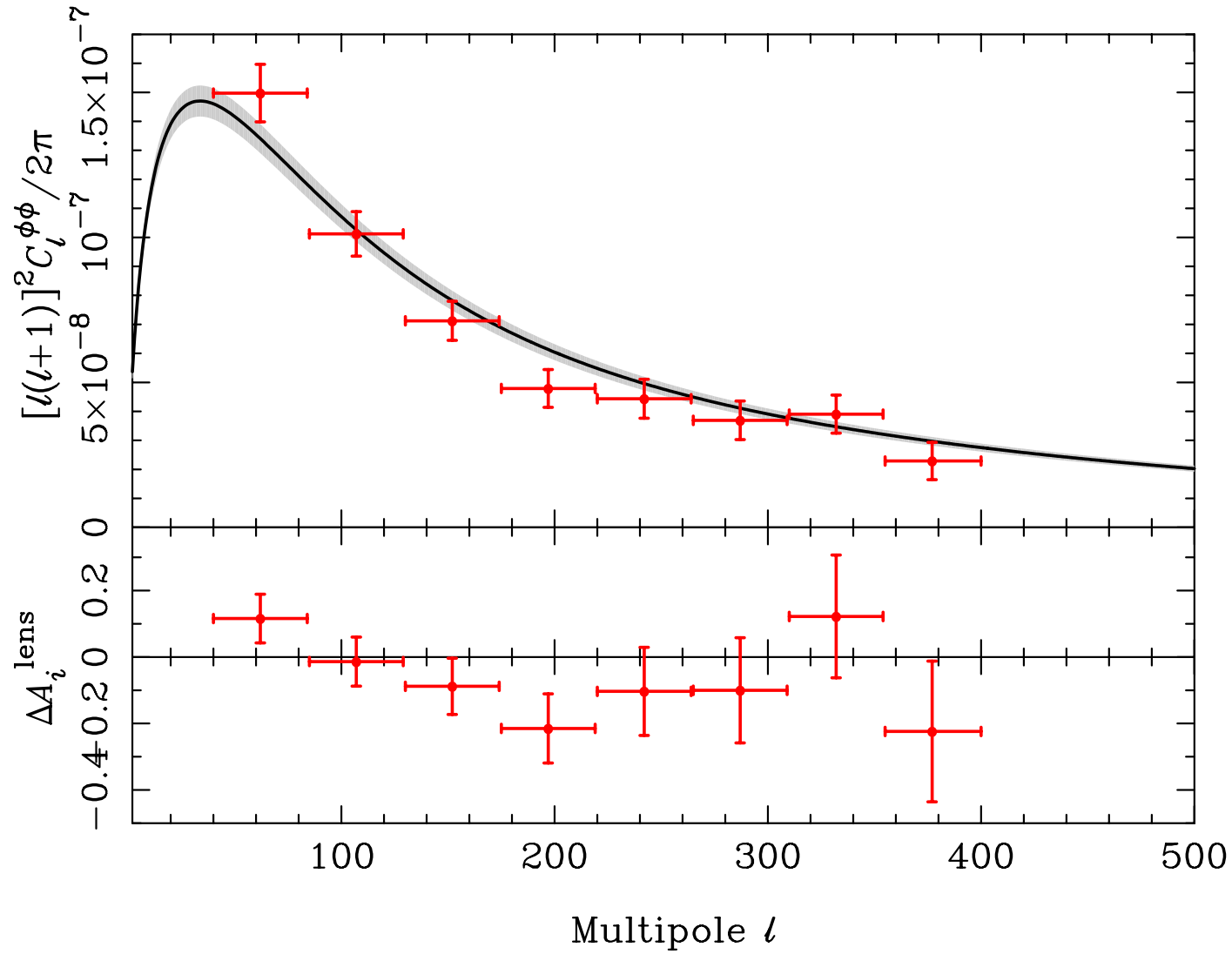


Outline

- A few words on Planck
- CMB lensing
- Reconstruction from Planck data
- **Cosmology from CMB lensing**
- Cross-correlations

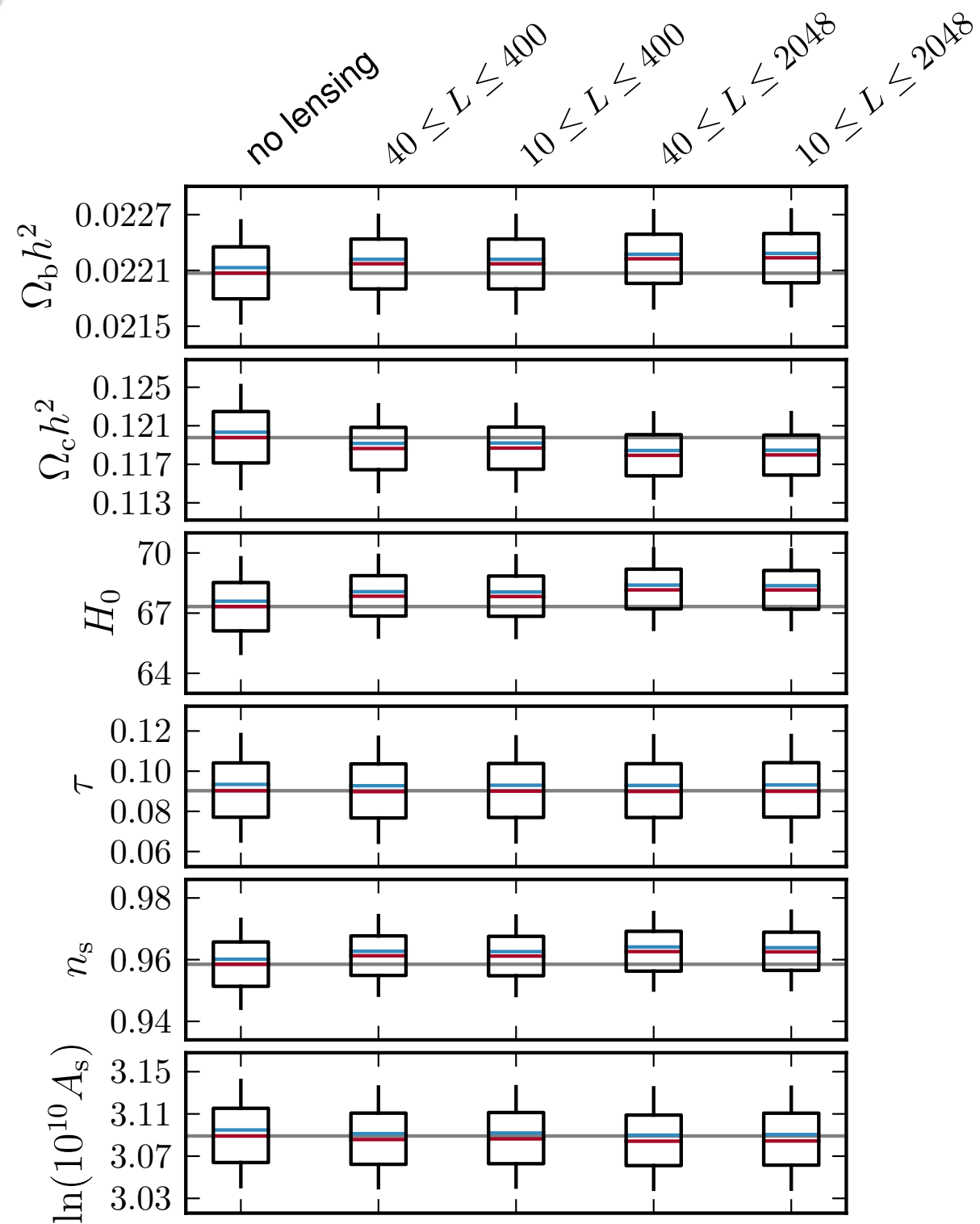


Cosmology





Cosmology



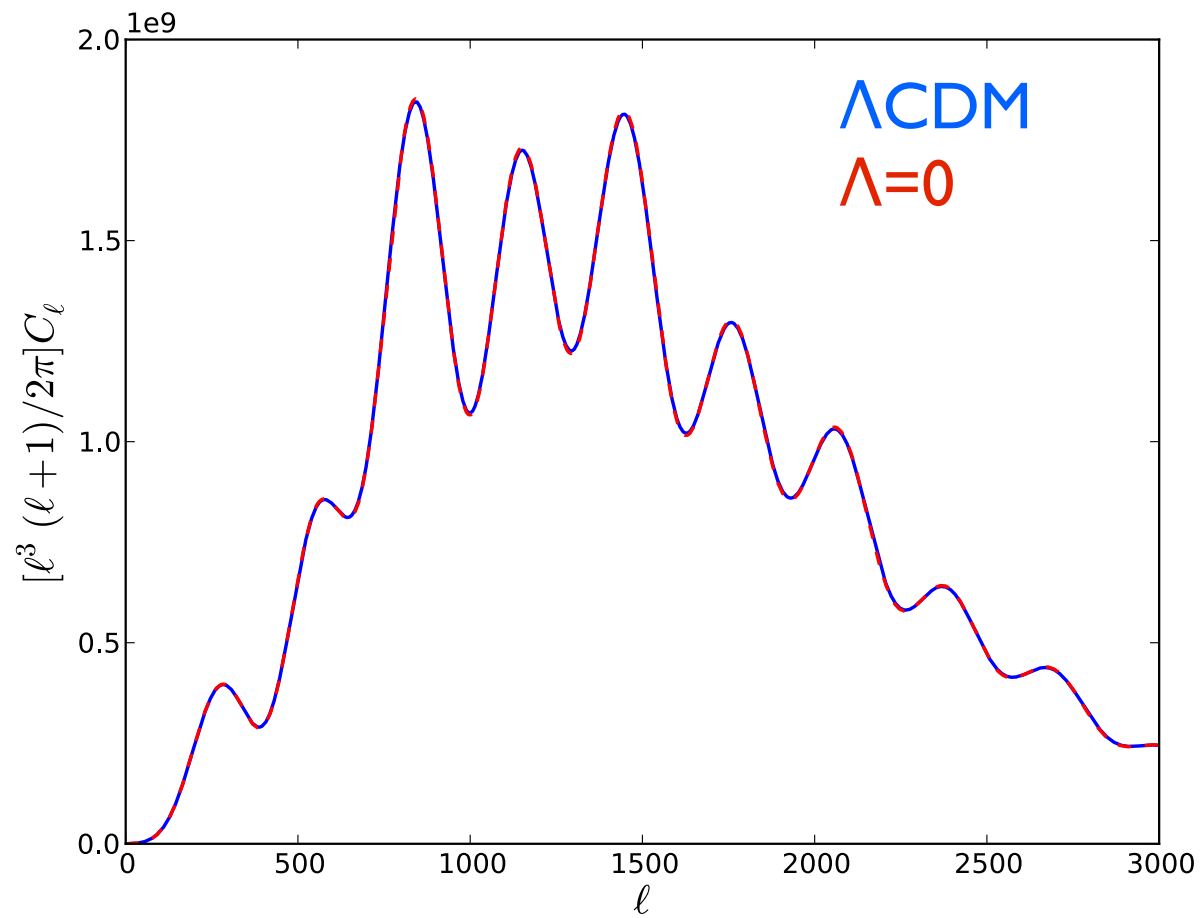
**Adding lensing reconstruction brings
~20% improvement on some parameters**

