

Nuclear Forces and Exotic Oxygen and Calcium Isotopes

Jason D. Holt



TECHNISCHE
UNIVERSITÄT
DARMSTADT

References

- Otsuka, Suzuki, JDH, Schwenk, Akaishi PRL **105**, 032501 (2010)
- JDH, Menendez, Schwenk, EPJA **49**, 39 (2013)
- Caesar et al. (R3B), Simonis, JDH, Menendez, Schwenk PRC **88**, 034313 (2013)
- Bogner, Hergert, JDH, Schwenk, Binder, Calci, Langhammer, Roth, arXiv:1402.1407



Bundesministerium
für Bildung
und Forschung



Drip Lines and Magic Numbers: The Nuclear Landscape Toward the Extremes

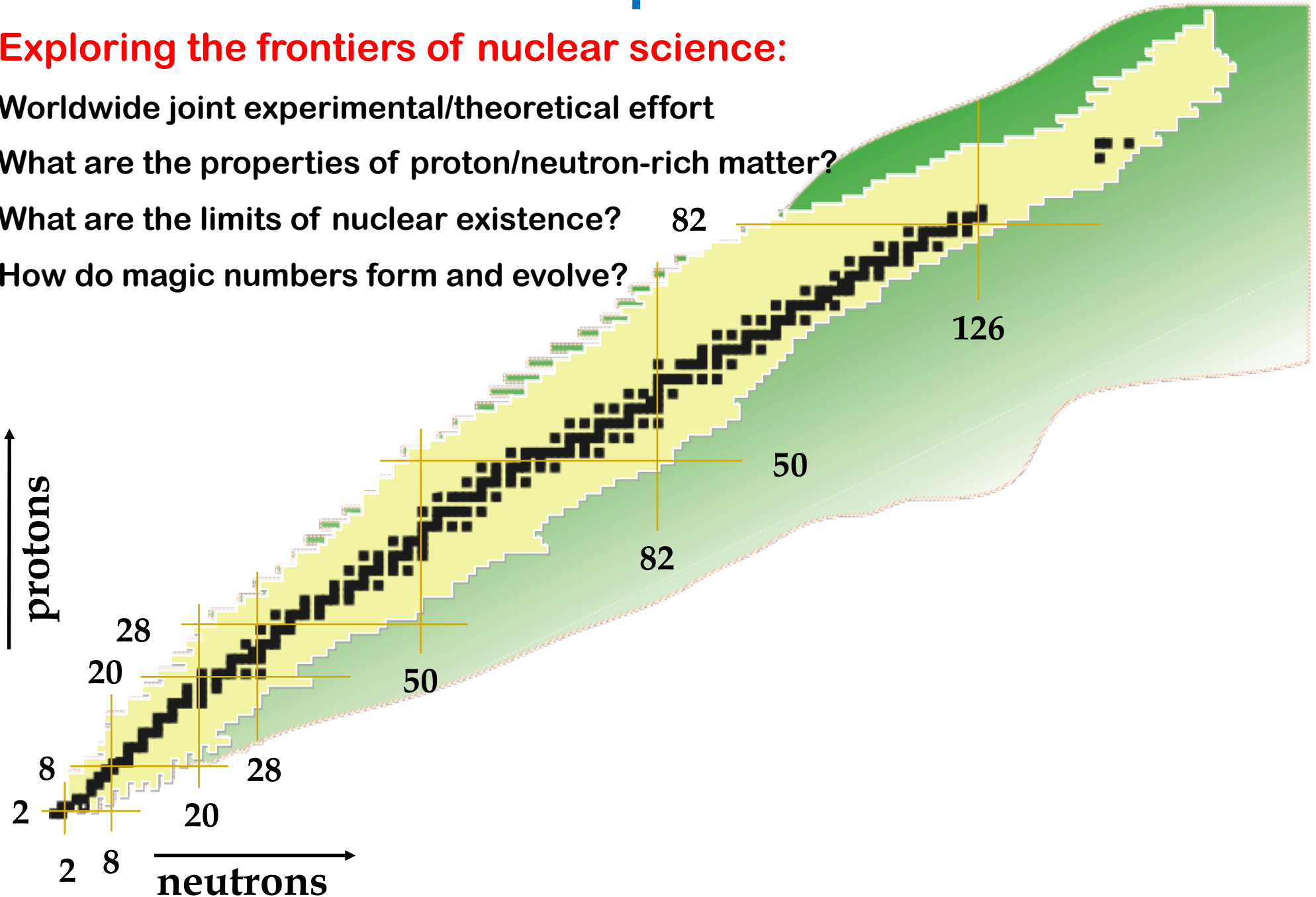
Exploring the frontiers of nuclear science:

Worldwide joint experimental/theoretical effort

What are the properties of proton/neutron-rich matter?

What are the limits of nuclear existence?

How do magic numbers form and evolve?



Drip Lines and Magic Numbers: The Nuclear Landscape Toward the Extremes

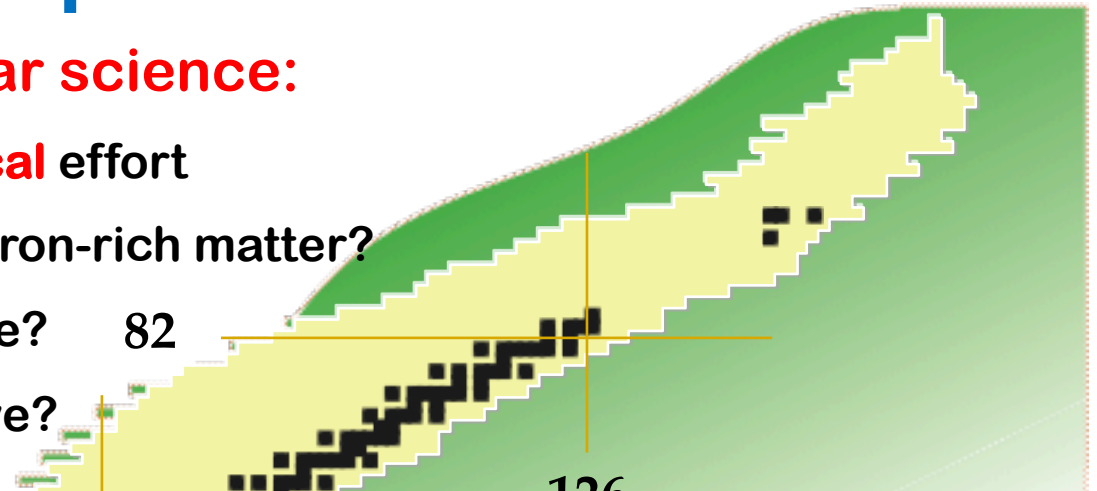
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What are the properties of proton/neutron-rich matter?

What are the limits of nuclear existence? 82

How do magic numbers form and evolve? 126



Advances in many-body methods

Green's Function Monte Carlo
(Gezerlis, Carlson, Pieper, Wiringa)

Hyperspherical Harmonics
(Bacca)

No-Core Shell Model
(Navratil, Barrett, Vary, Roth)

Coupled Cluster

(Hagen, Papenbrock, Dean, Roth)

In-Medium SRG

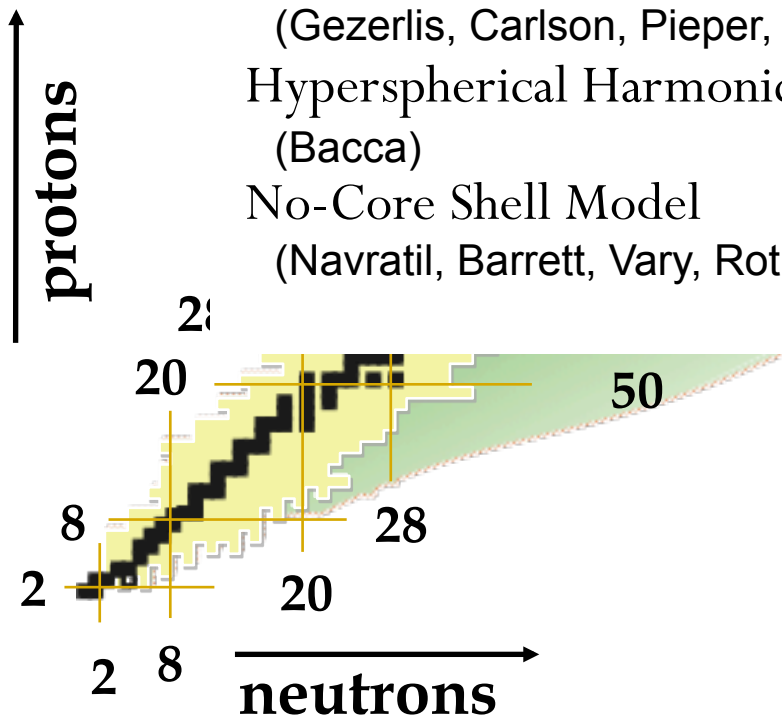
(Bogner, Hergert, JDH, Schwenk)

Many-Body Perturbation Theory

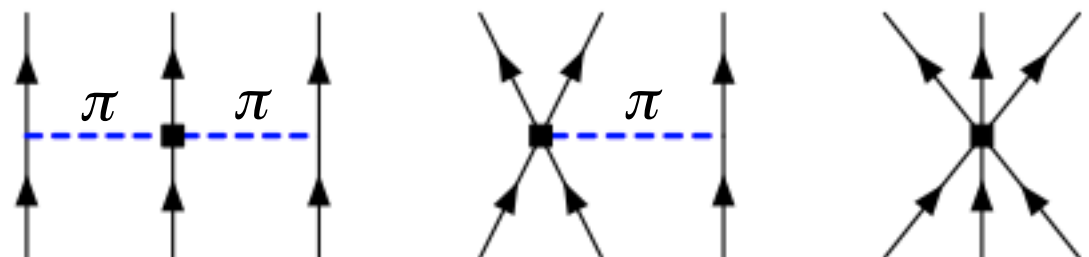
(JDH, Hjorth-Jensen, Schwenk)

Self-Consistent Green's Function

(Barbieri, Soma, Duguet)



3N forces essential for exotic nuclei



Drip Lines and Magic Numbers: The Nuclear Landscape Toward the Extremes

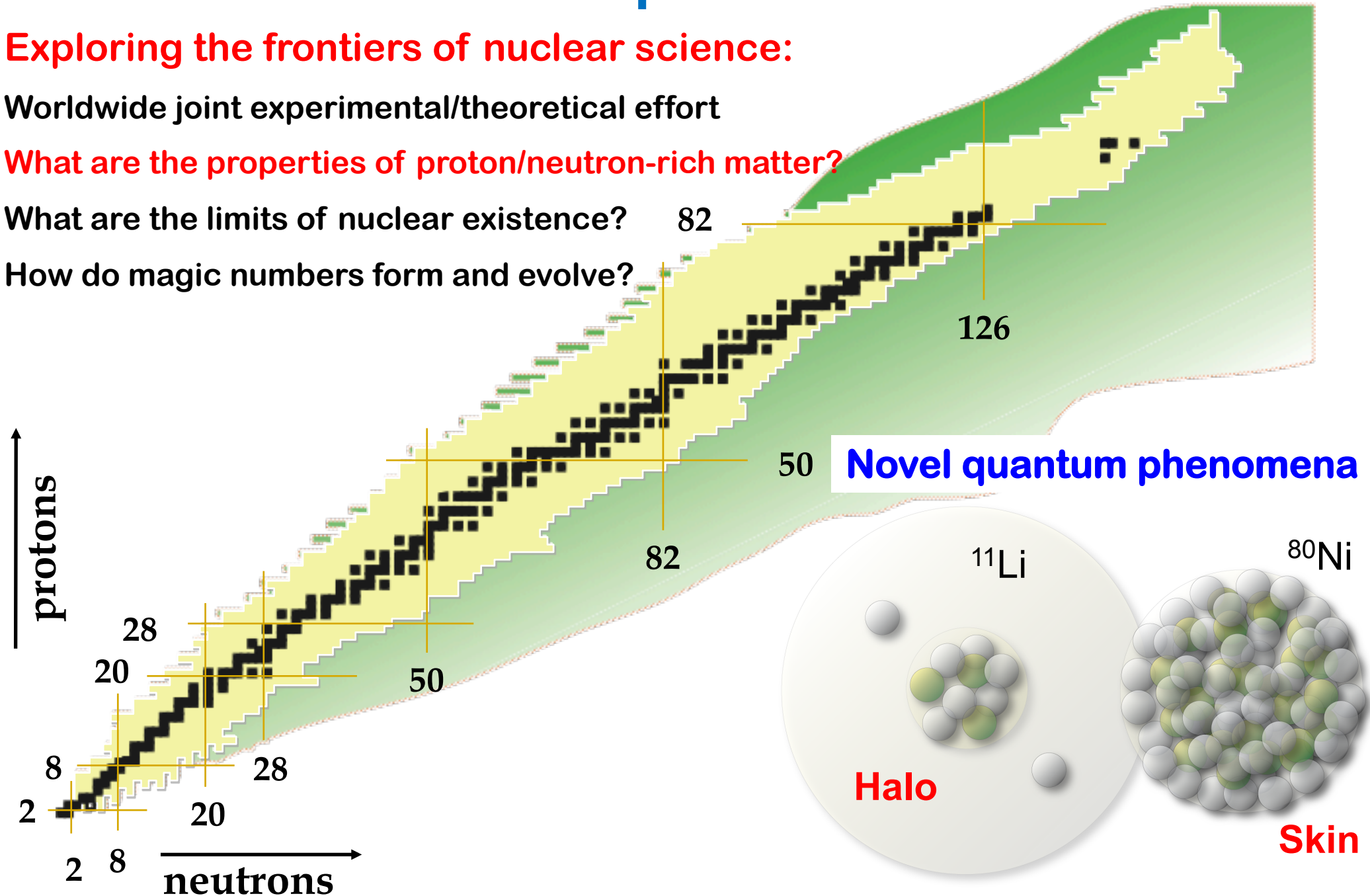
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Drip Lines and Magic Numbers: 3N Forces in Medium-Mass Nuclei

Exploring the frontiers of nuclear science:

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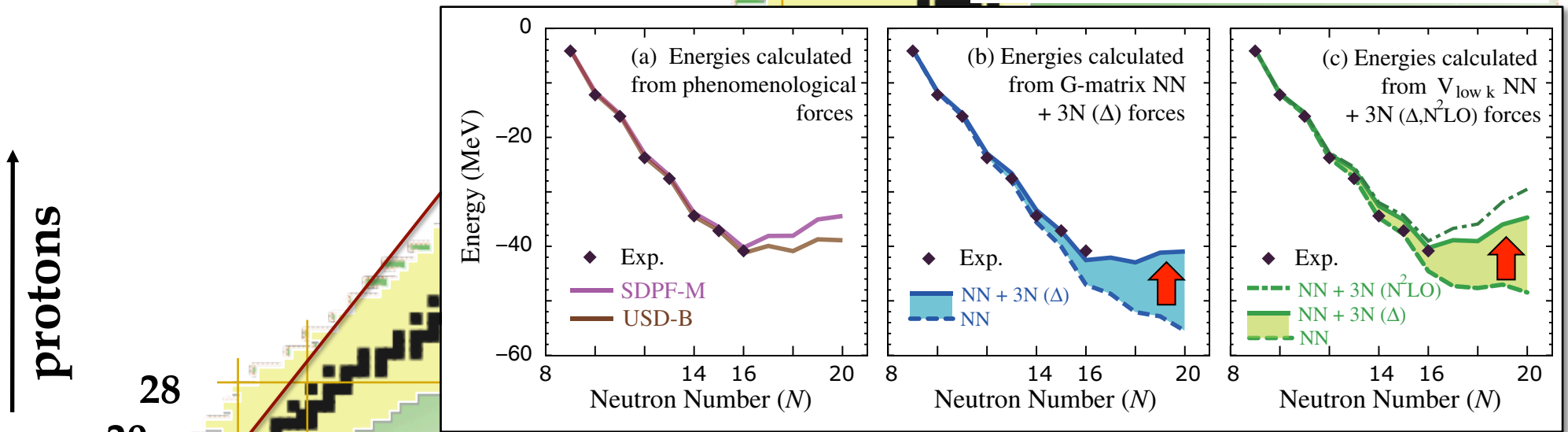
What are the properties of proton/neutron-rich matter?

What are the limits of nuclear existence?

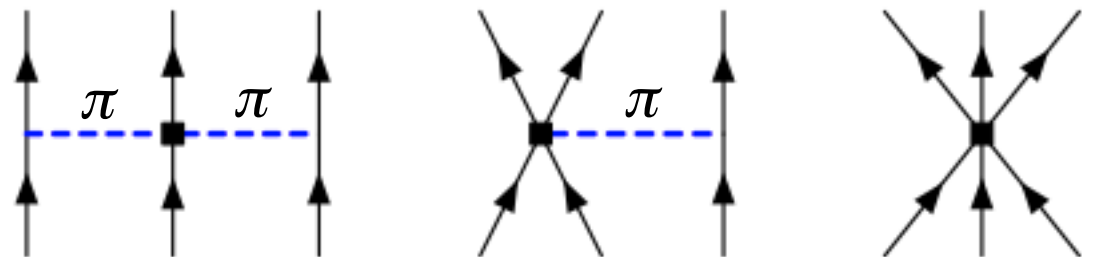
How do magic numbers form and evolve?

82

Heaviest oxygen isotope



Otsuka, Suzuki, JDH, Schwenk, Akaishi, PRL (2010)



Drip Lines and Magic Numbers: 3N Forces in Medium-Mass Nuclei

Exploring the frontiers of nuclear science:

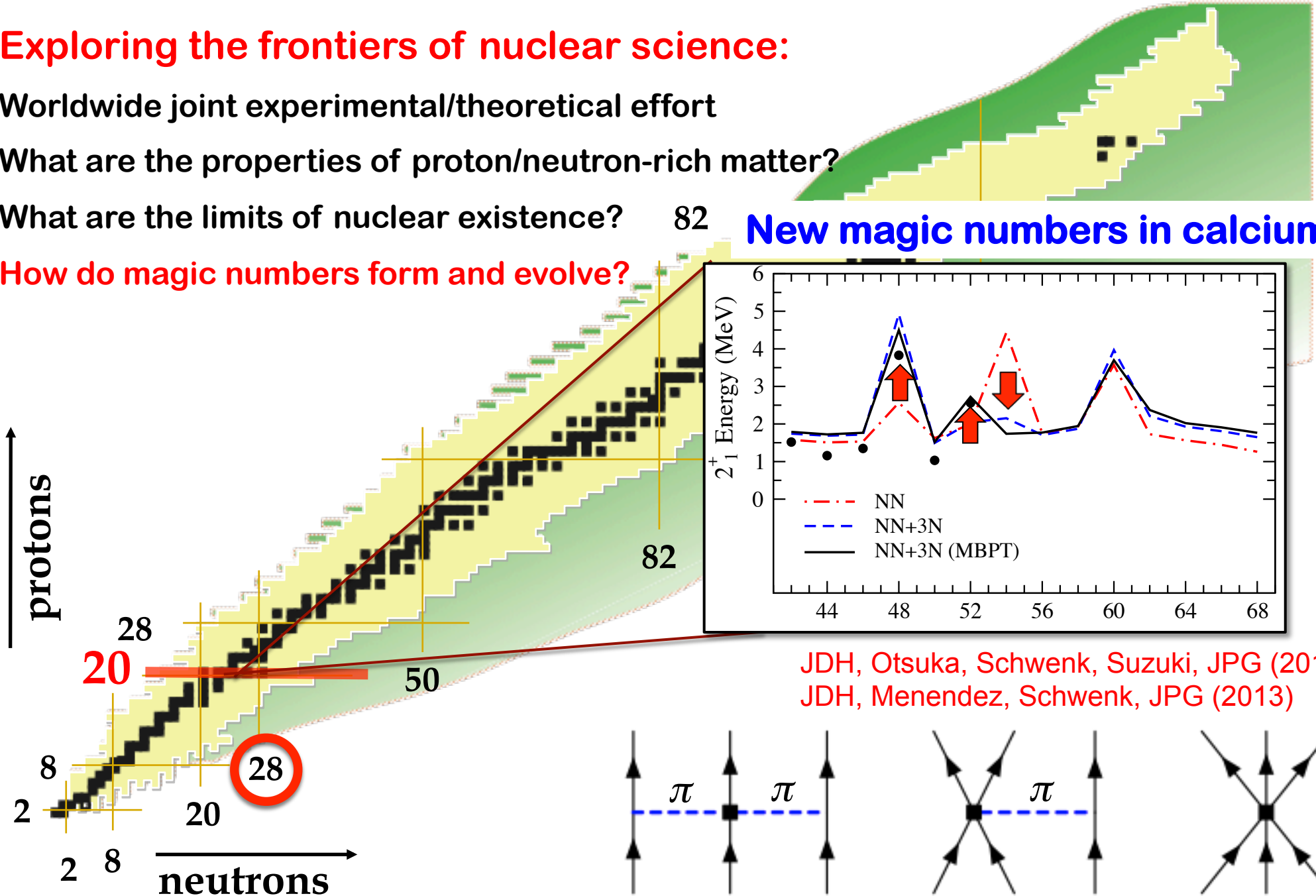
Worldwide joint experimental/theoretical effort

What are the properties of proton/neutron-rich matter?

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New magic numbers in calcium



JDH, Otsuka, Schwenk, Suzuki, JPG (2012)

JDH, Menendez, Schwenk, JPG (2013)

Drip Lines and Magic Numbers: 3N Forces in Medium-Mass Nuclei



nuclear science:

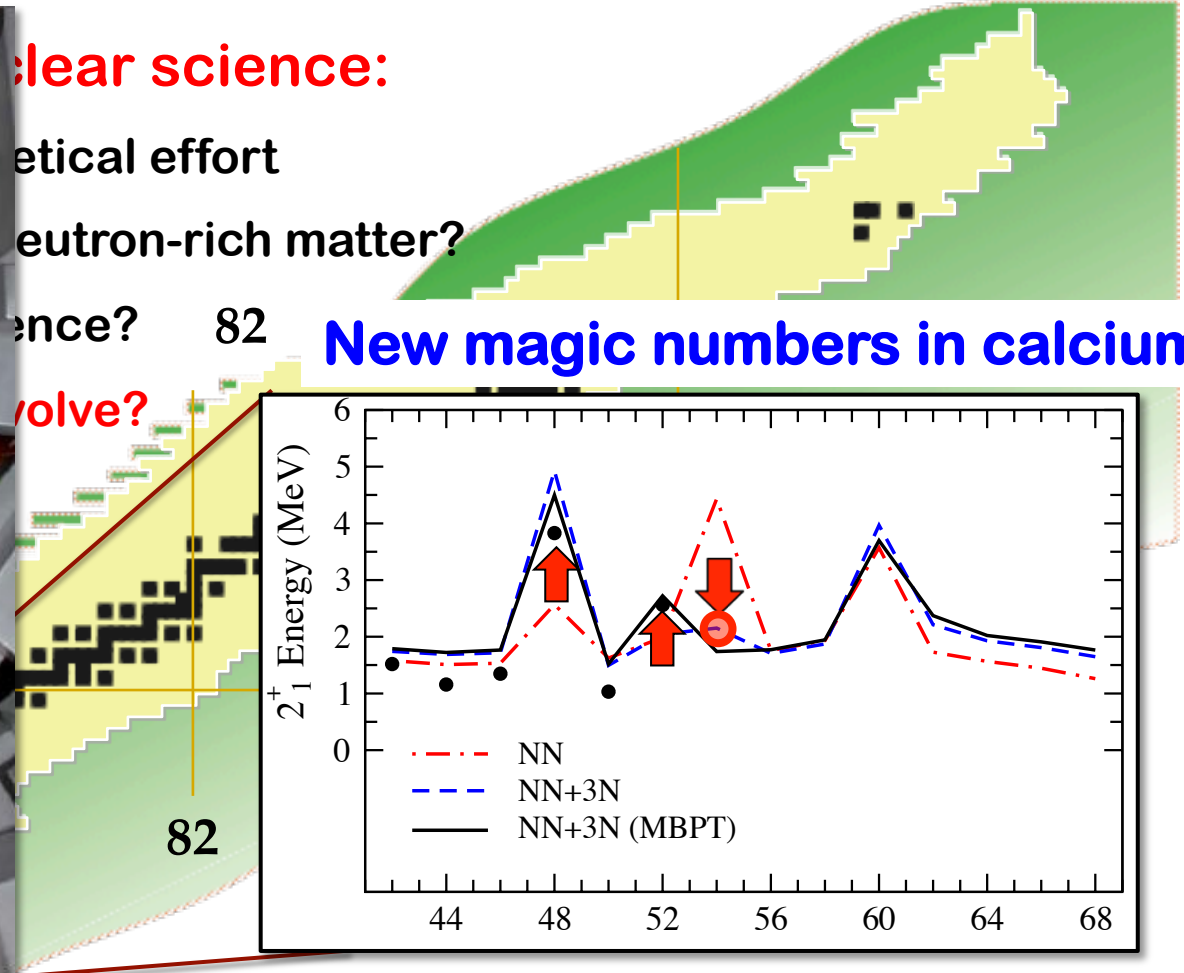
theoretical effort

neutron-rich matter?

importance? 82

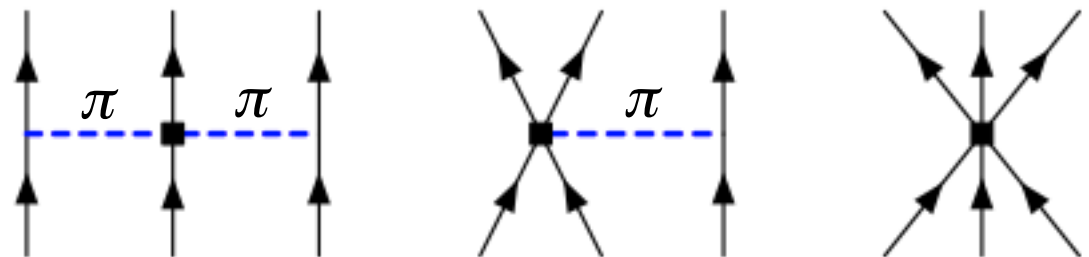
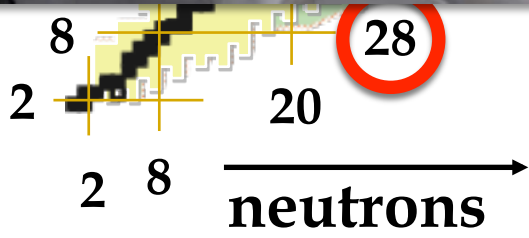
evolve?

