Espace de Structure Nucléaire et de réactions Théorique (ESNT) – 11 Dec. 2019



Recent ab initio studies of nuclei from self-consistent Green's functions theory



Carlo Barbieri — University of Surrey

11 December 2019





Reach of ab initio methods across the nuclear chart



Slide, courtesy of V. Somà

The FRPA Method in Two Words

Particle vibration coupling is the main mechanism driving the redistribution and fragmentation of particle strength—expecially in the quasielastic regions around the Fermi surface...



Self-Consistent Green's Function Approach





Self-Consistent Green's Function Approach



One-nucleon spectral function



W. Dickhoff, CB, Prog. Part. Nucl. Phys. 53, 377 (2004) CB, M.Hjorth-Jensen, Pys. Rev. C**79**, 064313 (2009)



Ab-initio Nuclear Computation & BcDor code

Lecture Notes in Physics 936

Morten Hjorth-Jensen Maria Paola Lombardo Ubirajara van Kolck *Editors*

An Advanced Course in Computational Nuclear Physics

Bridging the Scales from Quarks to Neutron Stars

🖄 Springer

CB and A. Carbone, *chapter 11* of Lecture Notes in Physics 936 (2017)

http://personal.ph.surrey.ac.uk/~cb0023/bcdor/

Computational Many-Body Physics



Open-shells: 1st & 2nd order Gorkov diagrams

V. Somà, CB, T. Duguet, , Phys. Rev. C 89, 024323 (2014)
V. Somà, CB, T. Duguet, Phys. Rev. C 87, 011303R (2013)
V. Somà, T. Duguet, CB, Phys. Rev. C 84, 064317 (2011)



Gorkov espressions for 1st & 2nd order diagrams



Reaching (Gorkov - 3NF - higher ordes...) is a mess

Gorkov at 2nd order and ONLY NN forces:



Gorkov at 3rd order and ONLY NN forces:





Inclusion of NNN forces

→ 3p2h/3h2p terms relevant to next-generation high-precision methods.



Automatic Diagrammatic Generation (ADG) of the self-energy

Goal: <u>Drawing</u> of self-energy Feynman diagrams and <u>derivation</u> of corresponding algebraic expressions are performed automatically

Background: ADG of the BMBPT expansion (P. Arthuis et al Comp. Phys. Comm. 240, 202 (2019))



Chiral EFT interactions and 3-nucleon forces

in mid-mass isotopes



Benchmark of ab-initio methods for oxygen isotopic chain



Local vs. non-local chiral N²LO NNN interaction — by P. Navrátil





$$f_{\Lambda}^{\text{long}}(\mathbf{p}, \mathbf{q}) = \exp\left[-((\mathbf{p}^2 + 3/4 \mathbf{q}^2)/\Lambda^2)^n\right]$$
$$\left\langle \mathbf{p}' \mathbf{q}' | V_{3N}^{\text{reg}} | \mathbf{p} \mathbf{q} \right\rangle = f_R(\mathbf{p}', \mathbf{q}') \left\langle \mathbf{p}' \mathbf{q}' | V_{3N} | \mathbf{p} \mathbf{q} \right\rangle f_R(\mathbf{p}, \mathbf{q})$$

$$f_{\Lambda}^{\text{reg}}(\mathbf{Q}_{i}) = \exp\left[-(\mathbf{Q}_{i}^{2}/\Lambda^{2})^{2}\right]$$

$$\left\langle \mathbf{p}'\mathbf{q}'|V_{3N}^{\text{reg}}|\mathbf{p}\mathbf{q}\right\rangle = \left\langle \mathbf{p}'\mathbf{q}'|V_{3N}|\mathbf{p}\mathbf{q}\right\rangle \prod_{i} f_{R}(\mathbf{Q}_{i})$$

$$\xi^{2} = p^{2} + 3/4q^{2} \approx 3\text{-nucleon tot.}$$
kinetic energy

 $[(a_2, a_3)^2]$

along a

- Local: chiral N³LO NN+ N²LO 3N500
 - c_D =-0.2 c_E=-0.205 (³H E_{gs}=-8.48 MeV)
- Non-local: chiral N²LO_{sat} NN+3N