**Adding low-L and high-L lensing
information does not improve precision
but slightly shift central values**

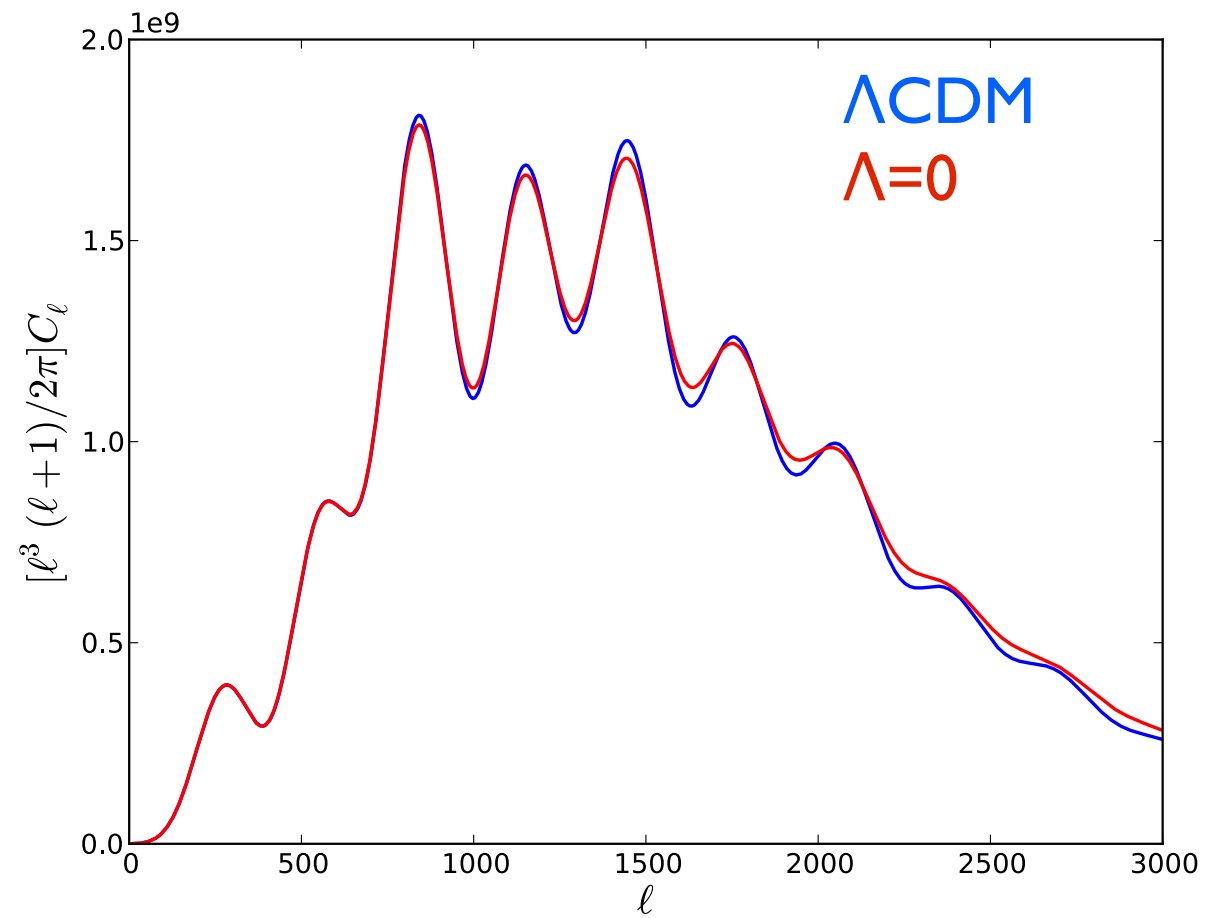


Cosmology

- CMB lensing breaks the angular diameter degeneracy



Unlensed TT



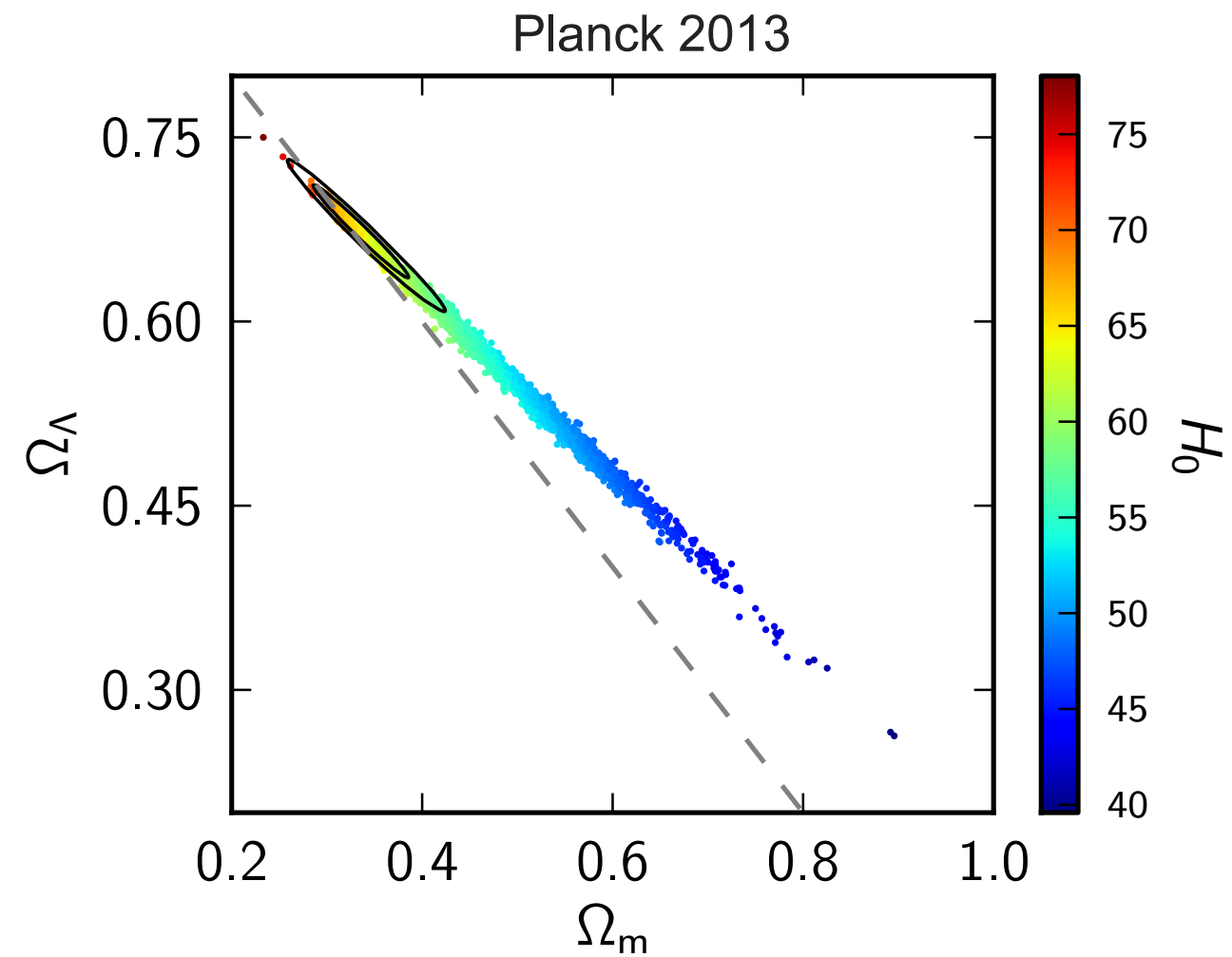
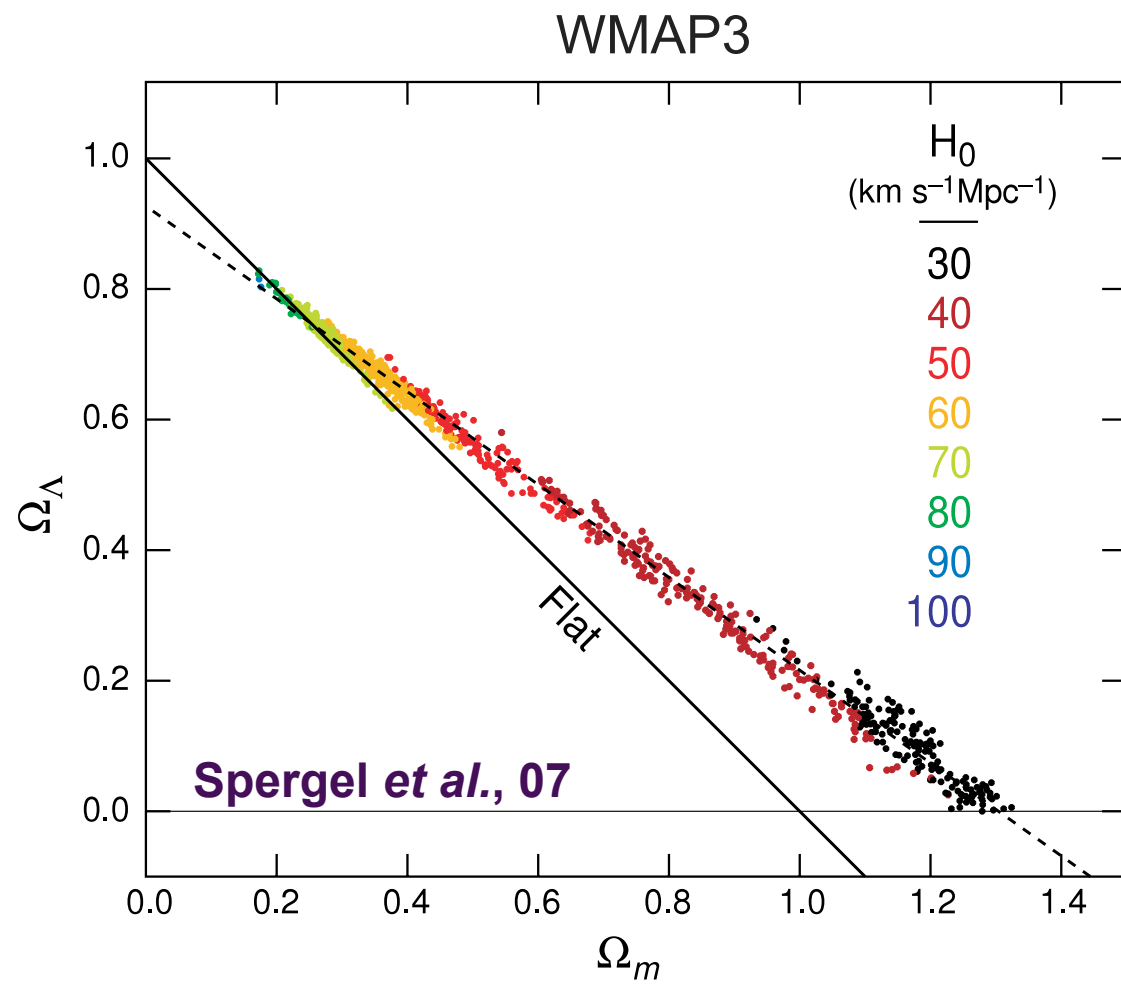
Lensed TT

see also [Sherwin et al, 2011](#),
[Van Engelen et al., 2012](#)