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JDH, Otsuka, Schwenk, Suzuki, JPG (2012)

JDH, Menendez, Schwenk, JPG (2013)



Drip Lines and Magic Numbers: 3N Forces in Medium-Mass Nuclei

LETTER

doi:10.1038/nature12522

Evidence for a new nuclear ‘magic number’ from the level structure of ^{54}Ca

D. Steppenbeck¹, S. Takeuchi², N. Aoi³, P. Doornenbal², M. Matsushita¹, H. Wang², H. Baba², N. Fukuda², S. Go¹, M. Honma⁴, J. Lee², K. Matsui⁵, S. Michimasa¹, T. Motobayashi², D. Nishimura⁶, T. Otsuka^{1,5}, H. Sakurai^{2,5}, Y. Shiga⁷, P.-A. Söderström², T. Sumikama

LETTER

doi:10.1038/nature12226

Masses of exotic calcium isotopes pin down nuclear forces

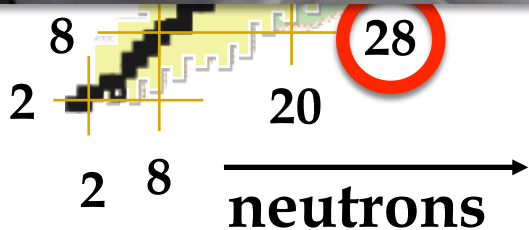
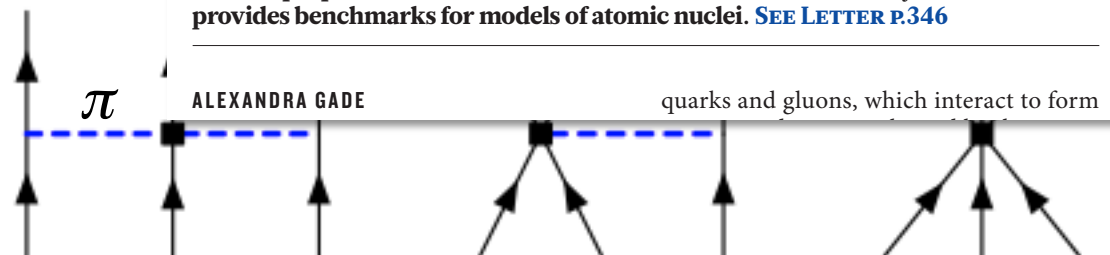
F. Wienholtz¹, D. Beck², K. Blaum³, Ch. Borgmann³, M. Breitenfeldt⁴, R. B. Cakirli^{3,5}, S. George¹, F. Herfurth², J. D. Holt^{6,7}, M. Kowalska⁸, S. Kreim^{3,8}, D. Lunney⁹, V. Manea⁹, J. Menéndez^{6,7}, D. Neidherr², M. Rosenbusch¹, L. Schweikhard¹, A. Schwenk^{7,6}, J. Simonis^{6,7}, J. Stanja¹⁰, R. N. Wo

PHYSICS

NEWS & VIEWS RESEARCH

Heavy calcium nuclei weigh in

The configurations of calcium nuclei make them good test cases for studies of nuclear properties. The measurement of the masses of two heavy calcium nuclei provides benchmarks for models of atomic nuclei. [SEE LETTER P.346](#)



Oxygen Isotopes

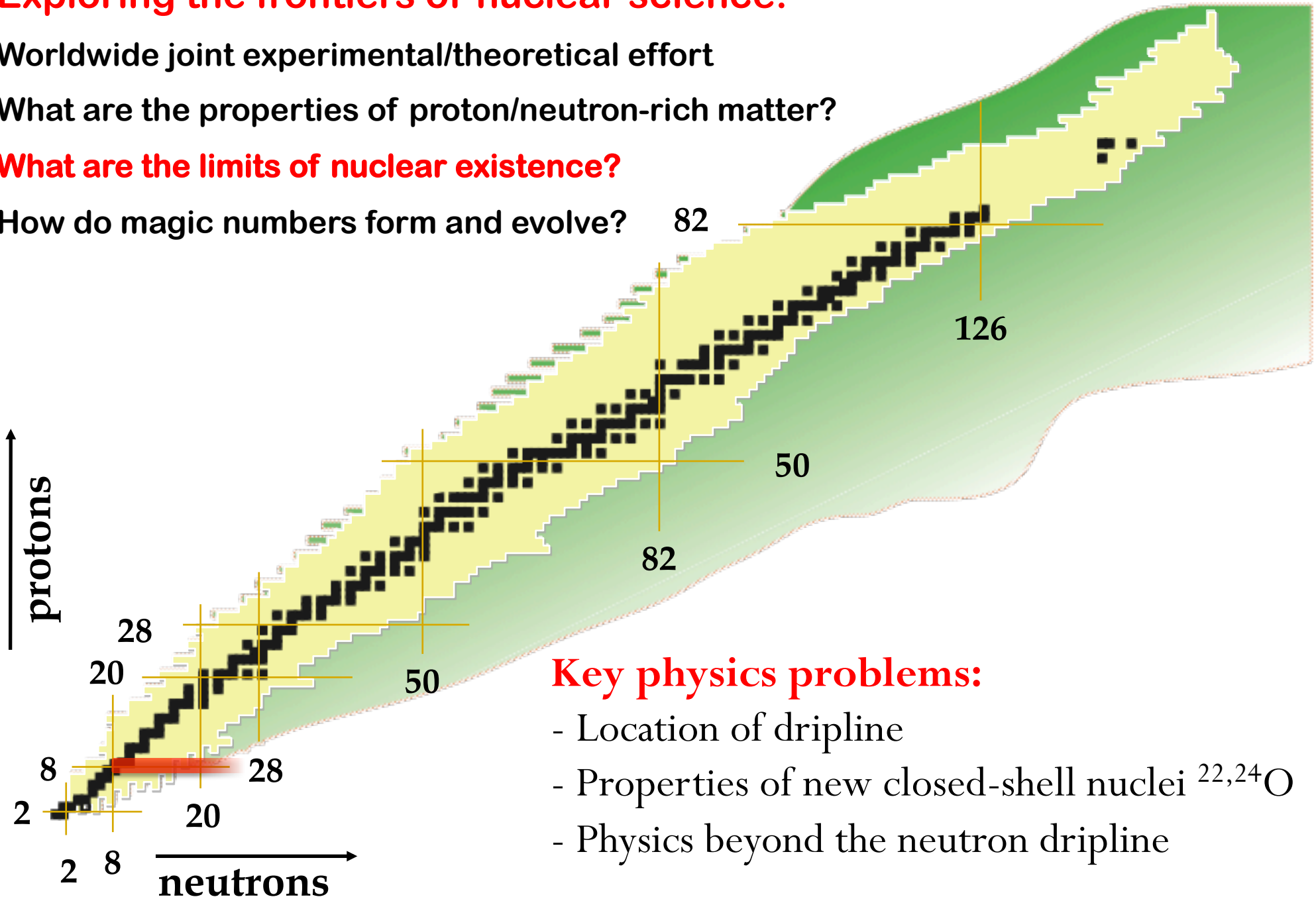
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Key physics problems:

- Location of dripline
- Properties of new closed-shell nuclei $^{22,24}\text{O}$
- Physics beyond the neutron dripline

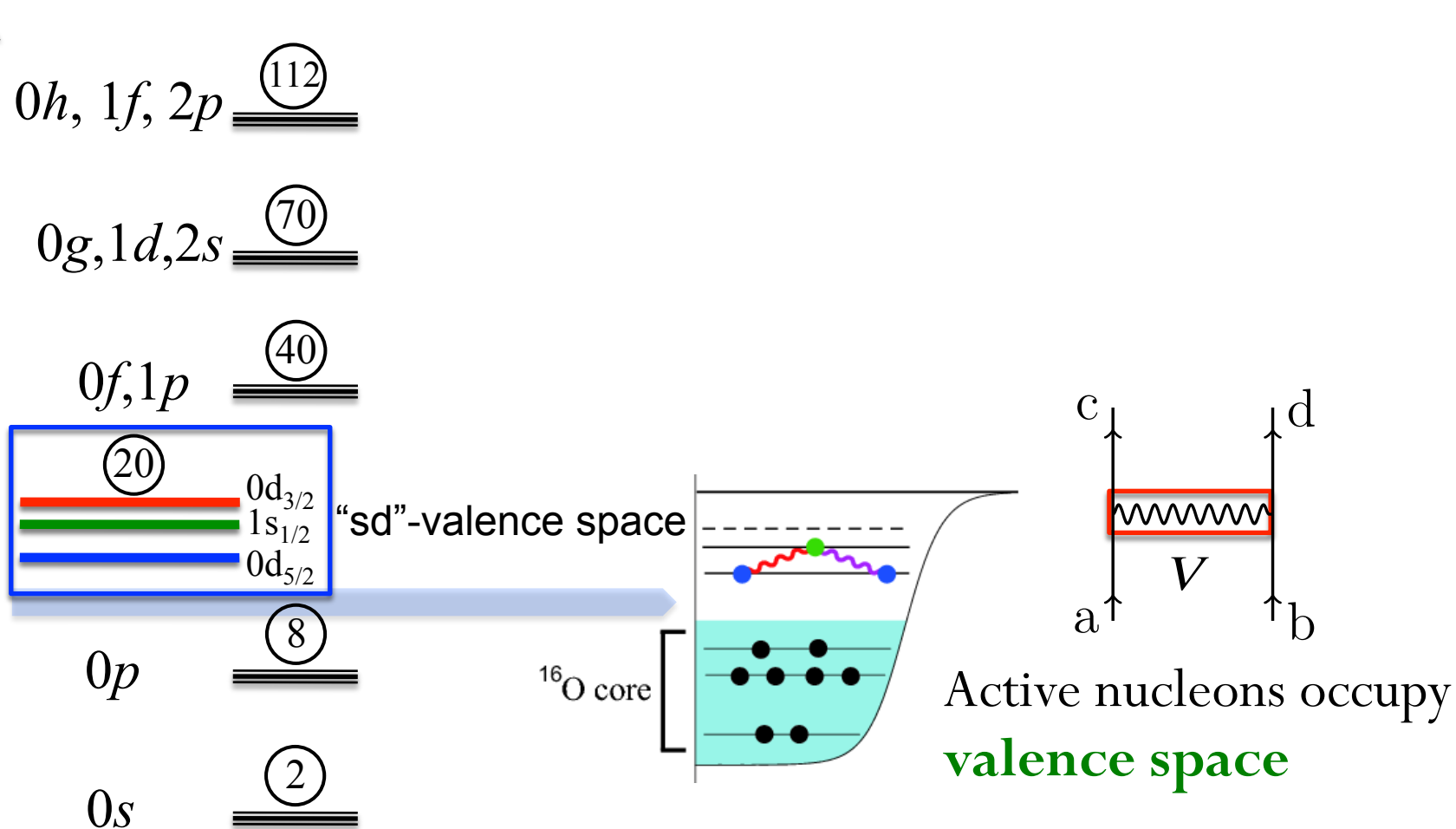
The Nuclear Many-Body Problem

Nuclei understood as many-body system starting from closed shell, add nucleons

Calculate **valence-space** Hamiltonian inputs from nuclear forces

Interaction matrix elements

Single-particle energies (SPEs)



Active nucleons occupy **valence space**

Inert core: **does not reproduce experiment**

The Nuclear Many-Body Problem

Nuclei understood as many-body system starting from closed shell, add nucleons

Calculate **valence-space** Hamiltonian inputs from nuclear forces

Interaction matrix elements

Single-particle energies (SPEs)

$0h, 1f, 2p$ $\underline{\underline{\textcircled{112}}}$

Solution: allow breaking of core

$0g, 1d, 2s$ $\underline{\underline{\textcircled{70}}}$

Effective Hamiltonian for valence nucleons

$0f, 1p$ $\underline{\underline{\textcircled{40}}}$

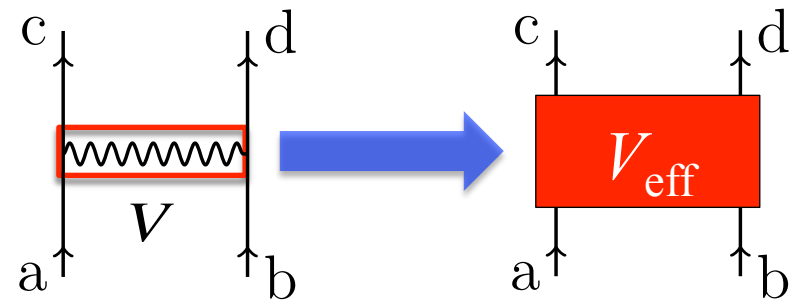
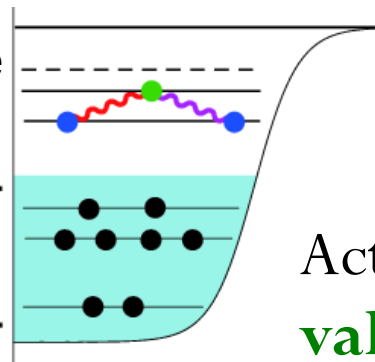
$\underline{\underline{\textcircled{20}}}$
 $0d_{3/2}$
 $1s_{1/2}$
 $0d_{5/2}$

"sd"-valence space

$0p$ $\underline{\underline{\textcircled{8}}}$

^{16}O core

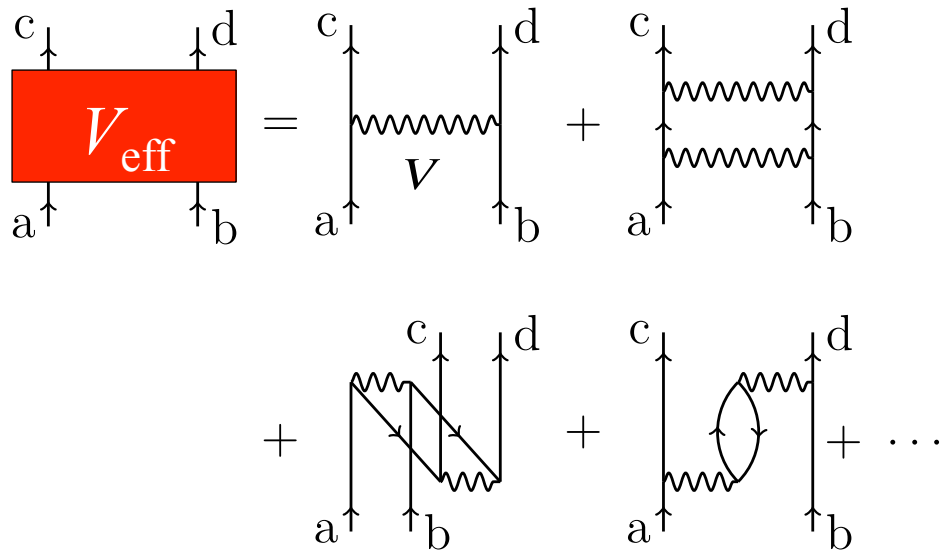
$0s$ $\underline{\underline{\textcircled{2}}}$



Active nucleons occupy **valence space**

Valence-Space Strategy

- ★ 1) Effective interaction: sum excitations outside valence space to **3rd order**
- ★ 2) Single-particle energies calculated self consistently
- ★ 3) Harmonic-oscillator basis of 13 major shells: **converged**
- 4) NN and 3N forces from chiral EFT – to 3rd-order MBPT
- 5) Explore extended valence spaces



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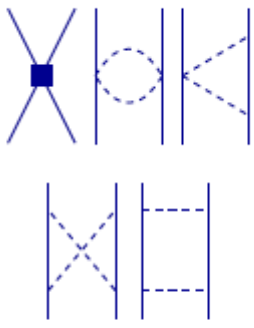


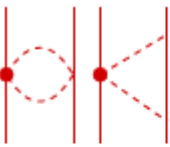
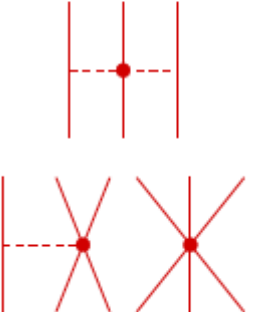


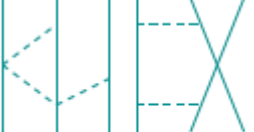

NN matrix elements

- Chiral N³LO (Machleidt, $\Lambda_{\text{NN}} = 500\text{MeV}$); smooth-regulator $V_{\text{low } k}(\Lambda)$

3N force contributions

- Chiral N²LO
 - $c_{\text{D}}, c_{\text{E}}$ fit to properties of light nuclei with $V_{\text{low } k}(\Lambda = \Lambda_{3\text{N}} = 2.0\text{fm}^{-1})$
- Included to 5 major HO shells

Chiral Effective Field Theory: Nuclear Forces

	2N forces	3N forces	4N forces
LO			
NLO			
N ² LO			
N ³ LO			
	+ ...	+ ...	+ ...

Nucleons interact via pion exchanges and contact interactions

Consistent treatment of NN, 3N, ...

3N couplings fit to properties of light nuclei at low momentum

Improve convergence of many-body methods:

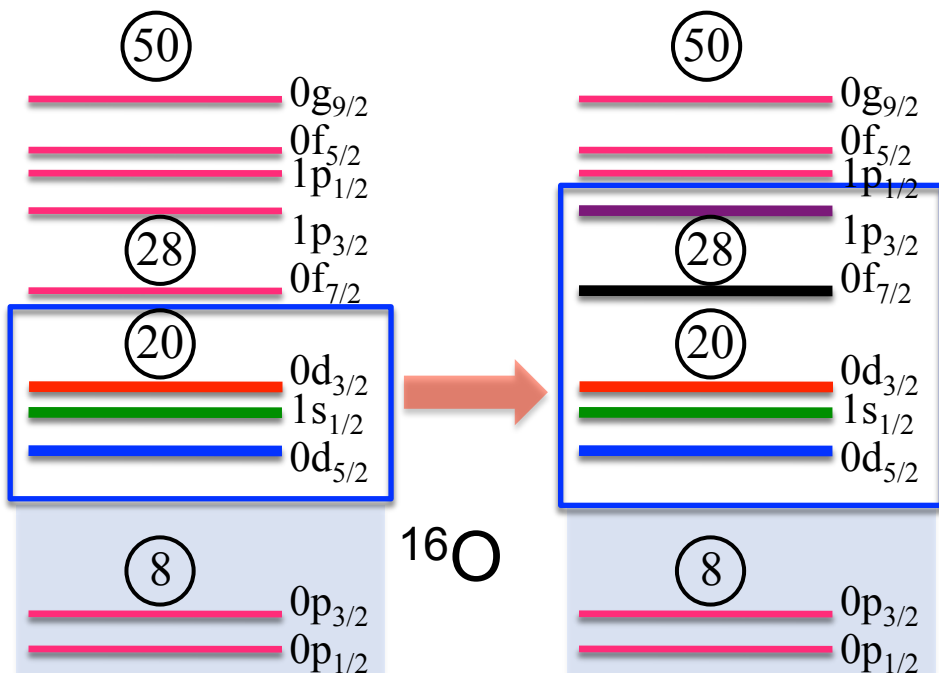
$$V_{\text{low } k} \quad \text{or} \quad V_{\text{SRG}}$$

Weinberg, van Kolck, Kaplan, Savage, Wise, Epelbaum, Kaiser, Meissner, ...