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- c_D =+0.8168 c_E =-0.0396 (³H E_{gs}=-8.53 MeV)
- Local/Non-local: chiral N³LO NN+ N²LO
 - $c_D = +0.7 c_E = -0.06 (^{3}H E_{gs} = -8.44 MeV)$



Plots courtesy of K. Hebeler (from his 7/1/19 talk)

Comparison of nuclear forces - ^ANi



V. Somà, P. Navrátil, F. Raimondi, CB, T. Duguet, in preparation – arXiv:1907:1907.09790

N3LO(500) + nln 3NF

SCGF – Gorkov-ADC(2)



UNIVERSITY OF V. Somà, P. Navrátil, F. Raimondi, CB, T. Duguet, in preparation – arXiv:1907:1907.09790

$d_{3/2} - s_{1/2}$ inversion in K isotopes



SDPF-MUr SDPF-MUs $E(1/2_1^+) - E(3/2_1^+)[MeV]$ -1• Data, literature Data, this work -2₁₈ Neutron Number

Mass Number

NNLO_{sat} NN+3N(lnl)

V. Somà, CB, et al., arXiv:1907:1907.09790

Papuga et al., PRL110, 172503 (2013); PRC90, 034321 (2014)

RIKEN, SEASTAR coll. (unpublished)

SDPF-U SDPF-Umod SDPF-MU



Ab initio optical potentials from propagator theory

Relation to Fesbach theory: Mahaux & Sartor, Adv. Nucl. Phys. 20 (1991) Escher & Jennings Phys. Rev. C**66**, 034313 (2002)

Previous SCGF work: CB, B. Jennings, Phys. Rev. C**72**, 014613 (2005) S. Waldecker, CB, W. Dickhoff, Phys. Rev. C**84**, 034616 (2011) A. Idini, CB, P. Navrátil, Phys. Rv. Lett. **123**, 092501 (2019)



Microscopic optical potential



Nuclear self-energy $\Sigma^{\star}(\mathbf{r}, \mathbf{r}'; \varepsilon)$:

- contains both particle and hole props.
- it is proven to be a Feshbach opt. pot → in general it is non-local !



Solve scattering and overlap functions directly in momentum space:

$$\Sigma^{\star l,j}(k,k';E) = \sum_{n,n'} R_{n\,l}(k) \Sigma^{\star l,j}_{n,n'} R_{n\,l}(k')$$
$$\frac{k^2}{2\mu} \psi_{l,j}(k) + \int dk' \, k'^2 \, \Sigma^{\star l,j}(k,k';E_{c.m.}) \psi_{l,j}(k') = E_{c.m.} \psi_{l,j}(k)$$

Low energy scattering - from SCGF

Benchmark with NCSM-based scattering.

Scattering from mean-field only:



[A. Idini, CB, Navratil, Phys. Rev. Lett. **123**, 092501 (2019)]

Low energy scattering - from SCGF

Benchmark with NCSM-based scattering.

[A. Idini, CB, Navratil, Phys. Rev. Lett. **123**, 092501 (2019)]

Full self-energy from SCGF:



Scattering from mean-field only:



Low energy scattering - from SCGF

10 3 $^{16}O(n,n)^{16}O$ $E_n = 3.286 \text{ MeV}$ • Lister and Sayres, Phys Rev 143, 745 - This Work $d\sigma/d\Omega ~(b/sr)$ 0.01 0.001 0 20 40 60 80 100 120 140 160 180 θ (deg) ${}^{40}Ca(n,n){}^{40}Ca$ $E_n = 3.2 \text{ MeV}$ 10 $d\sigma/d\Omega ~(b/sr)$ • Becker et al., Nucl. Phys. 89, 154 - This Work 0.01 $\stackrel{80}{\theta} \stackrel{100}{(\text{deg})}$ 0 20 60 120 140 160 40 180

[A. Idini, CB, Navrátil, PRL123, 092501 (2019)]



Role of intermediate state configurations (ISCs)



Reaching large isotopes (electron scattering and charge radii)

CB, P. Arthuis – Preliminary... (work in progress)



Electron-Ion Trap colliders...