Cosmology

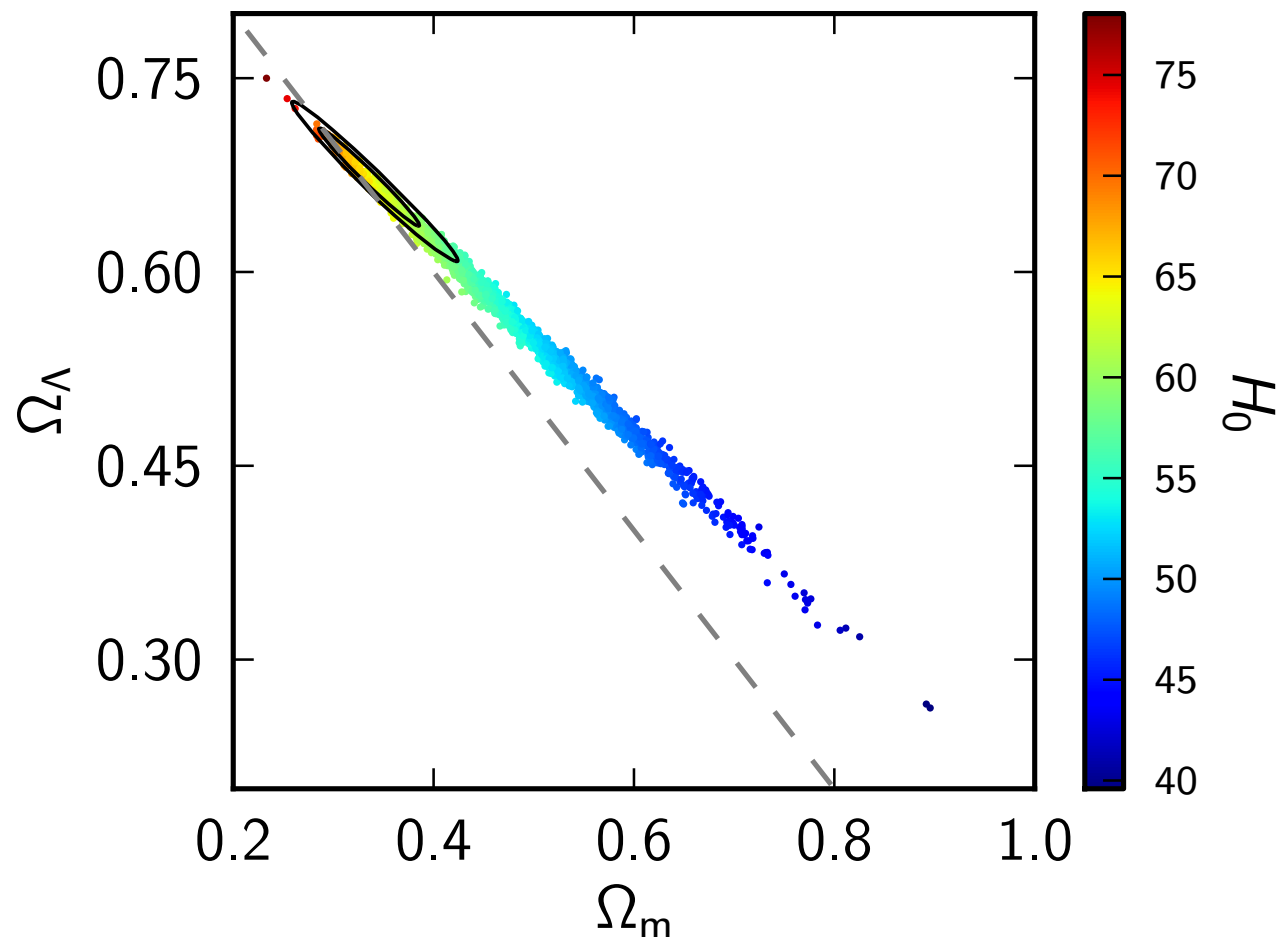
- CMB lensing breaks the angular diameter degeneracy



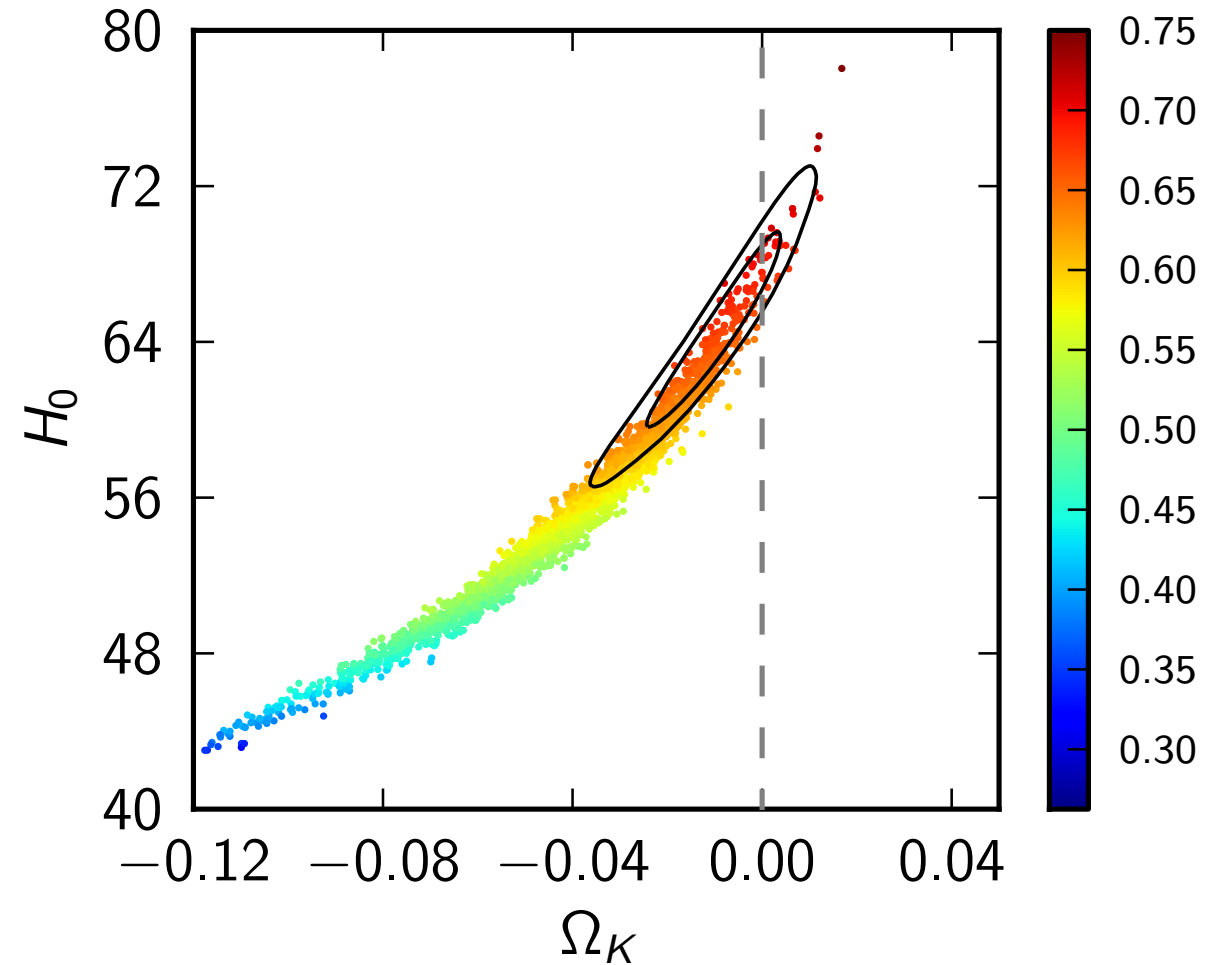


Cosmology

■ CMB lensing breaks the angular diameter degeneracy



$$\Omega_\Lambda = 0.57^{+0.073}_{-0.055} \quad (68\%; \text{Planck+WP+highL})$$
$$\Omega_\Lambda = 0.67^{+0.027}_{-0.023} \quad (68\%; \text{Planck+lensing+WP+highL}).$$



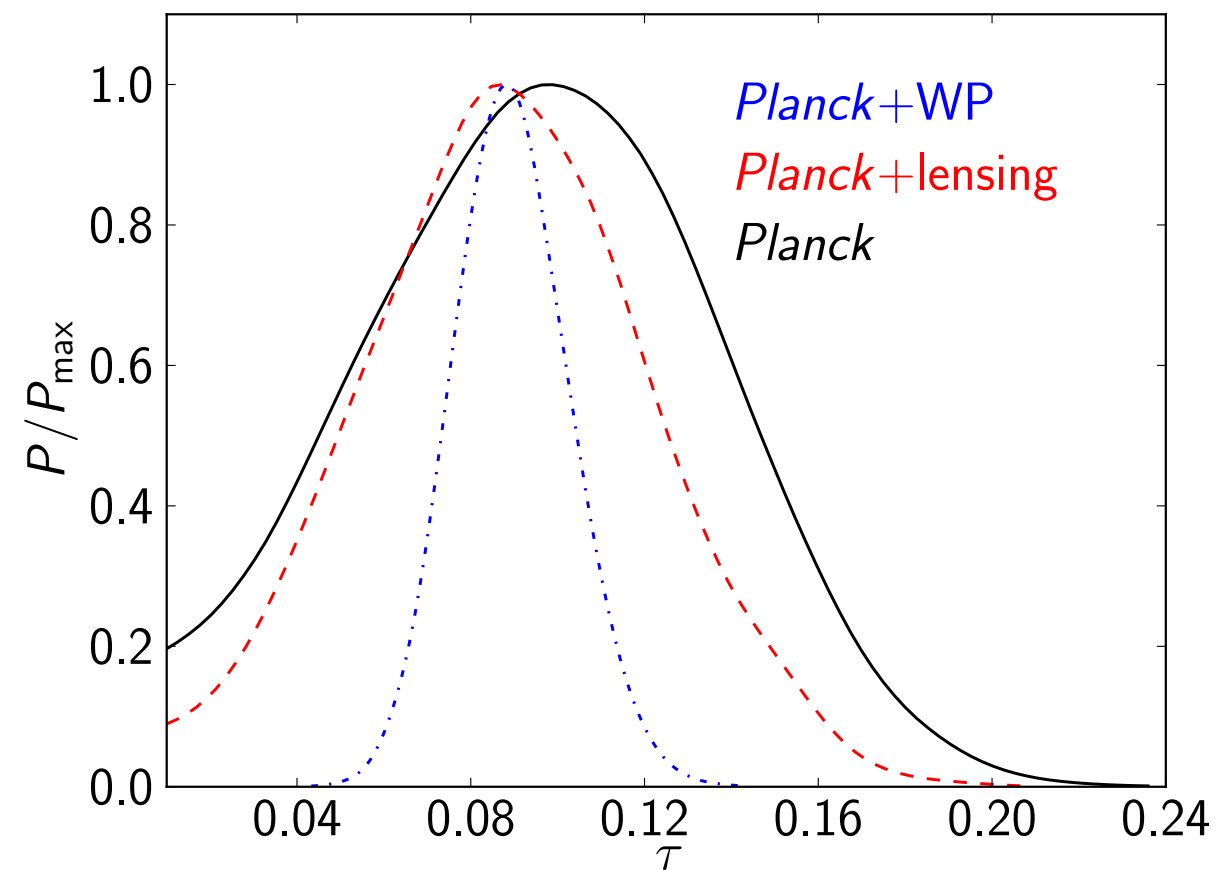
$$100\Omega_K = -4.2^{+4.3}_{-4.8} \quad (95\%; \text{Planck+WP+highL});$$
$$100\Omega_K = -1.0^{+1.8}_{-1.9} \quad (95\%; \text{Planck+lensing} \\ + \text{WP+highL}).$$