Valence-Space Strategy

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- ★ 5) Explore **extended valence spaces**

Philosophy: diagonalize in largest possible valence space (where orbits relevant)

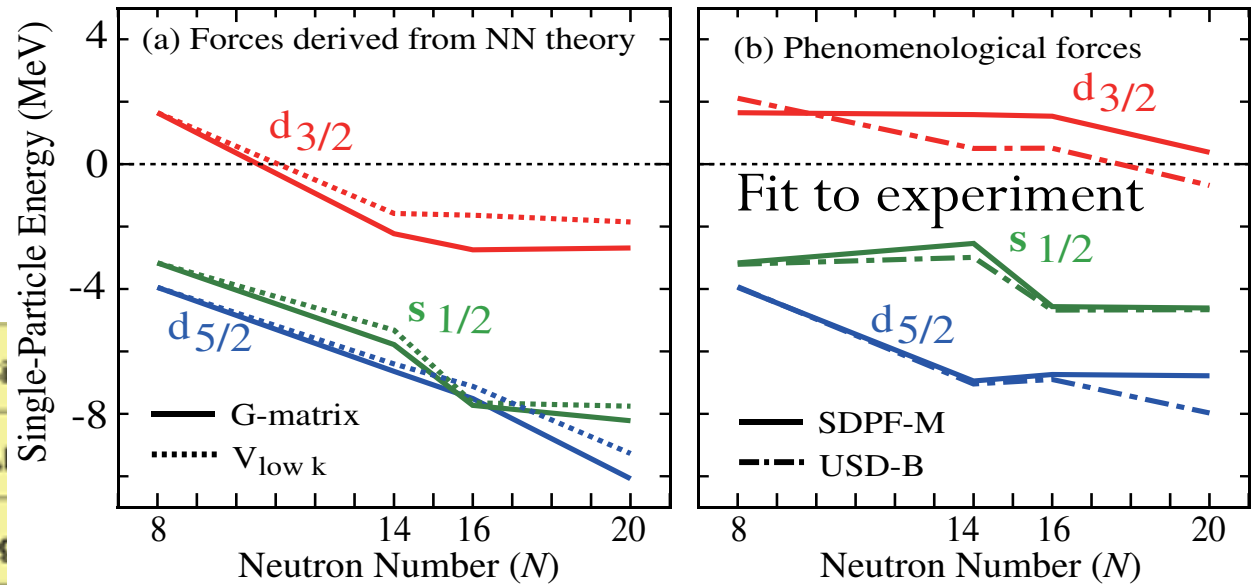
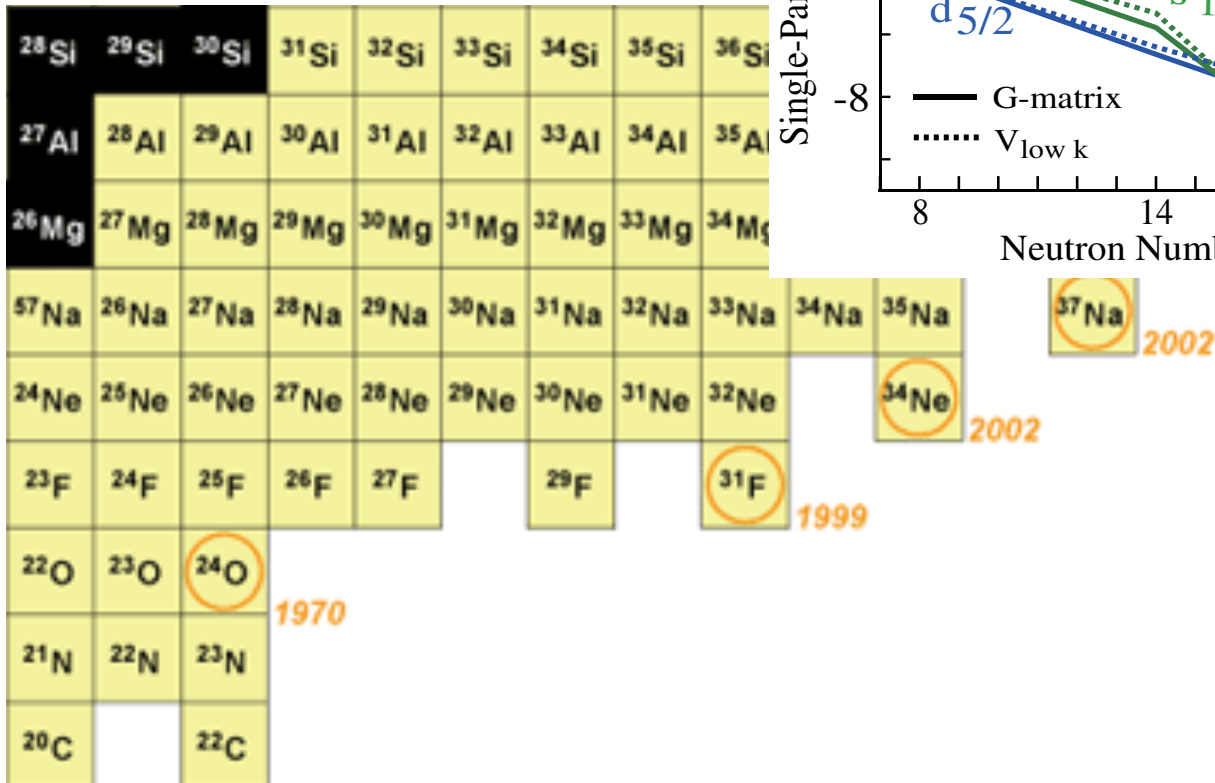


Treats higher orbits nonperturbatively
When important for exotic nuclei?

Limits of Nuclear Existence: Oxygen Anomaly

Microscopic picture:

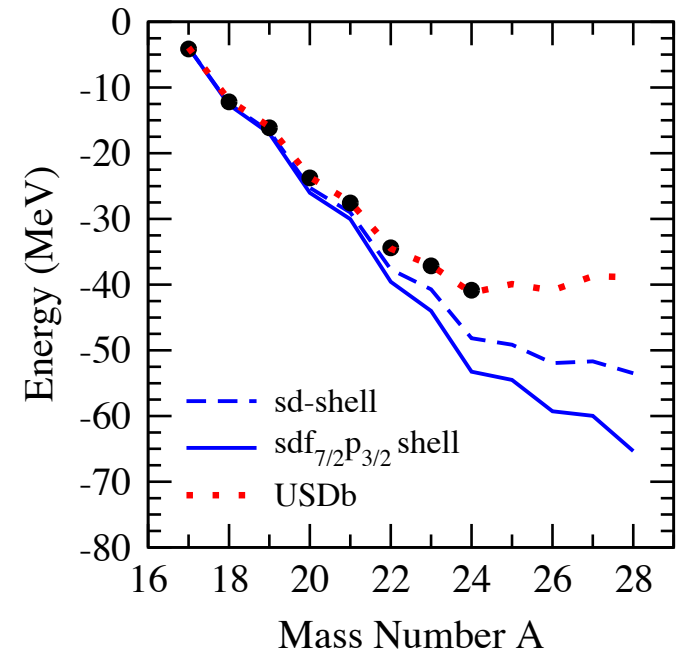
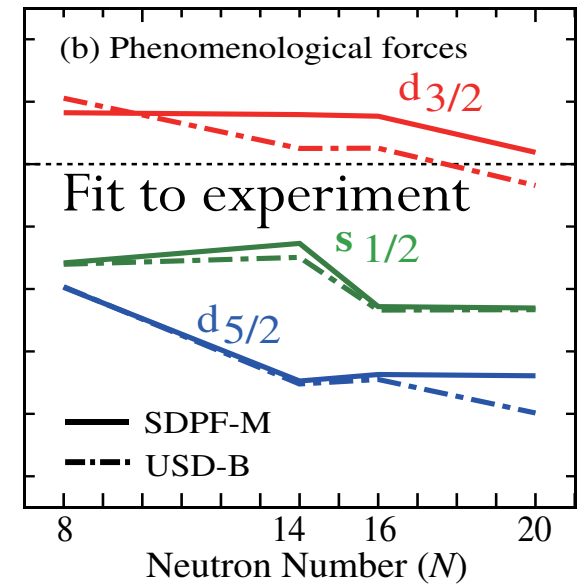
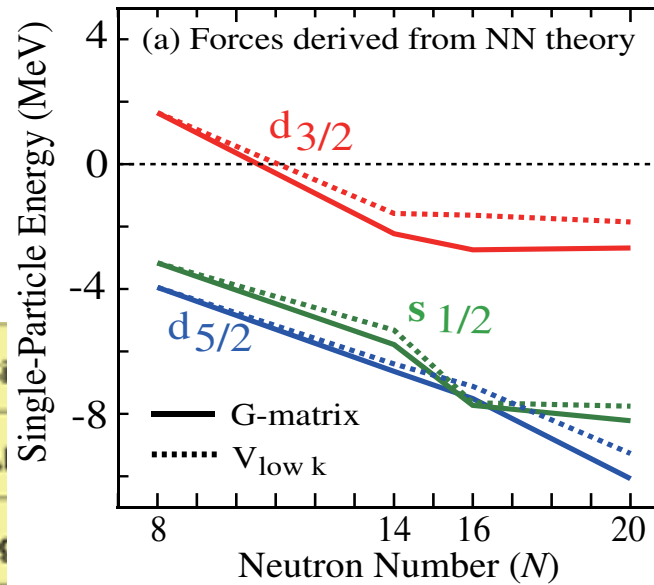
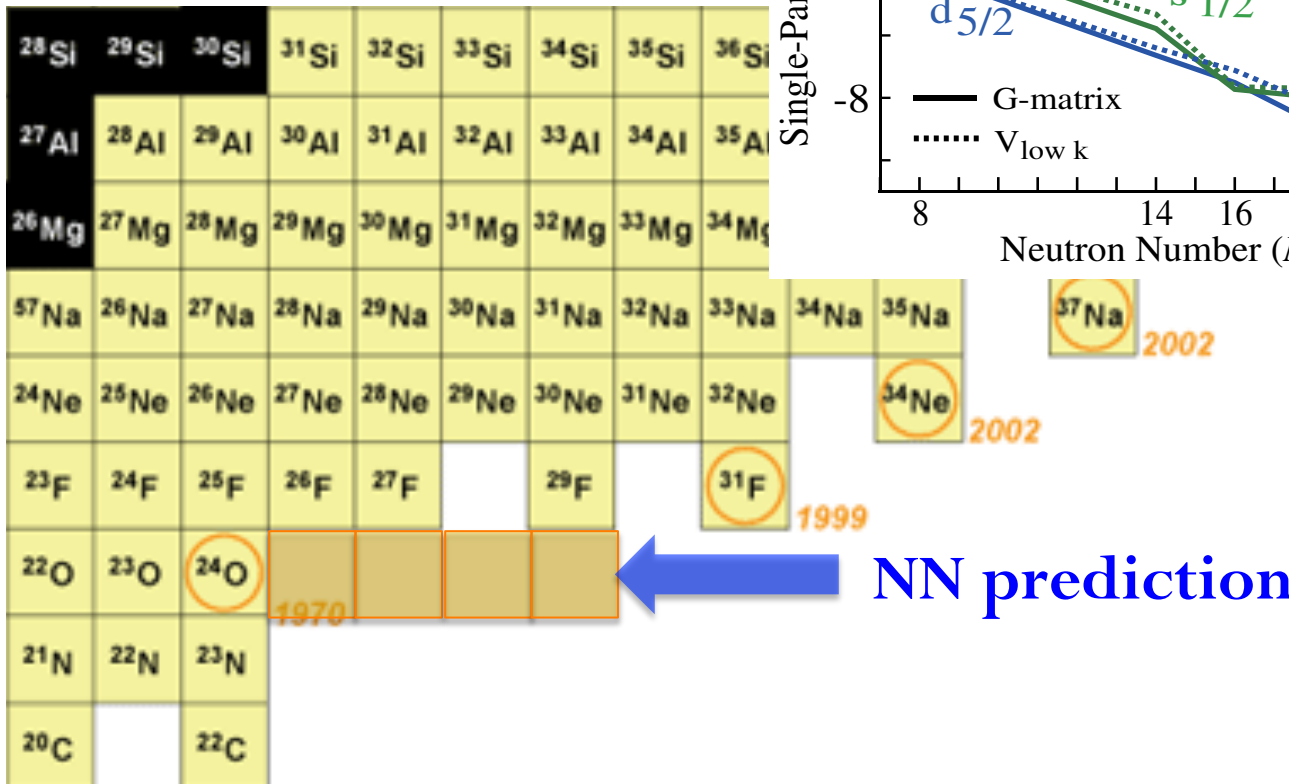
NN-forces too attractive



Limits of Nuclear Existence: Oxygen Anomaly

Microscopic picture:

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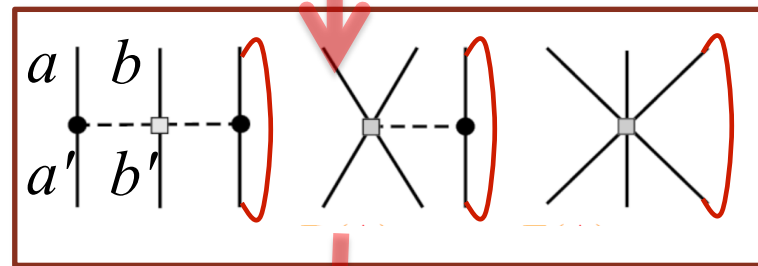
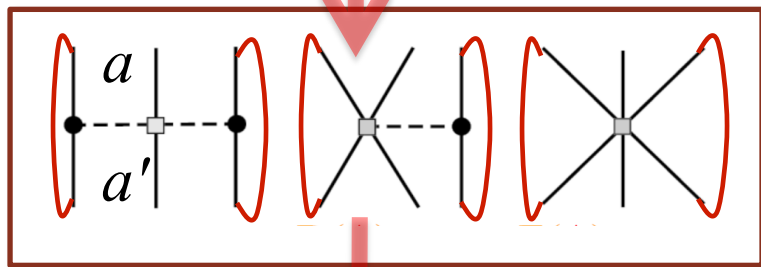
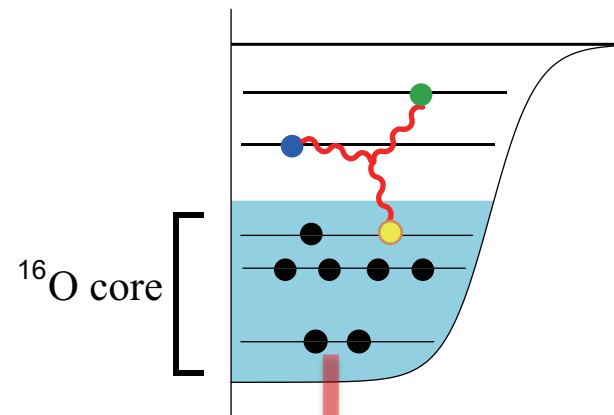
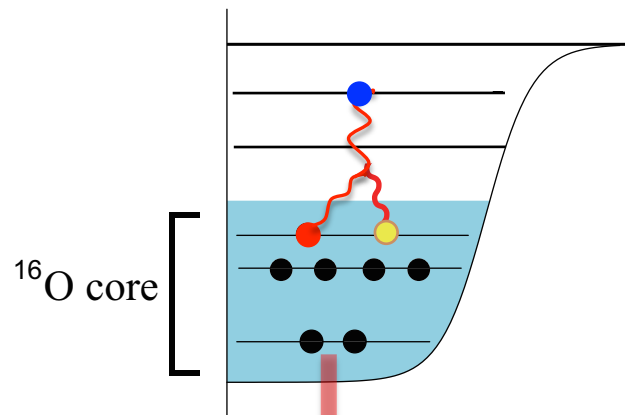
Incorrect prediction of oxygen dripline
 Extended-space – more binding

3N Forces for Valence-Shell Theories

Normal-ordered 3N: contribution to valence-space Hamiltonian

Effective one-body

Effective two-body



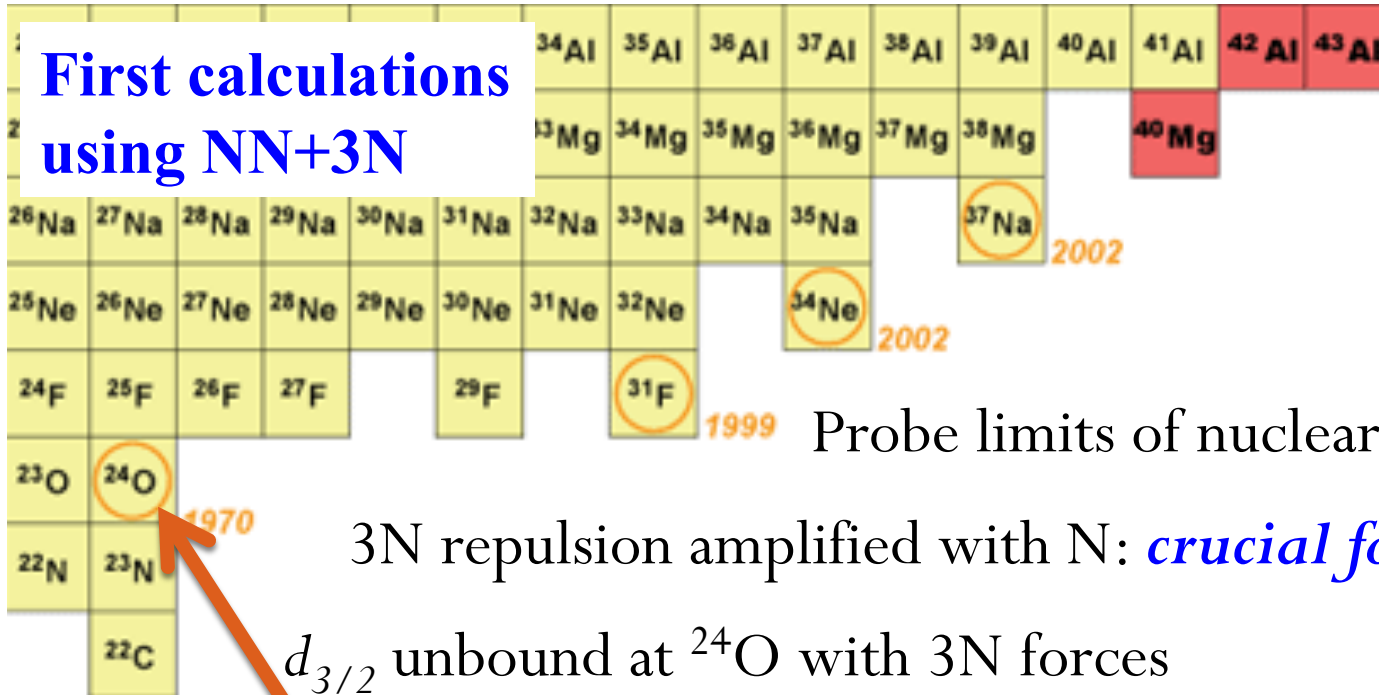
$$\langle a | V_{3N,\text{eff}} | a' \rangle = \frac{1}{2} \sum_{\alpha\beta=\text{core}} \langle \alpha\beta a | V_{3N} | \alpha\beta a' \rangle$$

$$\langle ab | V_{3N,\text{eff}} | a' b' \rangle = \sum_{\alpha=\text{core}} \langle \alpha ab | V_{3N} | \alpha a' b' \rangle$$

Combine with NN (**Third Order**): no empirical adjustments

Oxygen Anomaly

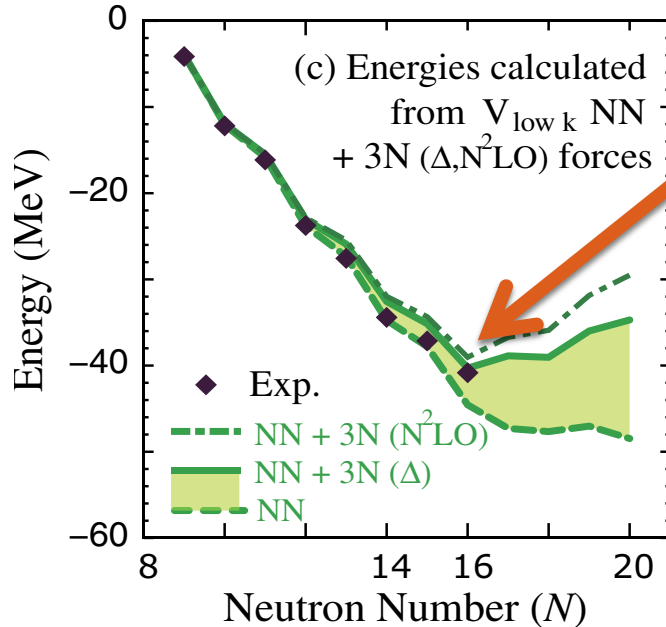
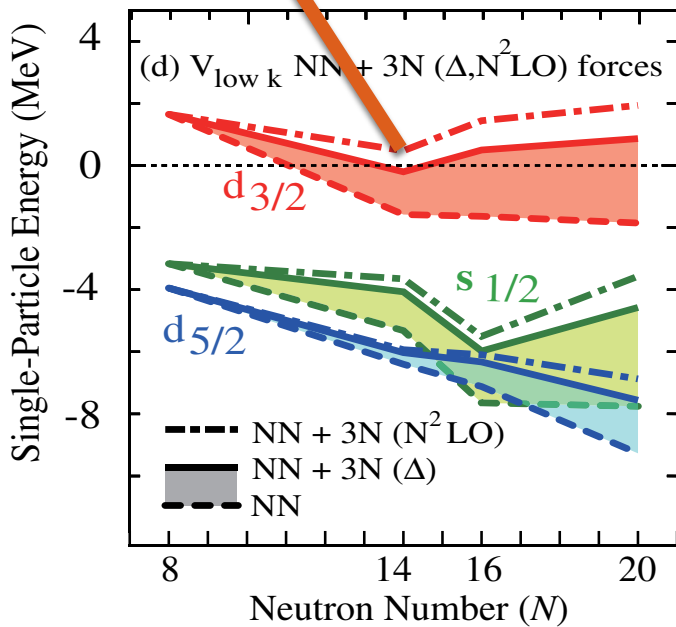
First calculations using NN+3N