FIG. 1. Overview of the SCRIT electron scattering facility.

Comparison of the second secon

FIG. 3. Reconstructed momentum spectra of ¹³²Xe target after background subtraction. Red shaded lines are the simulated radiation tails following the elastic peaks.



First ever measurement of charge radii through electron scattering with and ion trap setting that <u>can</u> <u>be used on radioactive isotopes</u> !!

K. Tsukada et al., Phy rev Lett 118, 262501 (2017)



Convergence in large isotopes - e.g. ¹³²Xe

Gorkov ADC(2) with NNLOsat Hamiltonian



Energies still badly converging...

- Nmax converges slowly...

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- E3max (# of 3NFs elements) out of control



Radii converge much better and can be bracketed!

Convergence in large isotopes - e.g. ¹³²Xe

Gorkov ADC(2) with NNLOsat Hamiltonian



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Convergence in large isotopes - e.g. ¹³²Xe

Gorkov ADC(2) with NNLOsat Hamiltonian





Sn and Xe isotopes



Gorkov ADC(2) and Dyson ADC(3) with NNLOsat Hamiltonian

	SCGF	Exp.
100 Sn	4.525 - 4.707	
$^{132}\mathrm{Sn}$	4.725 - 4.956	4.7093
132 Xe	4.700 - 4.948	4.7859
$^{136}\mathrm{Xe}$	4.715 - 4.928	4.7964
$^{138}\mathrm{Xe}$	4.724 - 4.941	4.8279

Preliminary !!

Electron and neutrino

scattering off nuclei

N. Rocco, CB, Phys. Rev. C98, 025501 (2018)

N. Rocco, CB, O. Benhar, A. De Pace, A. Lovato, Phys. Rev. C99, 025502 (2019)

CB, N. Rocco, V. Somà, arXiv:1907.01122



Lepton-nucleon cross section

$$\left(\frac{d\sigma}{dT'd\cos\theta'}\right)_{\nu/\bar{\nu}} = \frac{G^2}{2\pi} \frac{k'}{2E_{\nu}} \left[\hat{L}_{CC}R_{CC} + 2\hat{L}_{CL}R_{CL} + \hat{L}_{LL}R_{LL} + \hat{L}_TR_T \pm 2\hat{L}_{T'}R_{T'} \right] \,,$$

Nuclear structure is in the hadronic tensor:





$$R_{CC} = W^{00} \qquad R_T = W^{11} + W^{22} \qquad R_{T} = -\frac{1}{2}(W^{03} + W^{30}) \qquad R_T = -\frac{i}{2}(W^{12} - W^{21}), \qquad W^{\mu\nu} = \sum_f \langle 0|j^{\mu\dagger}|f\rangle\langle f|j^{\nu}|0\rangle\delta(E_0 + \omega - E_f) \qquad R_{T'} = -\frac{i}{2}(W^{12} - W^{21}),$$

Lepton-nucleon cross section

$$\left(\frac{d\sigma}{dT'd\cos\theta'}\right)_{\nu/\bar{\nu}} = \frac{G^2}{2\pi} \frac{k'}{2E_{\nu}} \left[\hat{L}_{CC}R_{CC} + 2\hat{L}_{CL}R_{CL} + \hat{L}_{LL}R_{LL} + \hat{L}_TR_T \pm 2\hat{L}_{T'}R_{T'} \right] \,,$$