Cosmology

Reionization

Optical depth - Amplitude degeneracy $A_s e^{-2\tau}$



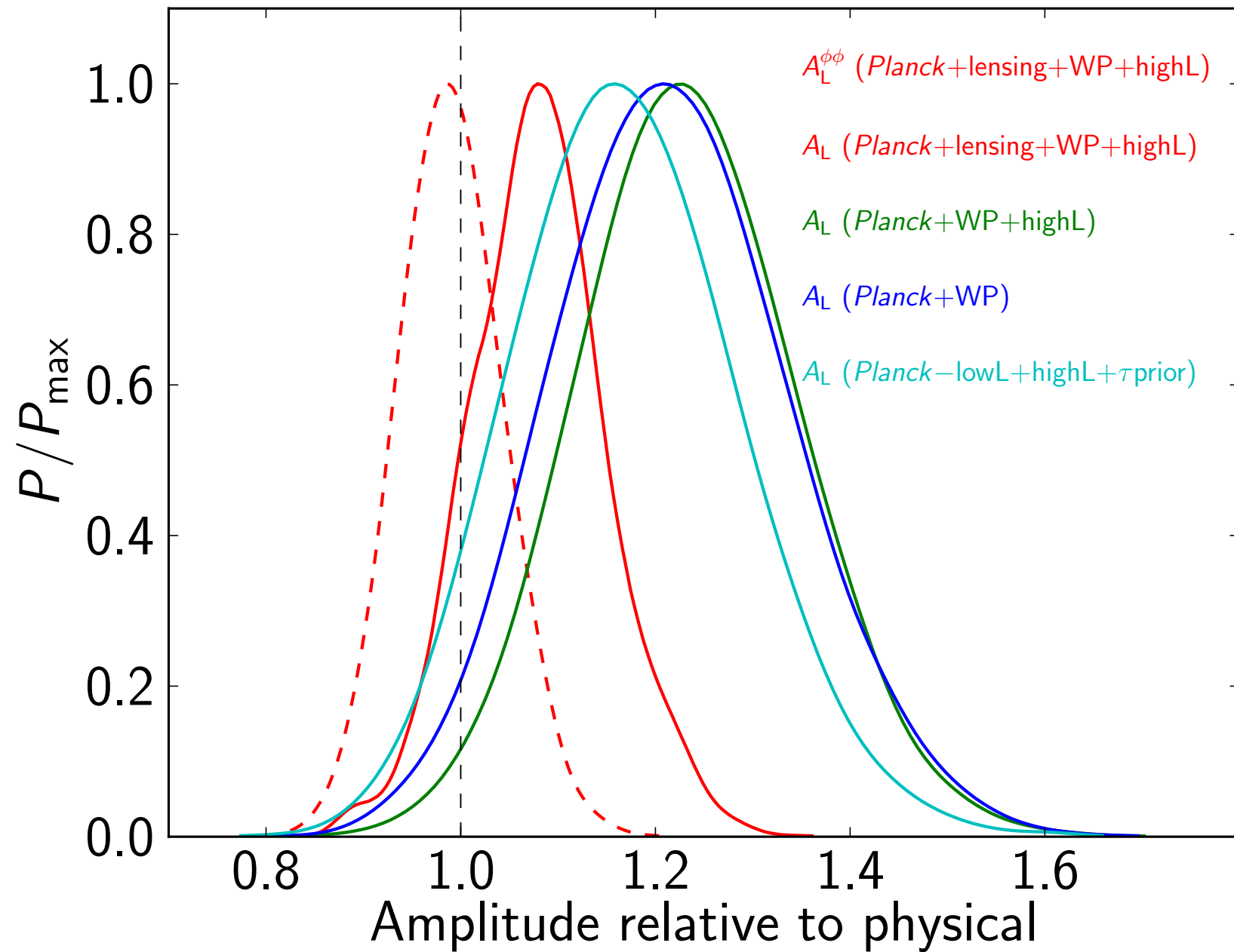
$$\tau = 0.097 \pm 0.038 \quad (68\%; \text{Planck})$$

$$\tau = 0.089 \pm 0.032 \quad (68\%; \text{Planck+lensing}).$$



A_{lens} higher than 1?

$$C_l^{\phi\phi} \rightarrow A_L C_l^{\phi\phi}$$



TT wants more lensing

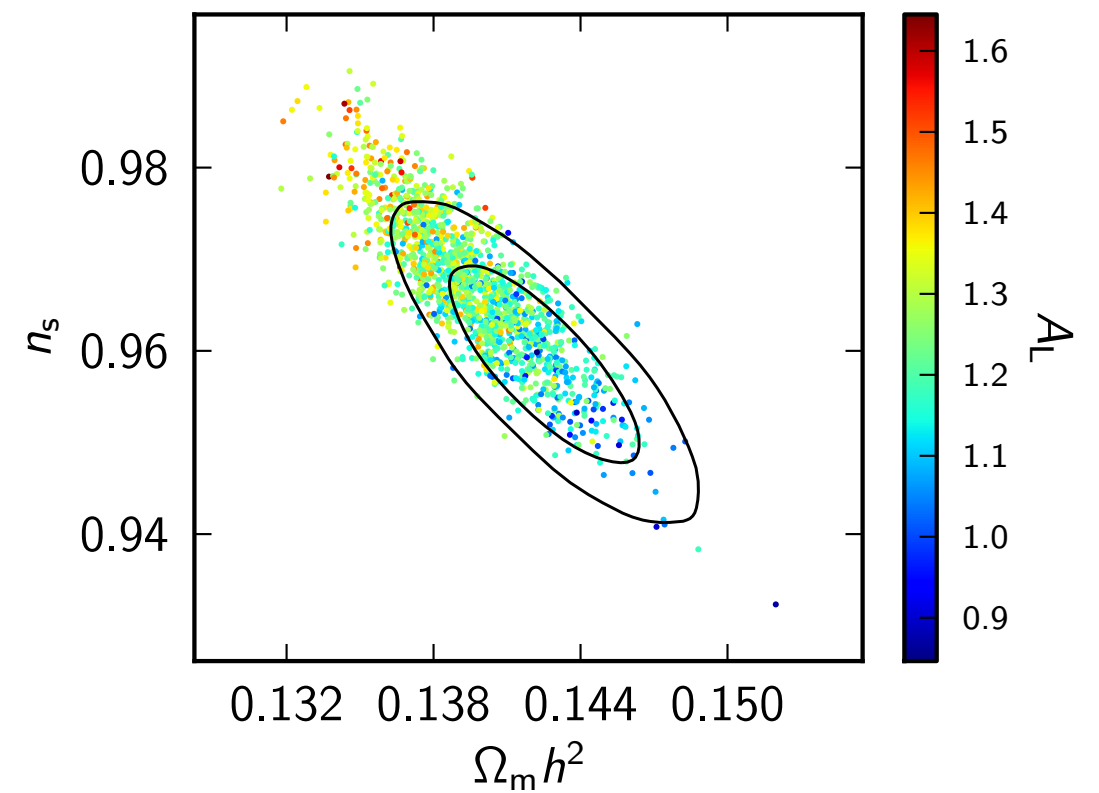
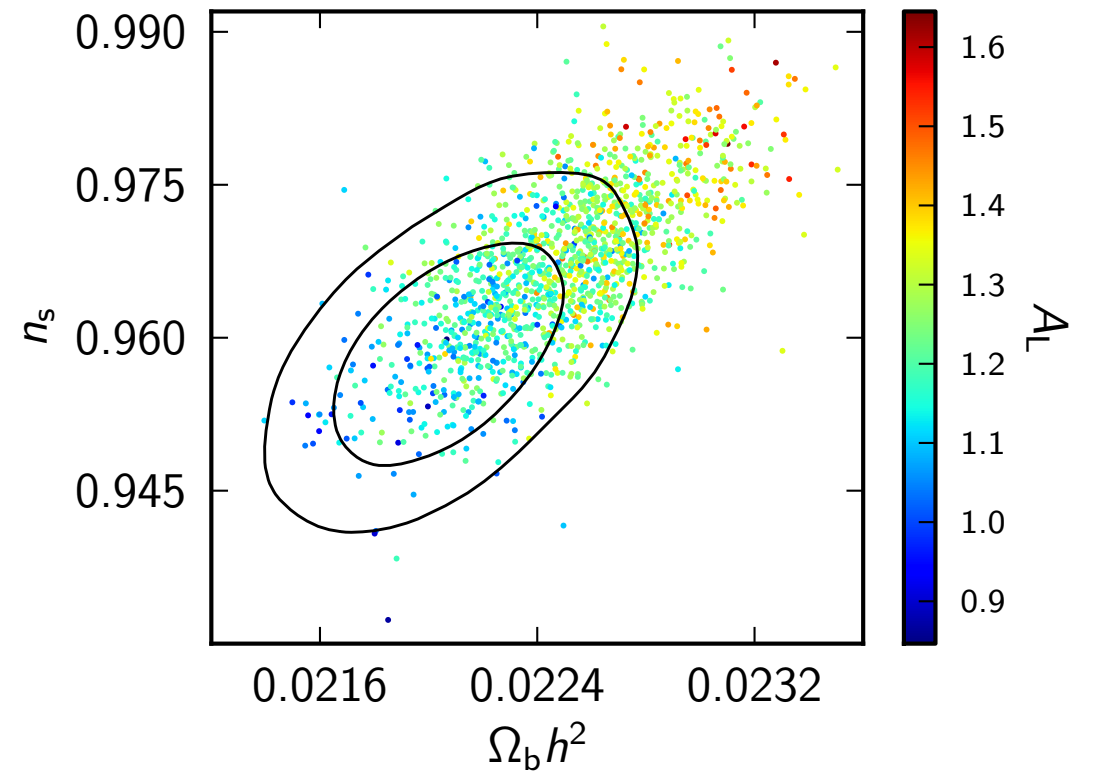
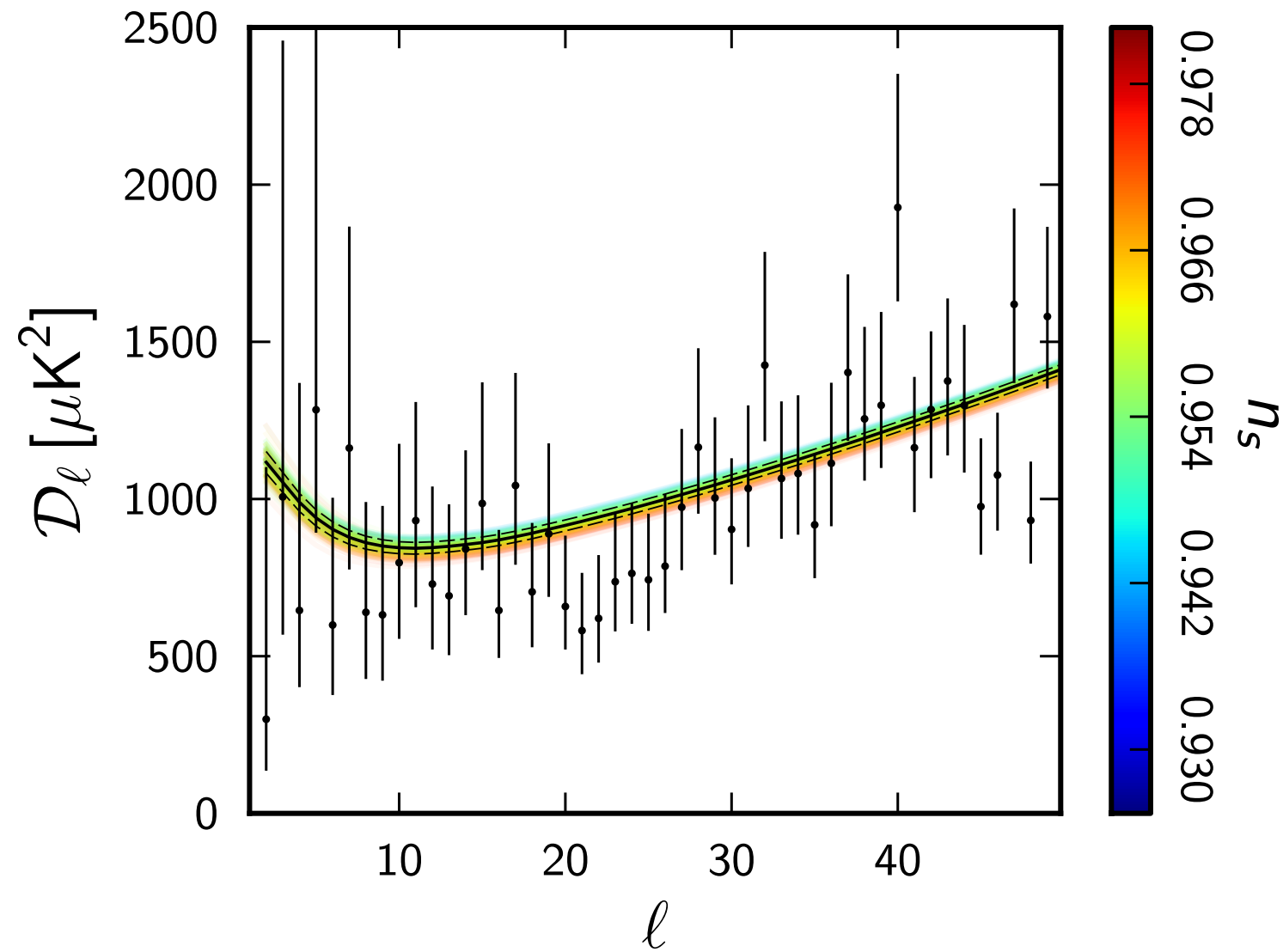
TTTT wants the right lensing
(even slightly less)