Probe limits of nuclear existence with 3N forces

3N repulsion amplified with N: *crucial for neutron-rich nuclei*

$d_{3/2}$ unbound at ^{24}O with 3N forces

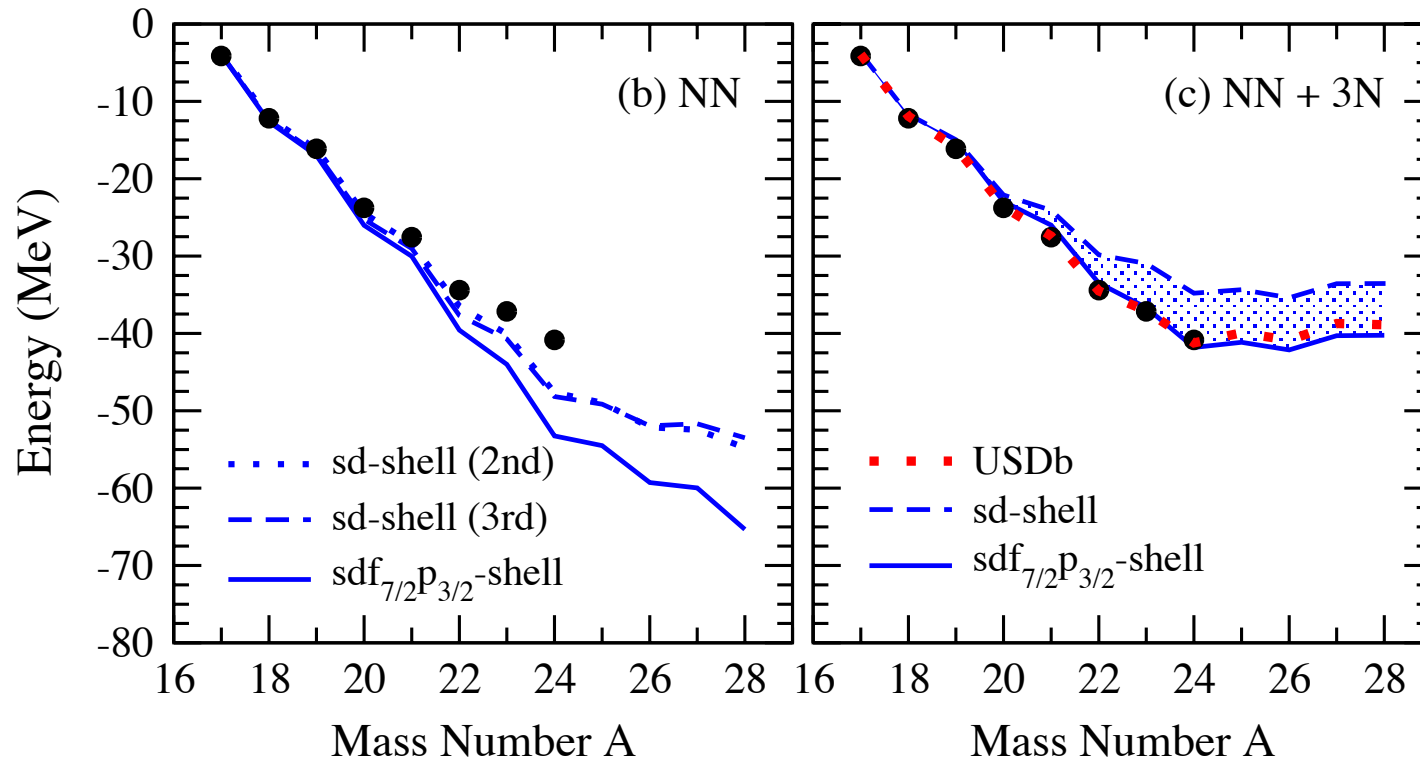


Isotopes unbound beyond ^{24}O

First microscopic explanation of oxygen anomaly

Ground-State Energies of Oxygen Isotopes

Valence-space interaction and SPEs from NN+3N



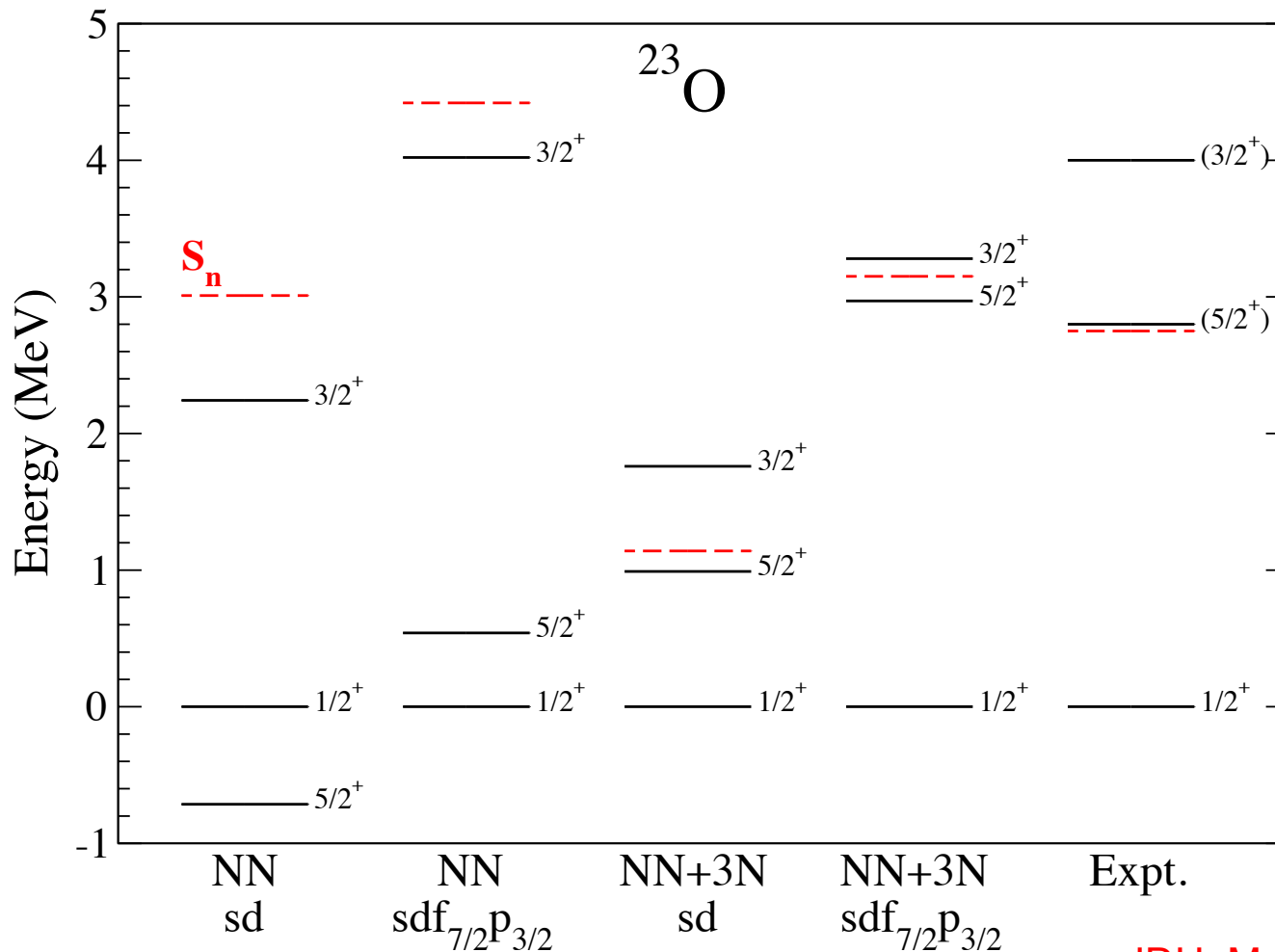
JDH, Menendez, Schwenk, EPJA (2013)

Repulsive character improves agreement with experiment
sd-shell results underbound; improved in **extended space**

Impact on Spectra: ^{23}O

Neutron-rich oxygen spectra with NN+3N

$5/2^+$, $3/2^+$ energies reflect $^{22,24}\text{O}$ shell closures



sd-shell NN only

Wrong ground state

$5/2^+$ too low

$3/2^+$ bound

NN+3N

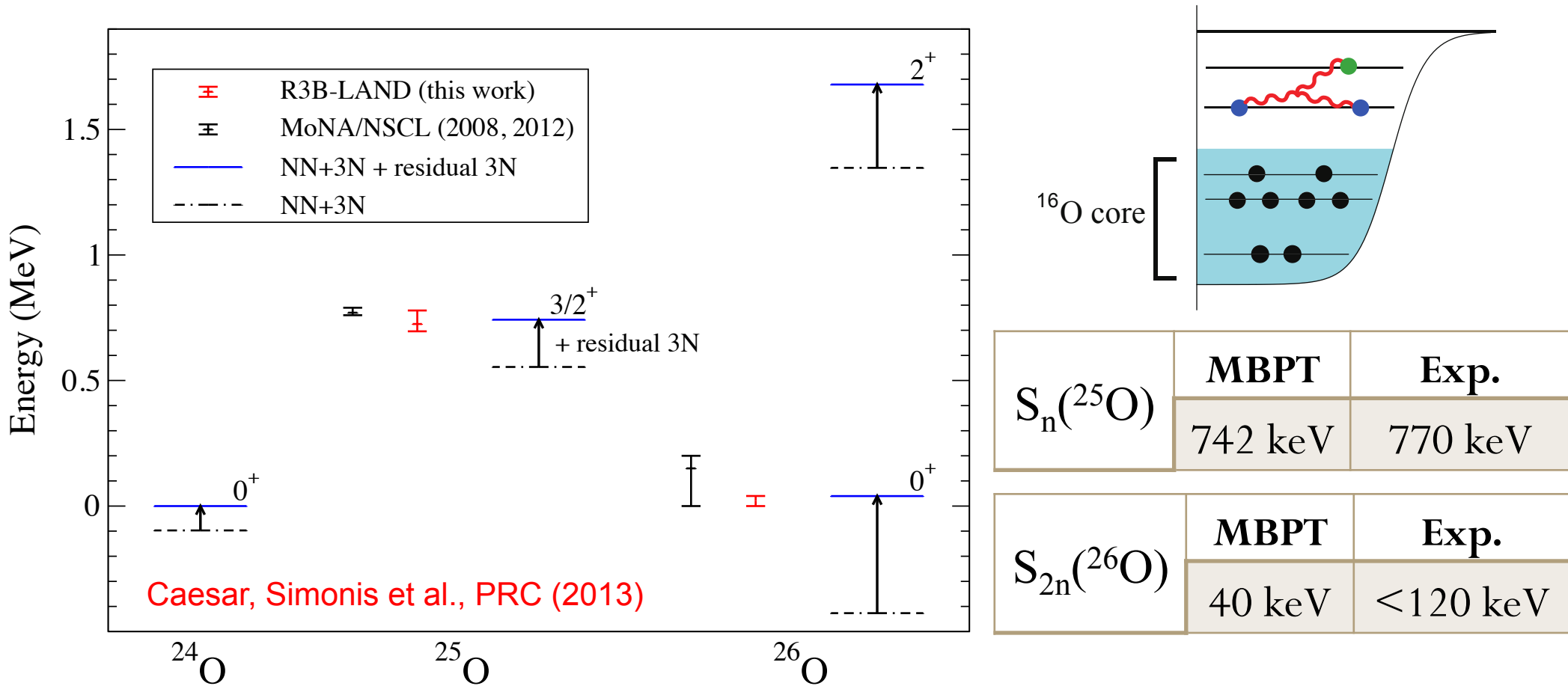
Clear improvement in extended valence space

JDH, Menendez, Schwenk, EPJA (2013)

Experimental Connection: Beyond the Dripline

Hoffman, Kanungo, Lunderberg... PRLs (2008+)

Valence-space Hamiltonian from NN + 3N + **residual 3N**



Repulsion more pronounced for neutron-rich systems: 400 keV at ^{26}O

Improved agreement with new data beyond ^{24}O dripline

Future: include coupling to continuum

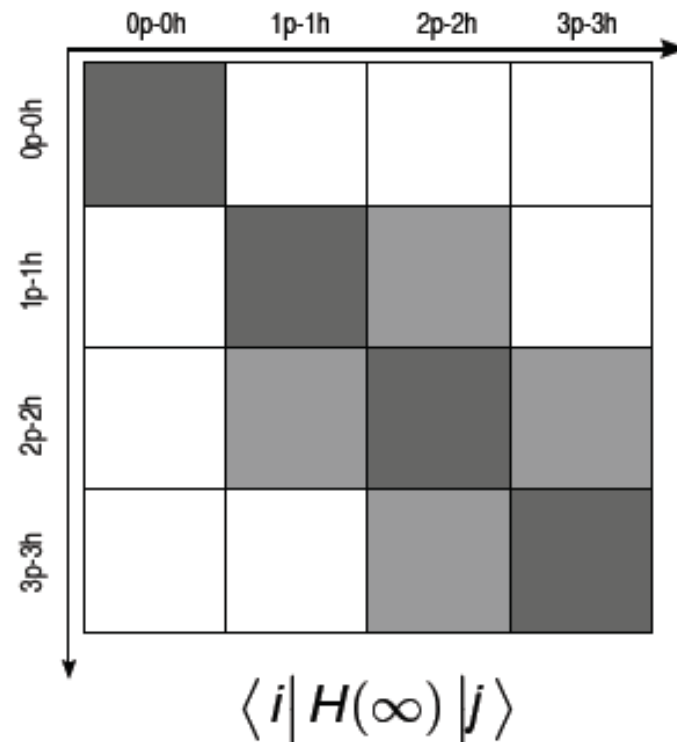
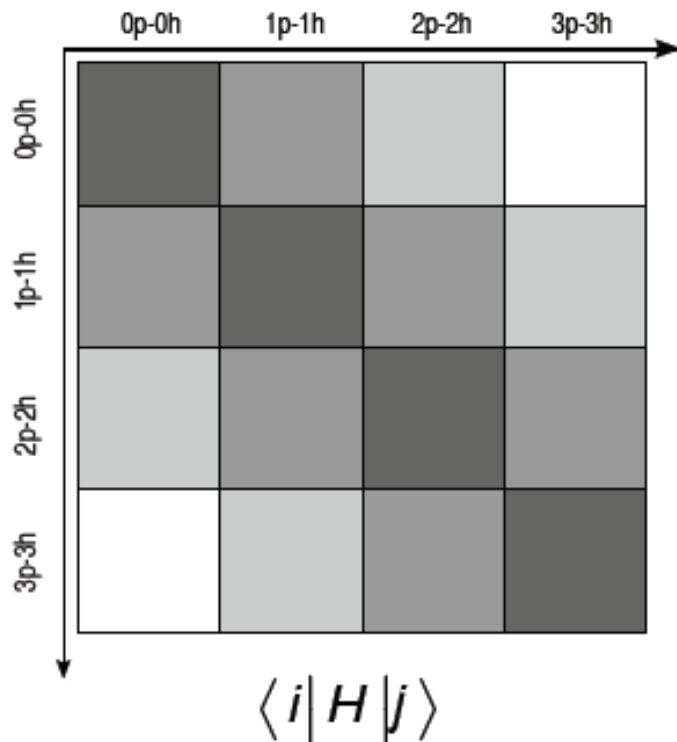
IM-SRG for Valence-Space Hamiltonians

In-Medium SRG applies continuous unitary transformation to drive off-diagonal physics to zero

Tsukiyama, Bogner, Schwenk, PRL (2011)

$$H(s) = U(s)HU^\dagger(s) \equiv H^d(s) + H^{\text{od}}(s) \rightarrow H^d(\infty)$$

Decouples reference state from excitations $\langle npnh | H(\infty) | \Phi_c \rangle = 0$



IM-SRG for Valence-Space Hamiltonians

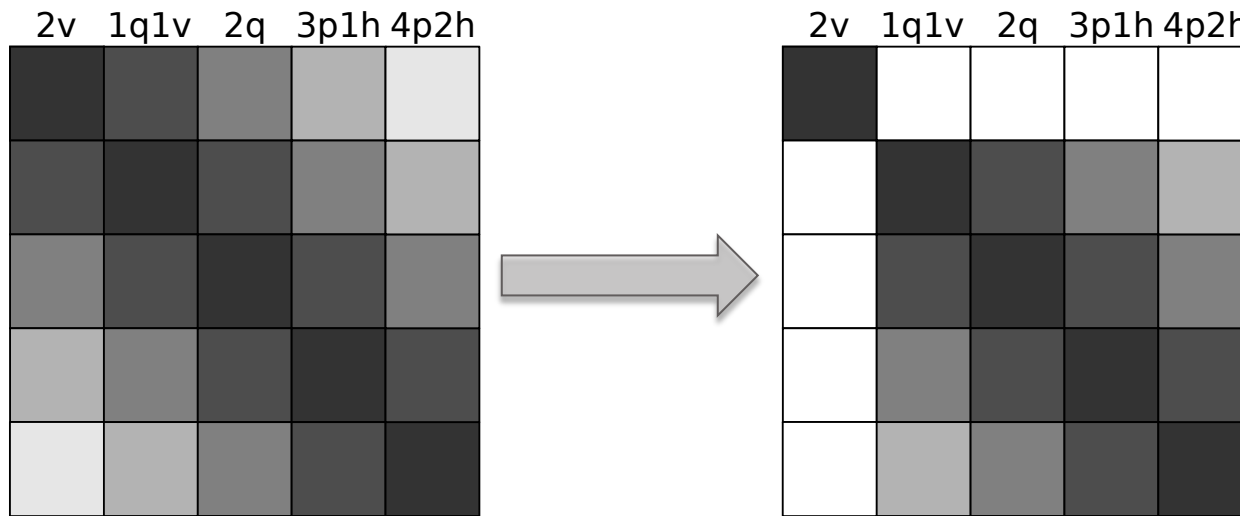
In-Medium SRG applies continuous unitary transformation to drive off-diagonal physics to zero

Tsukiyama, Bogner, Schwenk, PRC (2012)

Open shell systems:

split particle states into valence states, v , and those above valence space, q

Redefine “off-diagonal” to exclude valence particles



$$H(s=0) \rightarrow H(\infty)$$

IM-SRG for Valence-Space Hamiltonians

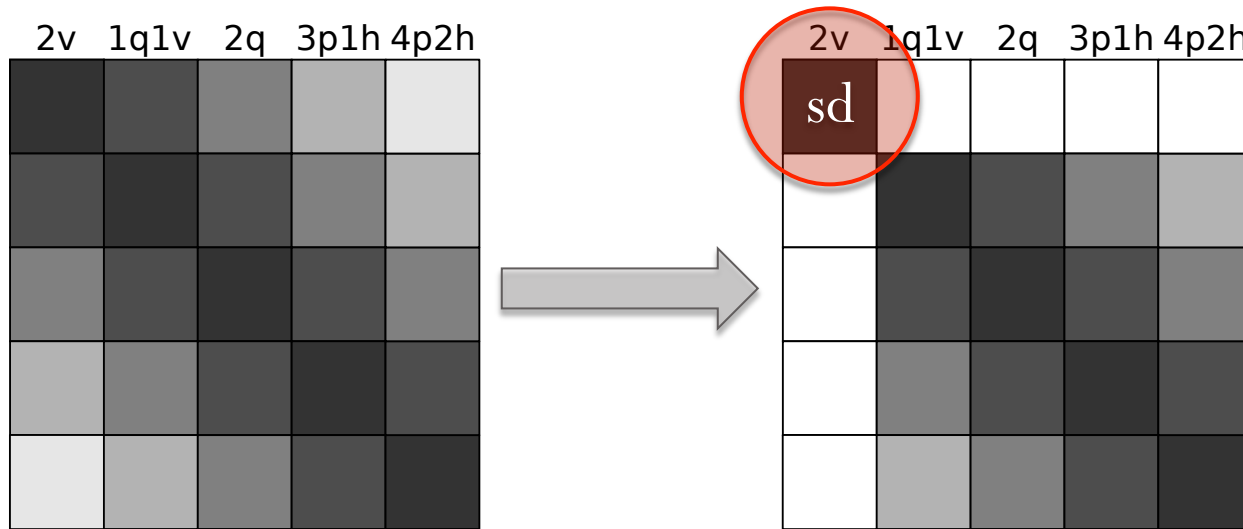
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Open shell systems:

split particle states into valence states, v , and those above valence space, q

Redefine “off-diagonal” to exclude valence particles



$$H(s=0) \rightarrow H(\infty)$$

Defines new effective valence-space Hamiltonian H_{eff}

States outside valence space are decoupled

Nonperturbative Valence-Space Strategy

- 1) Effective interaction: nonperturbative from IM-SRG
- 2) Single-particle energies: nonperturbative from IM-SRG
- 3) Hartree-Fock basis of $e_{\max} = 2n + l = 14$ **converged**
- ★ 4) NN and 3N forces from chiral EFT
- 5) Explore extended valence spaces – in progress

NN matrix elements

- Chiral N³LO (Machleidt, $\Lambda_{\text{NN}} = 500\text{MeV}$); free-space SRG evolution
- Cutoff variation $\lambda_{\text{SRG}} = 1.88 - 2.24\text{fm}^{-1}$
- Vary $\hbar\omega = 20 - 24\text{MeV}$
- Consistently include 3N forces induced by SRG evolution

Initial 3N force contributions

- Chiral N²LO $\Lambda_{3\text{N}} = 400\text{MeV}$
- Included with cut: $e_1 + e_2 + e_3 \leq E_{3\max} = 14$

Perturbative vs. Nonperturbative SPEs

3N forces: additional repulsion improves SPEs

Orbit	USD b	MBPT NN	MBPT NN+3N	IM-SRG NN	IM-SRG NN+3N-ind	IM-SRG NN+3N-full
$d_{5/2}$	-3.93	-5.43	-3.78	-7.90	-3.77	-4.62
$s_{1/2}$	-3.21	-5.32	-2.42	-6.87	-2.46	-2.96
$d_{3/2}$	2.11	-0.97	1.45	1.41	2.33	3.17

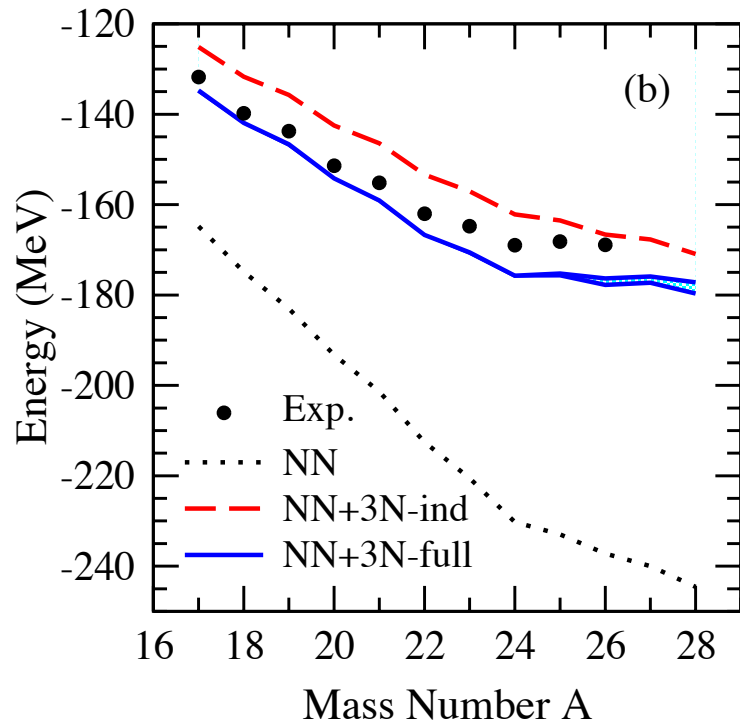
JDH, Menendez, Schwenk, EPJA (2013)
Bogner et al., arXiv:1402.1407

Similar contributions in standard/extended valence spaces

Comparable with phenomenology

IM-SRG Oxygen Ground-State Energies

Valence-space interaction and SPEs from IM-SRG in sd shell



Bogner et al., arXiv:1402.1407

NN+3N-induced reproduce exp well, not dripline

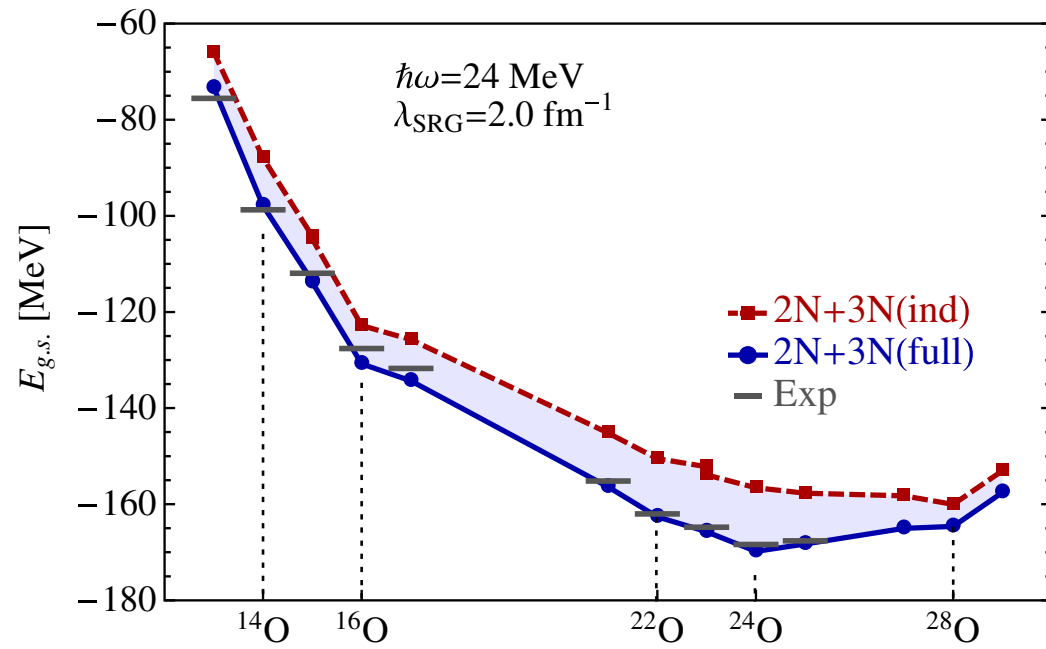
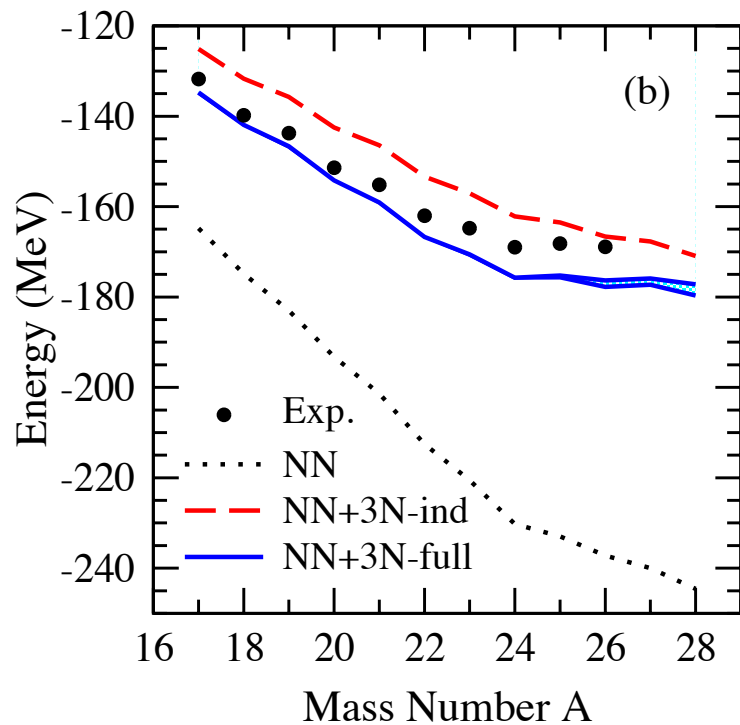
NN+3N-full modestly overbound – good behavior past dripline