Nuclear structure is in the hadronic tensor:

$$\begin{split} W^{\mu\nu}(\mathbf{q},\omega) &= \int \frac{d^3k}{(2\pi)^3} dE P_h(\mathbf{k},E) \frac{m^2}{e(\mathbf{k})e(\mathbf{k}+\mathbf{q})} \\ &\times \sum_i \langle k | j_i^{\mu\dagger} | k+q \rangle \langle k+q | j_i^{\nu} | k \rangle \\ &\times \delta(\omega+E-e(\mathbf{k}+\mathbf{q})) \,, \end{split}$$

$$W_{2\mathbf{b}}^{\mu\nu}(\mathbf{q},\omega) = \frac{V}{2} \int d\tilde{E} \frac{d^3k}{(2\pi)^3} d\tilde{E}' \frac{d^3k'}{(2\pi)^3} \frac{d^3p}{(2\pi)^3} \\ \times \frac{m^4}{e(\mathbf{k})e(\mathbf{k}')e(\mathbf{p})e(\mathbf{p}')} P_h^{\rm NM}(\mathbf{k},\tilde{E})P_h^{\rm NM}(\mathbf{k}',\tilde{E}') \\ \times \sum_{ij} \langle k \, k' | j_{ij}^{\mu\dagger} | p \, p' \rangle \langle p \, p' | j_{ij}^{\nu} | k \, k' \rangle \\ \times \delta(\omega + \tilde{E} + \tilde{E}' - e(\mathbf{p}) - e(\mathbf{p}')) \,.$$
(41)

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Two-body diagrams contributing to the axial and vector responses



N. Rocco, CB, O. Benhar, de Pace , A. Lovato, Phys. Rev. C99, 025502 (2019)

Charged-current reaction for 1 GeV neutrinos



One-body current describe quasi elastic peak

Difference between CBF(AV18) and SCGF(NNLOsat) from 1-b terms

Two-body currents fiull up dip region

Missing Delta and meson emission contributions

X-sec. droppin with scattering angle

<u>N. Rocco</u>, CB, O. Benhar, de Pace , A. Lovato, Phys. Rev. C**99**, 025502 (2019)

Neutrino Oscillations - next generation experiments



SANFORD LAB South Dakota Nebraska Illinois DUNE experiment will measure long base line neutrino oscillations to:

- Resolve neutrino mass hierarchy
- Search for CP violation in weak interaction
- Search for other physics beyond SM

Liquid Argon projection chamber is being used. It will require one order of magnitude ($20\% \rightarrow 2\%$) improvement in theoretical prediction for v-⁴⁰Ar cross sections to achieve proper event reconstruction.

➔ Need good knowledge of ⁴⁰Ar spectral functions and consistent structure-scattering theories.



Spectral function for ⁴⁰Ar and Ti

Jlab experiment E12-14-012 (Hall A) Phys. Rev. C 98, 014617 (2018); arXiv:1810.10575



 40 Ar(e,e'p) and Ti(e,e'p) data being analyzed



Spectral function for ⁴⁰Ar



- Experimental datat now available from Jlab: H. Dai et al., arXiv:1803.01910/ 1810.10575
- Ab initio simulations based on the ADC(2) truncation of the N2LO-sat Hamiltoninan

→ Want validation of initial state correlation <u>before</u> they are implementer in neutrino- 40 Ar simulations

CB, N. Rocco, V. Somà, arXiv:1907.01122

Electron and v scattering on ⁴⁰Ar and Ti

Jlab experiment E12-14-012 (Hall A) [Phys. Rev. C 98, 014617 (2018)]









Spectroscopic factors



Quenching of SF in stable nuclei



SRC are present and verified experimentally

BUT the are NOT the dominant mechanism for quenching SF !!!



Z/N asymmetry dependence of SFs - Theory

Ab-initio calculations explain (a very weak) the Z/N dependence but the effect is much lower than suggested by direct knockout

Rather the quenching is high correlated to the gap at the Femi surface.





Z/N asymmetry dependence of SFs

Calculated spectroscopic factors are found to be:

- correlated to p-h gaps
- independent of asymmetry
- consistent with experimental data