Not fully understood yet

Might have to do with low-ell
lack of power



A_{lens} higher than 1?

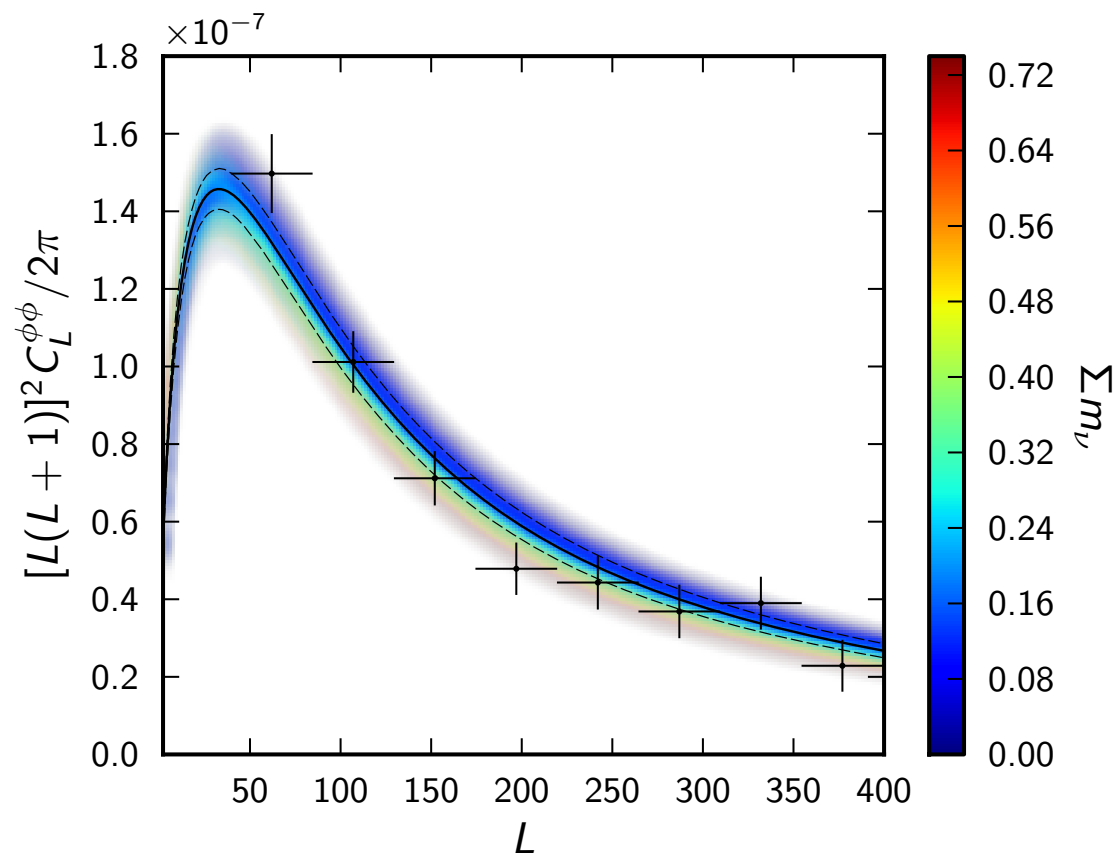




Cosmology

Sum of neutrinos masses

- Mild tension : constraint weaker than expected!
- Temperature power spectra: more lensing = smaller mass
- Reconstruction: less lensing = larger mass



$$\sum m_\nu < 0.66 \text{ eV}, \quad (95\%; \text{Planck}+\text{WP}+\text{highL}),$$
$$\sum m_\nu < 0.85 \text{ eV}, \quad (95\%; \text{Planck}+\text{lensing}+\text{WP}+\text{highL}),$$



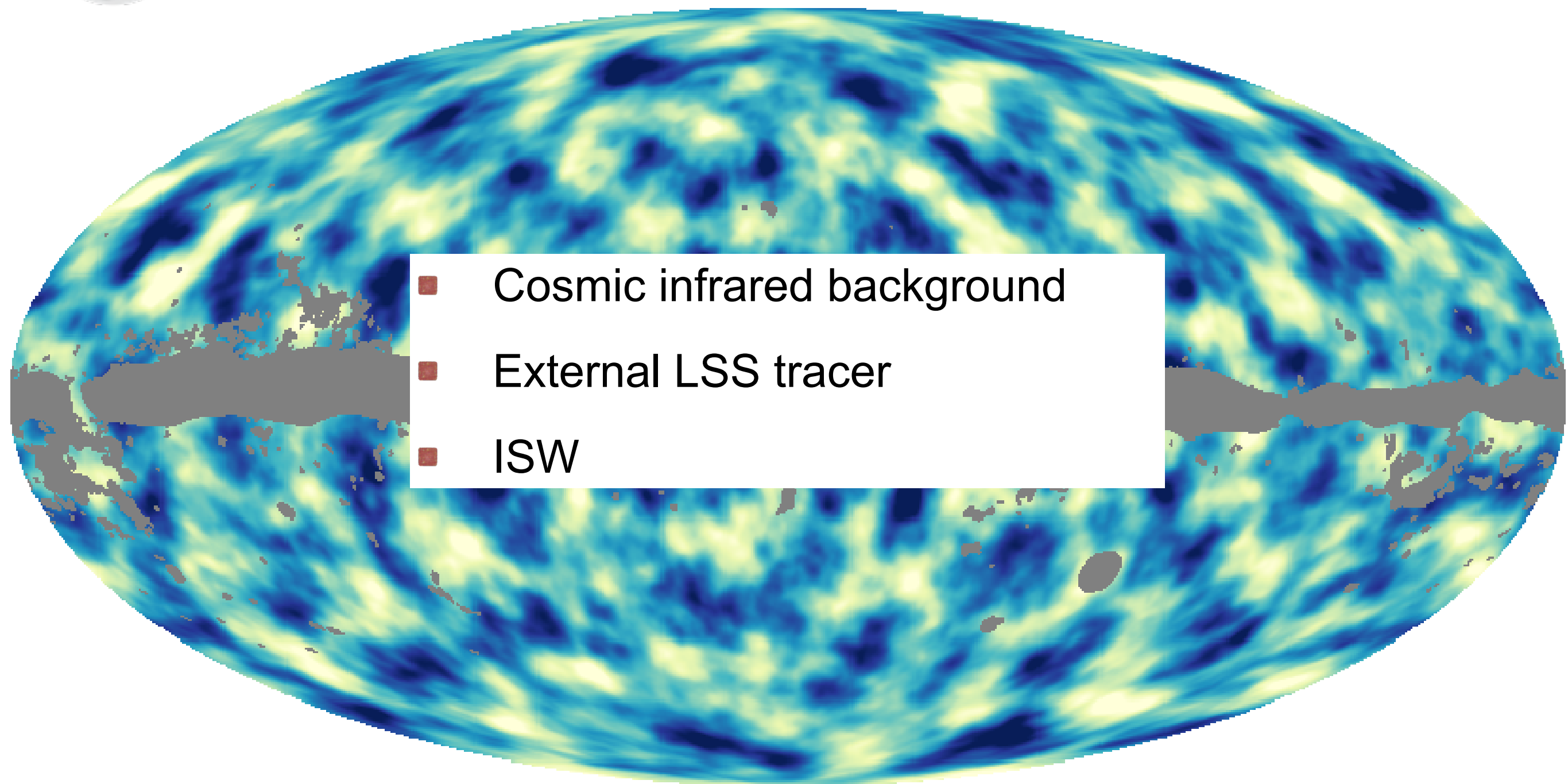
Outline

- A few words on Planck
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- Reconstruction from Planck data
- Cosmology from CMB lensing
- **Cross-correlations**