Good dripline properties

Very weak $\hbar\omega$ dependence

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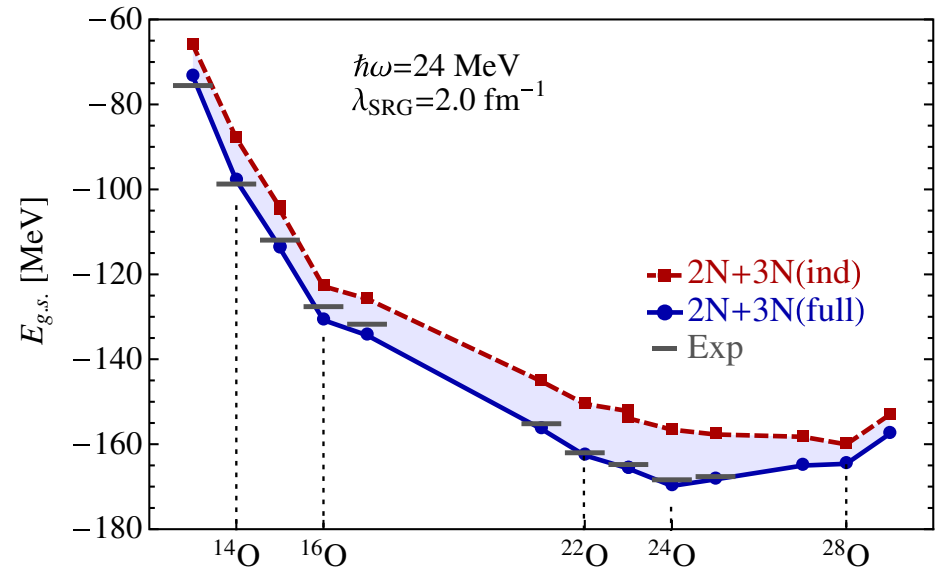
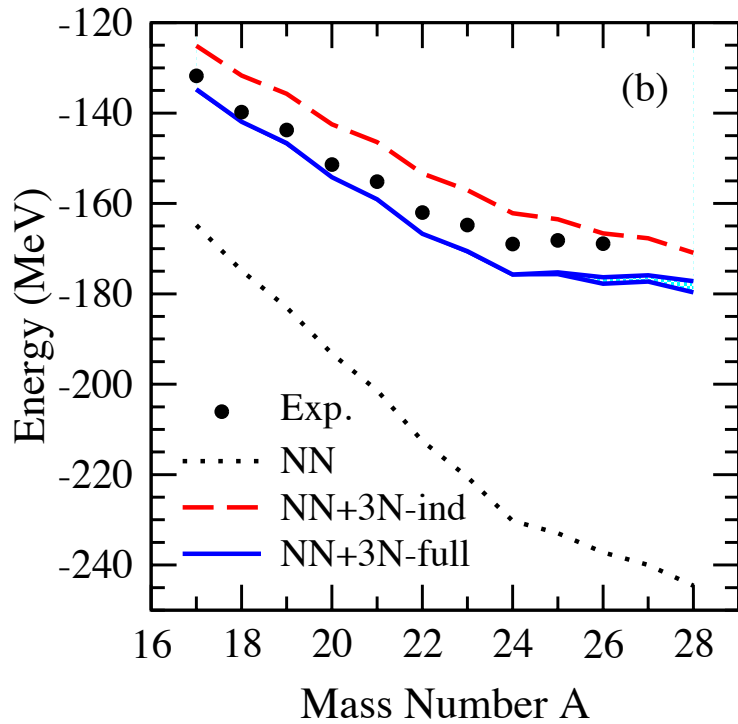
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Very weak $\hbar\omega$ dependence

Comparison with Large-Space Methods

Large-space methods with same SRG-evolved NN+3N forces

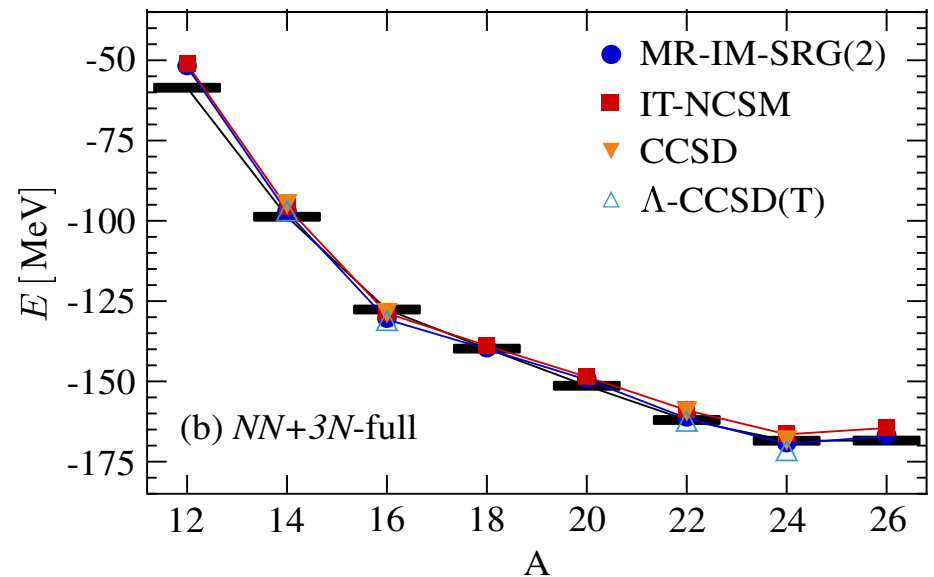


Cipollone, Barbieri, Navratil, PRL (2013)

Clear improvement with full NN+3N

Confirms valence-space results

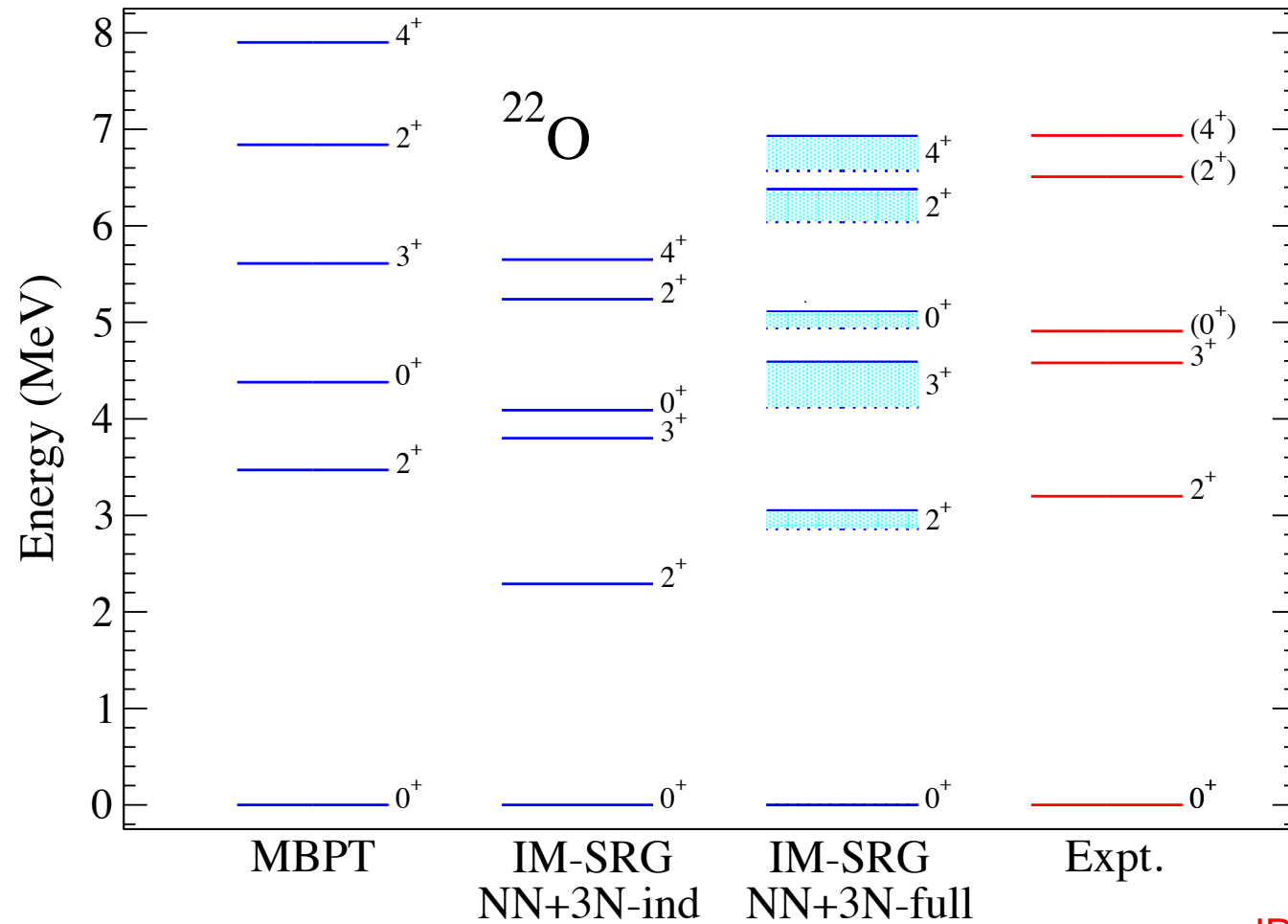
Remarkable agreement with same forces



Hergert et al., PRL (2013)

IM-SRG Oxygen Spectra

Oxygen spectra: extended-space MBPT and IM-SRG



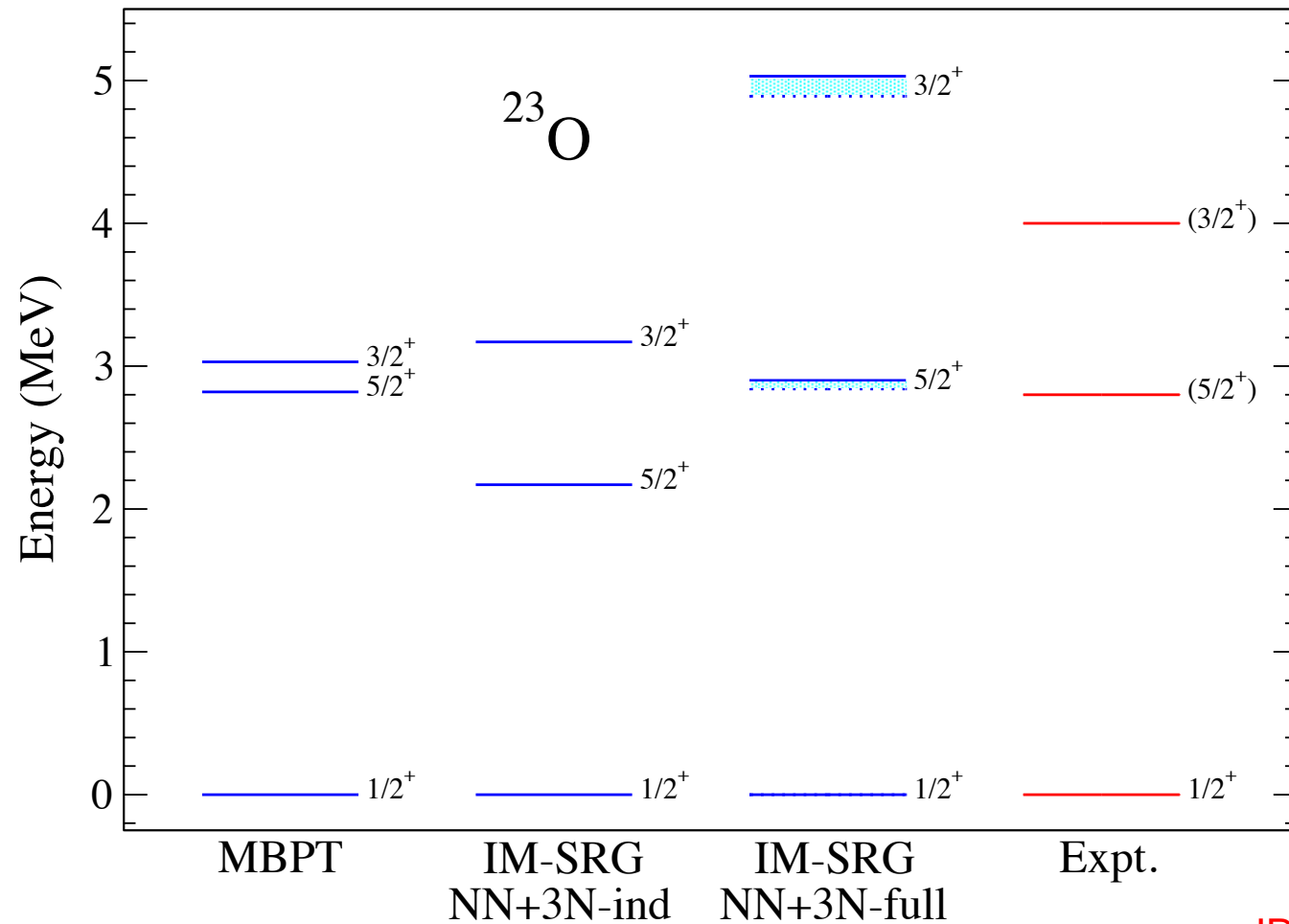
JDH, Menendez, Schwenk, EPJ (2013)
Bogner et al., arXiv:1402.1407

Clear improvement with NN+3N-full

IM-SRG: comparable with phenomenology

IM-SRG Oxygen Spectra

Oxygen spectra: extended-space MBPT and IM-SRG



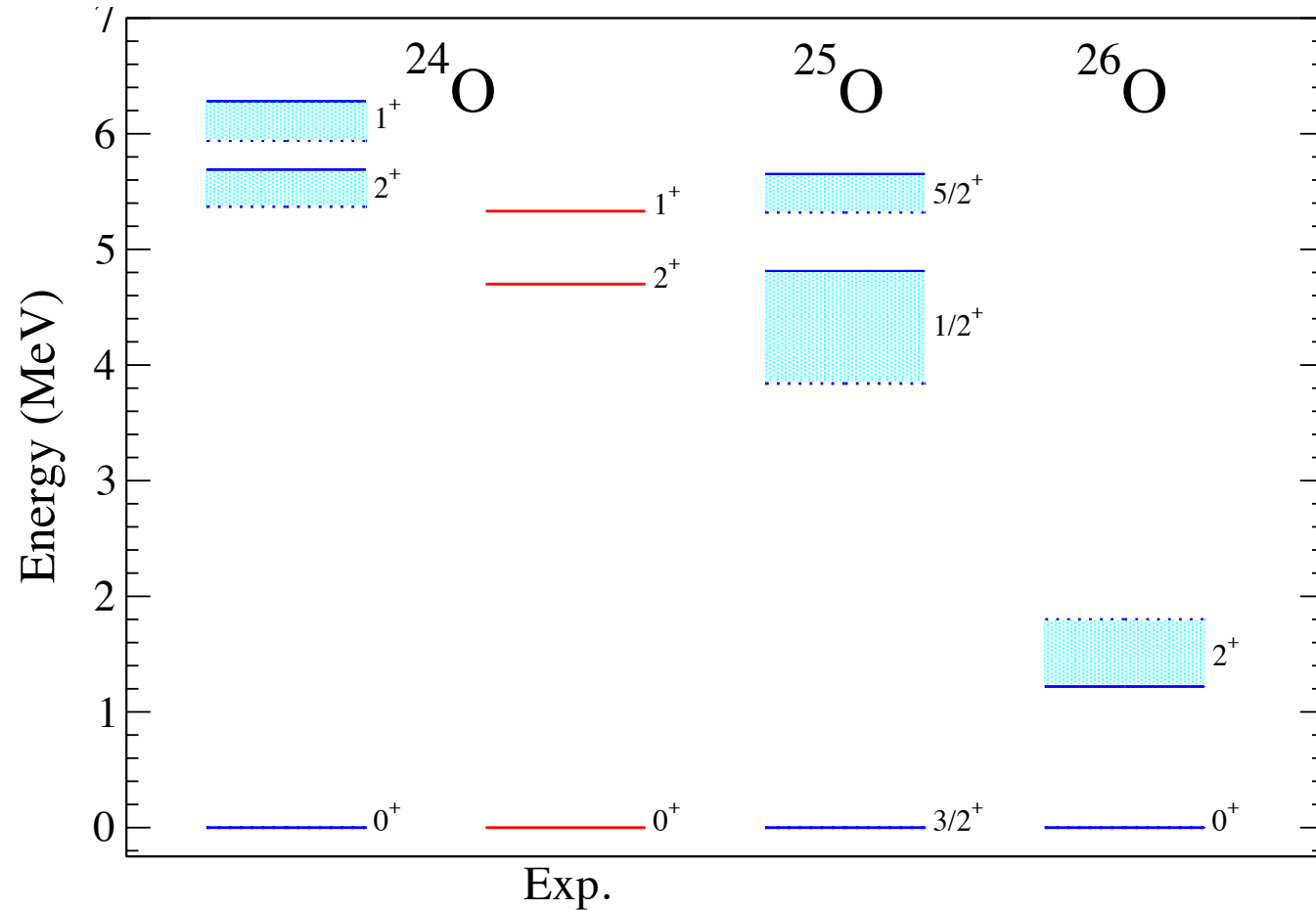
JDH, Menendez, Schwenk, EPJ (2013)
Bogner et al., arXiv:1402.1407

Clear improvement with NN+3N-full

Continuum neglected: expect to lower $d_{3/2}$

IM-SRG Oxygen Spectra

Oxygen spectra: IM-SRG predictions beyond the dripline



^{24}O closed shell (too high 2^+)

JDH, Menendez, Schwenk, EPJ (2013)
Bogner et al., arXiv:1402.1407

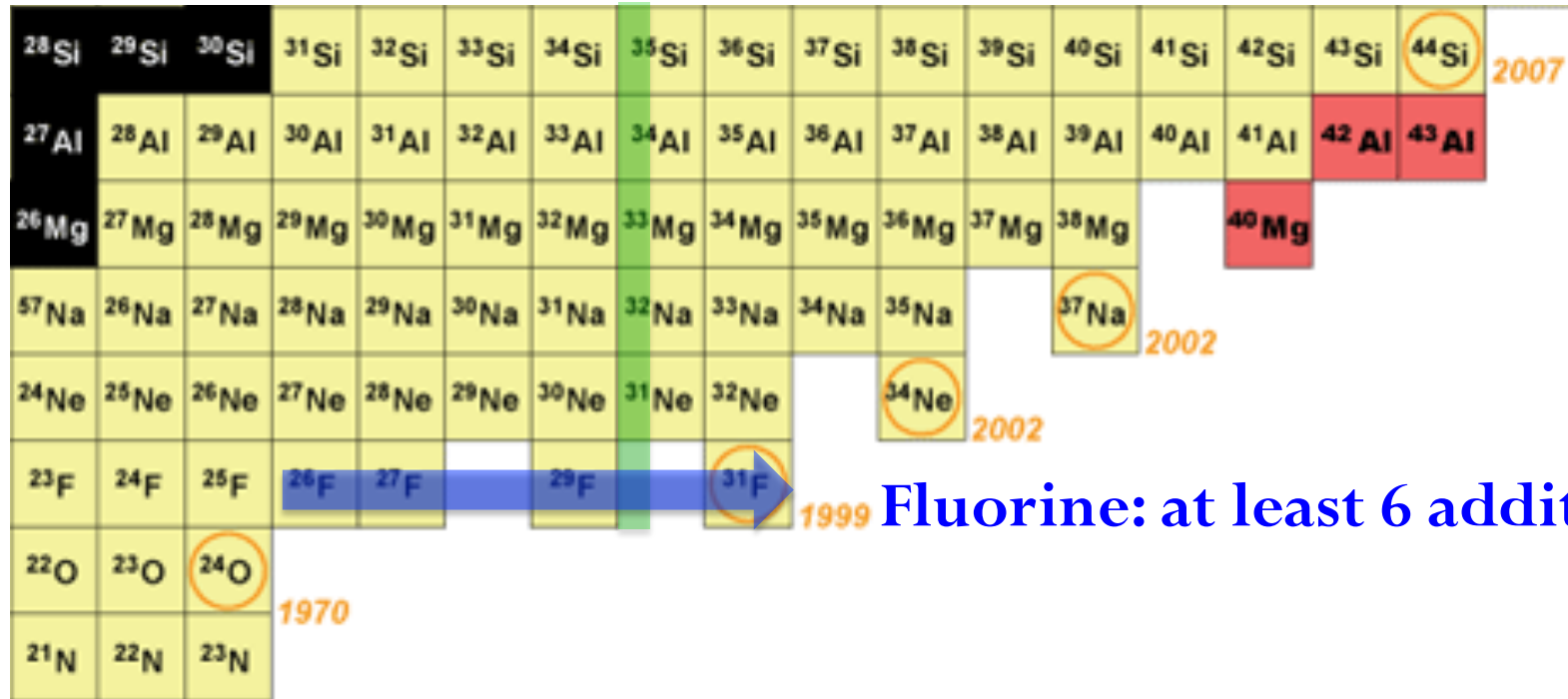
Continuum neglected: expect to lower spectrum

Only one excited state in ^{26}O below 6.5MeV

Towards Full sd-Shell with MBPT: Fluorine

Next challenge: **valence protons + neutrons**

Neutron-rich fluorine and neon



Fluorine: at least 6 additional neutrons

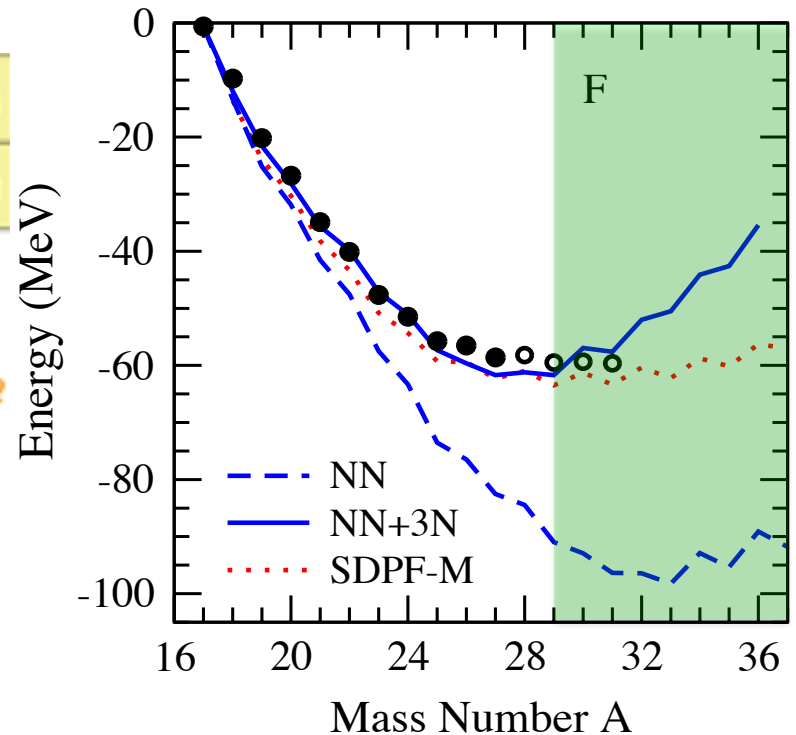
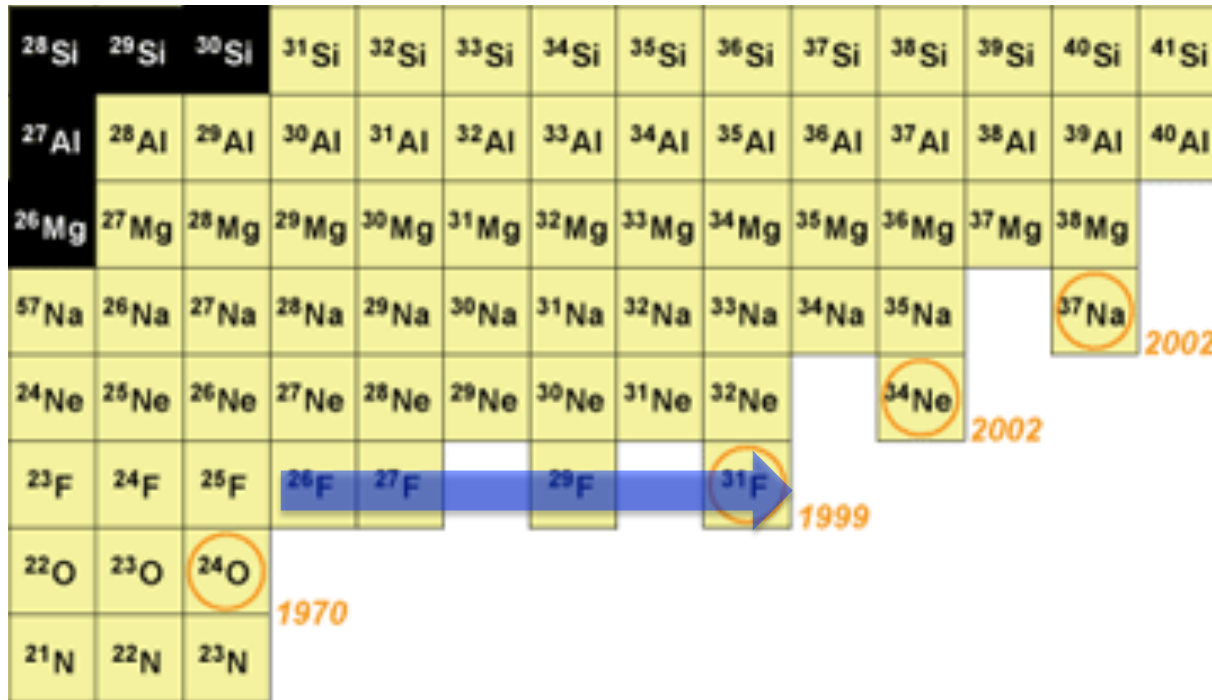
sd shell filled at ²⁹F/³⁰Ne

Need extended-space orbits

Towards Full sd-Shell with MBPT: Fluorine

Next challenge: **valence protons + neutrons**

Neutron-rich fluorine and neon



JDH, Menendez, Simonis,
Schwenk, in prep.