The lensing map traces the matter distribution up to the last scattering surface



Cross-correlations

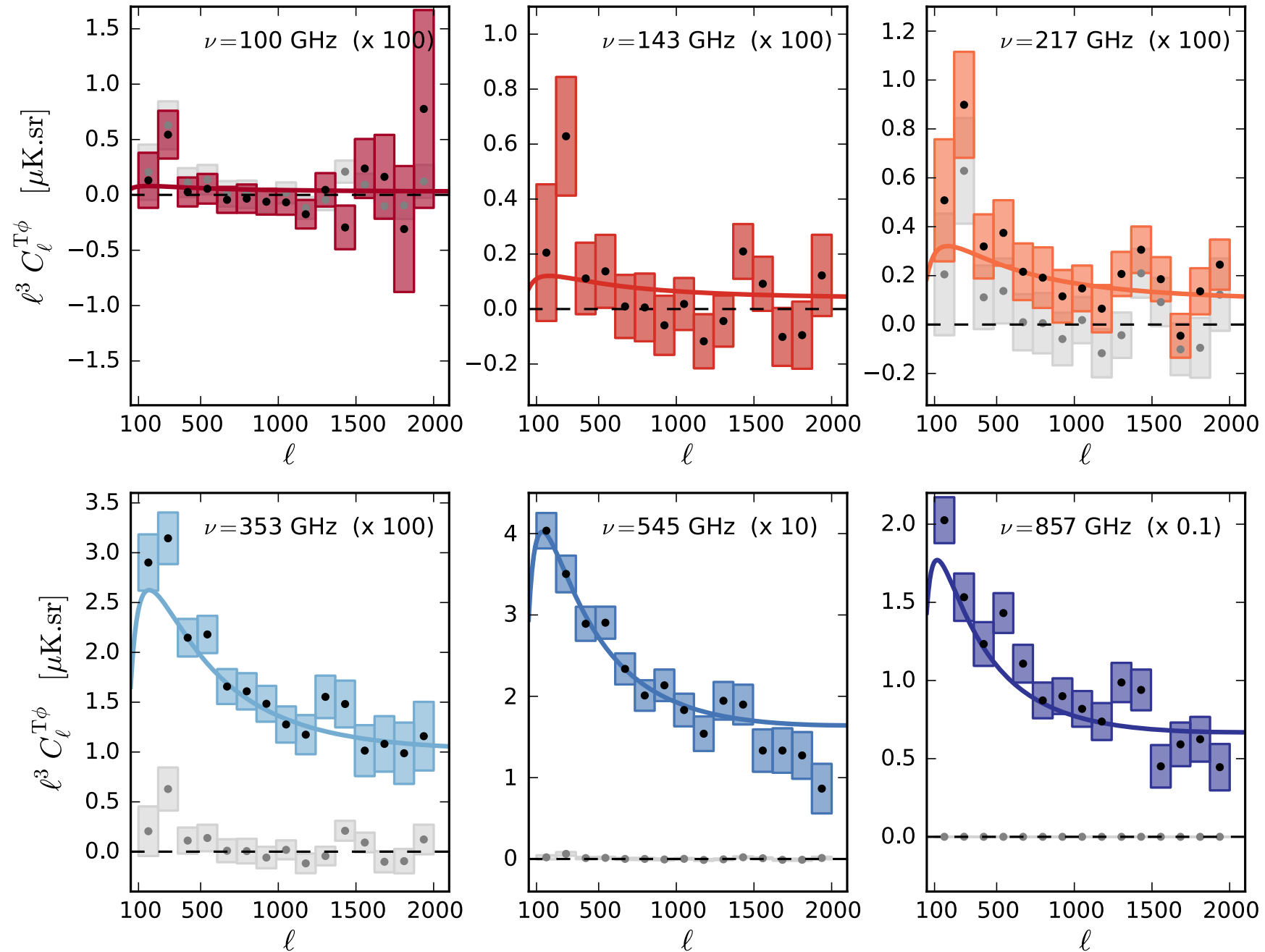


The lensing map traces the matter distribution up to the last scattering surface



CMB lensing - CIB

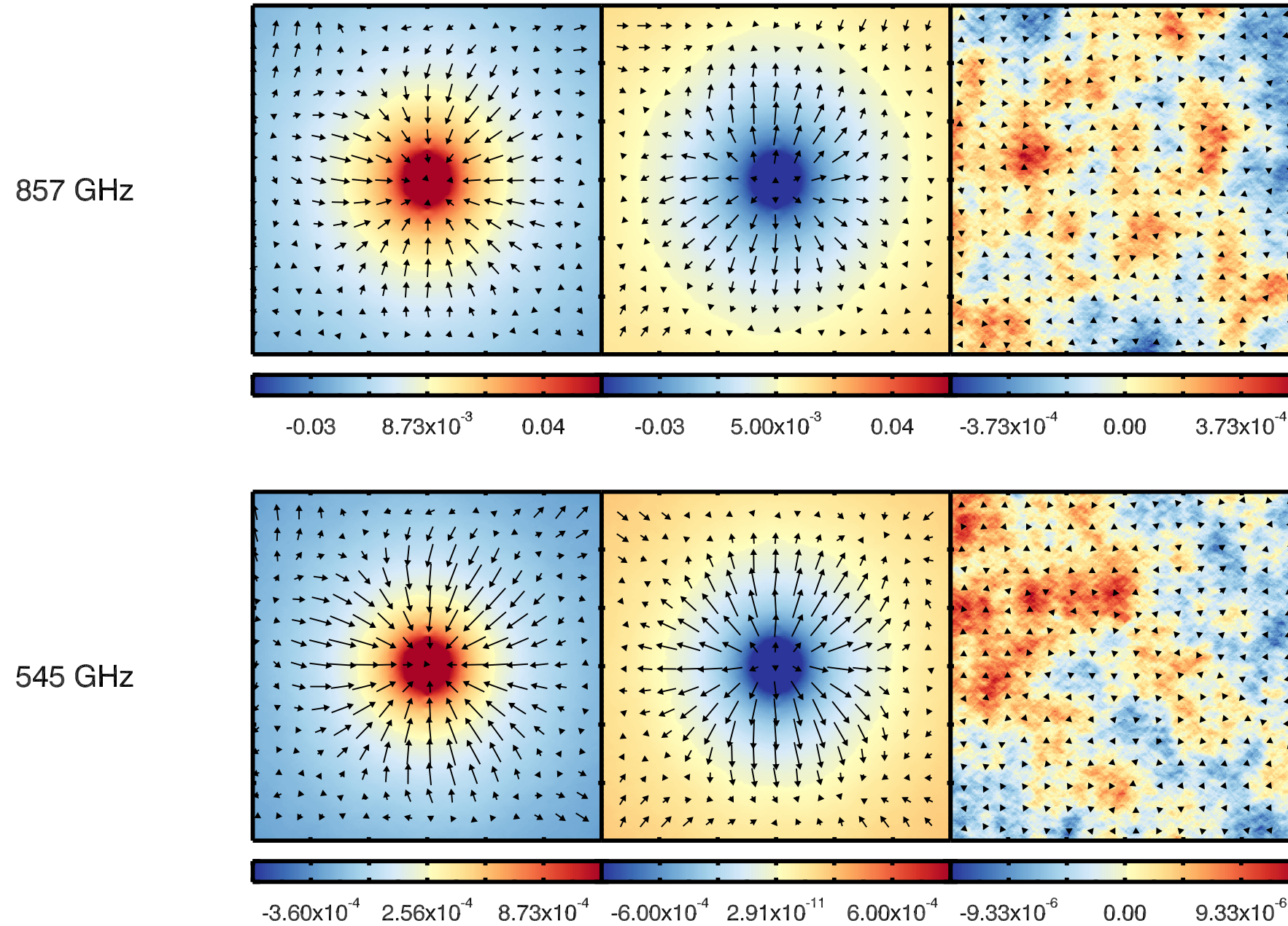
■ Lensing potential correlated with HFI temperature maps





CMB lensing - CIB

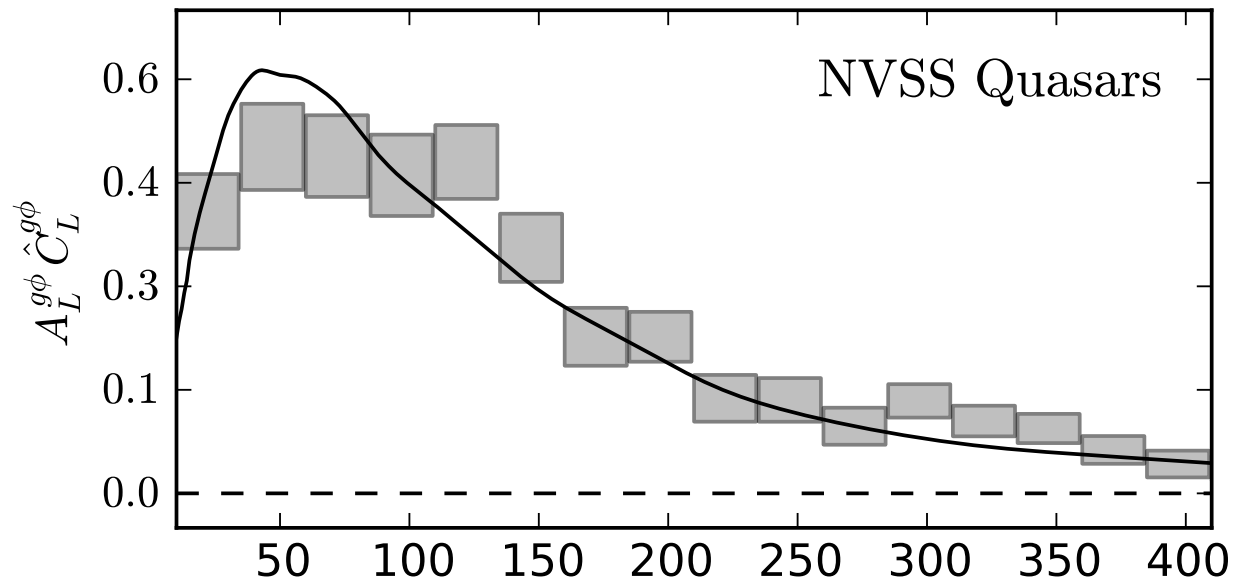
- Deflection stacked on 20.000 temperature extrema