NN only: severe overbinding

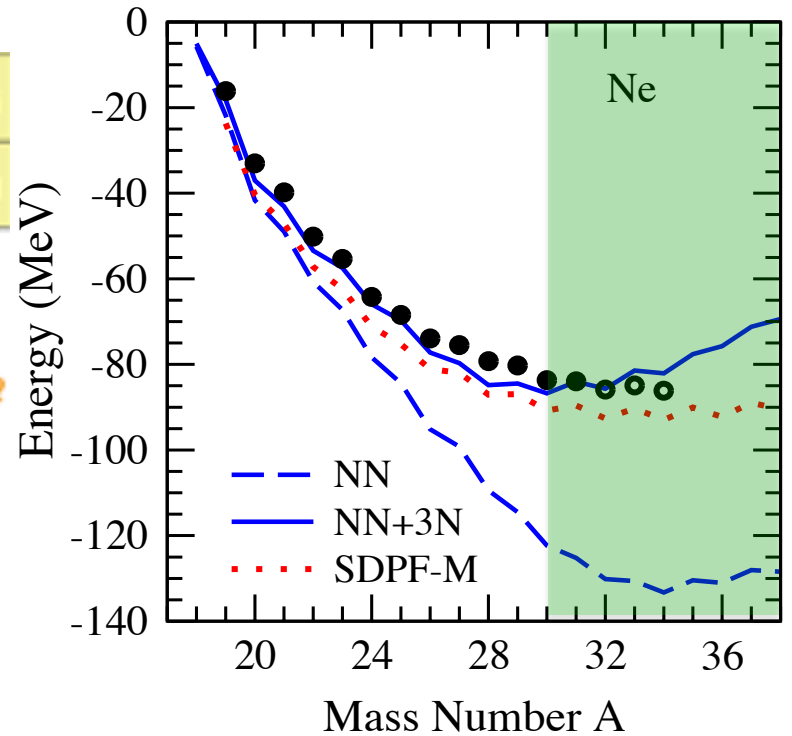
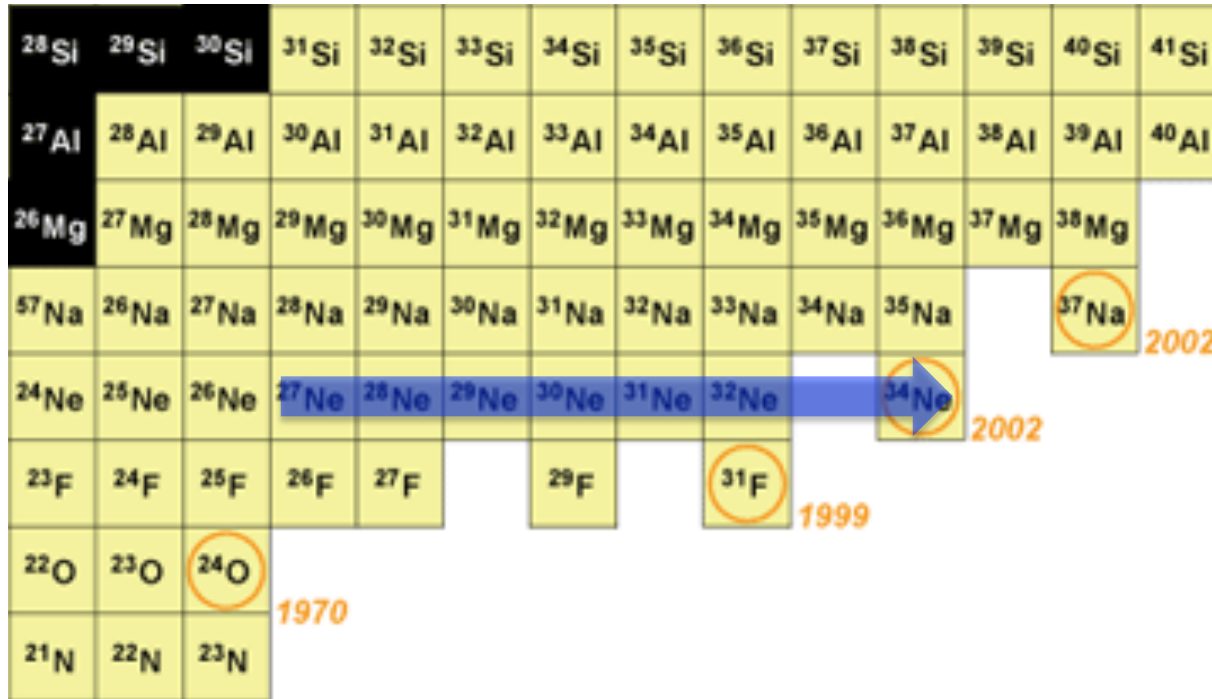
NN+3N: good experimental agreement through ^{29}F

Sharp increase in ground-state energies beyond ^{29}F : incorrect dripline

Towards Full sd-Shell with MBPT: Neon

Next challenge: **valence protons + neutrons**

Neutron-rich fluorine and neon



JDH, Menendez, Simonis,
Schwenk, in prep.

Similar behavior in Neon isotopes

Revisit cross-shell valence space theory – **non-degenerate valence spaces**

Tsunoda, Hjorth-Jensen, Otsuka

Calcium Isotopes

Exploring the frontiers of nuclear science:

Worldwide joint experimental/theoretical effort

What are the properties of proton/neutron-rich matter?

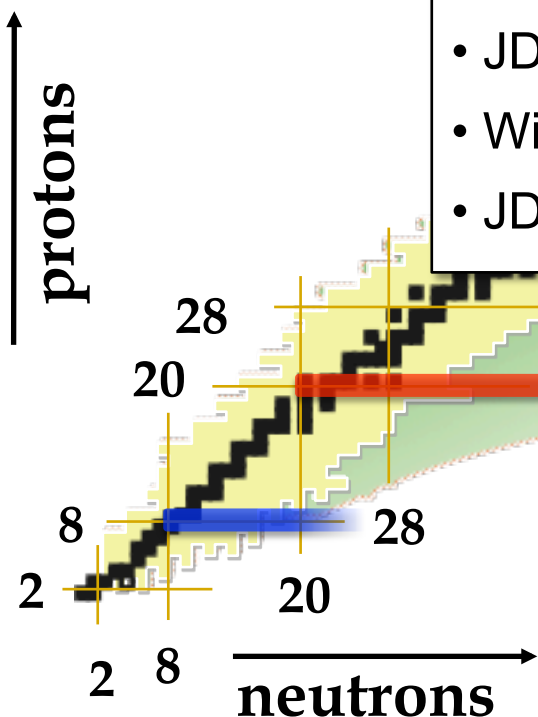
What are the limits of nuclear existence?

How do magic numbers form and evolve?

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References

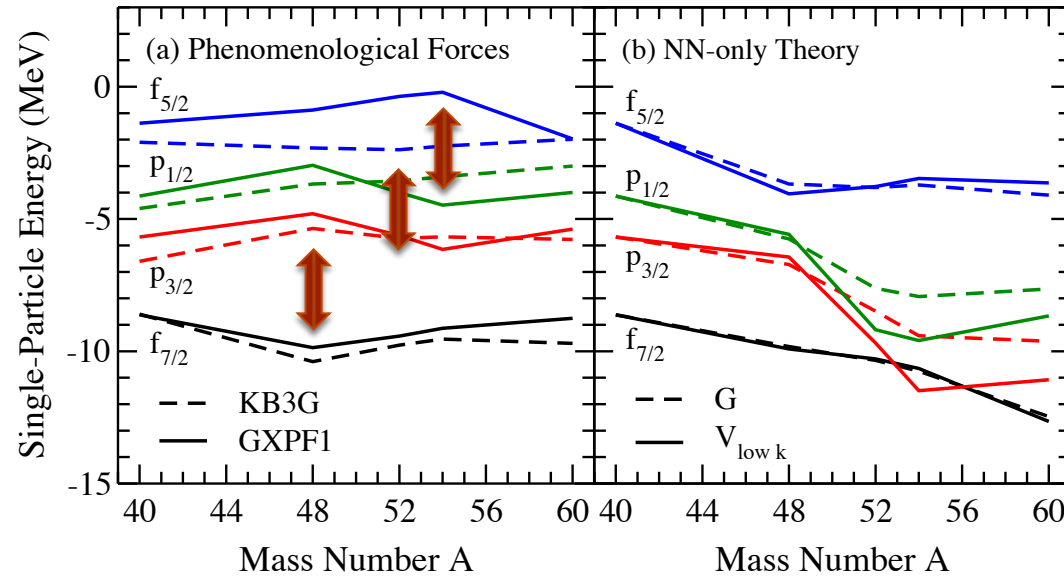
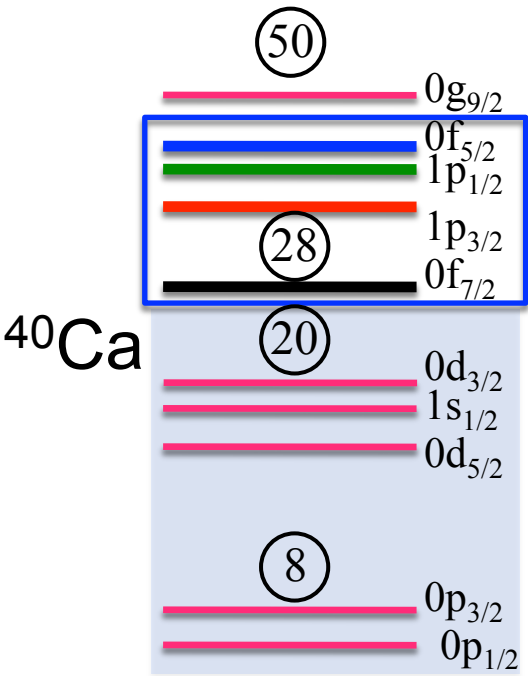
- JDH, Otsuka, Schwenk, Suzuki, JPG **39**, 085111 (2012)
- Gallant et al., PRL **109**, 032506 (2012)
- JDH, Menendez, Schwenk, JPG **40**, 075105 (2013)
- Wienholtz et al., Nature **486**, 346 (2013)
- JDH, Menendez, Simonis, Schwenk, in prep.



Key physics problems:

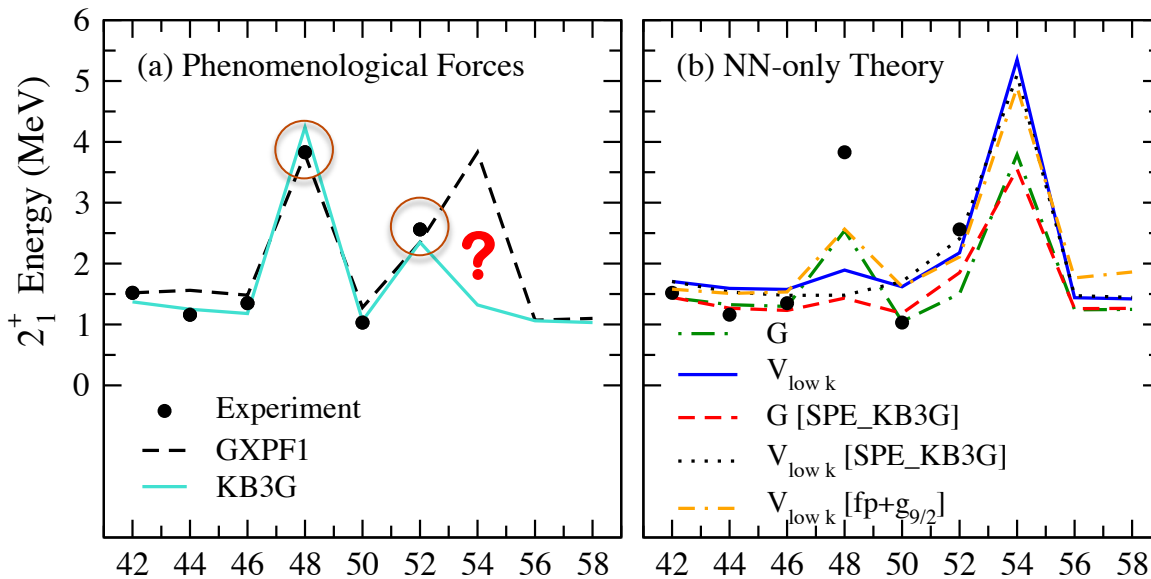
- $N=28$ magic number
- Shell evolution through ^{52}Ca , ^{54}Ca
- Spectra, transition rates
- Pairing gaps: interface with EDF

Calcium Isotopes: Magic Numbers



GXPF1: Honma, Otsuka, Brown, Mizusaki (2004)

KB3G: Poves, Sanchez-Solano, Caurier, Nowacki (2001)



Phenomenological Forces

Large gap at ^{48}Ca

Discrepancy at $N=34$

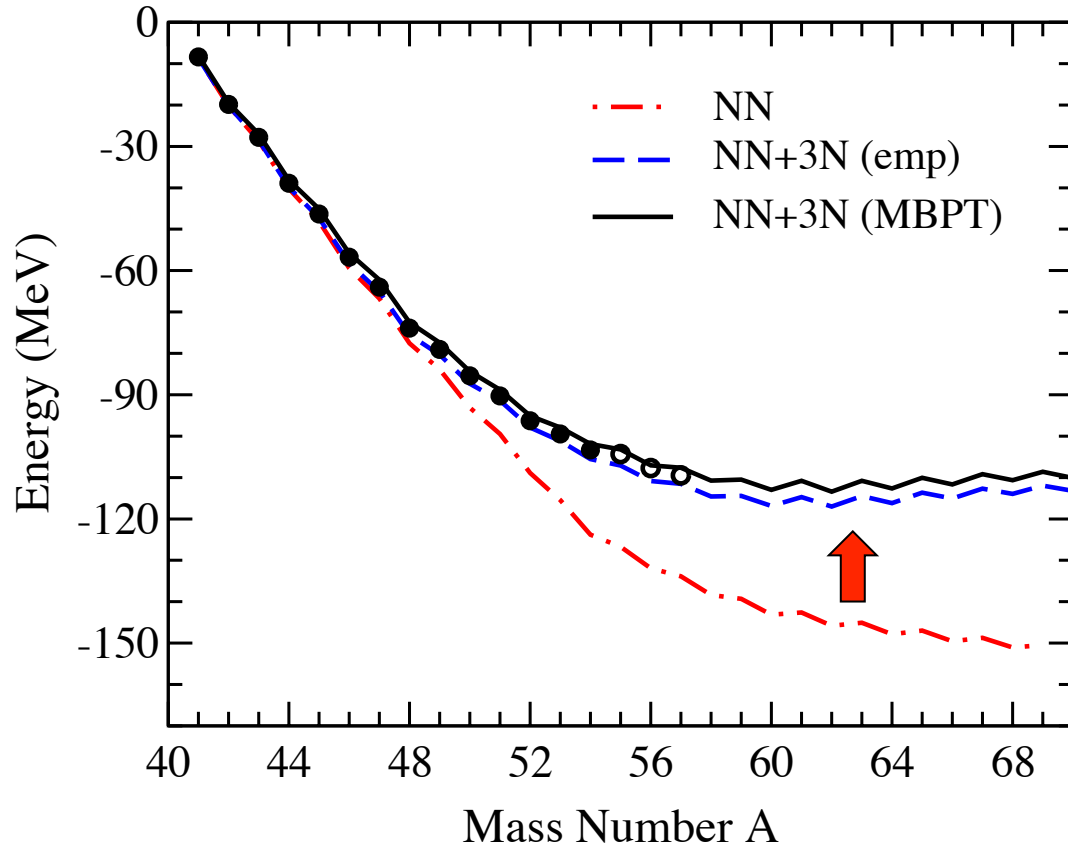
Microscopic NN Theory

Small gap at ^{48}Ca

N=28: first standard magic number not reproduced in microscopic NN theories

Calcium Ground State Energies and Dripline

Signatures of shell evolution from ground-state energies?



Holt, Otsuka, Schwenk, Suzuki, JPG (2012)

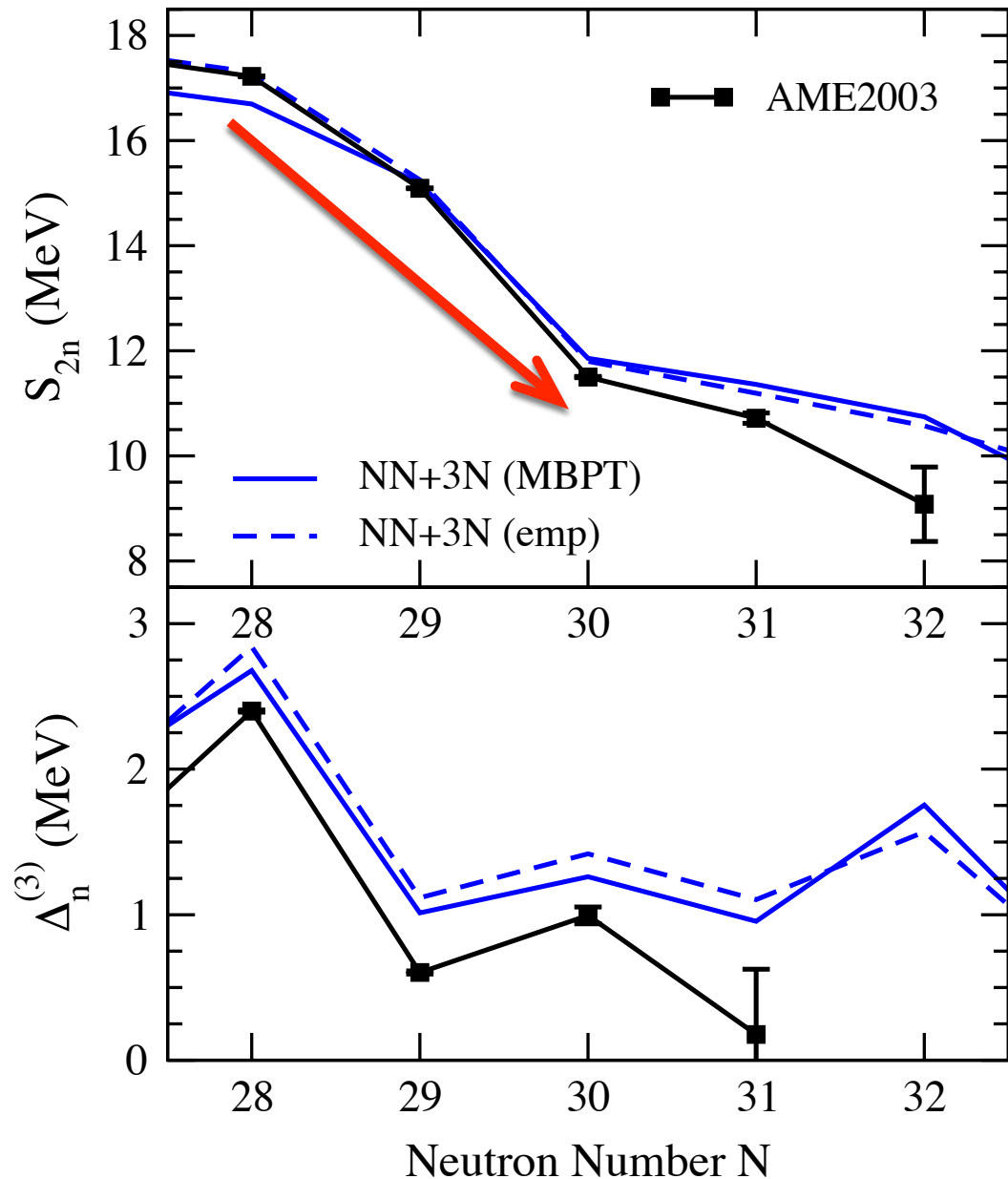
No clear dripline; flat behavior past ^{54}Ca – **Halos beyond ^{60}Ca ?**

$S_{2n} = -[BE(N, Z) - BE(N - 2, Z)]$ **sharp decrease indicates shell closure**

$\Delta_n^{(3)} = \frac{(-1)^N}{2} [BE(N + 1, Z) + BE(N - 1, Z) - 2BE(N, Z)]$ **peak indicates shell closure**

Two-Neutron Separation Energies: Mass of ^{52}Ca

Compare with AME2003 data



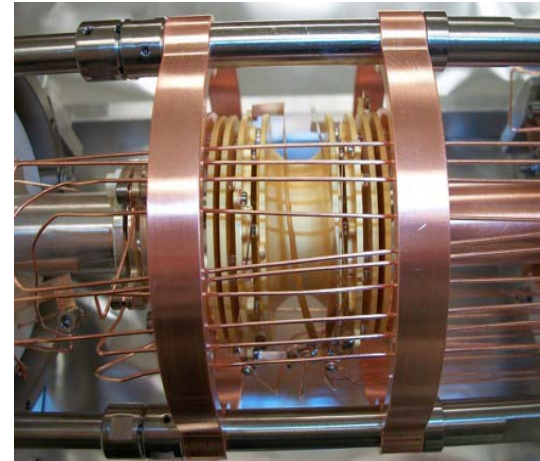
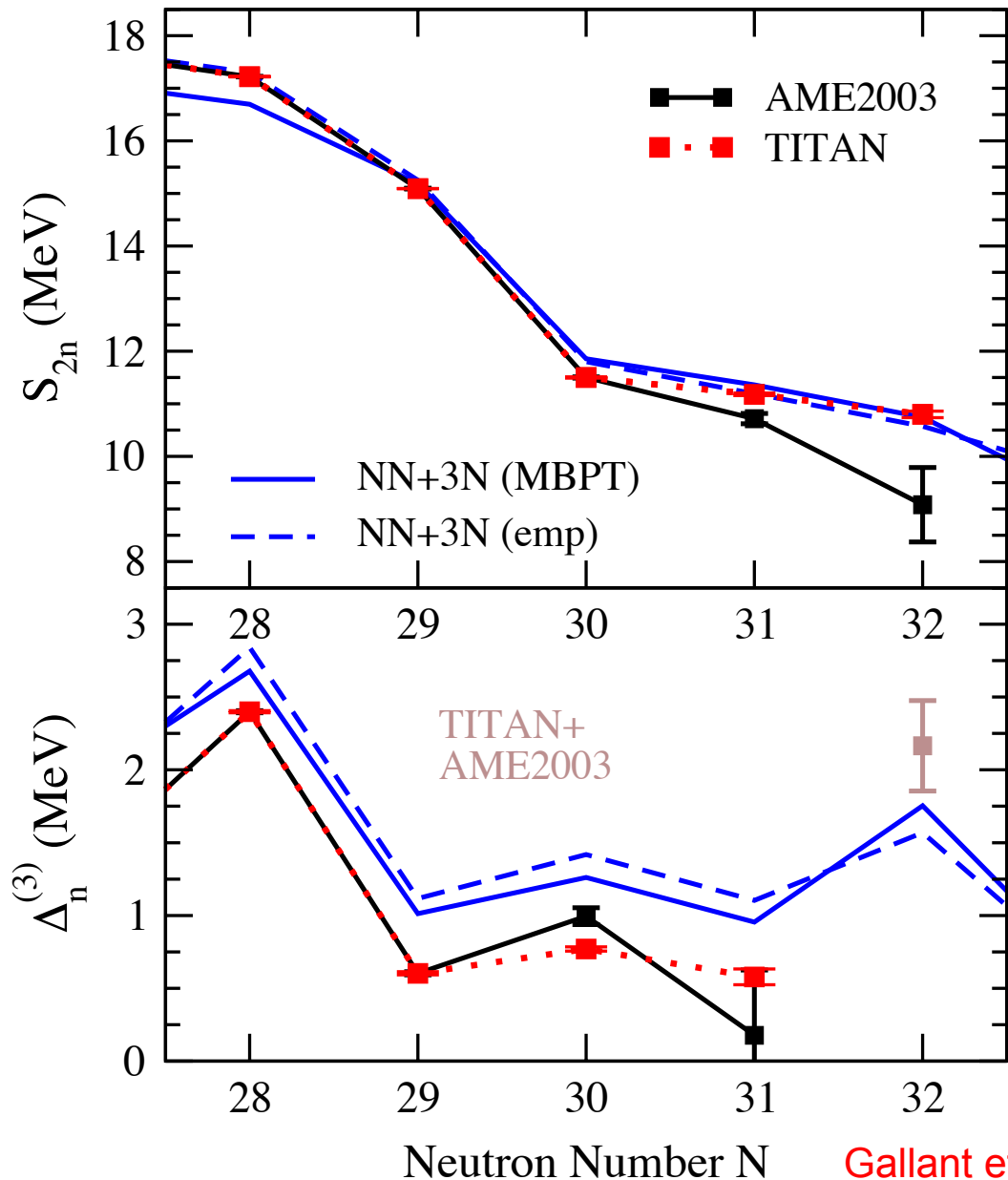
NN+3N Predictions

Reproduce ^{48}Ca shell closure

Predictions too bound past ^{50}Ca

Experimental Connection: Mass of ^{52}Ca

New mass measurements of $^{51,52}\text{Ca}$ at **TITAN**: Penning trap experiment



TITAN Measurement

^{52}Ca mass 1.75 MeV *more* bound than AME2003 value

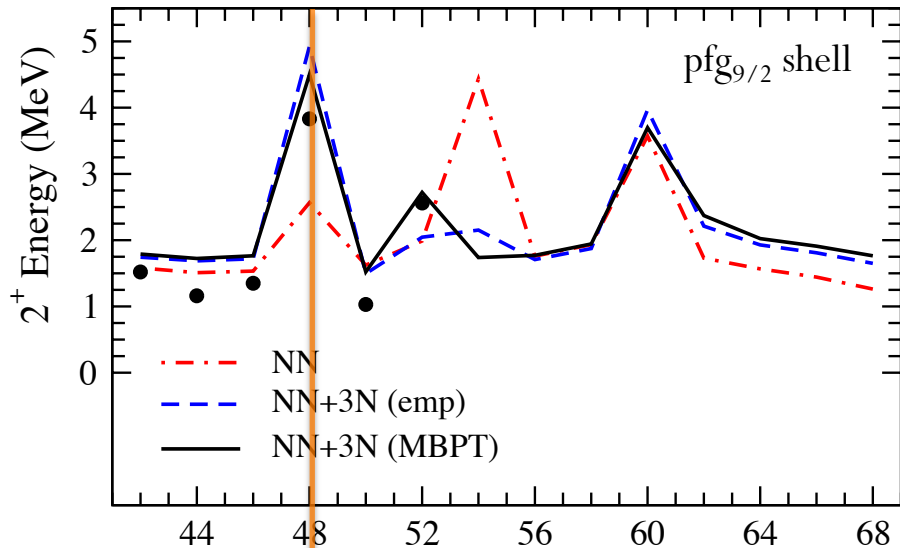
NN+3N Predictions

Confirmed with new measurements

Good reproduction of pairing gaps

Gallant et al., PRL (2012)

Pairing for Shell Evolution N=28



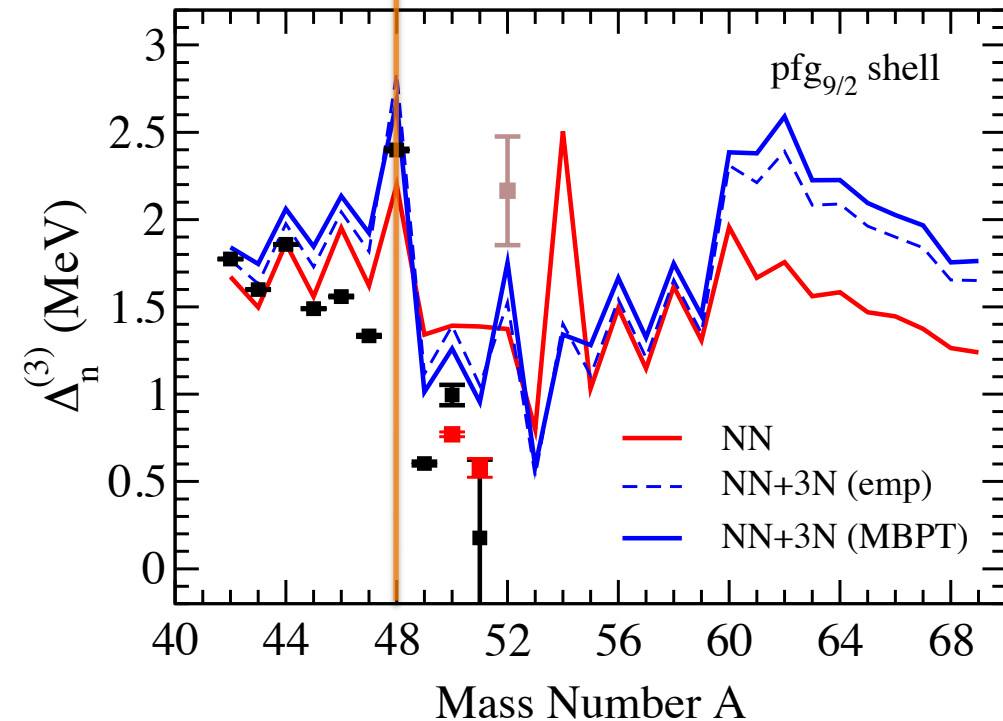
Peak in pairing gaps: complementary signature for shell closure

Compare with 2^+ energies for Ca

Agreement with CC throughout chain

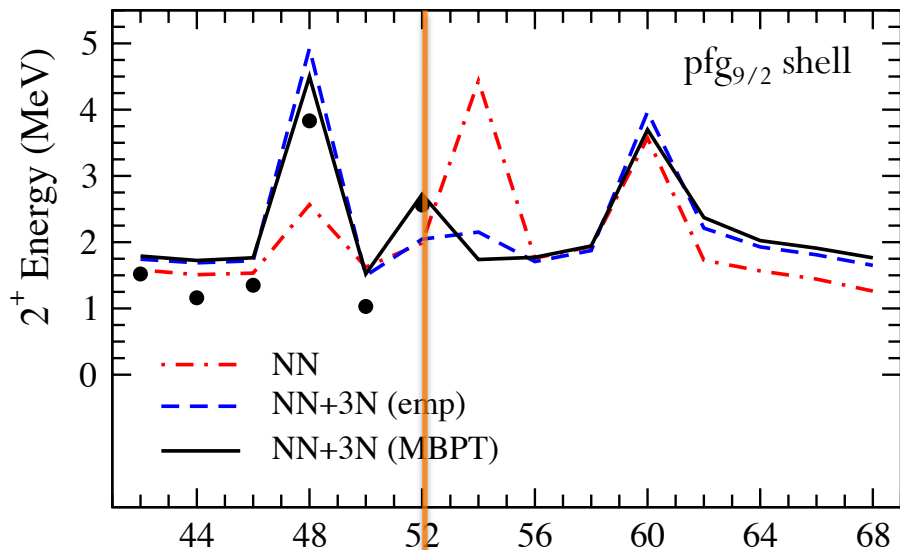
Hagen et al. PRL (2012)

N=28 strong peak



JDH, Menendez, Schwenk, JPG (2013)

Pairing for Shell Evolution N=32



Peak in pairing gaps: complementary signature for shell closure

Compare with 2^+ energies for Ca

Agreement with CC throughout chain

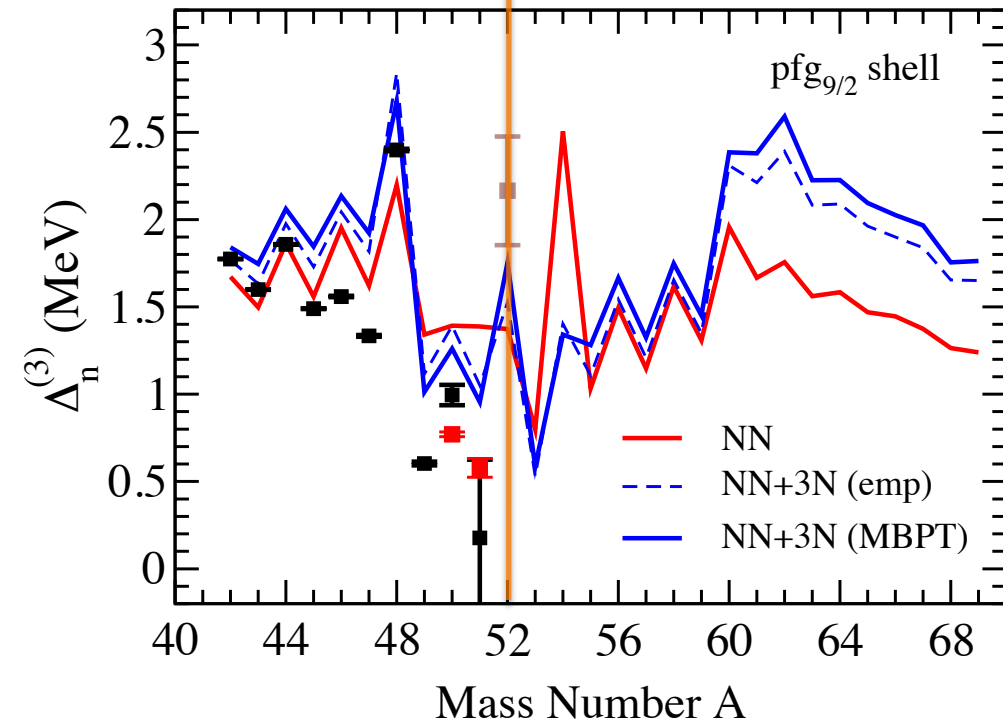
Hagen et al. PRL (2012)

N=28 strong peak

N=32 moderate peak

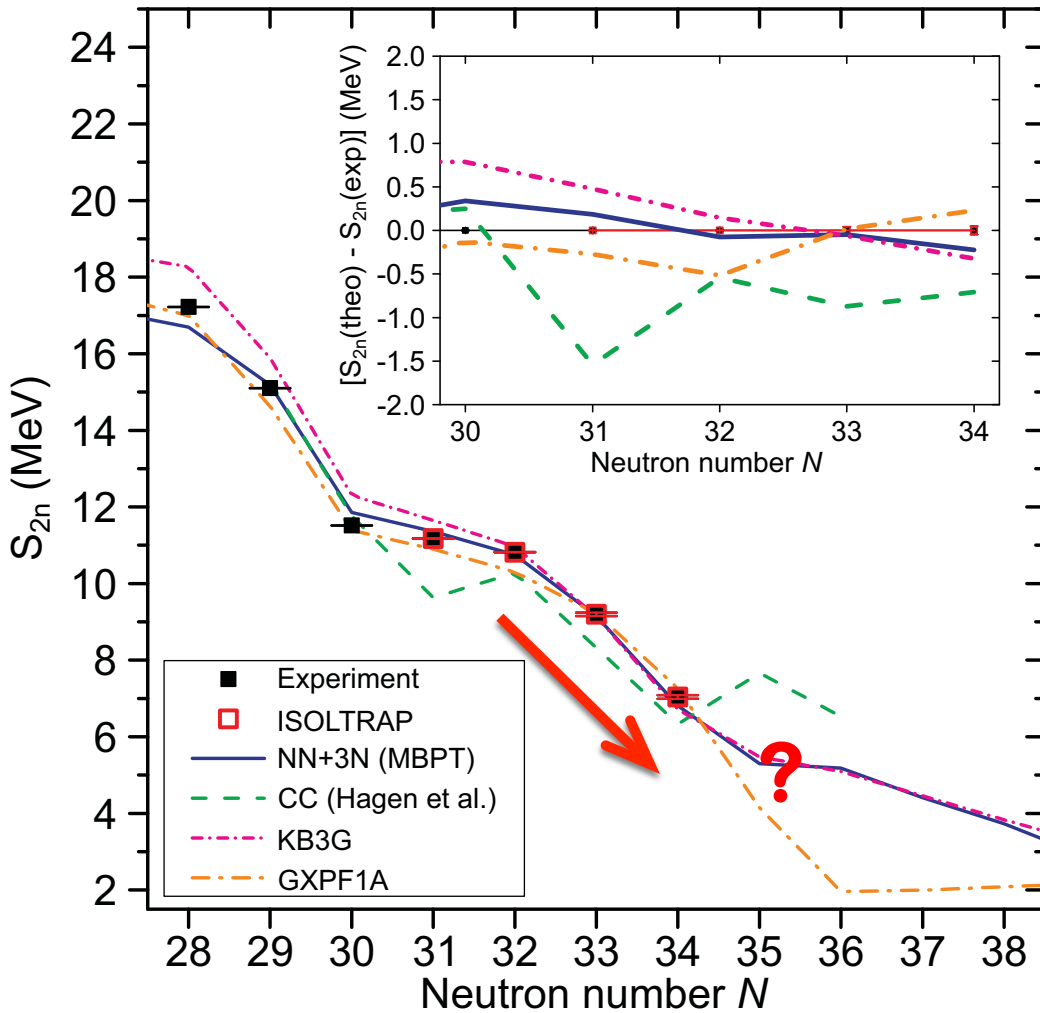
Close to data with new TITAN value

Experimental measurement of ^{53}Ca mass needed to reduce uncertainty

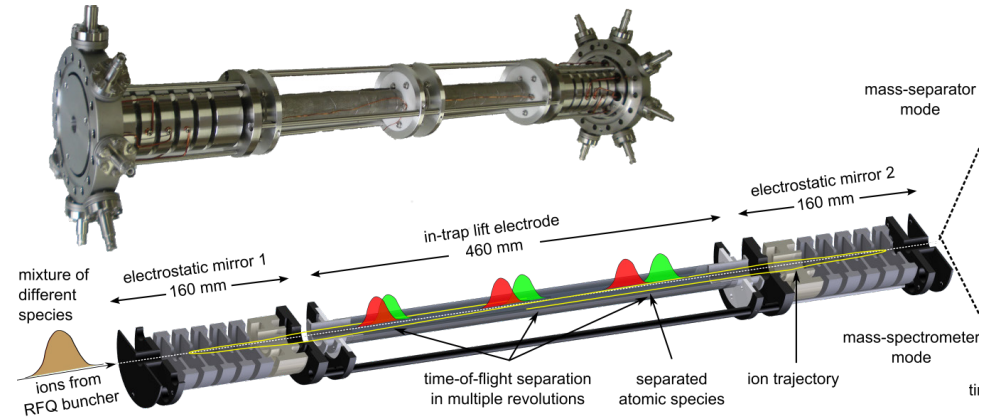


Experimental Connection: Mass of ^{54}Ca

New precision mass measurement of $^{53,54}\text{Ca}$ at **ISOLTRAP**: multi-reflection ToF



Wienholtz et al., Nature (2013)



ISOLTRAP Measurement

Sharp decrease past ^{52}Ca

Unambiguous closed-shell ^{52}Ca

Test predictions of various models

MBPT NN+3N

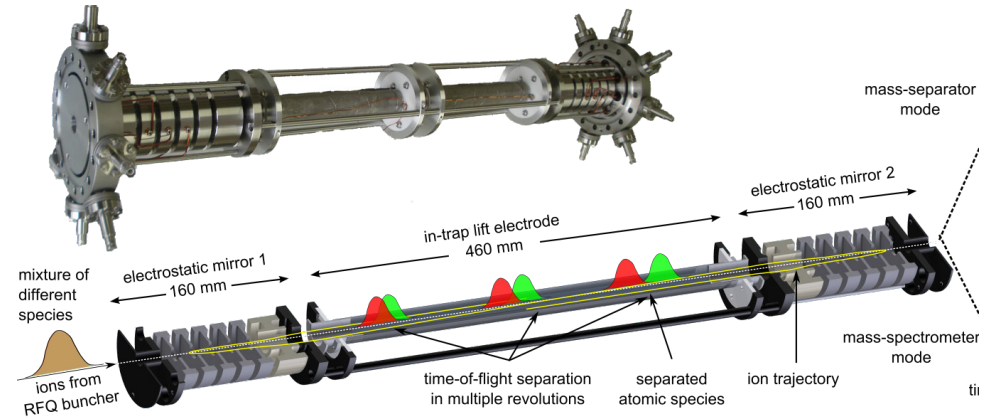
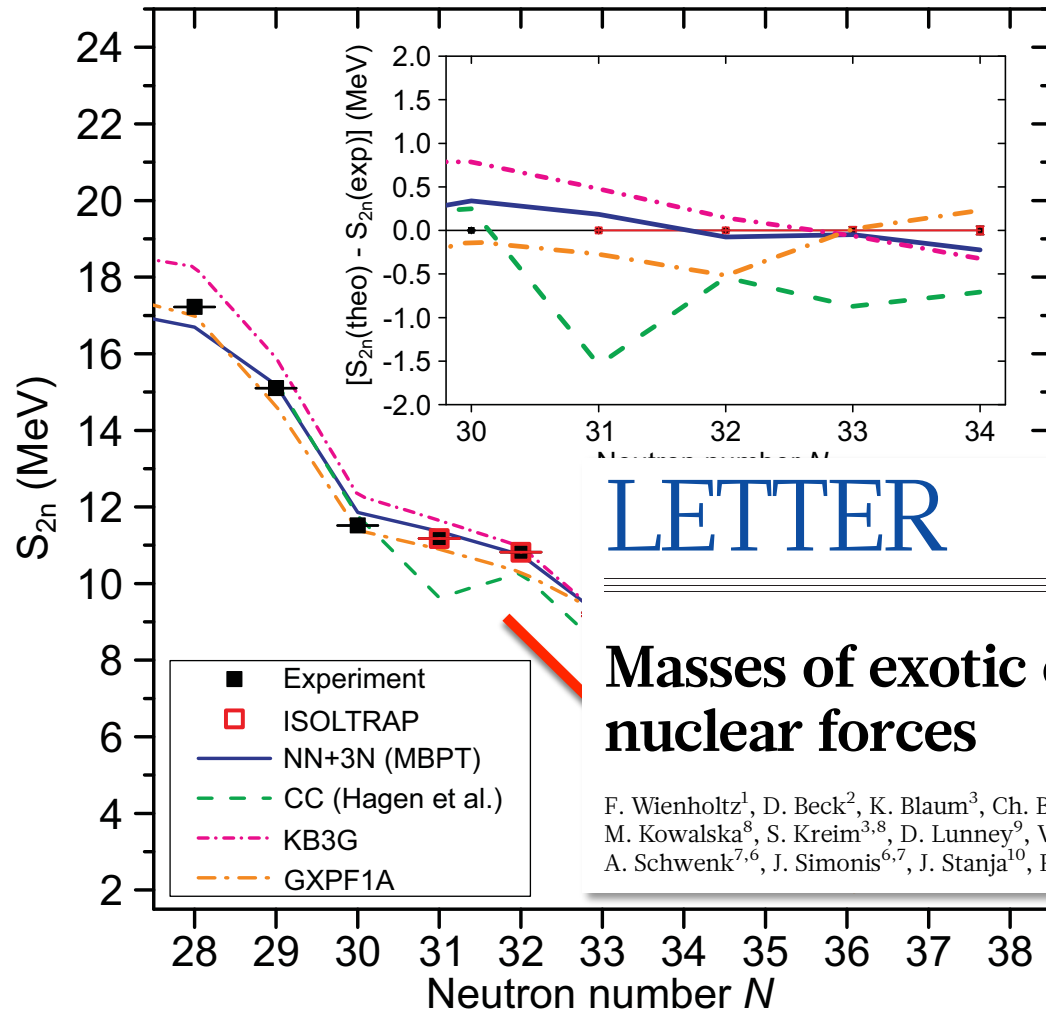
Excellent agreement with new data

Reproduces closed-shell $^{48,52}\text{Ca}$

Weak closed shell signature past ^{54}Ca

Experimental Connection: Mass of ^{54}Ca

New precision mass measurement of $^{53,54}\text{Ca}$ at **ISOLTRAP**: multi-reflection ToF



LETTER

Masses of exotic calcium isotopes pin down nuclear forces

F. Wienholtz¹, D. Beck², K. Blaum³, Ch. Borgmann³, M. Breitenfeldt⁴, R. B. Cakirli^{3,5}, S. George¹, F. Herfurth², J. D. Holt^{6,7}, M. Kowalska⁸, S. Kreim^{3,8}, D. Lunney⁹, V. Manea⁹, J. Menéndez^{6,7}, D. Neidherr², M. Rosenbusch¹, L. Schweikhard¹, A. Schwenk^{7,6}, J. Simonis^{6,7}, J. Stanja¹⁰, R. N. Wo

PHYSICS

doi:10.1038/nature12226

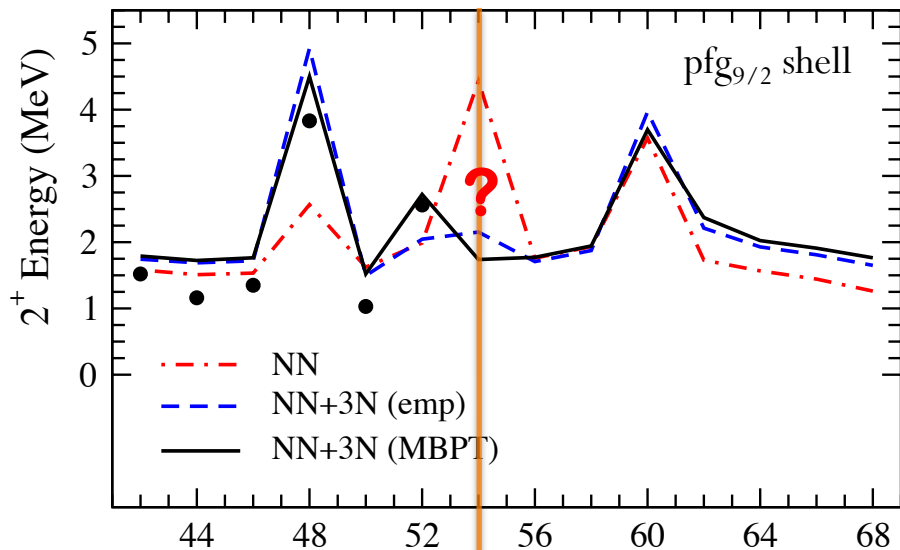
NEWS & VIEWS RESEARCH

Heavy calcium nuclei weigh in

The configurations of calcium nuclei make them good test cases for studies of nuclear properties. The measurement of the masses of two heavy calcium nuclei provides benchmarks for models of atomic nuclei. [SEE LETTER P.346](#)