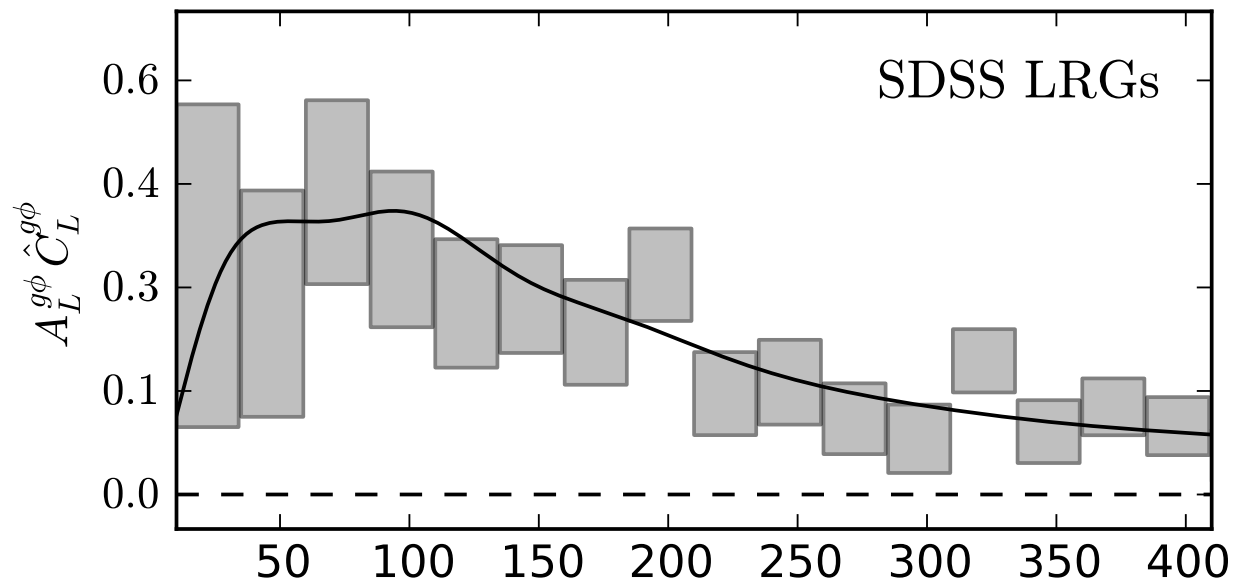
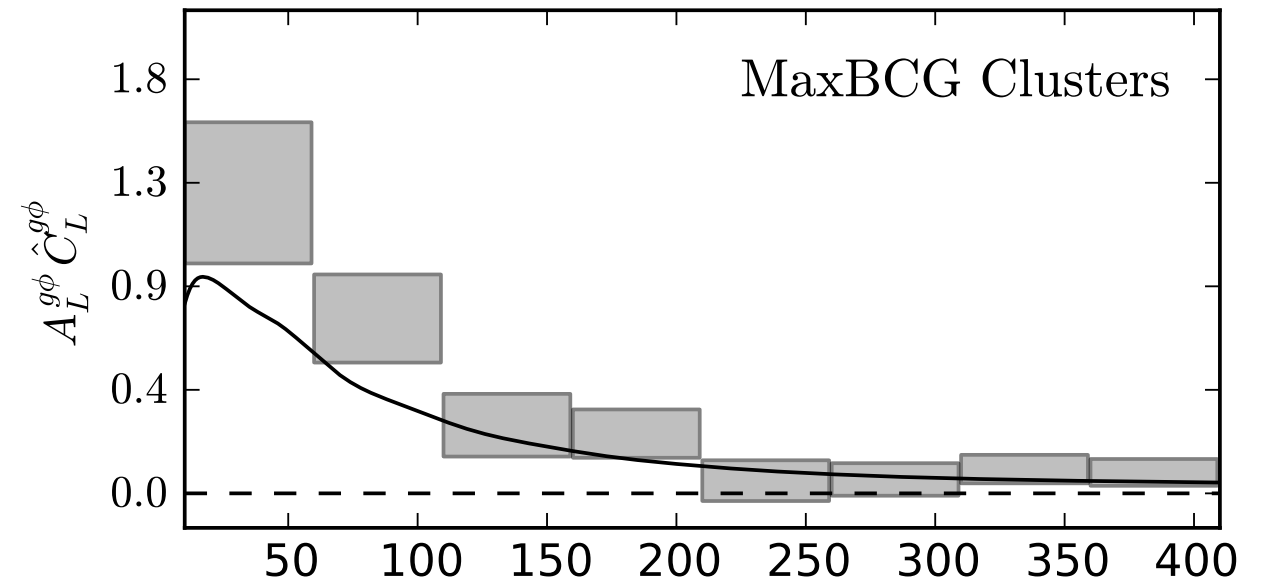


CMB lensing - External tracers

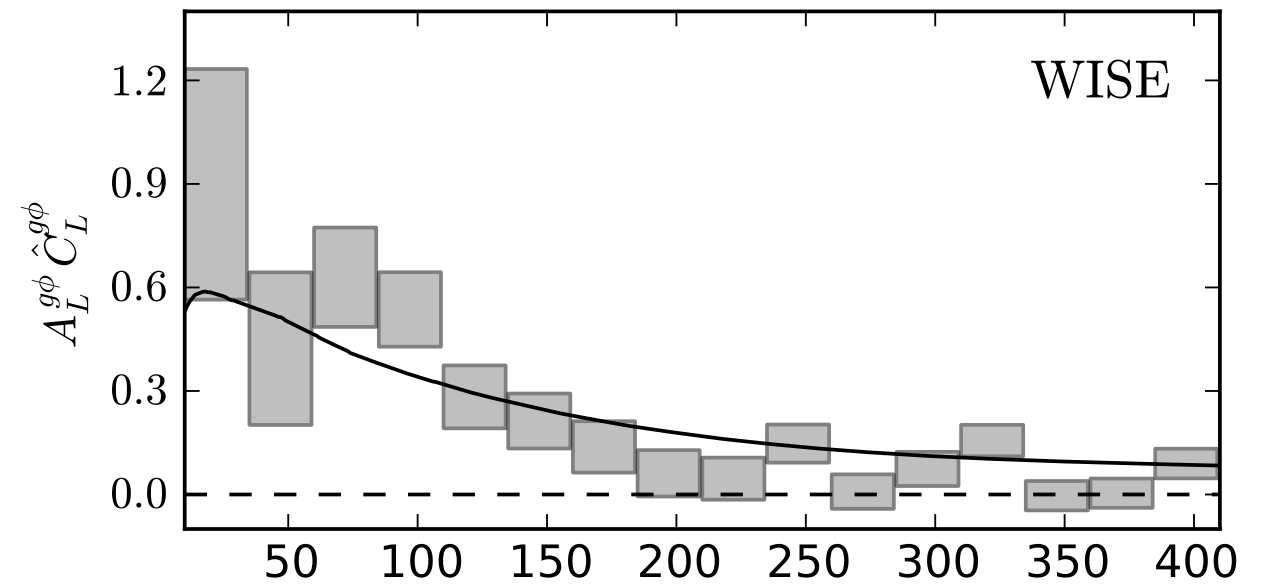
$$b(z) = 1.7 \rightarrow \hat{A}_{\text{NVSS}}^{g\phi} = 1.03 \pm 0.05 (\approx 20\sigma)$$



$$b(z) = 3 \rightarrow \hat{A}_{\text{MaxBCG}}^{g\phi} = 1.54 \pm 0.21 (\approx 7\sigma)$$



$$b(z) = 2 \rightarrow \hat{A}_{\text{LRGs}}^{g\phi} = 0.96 \pm 0.10 (\approx 10\sigma)$$

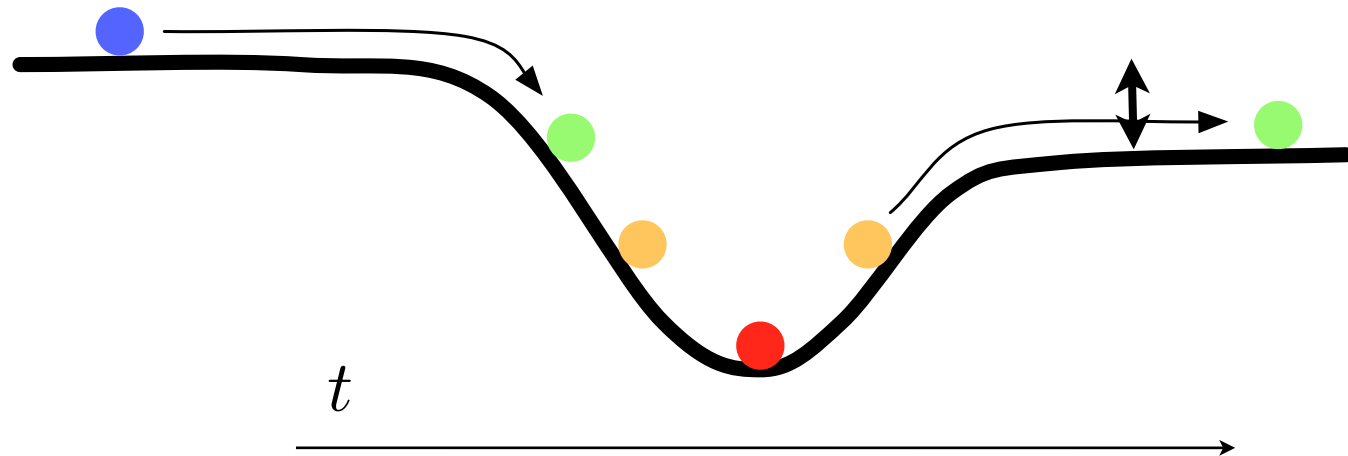


$$b(z) = 1 \rightarrow \hat{A}_{\text{WISE}}^{g\phi} = 0.97 \pm 0.13 (\approx 7\sigma)$$