Wienholtz et al., Nature (2013)

Pairing for Shell Evolution N=34



Peak in pairing gaps: complementary signature for shell closure

Compare with 2^+ energies for Ca

Agreement with CC throughout chain

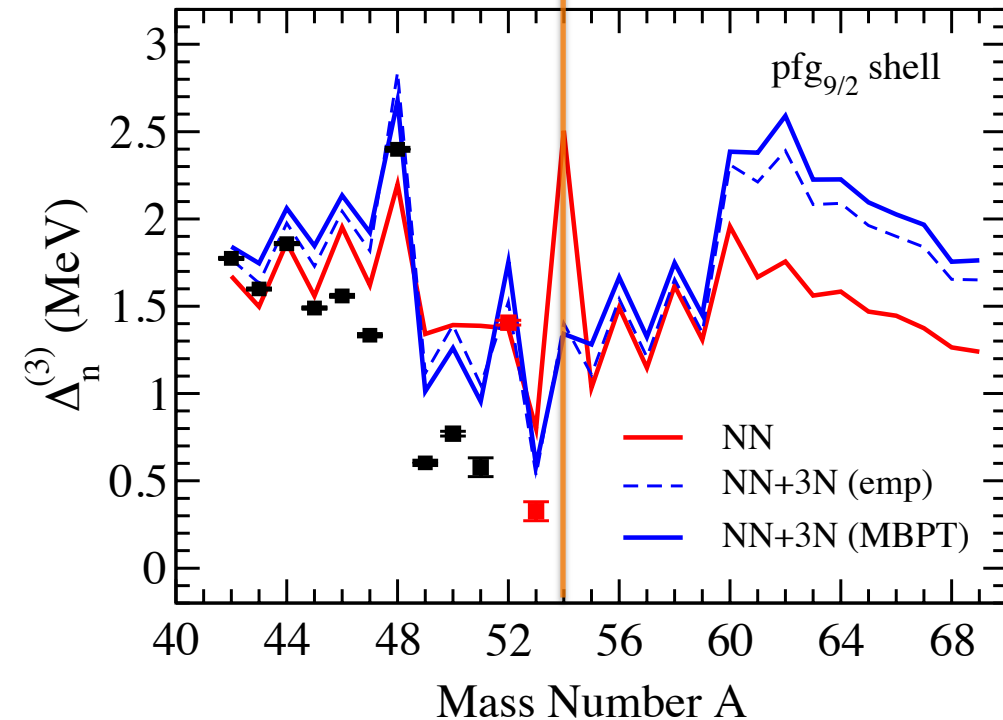
Hagen et al. PRL (2012)

N=28 strong peak

N=32 moderate peak

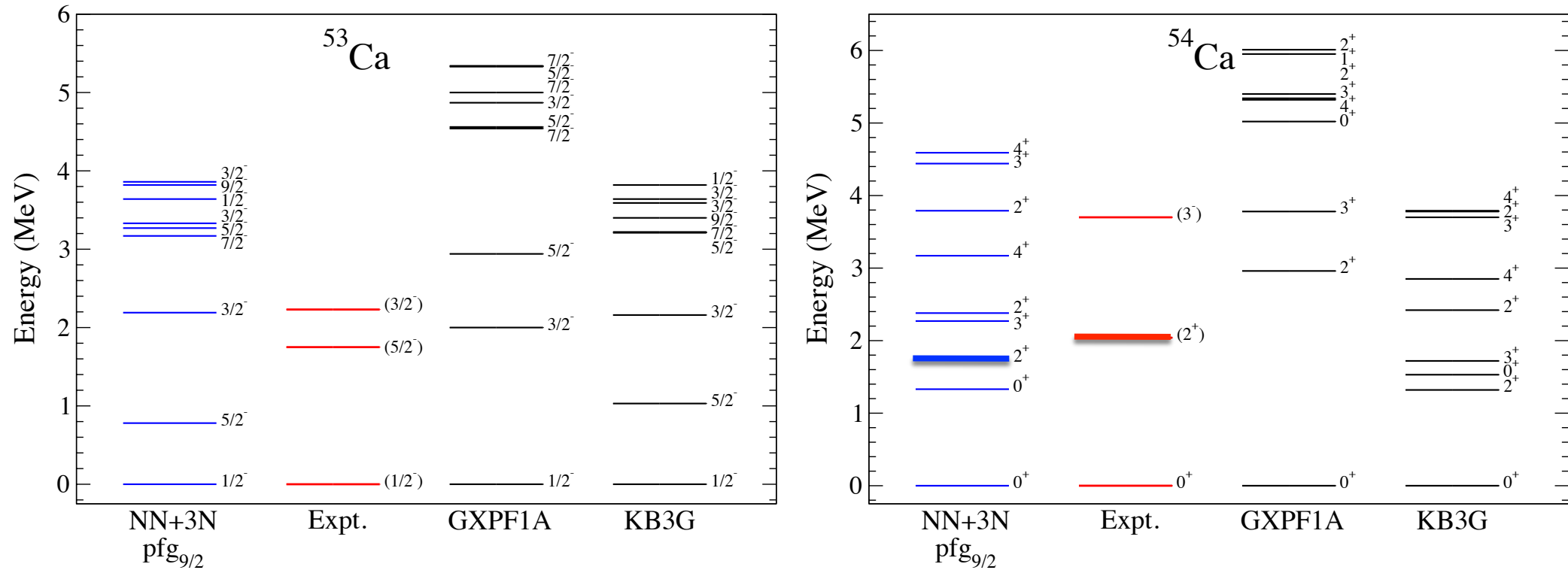
N=34 weak signature

3N forces suppress closed-shell feature



Neutron-Rich Ca Spectra Near N=34

Neutron-rich calcium spectra with NN+3N



JDH, Menendez, Schwenk, JPG (2013)
 JDH, Menendez, Simonis, Schwenk, in prep

Phenomenology: inconsistent predictions

NN+3N: signature of new $N=34$ magic number (also predicted in CC theory)

Agrees with new measurements from RIKEN

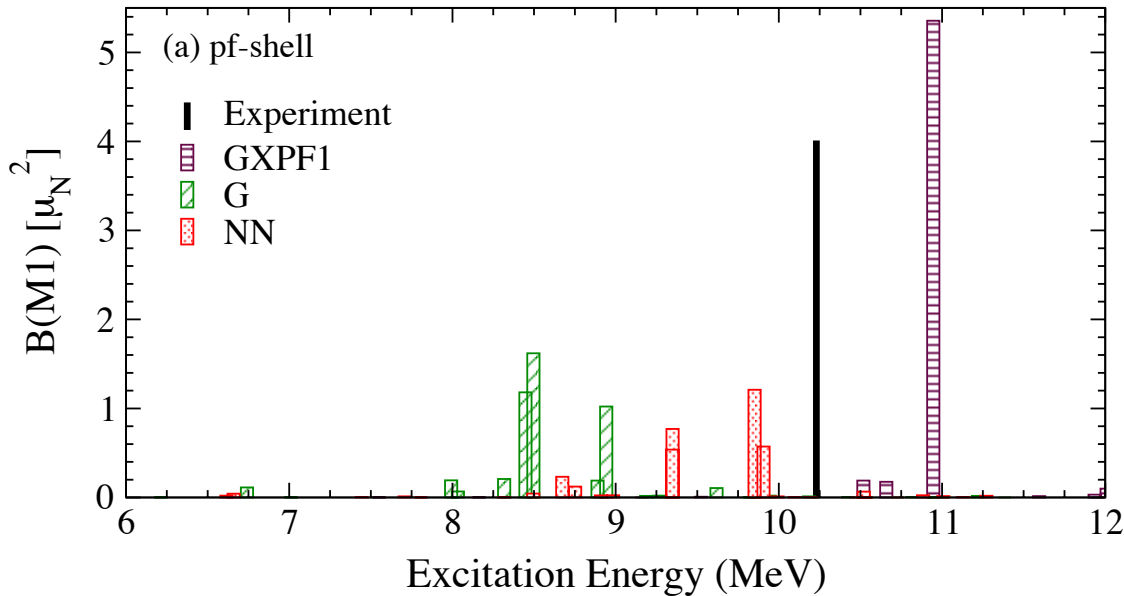
N=28 Magic Number: *M1* Transition Strength

$B(M1: 0_{gs}^+ \rightarrow 1^+)$ concentration indicates a single particle (spin-flip) transition

von Neumann-Coesel, *et al.* (1998)

Not reproduced in phenomenology

NN-only: highly fragmented strength, well below experiment



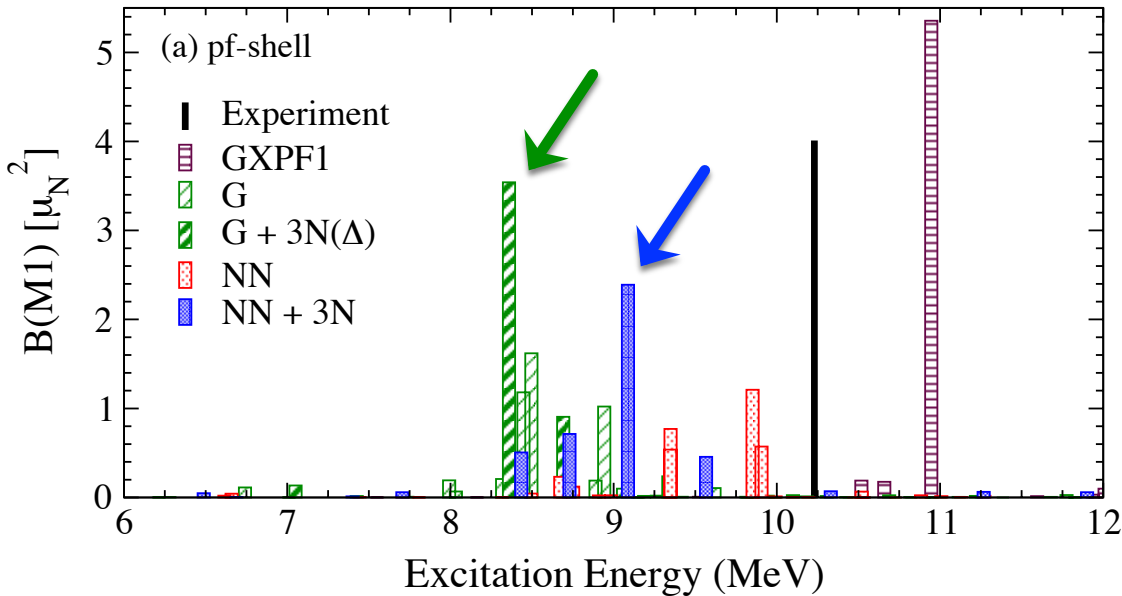
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pf-shell:

3N concentrates strength

Peaks below experiment

JDH, Otsuka, Schwenk, Suzuki, JPG (2012)

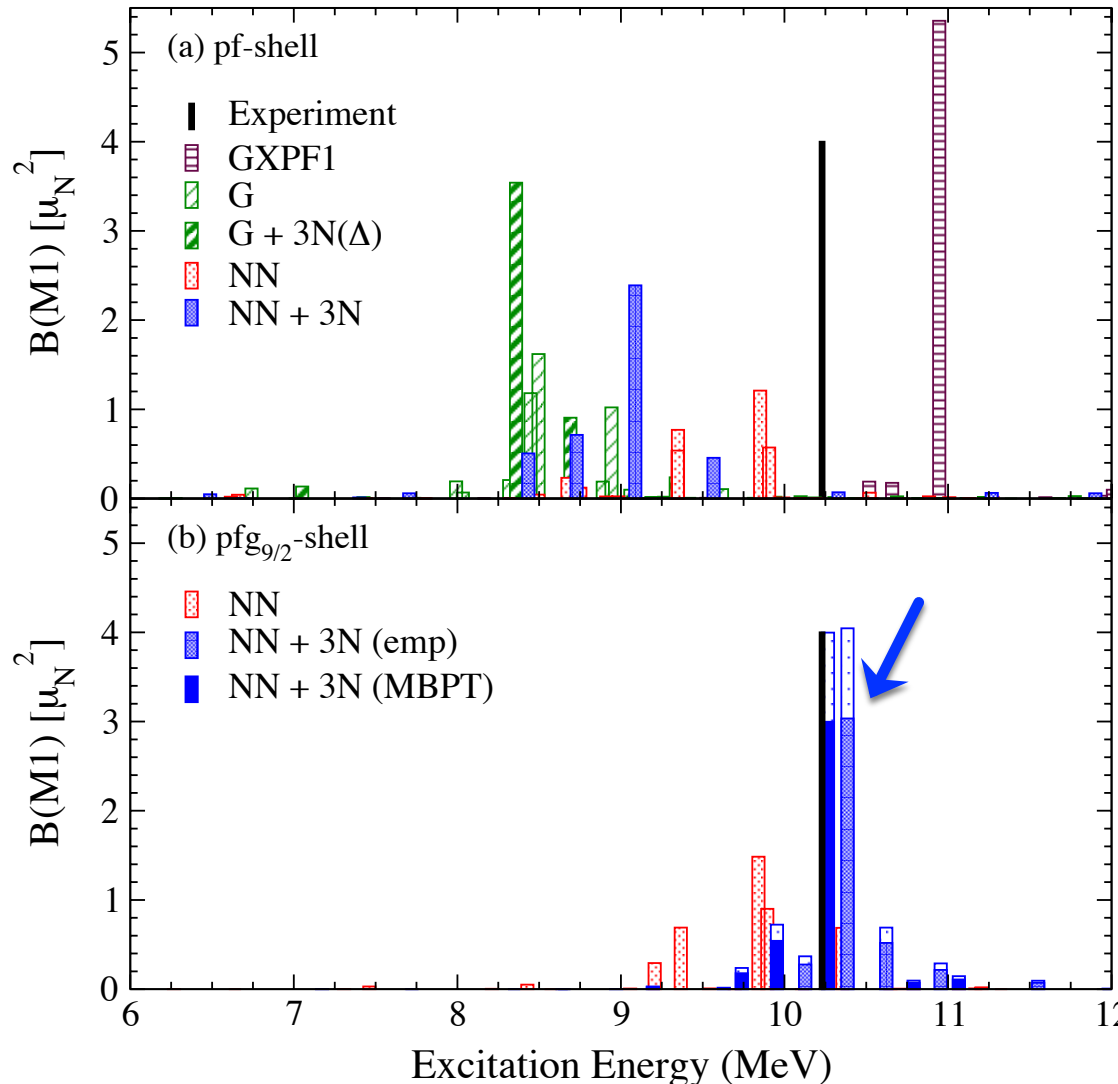
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Peaks below experiment

JDH, Otsuka, Schwenk, Suzuki, JPG (2012)

$pfg_{9/2}$ -shell:

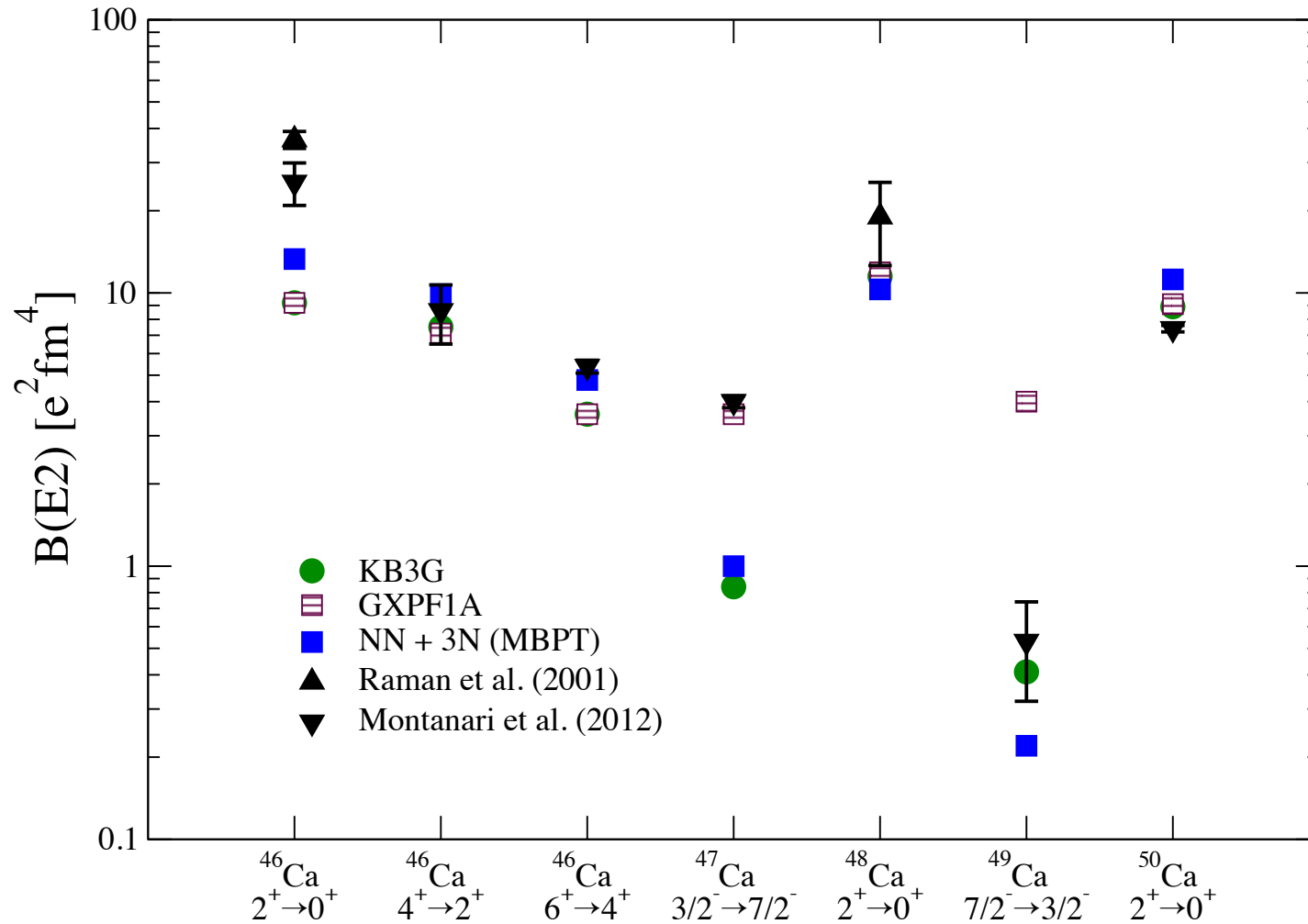
3N gives additional concentration

Peak close to experimental energy

Supports $N=28$ magic number

Transition Rates

Neutron-rich calcium B(E2) rates



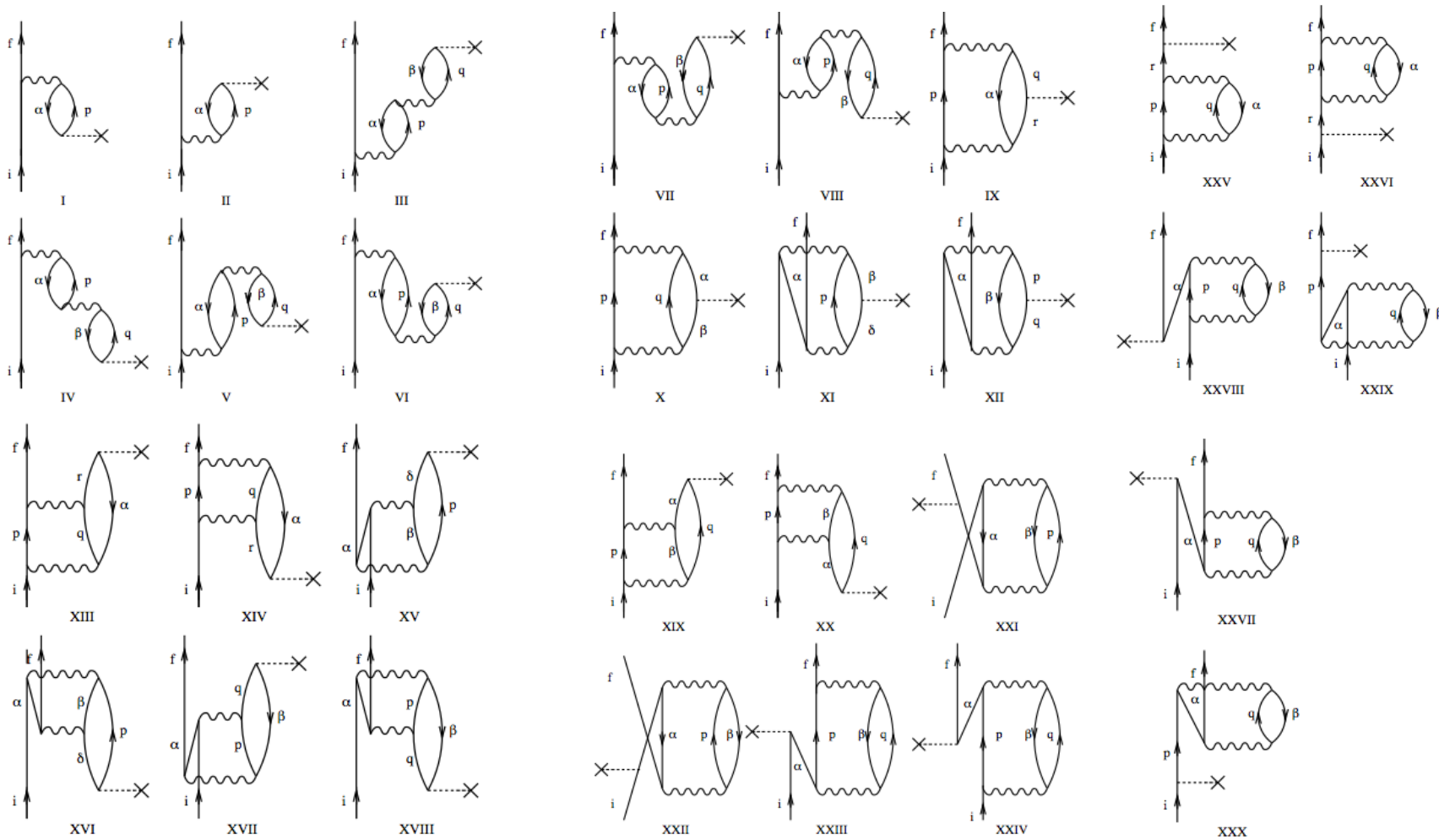
JDH, Menendez, Simonis, Schwenk, in prep.

Reasonable agreement with experiment – comparable to phenomenology

Uses effective charges

Effective Operators

Investigate many-body effects on effective charges and quenching of g_A



Use low-momentum interactions and 3N forces

Conclusion/Outlook

- Nuclear structure theory of medium-mass nuclei with 3N forces, extended spaces
- **Non-empirical valence-space methods**
 - First calculations based on NN+3N forces
 - Extended valence spaces needed
 - Cures NN-only failings: dripline, shell evolution, spectra
 - Residual 3N forces improve predictions beyond dripline
- **New directions**
 - Promising first results for F/Ne ground states to
 - Non-perturbative IM-SRG – excellent binding energies, spectra in sd shell only!
- **Large-space ab-initio methods**
 - Similar improvements with NN+3N as in valence-space methods
 - Agreement between methods encouraging for future – benchmarking valuable!

Acknowledgments

Collaborators



TECHNISCHE
UNIVERSITÄT
DARMSTADT

**J. Menendez, J. Simonis, A. Schwenk,
S. Binder, A. Calci, J. Langhammer, R. Roth**



S. Bogner



H. Hergert



T. Otsuka



T. Suzuki (Nihon U.)