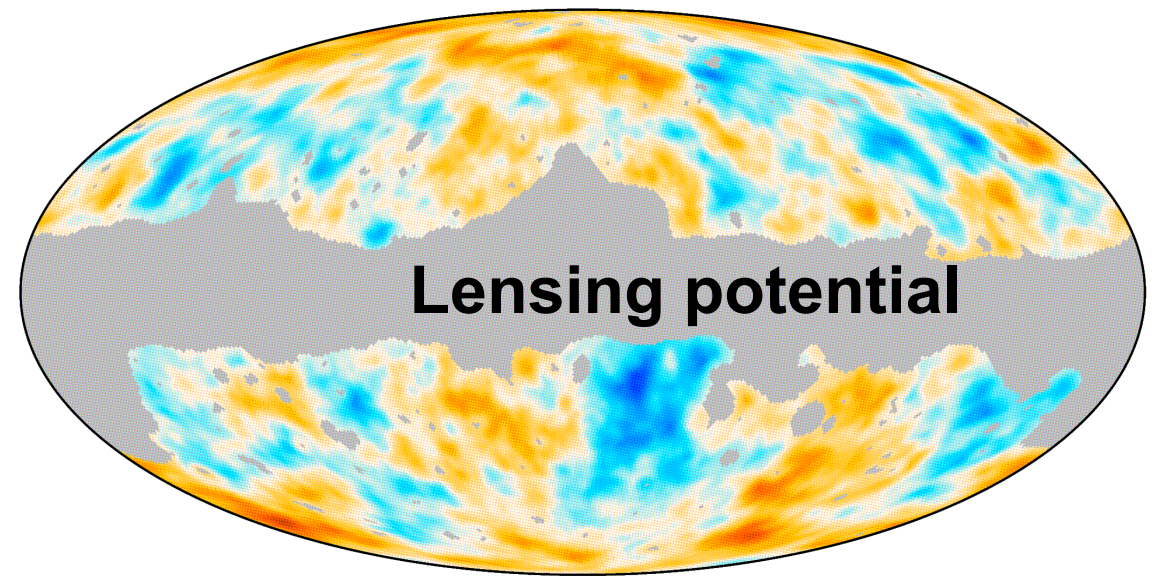
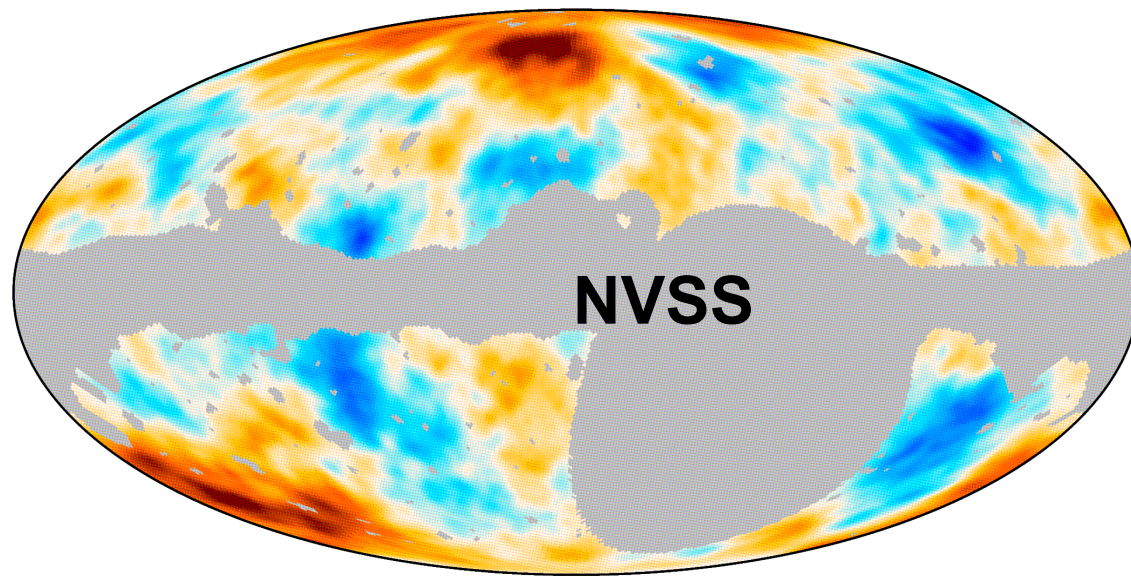
ISW

Shallowing of the potential due to expansion driven by dark energy



$$\frac{\Delta T}{T} = \frac{2}{c^3} \int_{\eta^*}^{\eta_0} d\eta \frac{\partial \Phi}{\partial \eta}$$

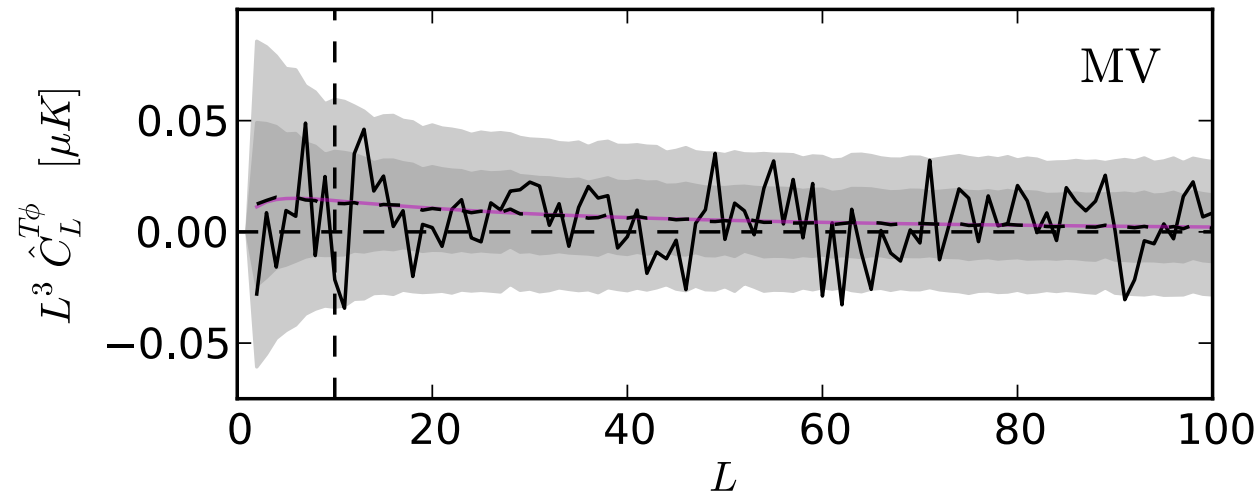
Courtesy: K. Benabed



Planck ISW maps



ISW - Lensing correlation

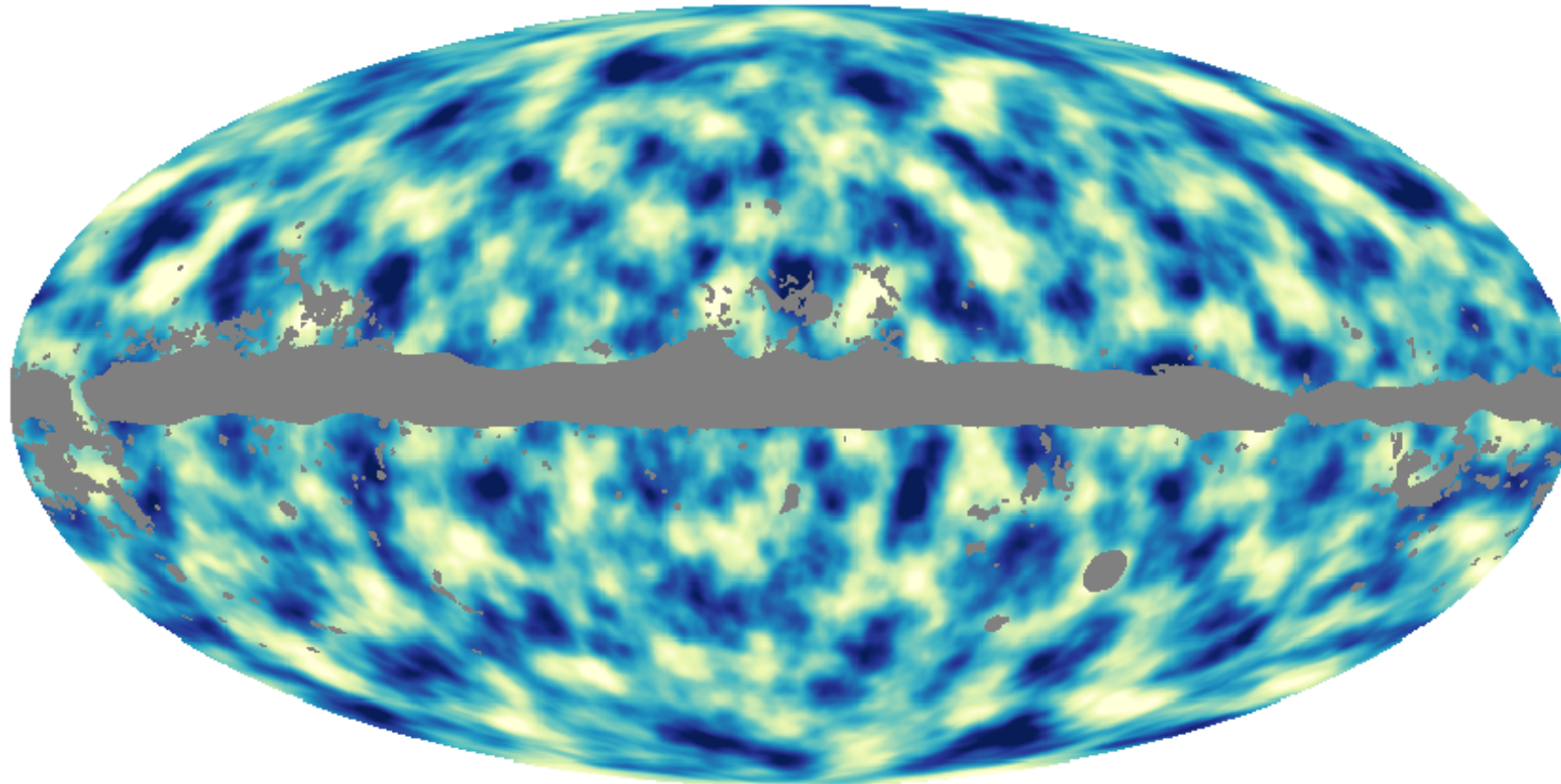


Estimator		C-R	σ	NILC	σ	SEVEM	σ	SMICA	σ	MV	
$T\phi$	$\ell \geq 10$	0.52 ± 0.33	1.5	0.72 ± 0.30	2.4	0.58 ± 0.31	1.9	0.68 ± 0.30	2.3	0.78 ± 0.32	2.4
	$\ell \geq 2$	0.52 ± 0.32	1.6	0.75 ± 0.28	2.7	0.62 ± 0.29	2.1	0.70 ± 0.28	2.5		
KSW		0.75 ± 0.32	2.3	0.85 ± 0.32	2.7	0.68 ± 0.32	2.1	0.81 ± 0.31	2.6		
binned		0.80 ± 0.40	2.0	1.03 ± 0.37	2.8	0.83 ± 0.39	2.1	0.91 ± 0.37	2.5		
modal		0.68 ± 0.39	1.7	0.93 ± 0.37	2.5	0.60 ± 0.37	1.6	0.77 ± 0.37	2.1		

- First 2.5sigma detection. Robust against dataset and estimator
- Links Λ and CDM



The Planck lensing map



- (Almost) Full-sky map of the large scale structure at $z \sim 2$
- Will be used for the next 10-20 years (DES, Euclid, LSST, ...)
- Available on the PLA